

# A Hardware and Software Task-Scheduling Framework Based on CPU+GPU Heterogeneous Architecture in Edge Computing Devices

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## **Abstract**

In the world of heterogeneous real-time systems, balancing result accuracy with power and time constraints presents a significant challenge. To combat the challenge, the researchers have proposed approximate computing tasks where the applications can be divided into two components, a mandatory part that produces an acceptable result, followed by an optional part that enhances the result's accuracy. This project proposes a scheduling algorithm for real-time dependent tasks on CPU-GPU based heterogeneous systems. The objective of the scheduling remains to maximize accuracy while considering both deadlines and power constraints. Given real-time applications, which are represented as Direct Acyclic Graph (DAG) of tasks, the algorithm topologically sorts tasks and identifies critical high (CH), and critical low (CL) tasks based on their execution time and task dependencies. These tasks are then scheduled appropriately across the Graphic Processing Unit (GPU) and Central Processing Unit (CPU) by considering power consumption while ensuring that all tasks meet the deadline. The effectiveness of this algorithm is evaluated by measuring the achieved result accuracy without exceeding power limits. Implementation of task scheduling on the NVIDIA Jetson Nano, which includes both CPU and GPU, demonstrates the practicality of the approach. Additionally, the results highlight the advantages of using heterogeneous systems over homogeneous systems, with an NQ of 81.1% being achieved.

**Keywords-** Real-time systems, heterogeneous systems, power consumption, task scheduling

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# Introduction

Heterogeneous multicore systems, which integrate various types of processors such as CPUs, GPUs, ASICs, and FPGAs, are increasingly prevalent across a wide range of technological fields, particularly in time-critical systems. These systems leverage specialized hardware components, known as accelerators, which are designed to perform specific computational tasks more efficiently than general-purpose CPUs. Accelerators are essential because they offload and speed up demanding tasks like parallel processing, encryption, and data compression, resulting in faster overall processing and reduced power consumption [1]. In edge computing environments, where real-time data processing and energy efficiency are paramount, the use of accelerators is crucial to meet the escalating demands for computational power and to manage the growing volume of data effectively. Heterogeneous task scheduling algorithm are being used in wide applications, such as optimizing allocation of tasks in cloud computing devices [2], transport-pick agents task scheduling (TPTS) problem [3], fog computing (FC) and cloud computing [4].

One of the biggest challenges in heterogeneous multicore systems is achieving accurate and reliable performance while adhering to strict power and timing constraints. This is especially critical in real-time systems where the timing of task execution can be a matter of life and death. Task scheduling in these environments becomes even more complex when dealing with real-time applications. Real-time applications represented as Directed Acyclic Graphs (DAGs) consist of tasks (nodes) with specific execution

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orders defined by dependencies (edges) between them. The DAG structure ensures that tasks are executed in a sequence that respects these dependencies, crucial for maintaining the timing and performance requirements of real-time systems [5].

To address these challenges, researchers have introduced the concept of approximate computing, where tasks are divided into two components. The first component, the mandatory part, ensures that the system meets its fundamental requirements by producing a minimally acceptable result within the specified deadline. The second component, the optional part, enhances the result's accuracy when additional resources and time are available. In this context, each task can have multiple versions, each representing different execution levels with varying degrees of accuracy and execution time. These task versions enable the system to balance accuracy with timing and power constraints by selecting the most suitable version based on the available resources. This approach optimizes the Quality of Service (QoS) while ensuring that deadlines are consistently met [6].

The effectiveness of this approach is demonstrated through its implementation on the NVIDIA Jetson Nano, a platform that includes both CPU and GPU [7]. The results of this implementation highlight not only the practicality of the proposed algorithm but also the inherent advantages of using heterogeneous systems over homogeneous ones. The introduction of this scheduling algorithm offers a promising approach to managing the complexities of task scheduling in heterogeneous real-time systems. More detailed explation is mentioned in 2.5. By effectively leveraging the unique strengths of different processing units and incorporating considerations of power and time constraints, this work contributes to the ongoing efforts to enhance the performance and reliability of critical real-time applications.

#### 1.1 Problem definition

In today's complex computing environments, particularly in heterogeneous multicore systems, efficient task scheduling is critically challenging. These tasks must handle real-time applications where tasks have varying execution requirements and multiple versions, each with different computational demands and power consumptions.

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The challenge lies in optimally assigning tasks to either the CPU or GPU while ensuring that all tasks and the scheduling process carefully balance performance and efficiency. The need to manage these constraints effectively supports the development of advanced scheduling algorithms that can navigate these complexities to optimize system performance, making this an essential area of research in real-time systems.

Given a set of tasks T represented as a Directed Acyclic Graph (DAG), which is a common representation of real-time systems, this DAG has different nodes or threads represented as  $T_i$  where i represents the task number that ranges from 1 to  $T_L$ , that is  $i = \{1, 2, 3, \dots, T_L\}$ . The system under consideration is a multicore heterogeneous computing environment, specifically the NVIDIA Jetson Nano, which integrates both CPU and GPU capabilities. [6] Each task  $T_i$  may have multiple versions (signifying different degrees of accuracy) denoted as  $T_i^j$ , where j represents the specific version of the task, with j ranging from 0 to  $T_L$ , that is  $j = \{0, 1, 2, \dots, T_L\}$ , indicating that a task can have one or more versions, or in some cases, no versions at all. Each task version  $T_i^j$ is characterized by its mandatory cycles  $M_i^j$  and optional cycles  $O_i^j$ , which define the essential and additional computation requirements of the task, respectively. The power consumption associated with these nodes is represented by the power factors  $Pow_i^j$ , L for critical low  $(C_L)$  tasks and  $Pow_i^j$ , H for critical high  $(C_H)$  nodes. The efficiency of [8] executing each task version in these critical modes is described by  $Y_i^{\jmath}$ , L for  $C_L$  and  $Y_i^{\jmath}$ , H for  $C_H$ . Additionally, each task must adhere to a specified deadline D, which defines the maximum allowable time for task completion. This structure presents a complex challenge in scheduling tasks in heterogeneous systems to optimize both performance and power consumption while ensuring all tasks meet their deadlines.

This research aims to develop an efficient scheduling algorithm for assigning tasks  $T_i$  in a heterogeneous computing system, specifically utilizing either the CPU or GPU of an NVIDIA Jetson Nano, within a given deadline D while optimizing power consumption Pow. The approach involves topologically sorting the tasks  $T_i$  to establish their execution order based on dependencies. Subsequently, the algorithm identifies critical low  $(C_L)$  and critical high  $(C_H)$  tasks by analyzing their execution times, represented as  $\mathrm{ET}_i^j$ , L and  $\mathrm{ET}_i^j$ , H for each task version  $T_i^j$ . By categorizing tasks into  $C_L$  and  $C_H$ , the algorithm can effectively manage power consumption and ensure that all tasks are

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completed within the specified deadline. This scheduling method seeks to balance computational efficiency and power usage, leveraging the strengths of the heterogeneous system to achieve optimal performance.

Additionally, the problem involves optimizing task scheduling in heterogeneous multicore systems, where the number of available cores significantly impacts the Quality of Service (QoS) delivered by the system. The proposed solution will explore current methodologies and leverage topological sorting, along with the identification of critical low and high tasks, to ensure efficient task execution within stringent deadlines. By carefully balancing computational efficiency and power usage, this work seeks to contribute a robust approach to managing real-time tasks in heterogeneous computing environments, ultimately enhancing system reliability and performance.

#### 1.2 Scope

The main goals of the thesis were:

- To ensure tasks are completed within the specified deadlines in real-time heterogeneous systems, particularly on both CPU and GPU components.
- To optimize the scheduling of time-critical, dependent tasks by balancing the trade-offs between execution speed and power consumption, ensuring that the system remains within specified power constraints.
- To conduct a comparative analysis that highlights the advantages of using heterogeneous systems, such as those integrating both CPU and GPU, over traditional homogeneous systems in handling the complex computational tasks.
- To investigate how the scalability of core counts within a heterogeneous system can improve the system's capacity to achieve near-ideal Quality of Service (QoS) in real-time applications, thereby enhancing overall systems performance.
- To evaluate the benchmark performance of the proposed scheduling in real-time applications, using the NVIDIA Jetson Nano as the representative heterogeneous systems in handling complex computational tasks.

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#### 1.3 Limitations

The scheduling algorithm developed in this project effectively optimizes the execution of a single set of tasks with six nodes on a heterogeneous system, balancing trade-offs between execution speed and power consumption. However, the algorithm faces significant challenges when applied to more complex, real-world scenarios. In practical applications, systems are often required to manage multiple sets of tasks, each with numerous nodes and varying task versions. The complexity of scheduling these tasks simultaneously across multiple cores, especially when considering dependencies and different versions, dramatically increases the computational load. This increase in complexity makes the current algorithm less efficient and difficult to scale. As the number of tasks and nodes grows, the algorithm may struggle to find optimal solutions within reasonable time frames, limiting its usefulness in larger, more dynamic environments.

Another limitation arises from the use of Python programming for data analysis and scheduling execution. In this project, data is managed using dictionaries and matrix methods, which are adequate for smaller datasets but may become inefficient when dealing with large-scale data typically encountered in real-world applications. The computational resources required to handle large volumes of data increase significantly, and the current approach may not be sufficient to process and analyze this data in a timely manner.

Moreover, in practical scenarios, data is often generated continuously and in large quantities, necessitating more advanced tools for real-time processing. The use of basic programming techniques without the support of AI or machine learning can hinder the algorithm's ability to adapt to changing conditions and optimize performance dynamically. For instance, AI-driven approaches could better handle the continuous data streams, predict task behaviors, and adjust scheduling in real-time, which is beyond the capabilities of the current implementation. The reliance on traditional programming methods thus represents a limitation when considering the scalability and adaptability required for real-time applications in more complex and data-intensive environments.

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#### 1.4 Work undertaken

The key achievements of this project were:

 Successfully implemented a scheduling algorithm using Python that ensures task completion within real-time constraints on heterogeneous systems, specifically utilizing the CPU and GPU components effectively.

- Optimized the scheduling of time-sensitive, dependent tasks by balancing between deadline and power efficiency, thereby maintain adherence to strict power consumption limits.
- Provided a detailed comparative analysis showcasing the significant benefits
  of heterogeneous systems over homogeneous ones, particularly in managing
  complex and computationally intensive tasks.
- Explored and confirmed that increasing the number of cores within a heterogeneous system significantly enhances its ability to approach near-ideal Quality of Service (QoS) in real-time scenarios, contributing to improved system performance.

#### 1.5 Structure of work

The structure of this report is organized as follows: Chapter 2 presents a comprehensive literature review, exploring key areas such as the role of heterogeneous systems, Directed Acyclic Graphs (DAGs), task scheduling, Jetson Nano, and power and energy optimization strategies. Chapter 3 explains the core methodology, detailing the design of the task scheduling algorithm and presenting the associated pseudocode. Chapter 4 discusses the results and observations derived from the project, highlighting the key findings. Finally, Chapter 5 provides an evaluation of the work completed, discussing its implications and suggesting directions for future research.

## Literature review

This chapter will cover all the fundamental background knowledge required to understand the research topic. The first section explores the advantages of heterogeneous systems, emphasizing their ability to optimize performance and energy efficiency by utilizing different types of processors, each designed to handle specific tasks effectively. The second section delves into the use of Directed Acyclic Graphs (DAGs) for representing real-time applications, which provide a clear structure for modeling task dependencies and execution sequences. The third section discusses real-time parallel tasks, focusing on the challenges of scheduling these tasks to meet strict timing requirements while maximizing the utilization of available resources. The final section examines algorithms used in CPU-GPU systems for task scheduling, highlighting the importance of efficiently distributing workloads across different processing units. Additionally, this chapter introduces the concept of task versions, which allow for varying levels of accuracy and execution time, offering a flexible approach to balancing performance and resource consumption in complex computing environments.

# 2.1 The Role of Heterogeneous Systems in Modern Computing

Heterogeneous systems offer distinct advantages over homogeneous systems, particularly when addressing the nonlinear impacts of core frequency and cache partitioning

on task execution, as highlighted in [9]. By leveraging the diverse strengths of different core types, such as performance-oriented and energy-efficient cores, these systems can achieve significant energy savings that would be challenging to realize with a homogeneous architecture. This makes heterogeneous systems an optimal choice for applications where minimizing energy consumption while meeting strict deadlines is critical.

The application of heterogeneous systems is particularly evident in the context of Network Function Virtualization (NFV), as discussed in [10]. These systems integrate different types of cores, like Performance cores (P-cores) and Efficient cores (E-cores), to optimize the deployment of virtual network functions (VNFs). By matching VNFs with the most suitable core type, heterogeneous systems enhance performance and energy efficiency, reducing overall power consumption [11]. The ability to dynamically allocate VNFs based on their computational needs also improves load balancing, ensuring even distribution of workloads and reducing latency. This flexibility and scalability make heterogeneous systems ideal for adapting to varying workloads and service demands, ensuring better Quality of Service (QoS) and positioning them as a sustainable solution for modern network environments.

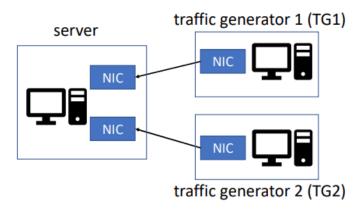


Figure 2.1: Hardware implementation [10]

Beyond NFV, heterogeneous systems play a crucial role in enhancing the computational power of edge computing systems, particularly within a CPU+FPGA heterogeneous architecture, as explored in [1]. In this architecture, FPGAs act as dynamic, reconfigurable accelerators that significantly improve system efficiency and perfor-

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mance. The FPGA's reconfigurability allows it to adapt its functionality at runtime, making it suitable for various computational tasks that demand high performance and low latency. The dynamic partial reconfiguration (DPR) capability enables specific portions of the hardware to be reconfigured while the rest of the system continues to operate, thereby minimizing downtime and optimizing resource utilization. These accelerators, particularly the FPGA [12], are essential for handling tasks that require parallel processing, low power consumption, and high computational efficiency, which are vital for meeting the real-time performance demands of edge computing systems.

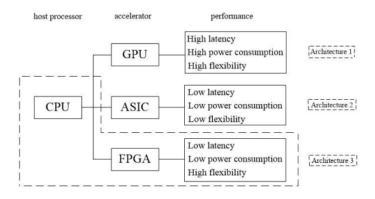


Figure 2.2: The characteristics of GPU, ASIC and FPGA[1]

Similarly, specialized hardware accelerators like Hotline, introduced in [13], further illustrate the efficiency of heterogeneous systems in specific applications such as training recommendation systems. Hotline optimizes training by dynamically classifying embedding entries based on their access frequency and strategically utilizing both CPU and [14] GPU resources. By fragmenting mini-batches into smaller micro-batches and scheduling them efficiently, Hotline minimizes idle time and improves throughput. This example underscores the value of accelerators in heterogeneous systems, where targeted optimization can lead to substantial performance gains.

Finally, integrated CPU/GPU systems represent another significant advancement in computing efficiency, particularly for latency-sensitive applications like autonomous systems and edge intelligence, as discussed in [15]. These platforms combine the general-purpose processing power of CPUs with the parallel processing capabilities of GPUs, all within a single chip, enabling more efficient handling of complex tasks. The Unified Memory (UM) model simplifies memory management by allowing both

CPUs and GPUs to share the same memory space, reducing the overhead associated with data transfers. To further optimize performance, [16] proposes a framework that intelligently selects between CPU, GPU, and hybrid data initialization modes based on the application's specific needs. This approach reduces latency and ensures that data is processed as efficiently as possible, which is particularly beneficial for real-time applications.

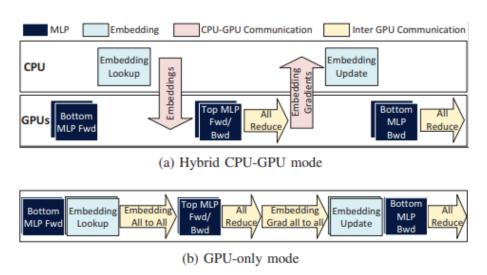


Figure 2.3: The execution flow of a typical recommendation model in the hybrid CPU-GPU and GPU-only. Due to their large sizes, the embedding tables are stored and processed on CPUs. The GPUs process the neural layers.[13]

In summary, heterogeneous systems, whether they integrate diverse cores, specialized accelerators, or CPU/GPU combinations, offer powerful solutions across various domains. Their ability to optimize resource utilization, improve energy efficiency, and enhance performance makes them indispensable in modern computing, from NFV and edge computing to autonomous systems.

#### 2.2 Directed Acyclic Graph (DAG) and real-time systems

In various research studies, Directed Acyclic Graphs (DAGs) have been effectively used to represent real-time applications, demonstrating their utility in optimizing scheduling and resource allocation. For instance, [17] discusses the representation of several benchmark and real-world applications as DAGs, including: CyberShake,

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Stencil, Gaussian Elimination, Epigenomics. Additionally, the paper features a case study on automotive control systems, where applications such as Adaptive Cruise Control (ACC), Traction Control (TC), and Electric Power Steering (EPS) are modeled as DAGs. In these models, tasks and their dependencies are represented as vertices and edges of the DAGs, respectively. The paper focuses on optimizing the scheduling of these DAGs on a distributed heterogeneous system to minimize energy consumption while ensuring that all tasks meet their real-time deadlines.

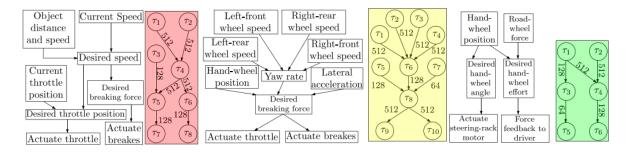


Figure 2.4: Representation of real-time applications as DAGs [17].

The [18] specifically considers a single periodic non-preemptive DAG running on a homogeneous multiprocessor platform. This setup is common in many real-time systems where tasks recur periodically and must be completed within specific time constraints. The non-preemptive nature means that once a task starts executing on a processor, it cannot be interrupted until it finishes. This is crucial in real-time systems to avoid overheads associated with task switching and to ensure predictability in task execution times.

In context of autonomous driving systems, [19] the real-time system represented as a Directed Acyclic Graph (DAG) is the Autoware framework, specifically a module related to the localization package used in autonomous driving systems. The paper models the Normal Distributions Transform (NDT) algorithm within Autoware as a DAG, showcasing different implementations of this algorithm on various processing engines, such as CPUs and GPUs, within a heterogeneous computing platform. The NDT algorithm is used to compute the precise position of an autonomous vehicle by matching Lidar data with offline map data. This DAG-based representation helps in scheduling tasks on a heterogeneous platform, ensuring real-time performance and efficient resource utilization.

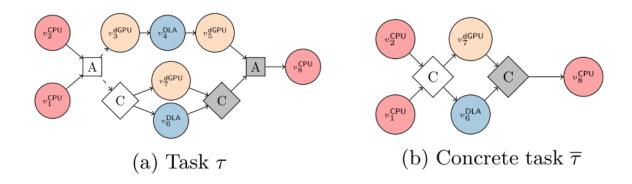


Figure 2.5: Task specification and concrete tasks [19].

The application of DAGs extends to OpenMP framework as well. In [20] the authors represent OpenMP tasks as Directed Acyclic Graphs (DAGs) to model the parallel execution structure. In this model, each task in OpenMP is represented as a vertex within the DAG. These tasks can be either implicit tasks, generated by constructs like omp parallel for or omp sections, or explicit tasks created by the omp task directive. Dependencies between tasks, such as those created by synchronization constructs like taskwait or depend clauses, are represented by edges in the DAG. These edges dictate the order in which tasks must be executed, ensuring that dependent tasks wait for their predecessors to complete. The DAG also incorporates execution constraints inherent in OpenMP. For example, the Thread Assignment (TA) constraint ensures that the number of threads assigned to a parallel region does not exceed what is specified in the OpenMP directive. Similarly, the Parallel-Region Execution (PRE) constraint ensures that once threads are assigned to a parallel region, only those threads can execute the tasks within that region. This structured representation allows for the analysis of critical properties like the longest path in terms of execution time (F-length) and total workload (F-volume), which are used to derive response time bounds for scheduling.

As per the above research, DAGs are instrumental in enhancing the understanding, optimization, and scheduling of real-time applications across various domains. This justifies my decision to implement DAGs in my project, leveraging their ability to represent complex task dependencies and ensure efficient, real-time performance.

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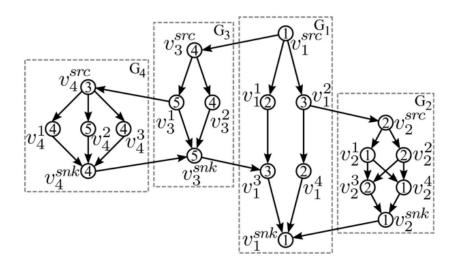


Figure 2.6: An example OpenMP DAG G (the label of each vertex is the worst-case execution time) [20].

# 2.3 Task Scheduling Algorithms in Heterogeneous CPU-GPU Systems

The realm of task scheduling in cloud and distributed computing environments has seen various innovative approaches aimed at optimizing energy efficiency, cost, and resource utilization, particularly in heterogeneous systems. The paper [21] presents an advanced scheduling method that prioritizes energy efficiency in a distributed green cloud (DGC) environment. It addresses the dynamic nature of power availability and costs across different geographical regions. By formulating the task scheduling as a constrained optimization problem, the study employs a novel Simulated-Annealing-Based Bees Algorithm (SBA) to intelligently allocate tasks among multiple green clouds. This method not only minimizes energy costs but also ensures that tasks meet their real-time deadlines by optimizing server allocation and operational speeds. However, the approach assumes homogeneity within data centers, which might not reflect the reality of mixed hardware environments, potentially leading to suboptimal scheduling decisions.

In a similar vein, the paper [22] introduces the Cost-Efficient Task Scheduling Strategy (CETSS), which focuses on managing workflow tasks in cloud environments with

strict deadline constraints. By modeling tasks as Directed Acyclic Graphs (DDAGs) and employing a critical path method, CETSS dynamically adjusts task deadlines and leverages a greedy algorithm to minimize execution costs. The strategy also reallocates tasks to maximize cost efficiency by optimizing VM usage. Despite its effectiveness, CETSS faces challenges in highly dynamic cloud environments where fluctuating resource availability and pricing can undermine its cost-saving strategies. Moreover, the complexity of handling heterogeneous resources and the reliance on accurate predictions for deadlines and power management introduce potential inefficiencies.

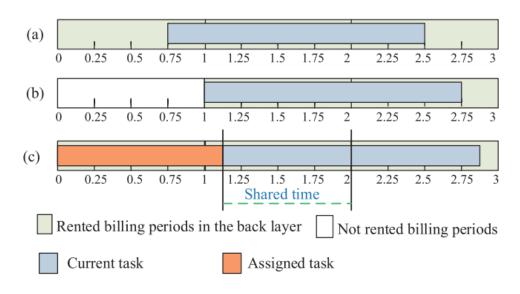


Figure 2.7: Example of task execution cost for a virtual machine [22]

The focus shifts to real-time parallel task scheduling on GPUs in paper [23], which proposes the RTGPU framework. This framework employs federated scheduling to allocate specific Streaming Multiprocessors (SMs) to tasks, ensuring predictable execution and preventing preemption. By using persistent threads and fine-grain GPU partitioning, RTGPU optimizes resource utilization and improves system throughput, particularly in scenarios where real-time deadlines are critical. However, the framework introduces complexities in managing the interdependencies between CPU, memory, and GPU segments, especially under high workloads. The non-preemptive nature of certain operations and the overhead of persistent thread management can further complicate the scheduling process, potentially leading to inefficiencies and underutilization of GPU resources.

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In this [24], the authors explore the dynamic variability of CPU and GPU utilization in task scheduling, proposing a hybrid algorithm (H-PSO) that combines a heuristic greedy strategy with Particle Swarm Optimization. This approach aims to enhance both energy efficiency and resource utilization in heterogeneous systems. While the H-PSO algorithm shows significant improvements, it also comes with increased computational overhead and complexity, making it less suitable for real-time or latency-sensitive applications. Additionally, the reliance on specific models for energy consumption and CPU-GPU utilization may limit the algorithm's applicability across different hardware configurations and emerging computing technologies.

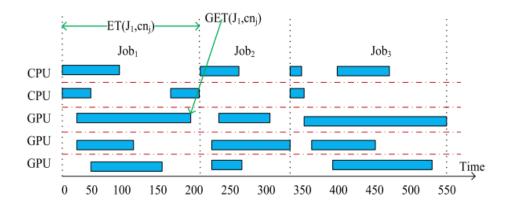


Figure 2.8: Computing node job execution [24].

In summary, real-time task scheduling in heterogeneous multicore systems, particularly those involving CPU-GPU architectures, is a complex challenge that requires balancing multiple factors such as energy efficiency, resource utilization, and meeting strict deadlines. While various algorithms have been proposed to address these challenges, each comes with its trade-offs, particularly in terms of computational complexity and the ability to adapt to diverse and dynamic computing environments. As these systems continue to evolve, future research will need to focus on developing more adaptable and efficient scheduling strategies that can operate effectively across a wider range of hardware configurations and application scenarios.

#### 2.4 Power and Energy Optimization

In [8], the authors explore the use of task versions to optimize task deployment on heterogeneous multicore platforms whereas [6]. Task versions allow the system to adapt to

2.5 Jetson Nano

varying resource availability and constraints, such as energy consumption and real-time execution requirements. The approach involves modeling tasks using an imprecise computation (IC) task model, where each task is decomposed into a mandatory subtask that must meet real-time constraints and an optional subtask that can be executed to improve the quality of service (QoS) if resources allow. By utilizing dynamic voltage and frequency scaling (DVFS) [25], the system adjusts the power factor by selecting appropriate voltage/frequency levels, enabling energy-efficient task execution while meeting QoS demands. The deployment method simultaneously optimizes task allocation, scheduling, frequency assignment, and task migration, allowing for more flexible and efficient use of heterogeneous cores.

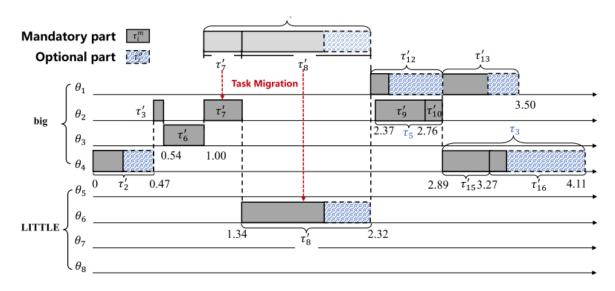


Figure 2.9: Task deployment results [8].

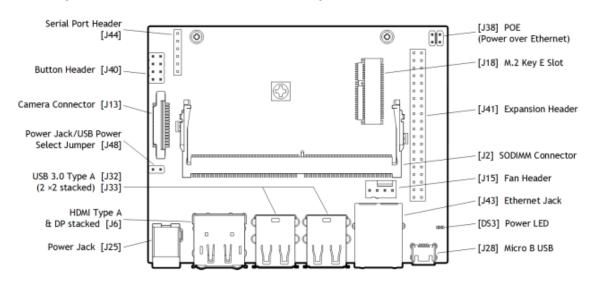
#### 2.5 Jetson Nano

The Jetson Nano is a compact AI computing platform featuring a 128-core NVIDIA Maxwell GPU with 472 GFLOPS of AI performance and a quad-core ARM Cortex-A57 CPU with a maximum frequency of 1.43GHz. It includes 4GB of 64-bit LPDDR4 memory with 25.6GB/s bandwidth and 16GB of eMMC 5.1 storage. [7] The Nano supports video encoding and decoding up to 4K resolution, connects up to four cameras via 12 MIPI CSI-2 lanes, and offers a variety of I/O options including PCIe Gen2, USB 3.0, and Gigabit Ethernet. It operates within a power range of 5W to 10W and is housed in a

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69.6mm x 45mm form factor with a 260-pin SO-DIMM connector.

#### Developer kit carrier boards: rev A02 top view



#### Developer kit module and carrier board: rev B01 top view

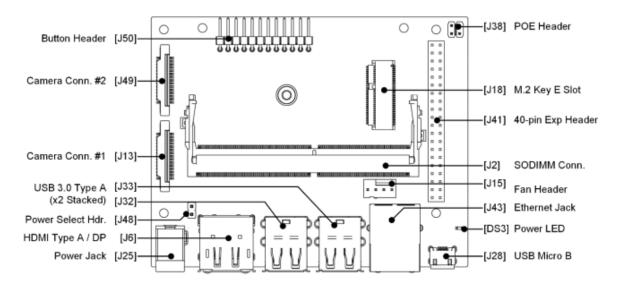


Figure 2.10: Jetson nano [26].

The NVIDIA Jetson Nano offers several advantages, particularly for developers looking to bring AI capabilities to edge devices. [26] It combines high performance with low power consumption, making it ideal for advanced robotics, IoT, and other autonomous applications. The Jetson Nano features a 128-core NVIDIA Maxwell GPU capable of 472 GFLOPS, providing substantial computational power for AI tasks. It

2.5 Jetson Nano

supports multiple camera inputs, making it suitable for vision-based applications. Additionally, it is part of the broader NVIDIA Jetson ecosystem, ensuring compatibility with a wide range of software tools like TensorRT, CUDA, and OpenCV [27]. The platform's compact size and cost-effective pricing further enhance its appeal, especially for projects requiring scalable, deployable AI solutions at the edge.

The Jetson Nano, with its quad-core ARM Cortex-A57 CPU and 128-core NVIDIA Maxwell GPU, offers a compact yet powerful platform for developers. Its ability to handle AI workloads with 472 GFLOPS of performance makes it ideal for testing and observing task scheduling algorithms in real-time. The built-in GPU accelerates complex computations, while the multi-core CPU ensures efficient processing of multiple tasks. This combination, along with its low power consumption and support for various interfaces, makes the Jetson Nano a versatile and accessible tool for developers to prototype and optimize their algorithms effectively.

# Methodology

The method used to accomplish the goals of this project involves a structured approach, beginning with the division of research into distinct groups to focus on specific tasks. The first crucial step was establishing the design specifications, which are essential for defining the objectives, methods, and inputs needed before starting any task. Following this, a basic architecture of the design flow was developed, represented as a block diagram with smaller components, allowing for a clear, step-by-step implementation process. The next step was designing the algorithm, which included writing the necessary code to ensure the research objectives were met. Finally, the project concluded with the simulation and implementation of the algorithm to achieve the desired outcomes.

## 3.1 Design specification

The first step is to thoroughly understand where and how to implement the design. The system used for writing, simulating, and checking results was <code>cseelab758.essex.ac.uk</code>, which has a 12th Gen Intel Core i7-12700 processor running at 2.10GHz, 16GB of RAM, and operates on a 64-bit Windows 11 Education (version 23H2) Operating System.

The algorithm is developed in Python, a language renowned for its simplicity, readability, and versatility, making it an ideal choice for both beginners and experienced developers. Python's extensive libraries such as NumPy, Pandas, and NetworkX, offer powerful tools for handling complex tasks like data analysis, machine learning,

3.2 Architecture 25

and task scheduling [28]. The Jupyter Notebook is used as the the programming environment due to its interactive nature, which allows for the integration of live code, equations, visualizations, and narrative text into a single, coherent document [29]. This combination of Python and Jupyter Notebook provides a flexible and efficient environment for developing data-driven projects.

To design the algorithm, several key Python libraries were used. NumPy handled numerical computations, and Pandas managed and analyzed data in structured formats. Defaultdict from collections simplified dictionary operations with default values, while combinations from itertools generated task combinations. NetworkX was crucial for creating and analyzing task dependency graphs (DAGs). Matplotlib.pyplot and matplotlib.patches provided tools for visualizing data and adding graphical elements. Dequing managed efficient data structures for queue operations, Pprint made data structures more readable, and json and pickle enabled data serialization and storage. Each library played a vital role in building a flexible and efficient algorithm [30].

To perform the implementations, the NVIDIA Jetson Nnao was used as the core processing unit due to its capability to handle high-performance, real-time AI and machine learning task, such as object detection and image processing, in a compact and cost-effective manner [31]. Despite its small size and limited processing threads, the Jetson Nano efficiently runs critical algorithms like the SSD (Single Shot Multibox Detector) for managing flow and detecting violations. Its power-efficient design makes it ideal for implementing a smart traffic control system in resource-constrained environments.

#### 3.2 Architecture

At the heart of the system are the initial inputs, which includes Directed Acyclic Graph (DAG) representing the real-time applications that maps out the dependencies between tasks, as well as critical parameters like the deadline, power factor, and the number of processing cores available. These inputs are crucial in shaping the scheduling strategy, particularly in environments like the NVIDIA Jetson Nano, where tasks must be allocated efficiently between CPU and GPU cores. The DAG ensures that tasks are executed in an order that respects their dependencies, which are essential for maintain the

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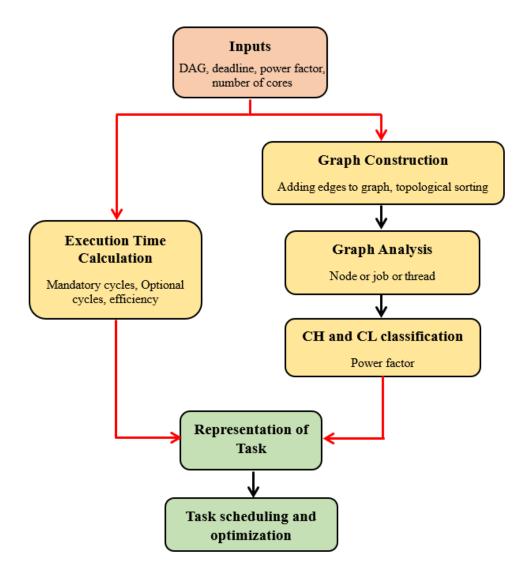


Figure 3.1: Architecture of the design

real-time requirements of the system. Also, considering power and deadlines ensures that the system not only meets the timing constraints but also operates within its power budget. Using these as inputs execution time and graphs are analysed.

In the Graph Construction phase, this involves adding edges to the DAG to represent task dependencies and performing topological sorting to determine the correct execution order of tasks. Topological sorting is a critical step as it organizes tasks in a sequence that ensures all dependencies are respected also, no task can be executed before all its prerequisites are completed. This phase is particularly important in heterogeneous systems, where tasks must be carefully scheduled across different types of processing units (CPU and GPU). The output of this phase directly influences the subsequent steps, as it determines the execution order that will be used for further analysis and

3.2 Architecture 27

optimization. The ability to correctly construct and sort the graph is fundamental to the success of the overall scheduling process.

Once the graph is constructed and sorted, the system analyses the DAG to identify task dependencies and opportunities for parallel execution as required. Task are classified into critical high (CH) and critical low (CL) tasks based on their dependencies of tasks. Once they are classified power factors are taken into consideration by analysing versions of each task. This strategic allocation helps in balancing the load across the system, ensuring that tasks are executed efficiently while adhering to the power and timing constraints.

The next block is Execution Time Calculation, where the system calculates the execution times for each task version. This includes considering both mandatory cycles, which are essential for producing a minimally acceptable result, and optional cycles. This stage is crucial for determining whether tasks can be completed within the given deadlines and how much power will be consumed in the process. By calculating the execution times, the system can make informed decisions about which task versions to execute, balancing the need for accuracy with the constraints of time and power. This step directly feeds into the representation of tasks in a matrix, where tasks are organized by their start and finish times, aligned with the available cores.

In the Task Scheduling and Optimization phase, where the system optimizes the schedule of tasks across the available processing cores. The goal is to ensure that all tasks are completed within the specified deadline while minimizing power consumption. The representation of tasks in a matrix form provides a clear visualization of the scheduling process, helping the system to identify the best allocation of tasks to the available cores. The architecture also incorporates feedback loops, which allow the system to iterative refine the schedule by revisiting earlier steps if necessary. For example, if the execution time calculation reveals that a particular task cannot be completed within the deadline, the system might adjust the topological order or reclassify tasks to ensure that the schedule remains feasible.

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#### 3.3 Designing task scheduling algorithm

The algorithm design requires inputs such as essential libraries (3.1), node/job/thread data, deadlines, maximum power factor, fixed cores, and the DAG graph structure. Additionally, it considers which nodes/jobs/threads can be executed in parallel. These inputs collectively enable efficient task scheduling and execution. The schedule is generated by prioritizing tasks based on their As Late As Possible (ALAP) [6] times to ensure that precedence constraints are respected. If the initial schedule exceeds the deadline, the algorithm iterative downgrades the versions of selected tasks—those with the least impact on overall accuracy—until a feasible schedule is obtained.

#### 3.3.1 Defining inputs

In a Directed Acyclic Graph (DAG) representing a real-time application, a single DAG encapsulates the structure of a task. The basic components of this structure are nodes and edges. Nodes, which can represent tasks, operations, threads, jobs, or various applications, are the key entities within the DAG. These nodes are interconnected by edges, also known as arcs, which define the relationships and dependencies between them. The direction of the edges is crucial, as it indicates the flow of execution or the precedence constraints between nodes. In essence, edges signify that one node (task or operation) must be completed before another can commence, establishing a clear sequence of execution. The acyclic nature of the DAG ensures that there are no cycles, meaning there is no way to return to a node once it has been visited, which is vital for accurately modelling task dependencies in real-time systems. DAG can be represented in different structures as shown in 3.2, in this thesis fork-join structure is used.

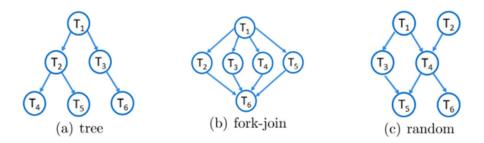


Figure 3.2: DAG Structures examples [5]

Given a set of tasks, each task is represented in a node (Node1, Node2, etc.) as  $T_i$ , each associated with multiple versions  $T_i^j$  of tasks. Each version contains two configurations:  $C_L$  (low configuration) and  $C_H$  (high configuration). These configurations specify parameters like  $M_i$  (mandatory cycles),  $O_i$  (optional cycles),  $Pow_i^j$  (power or energy consumption), and  $Y_i$ , L or  $Y_i$ , H (performance or efficiency metrics under low and high configurations, respectively). For example, Task1 has one version where the low configuration ( $C_L$ ) has  $M_i = 4$ ,  $O_i = 2$ ,  $Pow_i^j = 10$ , and  $Y_i$ , L = 0.5, while the high configuration ( $C_H$ ) increases  $Pow_i^j$  to 13 and  $Y_i$ , H to 0.7. The other tasks have similar versions with different values for these parameters, providing a comprehensive set of possible task configurations across different nodes. Other inputs include a deadline of 142 units, requiring the task to be completed within this time-frame, and a maximum power factor of 50 units, meaning no job should exceed 50 units of power. The number of cores is fixed at two, ensuring that complex tasks are efficiently scheduled.

Table 3.1: Defining Inputs

| Tasks | Versions | CL |    |       | СН   |    |    |       |      |
|-------|----------|----|----|-------|------|----|----|-------|------|
|       |          | Mi | Oi | Pow_i | Yi,L | Mi | Oi | Pow_i | Yi,H |
| Task1 | 1        | 4  | 2  | 10    | 0.5  | 4  | 2  | 13    | 0.7  |
| Task2 | 1        | 10 | 5  | 20    | 0.4  | 10 | 5  | 26    | 0.6  |
|       | 2        | 10 | 8  | 22    | 0.4  | 10 | 8  | 29    | 0.6  |
|       | 3        | 10 | 8  | 24    | 0.4  | 10 | 10 | 30    | 0.6  |
| Task3 | 1        | 10 | 2  | 12    | 0.5  | 10 | 2  | 12    | 0.6  |
|       | 2        | 10 | 4  | 12    | 0.5  | 10 | 4  | 14    | 0.6  |
|       | 3        | 10 | 6  | 15    | 0.4  | 10 | 6  | 17    | 0.6  |
| Task4 | 1        | 28 | 16 | 15    | 0.8  | 28 | 16 | 20    | 0.8  |
|       | 2        | 28 | 20 | 18    | 0.8  | 28 | 20 | 25    | 0.7  |
| Task5 | 1        | 8  | 4  | 24    | 0.5  | 8  | 4  | 28    | 0.7  |
|       | 2        | 8  | 4  | 24    | 0.5  | 8  | 4  | 28    | 0.7  |
|       | 3        | 8  | 5  | 27    | 0.4  | 8  | 5  | 31    | 0.7  |
| Task6 | 1        | 10 | 3  | 12    | 0.7  | 10 | 3  | 12    | 0.7  |
|       | 3        | 10 | 9  | 14    | 0.7  | 10 | 9  | 16    | 0.7  |

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#### 3.3.2 Defining graph and sorting topologically

Once the above parameters are given as input, next is to define a class for constructing and managing DAG with functionalities to add edges, perform a non-recursive topological sort, and identify the successors of specific tasks. For this research task from [6] is taken as shown in 3.3. The graph is populated with tasks (represented as nodes) and their dependencies (represented as directed edges). The topological sort of method is implemented non-recursively, which is beneficial in avoiding the potential hidden recursion, such as stack overflow in cases where the graph is large or has a deep hierarchy. The non-recursive approach uses an explicit stack to manage the nodes, making the algorithm more robust and capable of handling larger graphs without risking the limitations of Python's recursion depth. Additionally, the code identifies parallel tasks and finds their successor tasks within the graph, providing insights into how tasks can be scheduled concurrently. The graph is then visualized using the 'networkx' and 'matplotlib' libraries, with the layout manually adjusted for the clarity.

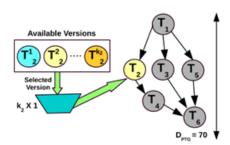


Figure 3.3: Task graph [6]

#### 3.3.3 Execution time calculation

In the context of scheduling and resource management, particularly when working with tasks represented in clock cycles, it's important to convert these cycles into timing in seconds to achieve accurate planning and execution. The inputs and the structure of the task graph are outlined in Sections 3.3.1 and 3.3.2. After defining the task graph, the next crucial step is to calculate the execution times for each task and their respective versions, as these tasks include both mandatory and optional components, represented

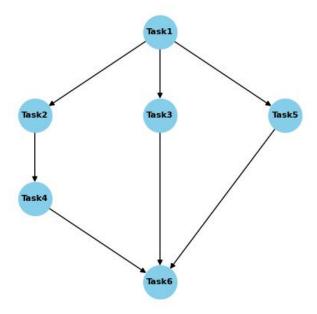


Figure 3.4: Task graph [6]

by clock cycles. The length of the  $j^{th}$  version of task  $T_i$  (len<sub>i</sub>) is expressed as:

$$\operatorname{len}_{i}^{j} = M_{i} + O_{i}^{j}[6] \tag{3.1}$$

This formula calculates the total number of clock cycles required for a specific version of a task, incorporating both its critical (mandatory) and additional (optional) components. Once the length in clock cycles is determined, the execution time in seconds can be calculated for different task configurations, such as critical low ( $C_L$ ) and critical high ( $C_H$ ). The execution time is crucial for understanding how long a task will take to complete under different configurations, which in turn affects how tasks are scheduled within the available resources, ensuring that deadlines are met without exceeding the system's power constraints. For example, the execution time for a critical low task  $T_i$  under a specific version is calculated using the following formula: [6]

Execution time for task 
$$T_i^j, C_L = \frac{\text{len}_i^j}{Y_i^j, L \times 0.5}$$
 (3.2)

Execution time for task 
$$T_i^j, C_H = \frac{\operatorname{len}_i^j}{Y_i^j, H \times 1}$$
 (3.3)

These calculations are vital for determining the exact time required to execute each

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task version, allowing for precise scheduling that considers both the time constraints (deadlines) and the system's power limitations. This approach helps in optimizing the overall performance and ensuring that the system runs efficiently without overloading any resources.

#### 3.3.4 Classification of tasks as critical high and critical low

In task scheduling and optimization, tasks are categorized into two primary groups: Critical High ( $C_H$ ) and Critical Low ( $C_L$ ). This classification hinges on the number of successors a task has within a dependency graph. Tasks with multiple successors are deemed more critical because they significantly influence the execution of subsequent tasks, leading to their classification as  $C_H$ . Conversely, tasks with fewer or no successors are classified as  $C_L$ , as they have a lower impact on the overall sequence of task execution.

After classification, the next critical step is to select the most appropriate versions of these tasks while carefully considering power consumption constraints. Each task version comes with associated power consumption and execution time. Initially, values with the maximum optional parts are considered as the ideal case. But the goal is to choose versions that maximize system performance without exceeding a predefined power consumption limit. When parallel tasks are identified, such as Task5 and Task3 being set as  $C_H$  tasks and Task2 as a  $C_L$  task, a power factor formula is applied to ensure efficient resource use:

$$Pow(T_2^j), C_H + Pow(T_5^j), C_H \le 50$$
 (3.4)

$$Pow(T_2^j), C_H + Pow(T_3^j), C_H \le 50$$
 (3.5)

If the total power consumption exceeds the limit of 50 units, the algorithm adjusts by examining the versions of the  $C_L$  tasks. It downgrades [6] to the next lower version (j-1) and recalculates the power factor. This iterative process continues until the combined power factors of the parallel tasks are within the acceptable range. The

outcome is an optimized task schedule where critical tasks are executed with maximum efficiency, and less critical tasks are adjusted to ensure that the system operates within its power and resource constraints. This balanced approach is vital in systems where both performance and power consumption are tightly controlled, ensuring tasks are completed within required timeframes without overloading the system's resources.

#### 3.3.5 Representing tasks as matrix

In the initial stage of the project, parallel tasks assigned to Critical Low ( $C_L$ ) and Critical High ( $C_H$ ) categories, after considering power constraints, are stored in a matrix format. The matrix is structured with the number of columns equal to the number of levels in the Directed Acyclic Graph (DAG), and the number of rows corresponding to the number of available cores—in this case, two cores.

To populate this matrix, the topological sort of the tasks is considered. The tasks are processed sequentially from the topological list, where each element represents a task number. If a task is scheduled under the  $C_L$  category, the 'count-cl' variable tracks its position, and the task is placed in the corresponding row in the matrix. Similarly, if a task is scheduled under  $C_H$ , it is tracked by the 'count-ch' variable and placed in the respective row. If no task is scheduled for a particular level, the matrix column for that level is left as 'None'. For example, consider a scenario where tasks 2, 3, and 5 are running in parallel, and the DAG has 4 levels. Based on the topological sorting and the classification from the earlier section, the matrix looks as follows:

$$\begin{bmatrix} \text{None} & \text{Task } T_5^j & \text{Task } T_3^j & \text{None} \\ \text{None} & \text{Task } T_2^j & \text{None} & \text{None} \end{bmatrix}$$

In this matrix, Task5 and Task3 are allocated under the  $C_L$  row, while Task2 is allocated under the  $C_H$  row. The other values remain as 'None' since no tasks are assigned to those levels. This matrix provides a clear and structured representation of how tasks are distributed across cores and levels, reflecting the scheduling decisions based on criticality and power considerations.

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To allocate the remaining tasks after the initial assignment, the process involves checking columns in the matrix that currently have 'None' values, which indicate unassigned tasks, and then focusing on their corresponding levels. For instance, if levels 1 and 4 have unassigned tasks, the tasks associated with these levels need to be identified and assigned to the appropriate columns (level 1 and level 4).

When determining which row (representing a core) to assign these tasks to, the decision is based on the execution times of the tasks, considering both the mandatory and optional parts, regardless of whether the task is classified as Critical Low ( $C_L$ ) or Critical High ( $C_H$ ). The approach involves calculating the total execution time for the tasks already assigned in each row by summing the execution times in that row. Next, compare the summed execution times across the rows to identify the row with the maximum total execution time. This total is then subtracted from the overall deadline to determine the remaining available time for scheduling the unassigned tasks. For example, consider the following matrix:

$$\begin{bmatrix} \text{None} & \text{Task } T_5^j = 50 & \text{Task } T_3^j = 20 & \text{None} \\ \text{None} & \text{Task } T_2^j = 30 & \text{None} & \text{None} \end{bmatrix}$$

Task 
$$T_5^j(50) + T_3^j(20) = 70 > T_2^j(30)$$

Therefore, Deadline -70 = remaining deadline

Since 70 units is greater than 30 units, the row with the maximum execution time (row 1) is used to calculate the remaining deadline by subtracting 70 from the initial deadline. The remaining tasks in levels 1 and 4 are then considered for assignment to the row that allows their combined execution times to fit within the remaining available time, ensuring that the system remains within its operational constraints. This approach ensures an efficient and balanced distribution of tasks across the available cores while respecting the overall deadline.

Now, the algorithm checks for the remaining tasks and their respective level. A task is placed in the column which is equal to the level, and the row is decided based on the free space available ('None'). If the task is placed below another task, for example, if

3.4 Pseudo code

 $Task_i^j$  is placed below  $Task_3^j$ , the power factor is calculated as explained above.

If a task is placed below another task in the same column (for instance, if  $Task_i^j$  is placed below  $Task_3^j$ ), the algorithm recalculates the power factor, as previously described. This ensures that the combined power consumption of the tasks in the same column does not exceed the predefined power limit. The algorithm continues this process of placing tasks and recalculating power factors until all tasks are assigned appropriately, ensuring that the system remains within its operational constraints and the tasks are efficiently distributed across the available cores.

This is how the scheduled tasks are organized and displayed in a matrix format for further analysis and representation. The matrix structure provides a clear and systematic way to visualize how tasks are allocated across different levels and cores, ensuring that all scheduling constraints, such as power factors and execution times, are met. Outputs are shown in the results section, where they provide a detailed overview of the scheduling outcomes, including how effectively the system meets its deadlines and resource limitations. This representation not only facilitates easy tracking of task distribution but also helps in identifying potential bottlenecks or inefficiencies, ensuring that tasks are efficiently managed and system resources are fully optimized.

#### 3.4 Pseudo code

This section presents the pseudocode for task scheduling in heterogeneous multicore real-time systems modeled as Directed Acyclic Graphs (DAGs). In such systems, tasks must be efficiently managed to ensure they meet strict deadlines while operating within constraints like power consumption and core availability. The pseudocode outlines the key steps required to organize and execute tasks across multiple cores, considering the specific characteristics and requirements of each task version. This approach aims to optimize system performance and guarantee that all tasks are completed within the designated timeframe.

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#### Algorithm 1 Task Scheduling Algorithm

```
1: Inputs:
```

- 2: SET DAG, Deadline D=142, Pow<sub>max</sub> = 50, Cores C=2
- 3: DEFINE tasks with  $M_i$ ,  $O_i^j$ , Pow<sub>i</sub>,  $Y_{i,L}$ ,  $Y_{i,H}$
- 4: Topological Sort:
- 5: INITIALIZE T<sub>sorted</sub>
- FOR each task  $T_i$ :
- 7: IF no predecessors:
- ADD  $T_i$  to  $T_{\text{sorted}}$ 8:
- 9: FOR each successor  $T_s$ :
- 10: DECREASE in-degree of  $T_s$
- 11: IF in-degree is 0, ADD to  $T_{\text{sorted}}$
- 12: OUTPUT  $T_{\text{sorted}}$
- 13: **Classify Tasks:**
- FOR each task  $T_i$  in  $T_{\text{sorted}}$ : 14:
- IF successors > 1, CLASSIFY as  $C_H$ 15:
- ELSE, CLASSIFY as  $C_L$ 16:
- 17: Calculate Execution Times:
- FOR each  $T_i^j$ : 18:
- SET Exec\_Time  $C_L = \frac{M_i + O_i^j}{Y_{i,L} \times 0.5}$ SET Exec\_Time  $C_H = \frac{M_i + O_i^j}{Y_{i,H}}$ 19:
- 20:
- 21: Assign to Matrix:
- 22: INITIALIZE M[2][L]
- FOR each task  $T_i$  in  $T_{\text{sorted}}$ : 23:
- IF  $C_L$ , ASSIGN to  $M[0][\mathsf{count}_{C_L}]$ 24:
- IF  $C_H$ , ASSIGN to  $M[1][count_{C_H}]$ 25:
- **Check Power Constraints:** 26:
- FOR each pair  $(T_{i1}^j, T_{i2}^j)$  in M: 27:
- 28: IF Pow\_combined > Pow<sub>max</sub>, DOWNGRADE  $C_L$  version
- 29: **Schedule Tasks:**
- 30: FOR each  $T_i$  in M:
- SET  $t_s = 0$  if first, ELSE  $t_s =$  predecessor finish time 31:
- SET  $t_f = t_s + \text{Exec\_Time}$ 32:
- 33: **Output:**
- 34: VALIDATE all tasks meet D and Pow<sub>max</sub>
- PRINT final schedule 35:

#### **Results and Observations**

## 4.1 Task Scheduling Ideal case vs. Actual case

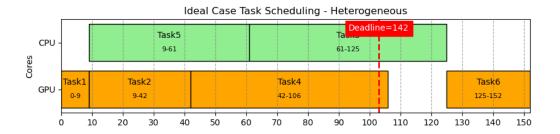


Figure 4.1: Ideal case task scheduling

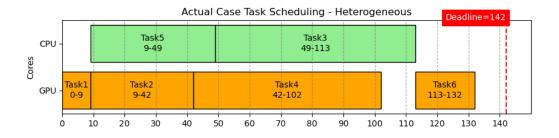


Figure 4.2: Actual case task scheduling

In an ideal scenario as shown in 4.1 where the maximum optional cycles are considered for each task, it is observed that the deadline is not met even with 2 cores, and scheduling tasks remains challenging despite topological sorting. However, by employing an algorithm that schedules tasks based on dependencies and power optimization,

it is possible to successfully schedule tasks within the given deadline using just 2 cores which is shown in 4.2. This demonstrates that, with efficient processor utilization and power optimization, tasks can be effectively scheduled even with a minimal number of processors.

#### 4.1.1 Task Scheduling in Homogeneous system

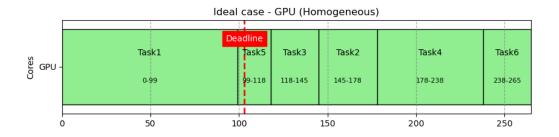


Figure 4.3: Ideal case GPU

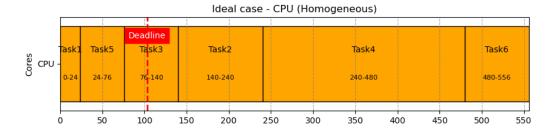


Figure 4.4: Ideal case GPU

The figures 4.4 and 4.3 clearly demonstrate that scheduling tasks within the minimum deadline is virtually impossible. While it is feasible to schedule these tasks in homogeneous systems, this requires extending the deadline. However, increasing the deadline entails prolonging both the mandatory and optional cycle times, which ultimately leads to a reduction in overall efficiency.

# 4.2 System Utilization in Homogeneous vs. Heterogeneous Systems

The first two charts represent ideal scenarios where either the CPU or GPU as shown in 4.5 is fully utilized without any idle capacity, likely pushing the system to its limits.

In contrast, the third chart illustrates a more practical heterogeneous scenario where both CPU and GPU are used together, leaving some idle capacity, which suggests a more balanced and potentially more efficient system. This comparison highlights the difference between theoretical maximum utilization and actual resource usage in a combined CPU-GPU setup.

In the actual case, the utilization of both the GPU and CPU is calculated separately by summing the execution times (ET) of all tasks for each processor and dividing by the system's deadline. The total system utilization is then determined by averaging the utilization of the GPU and CPU, and multiplying by 100 to express it as a percentage. This calculation provides a measure of how effectively the entire system's resources are being utilized within the given deadline.

Utilization of GPU = 
$$\frac{\sum ET_i^j}{Deadline}$$

Utilization of CPU = 
$$\frac{\sum ET_i^j}{\text{Deadline}}$$

$$\mbox{Total utilization} = \frac{(\mbox{Utilization of GPU} + \mbox{Utilization of CPU})}{2} \times 100$$

In ideal homogeneous systems, where tasks are scheduled exclusively on either the CPU or GPU, the utilization can exceed 100%. This over utilization indicates that the system is being pushed beyond its optimal capacity, which is not a desirable or efficient solution. It highlights the limitations of relying solely on one type of processor, as it can lead to performance degradation and potential system instability.

#### 4.3 Power Optimization and Consumption

In the ideal case, where the maximum optional parts of each version of the tasks are considered, we observe a significant issue when multiple tasks are running in parallel:

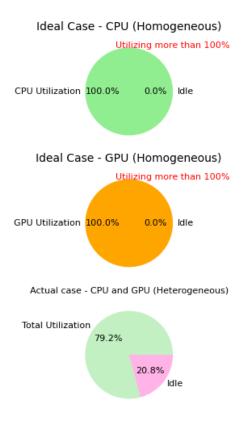


Figure 4.5: Utilization

the power consumption exceeds the defined maximum power limit. This situation, as illustrated in the graph, indicates that the combined power demands of certain task groupings, such as "Task2 + Task5," surpass the threshold of 50 units shown in 4.8. When power consumption exceeds this limit, it suggests that the system is operating inefficiently, consuming excessive energy, which could lead to overheating, reduced system lifespan, or failure to meet energy compliance standards. This is clearly not an optimal scenario for power management.

In contrast, the actual case employs an optimized approach where the algorithm carefully selects task versions, considering both their mandatory and optional parts, to ensure that power consumption remains within or at the maximum allowable limit 4.9. By strategically managing the task executions and choosing versions with lower power demands, the algorithm effectively reduces the overall power consumption. This

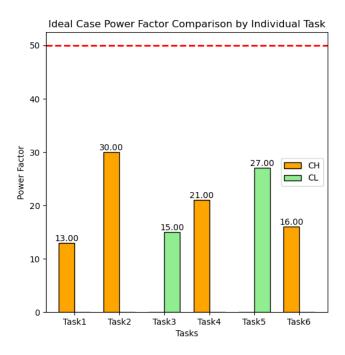


Figure 4.6: Ideal case power comparison by individual task

optimization is critical because it allows the system to run efficiently without exceeding power limits, which is crucial for maintaining system stability, preventing overheating, and ensuring the system's longevity.

The success of this optimization highlights the effectiveness of the algorithm used in this project. It demonstrates that, by intelligently scheduling tasks and selecting appropriate versions, it is possible to maintain a balance between performance and power consumption. The algorithm not only ensures that all tasks are completed within the given constraints but also optimizes power usage, making it a robust solution for managing complex, power-sensitive systems.

This optimized approach is particularly beneficial in environments where power resources are limited or where energy efficiency is a priority. By ensuring that the power consumption does not exceed the maximum limit, the algorithm contributes to a more sustainable and cost-effective operation. It reduces the risk of system failures due to power overloads and contributes to the overall reliability and efficiency of the system. This careful balance between task scheduling and power management is a key achievement of the project, demonstrating how advanced algorithms can be used to

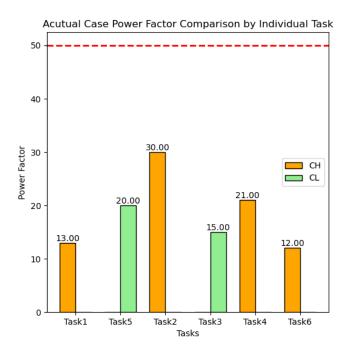


Figure 4.7: Actual case power comparison by individual task address real-world challenges in system design and operation.

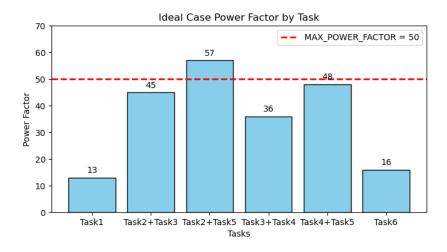


Figure 4.8: Ideal case power by task

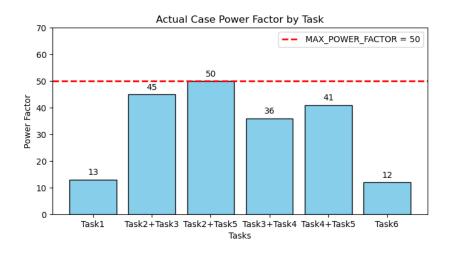


Figure 4.9: Actual case power by task

#### 4.4 Accuracy Analysis

Accuracy in this project is quantified by the metric NQ, where NQ is defined as the ratio of the sum of Actual Quality of Service (QoS) to the sum of Ideal Quality of Service (QoS). The equation:

$$NQ = \frac{\sum \text{Actual QoS}}{\sum \text{Ideal QoS}} = \frac{\sum \text{Actual Oi}}{\sum \text{Ideal Oi}}$$

[<del>6</del>]

serves as a critical measure for evaluating the Quality of Service (QoS) in the context of task scheduling and execution within a system. QoS is essentially a measure of the system's performance, specifically focusing on how well tasks adhere to their expected performance targets, such as meeting deadlines and achieving optimal execution efficiency. The "Actual QoS" refers to the performance level that is actually achieved by the system during execution, taking into account the sum of optional cycles (Oi) that were successfully executed for each task. In contrast, the "Ideal QoS" represents the theoretical best-case scenario, where all possible optional cycles are executed without any limitations. The ratio  $\frac{\sum Actual QoS}{\sum Ideal QoS}$  thus provides a comparison of the system's real-world performance against this ideal scenario. Similarly, the equation can be interpreted in terms of optional instructions or cycles, where "Actual Oi" refers to the sum of optional

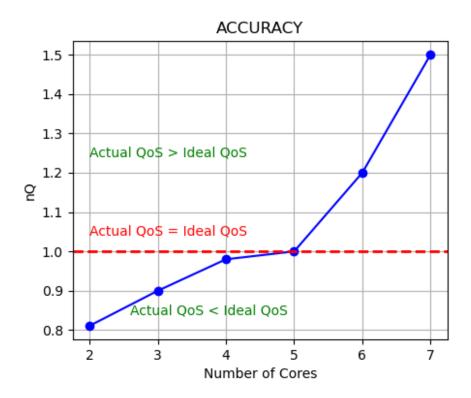


Figure 4.10: Accuracy

instructions that were executed, and "Ideal Oi" refers to the total possible optional instructions that could have been executed under optimal conditions. This metric, NQ, effectively captures the efficiency and effectiveness of the task scheduling algorithm by comparing actual performance to the ideal, thereby identifying how closely the system operates to its maximum potential.

In this project, NQ is calculated as:

$$NQ = \frac{\sum \text{Actual Oi}}{\sum \text{Ideal Oi}} = \frac{2+10+6+2+20+3}{2+10+6+20+5+9} \times 100 = 81.1\%$$

In addition to defining NQ, a graph plotting NQ versus the number of cores is created to further analyze system performance. This graph illustrates that as the number of cores increases, the system's availability also rises, allowing for better scheduling of tasks, particularly parallel tasks, with their maximum optional cycles. [17] The increase in the number of cores provides more computational resources, thereby enabling the system to more closely match the Ideal QoS. As the number of cores grows, the Actual

45

QoS approaches the Ideal QoS, indicating that the system is able to handle tasks more efficiently and effectively, especially under parallel execution conditions. This behavior demonstrates that with sufficient cores, the system can optimize the execution of tasks to their full potential, minimizing the gap between actual and ideal performance and thereby improving overall system accuracy.

#### **Conclusions**

Overall, the project successfully achieved its primary goal of developing a task scheduling algorithm for heterogeneous multicore systems, specifically targeting CPU-GPU real-time environments. The algorithm effectively scheduled tasks based on their dependencies, ensuring real-time performance while optimizing power consumption. Critical high tasks were efficiently managed on the GPU, while critical low tasks were allocated to the CPU, demonstrating a well-balanced approach to resource utilization. The implementation on the NVIDIA Jetson Nano provided a practical platform for testing, with the system maintaining power levels within acceptable limits and achieving an 80 percentage near-quality (nq) threshold. With lessons learned in time management and a deeper understanding of heterogeneous systems, future work could further refine and expand the capabilities of this scheduling algorithm.

#### 5.1 Future work

Future work should address the limitations encountered in scaling the scheduling algorithm for larger and more complex real-world applications. Enhancing the algorithm's ability to efficiently manage multiple sets of tasks with numerous nodes and varying versions is critical. This could involve refining the algorithm to reduce computational load and increase efficiency, particularly when dealing with large-scale data and multiple cores.

5.1 Future work

In addition, integrating AI and machine learning techniques could provide significant improvements in real-time adaptability and performance optimization. These technologies could help the algorithm predict task behaviors, manage continuous data streams more effectively, and adjust scheduling dynamically to meet varying demands.

Further, the current data management approach, which relies on Python and basic programming techniques, may not suffice for handling extensive data sets common in practical applications. Future efforts should explore more advanced data processing tools and real-time analysis techniques to ensure that the system can maintain high performance even under more demanding conditions.

By addressing these areas, the scheduling algorithm can be made more robust, scalable, and adaptable, making it suitable for a wider range of complex, real-world heterogeneous computing environments.

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## **Python Program for Task Scheduling**

```
import numpy as np
2 import pandas as pd
from collections import defaultdict
4 from itertools import combinations
5 import networkx as nx
6 import matplotlib.pyplot as plt
import matplotlib.patches as patches
8 from collections import deque
9 import pprint
10 import json
11 import pickle
13 # INPUT SECTION - Task data including versions and their attributes for
     multiple tasks
 tasks_data = {
     'Task1': {
         'Versions': [
              {'CL': {'Mi': 4, 'Oi': 2, 'Pow_i': 10, 'Yi,L': 0.5}, 'CH': {'Mi
     ': 4, 'Oi': 2, 'Pow_i': 13, 'Yi, H': 0.7}},
      },
19
     'Task2': {
```

```
'Versions': [
              {'CL': {'Mi': 10, 'Oi': 5, 'Pow_i': 20, 'Yi,L': 0.4}, 'CH': {'
22
     Mi': 10, 'Oi': 5, 'Pow_i': 26, 'Yi, H': 0.6}},
              {'CL': {'Mi': 10, 'Oi': 8, 'Pow_i': 22, 'Yi,L': 0.4}, 'CH': {'
23
     Mi': 10, 'Oi': 8, 'Pow_i': 29, 'Yi, H': 0.6}},
              {'CL': {'Mi': 10, 'Oi': 10, 'Pow_i': 24, 'Yi,L': 0.4}, 'CH': {'
24
     Mi': 10, 'Oi': 10, 'Pow_i': 30, 'Yi, H': 0.6}},
        1
25
      },
26
      'Task3': {
27
         'Versions': [
              {'CL': {'Mi': 10, 'Oi': 2, 'Pow_i': 10, 'Yi,L': 0.5}, 'CH': {'
29
     Mi': 10, 'Oi': 2, 'Pow_i': 12, 'Yi, H': 0.6}},
              {'CL': {'Mi': 10, 'Oi': 4, 'Pow_i': 12, 'Yi,L': 0.5}, 'CH': {'
30
     Mi': 10, 'Oi': 4, 'Pow_i': 14, 'Yi, H': 0.6}},
              {'CL': {'Mi': 10, 'Oi': 6, 'Pow_i': 15, 'Yi,L': 0.5}, 'CH': {'
     Mi': 10, 'Oi': 6, 'Pow i': 17, 'Yi, H': 0.6}},
      1
32
      },
33
      'Task4': {
34
         'Versions': [
              {'CL': {'Mi': 28, 'Oi': 16, 'Pow_i': 15, 'Yi,L': 0.4}, 'CH': {'
36
     Mi': 28, 'Oi': 16, 'Pow_i': 18, 'Yi, H': 0.8}},
              ('CL': {'Mi': 28, 'Oi': 20, 'Pow_i': 18, 'Yi,L': 0.4}, 'CH': {'
37
     Mi': 28, 'Oi': 20, 'Pow_i': 21, 'Yi, H': 0.8}},
39
      },
      'Task5': {
40
         'Versions': [
             {'CL': {'Mi': 8, 'Oi': 2, 'Pow_i': 20, 'Yi,L': 0.5}, 'CH': {'Mi
42
     ': 8, 'Oi': 2, 'Pow_i': 25, 'Yi,H': 0.7}},
              {'CL': {'Mi': 8, 'Oi': 4, 'Pow_i': 24, 'Yi,L': 0.5}, 'CH': {'Mi
43
     ': 8, 'Oi': 4, 'Pow_i': 28, 'Yi, H': 0.7}},
             {'CL': {'Mi': 8, 'Oi': 5, 'Pow_i': 27, 'Yi,L': 0.5}, 'CH': {'Mi
     ': 8, 'Oi': 5, 'Pow_i': 31, 'Yi, H': 0.7}},
45
      },
46
      'Task6': {
47
         'Versions': [
48
```

```
{'CL': {'Mi': 10, 'Oi': 3, 'Pow_i': 10, 'Yi,L': 0.5}, 'CH': {'
     Mi': 10, 'Oi': 3, 'Pow_i': 12, 'Yi, H': 0.7}},
              {'CL': {'Mi': 10, 'Oi': 6, 'Pow_i': 12, 'Yi,L': 0.5}, 'CH': {'
50
     Mi': 10, 'Oi': 6, 'Pow_i': 14, 'Yi, H': 0.7}},
              {'CL': {'Mi': 10, 'Oi': 9, 'Pow_i': 14, 'Yi,L': 0.5}, 'CH': {'
     Mi': 10, 'Oi': 9, 'Pow_i': 16, 'Yi, H': 0.7}},
      }
53
56 # Constants
57 Deadline = 142 # Deadline for completing the tasks
Number_of_types = 2 # Number of types (CL, CH)
59 types = ['CL', 'CH'] # Labels for types
60 MAX_POWER_FACTOR = 50 # Maximum allowed sum of power factors for task
     combinations
61
 # GRAPH AND TOPOLOGICAL SORT
63
 # Class representing a directed graph using adjacency list
 class Graph:
     def __init__(self, vertices):
66
          self.graph = defaultdict(list) # Dictionary containing adjacency
67
     lists
          self.V = vertices # Number of vertices
     def addEdge(self, u, v):
70
          # Add an edge from vertex u to vertex v
          self.graph[u].append(v)
73
     def neighbor_gen(self, v):
74
          # Generate neighbors of vertex v
75
          for k in self.graph[v]:
76
              yield k
78
     def nonRecursiveTopologicalSortUtil(self, v, visited, stack):
          # Non-recursive function to perform topological sort
80
          working_stack = [(v, self.neighbor_gen(v))] # Initialize stack
81
     with current node
```

```
while working_stack:
83
              v, gen = working_stack.pop() # Pop the vertex and generator
84
      from stack
              visited[v] = True # Mark the current node as visited
85
               for next_neighbor in gen: # Iterate through neighbors
87
                   if not visited[next_neighbor]: # If neighbor not visited
88
                       working_stack.append((v, gen)) # Push the current
89
      state back to stack
                       working_stack.append((next_neighbor, self.neighbor_gen())
     next_neighbor)))  # Add the neighbor to stack
                       break
91
               else:
                   stack.append(v) # Push the vertex to stack when all
93
      neighbors are processed
94
      def nonRecursiveTopologicalSort(self):
95
           # Perform topological sort on all vertices
          visited = [False] * self.V # Initialize all vertices as not
97
      visited
          stack = [] # Stack to store the topological order
98
99
          for i in range(1, self.V):
100
               if not visited[i]: # If vertex is not visited
                   self.nonRecursiveTopologicalSortUtil(i, visited, stack)
      Call the util function
103
          stack.reverse() # Reverse the stack to get the topological order
104
          return stack
105
106
      def find_successors(self, start_task):
107
           # Find all successors of a given task
108
          visited = set() # Set to track visited nodes
109
          successors = [] # List to store successors
          def dfs(v):
112
               if v in visited: # If node already visited, return
113
                   return
114
```

```
visited.add(v) # Mark node as visited
               for neighbor in self.graph[v]: # Iterate through neighbors
116
                   if neighbor not in visited: # If neighbor not visited
117
                       successors.append(neighbor) # Add neighbor to
118
      successors
                       dfs(neighbor)
                                      # Recursively visit neighbor
           dfs(start_task) # Start DFS from the given task
           return successors
122
123
  # Create and populate the graph with edges
  g = Graph(7)
125
  g.addEdge(1, 2)
127 g.addEdge(1, 3)
128 g.addEdge(1, 5)
  g.addEdge(2, 4)
  g.addEdge(3, 6)
130
  g.addEdge(4, 6)
  g.addEdge(5, 6)
132
133
  # Get the topological sort of tasks
topological_sort = g.nonRecursiveTopologicalSort()
task_list = [f'Task{num}' for num in topological_sort] # Convert to task
      format
137
  # Print the topological sort result
139
  print("\nTopological Sort of Tasks:")
  print(topological_sort)
140
141
  # SCHEDULING PARALLEL TASKS
142
143
  # Define parallel tasks (tasks that can be done in parallel)
144
  parallel_tasks = [
145
      [2, 3, 5] # Example set of parallel tasks
  ]
147
148
149 # Initialize a dictionary to store the results for parallel task successors
150 Sorted_results = {"Parallel Tasks Successors": {}}
151
```

```
# Loop through each set of parallel tasks
  for index, task_set in enumerate(parallel_tasks, start=1):
      # Initialize a dictionary for the current set of parallel tasks
154
      Sorted_results["Parallel Tasks Successors"][f"Parallel Task Set {index}
155
      "] = {}
      # Loop through each task in the current set of parallel tasks
      for task in task_set:
158
          successors = q.find_successors(task) # Find successors of the
159
      current task
           # Store the number of successors and the successor tasks in the
161
      result dictionary
          Sorted_results["Parallel Tasks Successors"][f"Parallel Task Set {
162
      index [task] = {
               "Number of Successors": len(successors),
               "Successor Tasks": successors
164
165
           }
166
# Print the successors for each set of parallel tasks
print("\nSuccessors of Parallel Tasks:")
  pprint.pprint(Sorted_results)
169
170
  # EXECUTION TIME CALCULATIONS
  # Function to calculate execution time for each version of each task
  def calculate_execution_time(data):
174
      # Loop through each task in the data
      for task, task_data in data.items():
           # Loop through each version of the task
          for version in task_data['Versions']:
178
               cl = version['CL'] # Get the 'CL' type data
179
               # Calculate execution time for 'CL' version
180
              cl_execution_time = round((cl['Mi'] + cl['Oi']) / (0.5 * cl['Yi
181
      , L']))
               cl['Execution_Time'] = cl_execution_time  # Store the
182
      calculated execution time
183
```

```
ch = version.get('CH', {}) # Get the 'CH' type data, if it
184
      exists
               if ch:
185
                   # Calculate execution time for 'CH' version
186
                   ch_execution_time = round((ch['Mi'] + ch['Oi']) / ch['Yi,H'
187
      1)
                   ch['Execution_Time'] = ch_execution_time # Store the
188
      calculated execution time
189
  # Call the function to calculate execution times for all tasks
190
  calculate_execution_time(tasks_data)
192
193
  # Print tasks with calculated execution times
  print("\nTasks with Calculated Execution Times:")
  pprint.pprint(tasks_data)
195
  # CLASSIFICATION BASED ON SUCCESSORS (CH/CL)
197
198
  # Initialize dictionaries to classify tasks into 'CH' and 'CL'
  task_classification = {'CH': [], 'CL': []}
200
201
  # Loop through each set of parallel tasks in the sorted results
202
  for task_set, tasks in Sorted_results['Parallel Tasks Successors'].items():
203
      # Loop through each task in the parallel task set
204
      for task, details in tasks.items():
205
           num_successors = details['Number of Successors'] # Get the number
      of successors
           task_name = f"Task{task}" # Convert task number to task name
207
           if num_successors > 1: # If more than one successor
               task_classification['CH'].append(task_name)
                                                             # Classify as 'CH'
209
           else:
               task_classification['CL'].append(task_name)
                                                             # Classify as 'CL'
211
212
213 # Print task classification into 'CH' and 'CL'
214 print("\nTask Classification (CH/CL):")
  pprint.pprint(task_classification)
216
  # POWER FACTOR AND VERSION SELECTION
217
218
```

```
# Initialize a dictionary to store the selected versions and their details
  result = {}
  # Loop through each 'CH' task
223 for ch_task in task_classification['CH']:
      if ch_task in tasks_data: # Check if the task exists in the data
          ch_versions = tasks_data[ch_task]['Versions'] # Get the versions
     of the task
          highest_ch_version = len(ch_versions) - 1 # Get the index of the
226
     highest version
          ch_data = ch_versions[highest_ch_version]['CH'] # Get the 'CH'
     data for the highest version
228
          ch_power_factor = ch_data['Pow_i'] # Get the power factor for the
     'CH' version
          ch_execution_time = ch_data.get('Execution_Time', None) # Get the
     execution time for the 'CH' version
230
          # Store the selected version and its details for the 'CH' task
231
          result[ch_task] = {
232
              'CH': {
233
                   'Version': f'Version {highest_ch_version + 1}',
                   'Power_Factor': ch_power_factor,
                   'Execution_Time': ch_execution_time
236
237
          }
238
240
          # Loop through each 'CL' task
          for cl_task in task_classification['CL']:
241
              if cl_task in tasks_data: # Check if the task exists in the
     data
                   cl_versions = tasks_data[cl_task]['Versions'] # Get the
243
     versions of the task
                   chosen_version_index = len(cl_versions) - 1 # Start with
244
     the highest version index
                   cl_data = cl_versions[chosen_version_index]['CL'] # Get
245
     the 'CL' data for the chosen version
                  cl_power_factor = cl_data['Pow_i'] # Get the power factor
246
      for the 'CL' version
```

```
cl_execution_time = cl_data.get('Execution_Time', None)
247
      Get the execution time for the 'CL' version
248
                   # Reduce the version index until the sum of power factors
249
      is within the limit
                   while (ch_power_factor + cl_power_factor) >
      MAX_POWER_FACTOR and chosen_version_index > 0:
                       chosen_version_index -= 1 # Decrease the version index
251
                       cl_data = cl_versions[chosen_version_index]['CL']
252
      Update the 'CL' data
                       cl_power_factor = cl_data['Pow_i'] # Update the power
      factor
                       cl_execution_time = cl_data.get('Execution_Time', None)
254
        # Update the execution time
255
256
                   # Store the selected version and its details for the 'CL'
      task
                   result[cl_task] = {
257
                       'CL': {
258
                            'Version': f'Version {chosen_version_index + 1}',
259
                            'Power_Factor': cl_power_factor,
260
                            'Execution_Time': cl_execution_time
261
262
                   }
263
264
  # Print the selected versions with power factor considerations
266
  print("\nSelected Versions with Power Factor Considerations:")
  pprint.pprint(result)
267
  # UPDATED TASKS
269
270
  # Initialize a dictionary to store the final updated tasks with selected
271
      versions
  final_result = {}
273
274 # Loop through each task in the result
  for task, details in result.items():
275
      task_type, task_data = list(details.items())[0] # Get the task type (
276
      CL/CH) and its data
```

```
version_number = int(task_data['Version'].split(' ')[1]) - 1 # Extract
       the version number
      updated_task_data = tasks_data[task]['Versions'][version_number][
278
      task_type] # Get the updated task data
      final_result[task] = {task_type: updated_task_data} # Store the
270
      updated task data in the final result
280
  # Print the final updated tasks with selected versions
281
print("\nFinal Updated Tasks with Selected Versions:")
283 pprint.pprint(final_result)
  # NUMBER OF LEVELS & TASKS AT EACH LEVEL
285
286
  # Function to calculate the number of levels in the task graph and tasks at
       each level
  def calculate_levels(graph):
288
      topo_sort = list(nx.topological_sort(graph)) # Get the topological
289
      sort of the graph
      levels = {node: 0 for node in graph.nodes} # Initialize levels for
      each node
      tasks_by_level = {} # Dictionary to store tasks by their level
291
292
      # Loop through each node in the topological order
293
      for node in topo_sort:
          current_level = levels[node] # Get the current level of the node
295
           # Update the level of each successor to be one higher than the
      current node
           for successor in graph.successors(node):
297
               levels[successor] = max(levels[successor], current_level + 1)
299
      # Organize tasks by their levels
300
      for node, level in levels.items():
301
          if level not in tasks_by_level:
302
               tasks_by_level[level] = []
303
          tasks_by_level[level].append(node)
304
305
      max_level = max(levels.values()) # Get the maximum level in the graph
306
      total_levels = max_level + 1  # Calculate the total number of levels
307
308
```

```
return total_levels, tasks_by_level
310
  # Initialize a directed graph and add nodes and edges for tasks
311
  task_graph = nx.DiGraph()
312
nodes = range(1, 7)
  task_graph.add_nodes_from(nodes)
  edges = [
315
       (1, 2),
316
       (1, 3),
317
       (1, 5),
318
       (2, 4),
       (3, 6),
321
       (4, 6),
       (5, 6)
322
323
  task_graph.add_edges_from(edges)
325
  # Calculate the total levels and tasks at each level in the graph
326
  total_levels, tasks_by_level = calculate_levels(task_graph)
328
  # Print the number of levels and tasks at each level
329
  print("\nTotal Number of Levels:", total_levels)
  print("Tasks at Each Level:")
  pprint.pprint(tasks_by_level)
333
  # ASSIGNING TASKS INTO MATRICES
334
  # Initialize matrices for execution times and task names
336
  execution_time_matrix = np.zeros((2, total_levels), dtype=object)
  task_name_matrix = np.full((2, total_levels), None, dtype=object)
338
339
  # Initialize counters for 'CL' and 'CH' tasks
340
  count_cl = 0
341
  count_ch = 0
342
343
# Loop through the tasks in the topological order
  for task in task_list:
345
       if task in final_result: # Check if the task is in the final result
346
```

```
task_type = list(final_result[task].keys())[0] # Get the task type
347
       (CL/CH)
           execution_time = final_result[task][task_type]['Execution_Time'] #
348
       Get the execution time
340
           if task_type == 'CL':
               count_cl += 1 # Increment the 'CL' task counter
351
               if count_cl < total_levels: # Ensure we stay within matrix</pre>
352
      bounds
                   execution_time_matrix[0][count_cl] = execution_time
353
      Assign execution time to matrix
                   task_name_matrix[0][count_cl] = task # Assign task name to
354
      matrix
           elif task_type == 'CH':
355
               count_ch += 1 # Increment the 'CH' task counter
356
               if count_ch < total_levels: # Ensure we stay within matrix</pre>
357
      bounds
                   execution_time_matrix[1][count_ch] = execution_time
358
      Assign execution time to matrix
                   task_name_matrix[1][count_ch] = task # Assign task name to
350
       matrix
360
  # Set the initial column (first task) to zero
361
  execution_time_matrix[0][0] = 0
| execution_time_matrix[1][0] = 0
  task_name_matrix[0][0] = None
365
  task_name_matrix[1][0] = None
366
367 # Print the initial matrices for execution times and task names
368 print ("\nInitial Execution Time Matrix:")
369 print (execution_time_matrix)
  print("\nInitial Task Name Matrix:")
  print(task_name_matrix)
371
372
373 # Determine which columns in the matrix are empty
374 zero_columns = []
  for col in range(total_levels):
375
      if execution_time_matrix[0][col] == 0 and execution_time_matrix[1][col]
376
       == 0:
```

```
zero_columns.append(col + 1) # Store empty column indices
378
  # HANDLE MISSING TASKS
379
380
  # Convert zero columns to levels
381
  zero_levels = [col - 1 for col in zero_columns]
  tasks_at_zero_levels = []
383
384
  # Identify tasks at levels that correspond to zero columns
385
  for level in zero_levels:
386
      if level in tasks_by_level:
           tasks_at_zero_levels.extend(tasks_by_level[level])
388
389
  # Assign missing tasks to the matrices based on the best available version
  for task in tasks_at_zero_levels:
391
      task_key = f"Task{task}" # Convert task number to task name
       if task_key in tasks_data:
393
           versions = tasks_data[task_key]['Versions'] # Get all versions for
394
       the task
           max oi = -1 # Initialize maximum Oi value
395
           max\_version = None
393
           # Loop through versions to find the one with the maximum Oi value
398
           for version in versions:
               for type_key, data in version.items():
400
                   if data['Oi'] > max_oi:
402
                        max_oi = data['Oi']
                       max version = data
403
404
           least_execution_time = float('inf') # Initialize least execution
405
      time
           best_type = None
406
407
           # Loop through versions again to find the one with the least
408
      execution time
           for version in versions:
409
               for type_key, data in version.items():
410
                   if data['Execution_Time'] < least_execution_time:</pre>
411
                        least_execution_time = data['Execution_Time']
412
```

```
best_type = type_key
414
           \# Assign the task to the matrix based on its type (CL/CH)
415
           index = zero_levels[tasks_at_zero_levels.index(task)]
416
           if best_type == 'CL':
417
               execution_time_matrix[0][index] = least_execution_time
               task_name_matrix[0][index] = task_key
419
           elif best_type == 'CH':
420
               execution_time_matrix[1][index] = least_execution_time
421
               task_name_matrix[1][index] = task_key
422
  # Print matrices after handling missing tasks
424
print("\nExecution Time Matrix After Handling Missing Tasks:")
426 print (execution_time_matrix)
427 print ("\nTask Name Matrix After Handling Missing Tasks:")
  print(task_name_matrix)
429
  # FIND AND HANDLE MISSING TASKS IN MATRICES
430
431
432 # Identify tasks that are missing from the matrices
433 tasks_in_matrix = set(task_name for row in task_name_matrix for task_name
      in row if task_name is not None)
434 task_list_set = set(task_list)
  missing_tasks = task_list_set - tasks_in_matrix
435
436
  # Assign missing tasks to the appropriate rows and columns
438
  for missing_task in missing_tasks:
      task_number = int(missing_task.replace('Task', ''))  # Extract task
439
      number
440
      task_level = None
441
       # Determine the level of the missing task
442
      for level, tasks in tasks_by_level.items():
443
           if task_number in tasks:
               task_level = level
445
               break
446
447
       # If the task level is identified, find an empty slot in the matrices
448
      if task_level is not None:
449
```

```
respective_column = task_level # The corresponding column in the
450
      matrix
           if execution_time_matrix[0][respective_column] == 0:
451
               available_row = 0 # Assign to row 0 (CL)
452
               row_type = 'CL'
453
          elif execution_time_matrix[1][respective_column] == 0:
               available_row = 1 # Assign to row 1 (CH)
455
               row_type = 'CH'
456
          else:
457
               available_row = None # No available row
458
           # Assign the task to the matrix based on the selected version
460
          if available_row is not None:
461
               max_oi = -1 # Initialize maximum Oi value
               selected_version = None
463
               # Loop through versions to select the one with the highest Oi
      value
               for version in tasks_data[missing_task]['Versions']:
465
                   if version[row_type]['Oi'] > max_oi:
466
                       max_oi = version[row_type]['Oi']
467
                       selected_version = version[row_type]
469
               # Assign the selected task version to the matrix
470
               if selected_version:
471
                   execution_time_matrix[available_row][respective_column] =
472
      selected_version['Execution_Time']
473
                   task_name_matrix[available_row][respective_column] =
     missing_task
474
475 # Print final matrices after assigning missing tasks
476 print("\nFinal Execution Time Matrix:")
  print (execution_time_matrix)
  print("\nFinal Task Name Matrix:")
  print(task_name_matrix)
480
 # Initialize the result dictionary for storing final task selections
  result = {}
482
483
484 # Iterate through the task_name_matrix and execution_time_matrix
```

```
rows, cols = task_name_matrix.shape
  for row in range(rows):
486
      for col in range(cols):
487
           task_name = task_name_matrix[row, col] # Get the task name from
488
      the matrix
          if task name:
               execution_time = execution_time_matrix[row, col] # Get the
490
      corresponding execution time
               versions = tasks_data[task_name]['Versions'] # Get all
491
      versions for the task
               # Determine whether the task is CL or CH based on the execution
493
       time
               selected_version = None
494
               for version in versions:
495
                   cl_data = version.get('CL', {})
                   ch_data = version.get('CH', {})
497
498
                   if cl_data.get('Execution_Time') == execution_time:
499
     Match execution time with CL
                       selected_version = cl_data
500
                       result[task_name] = {'CL': selected_version}
501
                   elif ch_data.get('Execution_Time') == execution_time:
502
     Match execution time with CH
                       selected_version = ch_data
503
                       result[task_name] = {'CH': selected_version}
504
505
506 # Print the final result dictionary containing selected versions for tasks
507 print("\nFinal Task Version Selections:")
508 pprint.pprint(result)
  print()
509
510
  # PROCESSING TASK EXECUTION SEQUENCE
511
512
513 # Initialize a dictionary to store the start and finish times of tasks
514 start_finish_times = {}
515
516 # Process each column in the matrices to understand the task execution flow
for col in range(task_name_matrix.shape[1]):
```

```
for row in range(task_name_matrix.shape[0]):
           task_name = task_name_matrix[row, col] # Get the task name from
519
      the matrix
           execution_time = execution_time_matrix[row, col] # Get the
520
      corresponding execution time
521
           if task_name is not None: # If there is a task in this cell
522
               task_type = 'CH' if row == 1 else 'CL' # Determine the task
523
      type based on the row
524
               if row == 1 and col == 0: # Task1 is executed first
                   start time = 0
526
527
               else: # For other tasks, determine the start time based on
      predecessor tasks
                   if task name == 'Task6':
528
                        # Task6 starts after Task3, Task5, and Task4 are
529
      completed
                       predecessor_tasks = ['Task3', 'Task5', 'Task4']
530
                   elif task_name == 'Task5':
531
                        # Task5 starts after Task1 is completed
532
                        predecessor_tasks = ['Task1']
533
                   elif task_name == 'Task3':
534
                        # Task3 starts after Task5 is completed
535
                       predecessor_tasks = ['Task5']
536
                   elif task_name == 'Task2':
537
                        # Task2 starts after Task1 is completed
538
539
                        predecessor_tasks = ['Task1']
                   elif task_name == 'Task4':
540
                        # Task4 starts after Task2 is completed
541
                       predecessor_tasks = ['Task2']
542
543
                   # Find the maximum finish time among the predecessor tasks
544
                   start\_time = max(
545
                        start_finish_times[predecessor][2]
546
                        for predecessor in predecessor_tasks
547
                        if predecessor in start_finish_times
548
549
550
```

```
551
               finish_time = start_time + execution_time # Calculate the
      finish time for the task
               start_finish_times[task_name] = (task_type, start_time,
552
      finish_time) # Store start and finish times
553
  # Store task execution sequence in a dictionary with the requested format
  task_execution_sequence = {}
555
556
  # Loop through the start and finish times to create the execution sequence
557
  for task, (task_type, start, finish) in start_finish_times.items():
558
      task_execution_sequence[task] = {
           'type': task_type,
560
           'Start_Time': start,
561
          'Finish_Time': finish
      }
563
  # Print the dictionary to see the final task execution sequence
565
566 print("Task Execution Sequence Dictionary:")
567 print (task_execution_sequence)
568 print ()
  # Identify columns with no zeros (valid columns)
570
  valid_columns = np.all(execution_time_matrix != 0, axis=0)
  columns_with_zeros = ~valid_columns
573
  # Filter the matrices to get only the valid columns
  filtered_execution_time_matrix = execution_time_matrix[:, valid_columns]
  filtered_task_name_matrix = task_name_matrix[:, valid_columns]
576
577
  # Initialize a list to store the unique task combinations and their
578
     corresponding power factors
  parallel_task_power_factors = []
579
580
581 # Use a set to keep track of seen combinations (unordered pairs)
seen_combinations = set()
583
  # Function to get the power factor from the result dictionary
584
  def get_power_factor(task, execution_time):
585
      task_data = result.get(task)
586
```

```
if task_data:
           for task_type, details in task_data.items():
               if details['Execution_Time'] == execution_time:
580
                   return details['Pow_i']
590
      return None
591
  # Generate all combinations of row1 + row2 across valid columns using power
593
       factors
  for i in range(filtered_execution_time_matrix.shape[1]):
       for j in range(i, filtered_execution_time_matrix.shape[1]):
595
           task1_row1 = filtered_task_name_matrix[0, i]
           task2_row2 = filtered_task_name_matrix[1, j]
597
598
           if task1_row1 and task2_row2:
               pow_i1 = get_power_factor(task1_row1,
600
      filtered_execution_time_matrix[0, i])
               pow_i2 = get_power_factor(task2_row2,
601
      filtered_execution_time_matrix[1, j])
               if pow_i1 is not None and pow_i2 is not None:
602
                   tasks = tuple(sorted([task1_row1, task2_row2]))
603
                   if tasks not in seen_combinations:
                        combined_power = pow_i1 + pow_i2
605
                       parallel_task_power_factors.append((f'{tasks[0]} + {
606
      tasks[1] }', combined_power))
                       seen combinations.add(tasks)
607
609
           # Also add the reverse combination (row2 + row1)
           task1_row2 = filtered_task_name_matrix[1, i]
610
           task2_row1 = filtered_task_name_matrix[0, j]
612
           if task1_row2 and task2_row1:
613
               pow_i1 = get_power_factor(task1_row2,
614
      filtered_execution_time_matrix[1, i])
               pow_i2 = get_power_factor(task2_row1,
615
      filtered_execution_time_matrix[0, j])
               if pow_i1 is not None and pow_i2 is not None:
616
                   tasks = tuple(sorted([task1_row2, task2_row1]))
617
                   if tasks not in seen_combinations:
618
                       combined_power = pow_i1 + pow_i2
619
```

```
parallel_task_power_factors.append((f'{tasks[0]} + {
      tasks[1] }', combined_power))
                       seen_combinations.add(tasks)
62
622
  # Handle columns with zeros separately
623
  for col in range(execution_time_matrix.shape[1]):
      if columns_with_zeros[col]:
625
          task = task_name_matrix[1, col] # Take the task from row 2, as row
626
       1 has zero
          if task:
627
               sum_value = get_power_factor(task, execution_time_matrix[1, col
      1)
629
               if sum_value is not None:
                   parallel_task_power_factors.append((task, sum_value))
631
  # Sort the combined list of tasks and power factors by task name
  parallel_task_power_factors.sort()
634
  # Print the sorted list of parallel tasks and their corresponding power
      factors
print ("Parallel tasks and their corresponding power factors (sorted):")
  for task in parallel_task_power_factors:
      print (task)
638
```

Listing A.1: Python Program for Task Scheduling

#### **Python Program for Graph generations**

```
plt.figure(figsize=(3, 2))

pos = nx.spring_layout(task_graph) # Position nodes using the spring
    layout

nx.draw(task_graph, pos, with_labels=True, node_color='red', node_size=500,
    edge_color='black', font_size=11), #font_weight='bold')

#nx.draw_networkx_edge_labels(task_graph, pos, edge_labels={(u, v): f'{u} }->{v}' for u, v in edges})

plt.title("Task Dependency Graph")
```

```
plt.show()
10
print()
# Set up the figure and axis
14 fig, ax = plt.subplots(figsize=(10, 2))
16 # Define y-axis positions for CPU and GPU
17 y_positions = {'CH': 1, 'CL': 2}
18 colors = {'CH': 'orange', 'CL': 'lightgreen'}
20 # Plot each task as a rectangle
 for task, details in task_execution_sequence.items():
     task_type = details['type']
     start_time = details['Start_Time']
      finish_time = details['Finish_Time']
25
      # Determine the y position based on the task type
26
     y_position = y_positions[task_type]
27
28
      # Calculate width of the box
     width = finish_time - start_time
30
31
      # Draw the rectangle with a height of 0.8 units
     rect = patches.Rectangle((start_time, y_position - 0.4), width, 0.8,
     edgecolor='black', facecolor=colors[task_type])
     ax.add_patch(rect)
34
     # Add task label and execution time inside the box
     ax.text(start_time + width / 2, y_position, f'{task}\n{start_time}-{
     finish_time}', ha='center', va='center', fontsize=10, color='black')
39 # Set y-axis limits and labels
40 ax.set_ylim(0.5, 2.5) # y-axis to accommodate both CPU and GPU stacked
41 ax.set_yticks([1, 2])
42 ax.set_yticklabels(['GPU', 'CPU'])
44 # Set x-axis limits and labels
45 ax.set_xlim(0, 150) # Set x-axis limit
```

```
46 ax.set_xticks(range(0, Deadline + 1, 10)) # Mark every 5 units on the x-
    axis
plt.axvline(x=142, color='red', linestyle='--', label=''); plt.text(142,
    plt.ylim()[1], 'Deadline=142', color='white', backgroundcolor='red', ha=
    'right')
50 # Add grid lines for better readability
si ax.grid(True, which='both', axis='x', linestyle='--', color='gray', alpha
    =0.7)
53 # Add labels and title
54 ax.set_xlabel('Execution Time')
55 ax.set_ylabel('Cores')
56 ax.set_title('Actual Case Task Scheduling - Heterogeneous')
plt.savefig('actualcasetaskscheduling.png')
59 # Show the plot
60 plt.tight_layout()
61 plt.show()
64
     65 import matplotlib.pyplot as plt
66 import matplotlib.patches as patches
68 # Define y-axis positions for CPU and GPU
69 y_positions = {'CPU': 2, 'GPU': 1}
colors = {'CPU': 'lightgreen', 'GPU': 'orange'}
72 # Task details manually set according to the specified start and end times
73 tasks = {
74
     'CPU': [(9, 61), (61, 125)],
     'GPU': [(0, 9), (9, 42), (42, 106), (125, 152)]
78 # Task names corresponding to each time segment
```

```
task_names = {
      'CPU': ['Task5', 'Task3'],
80
      'GPU': ['Task1', 'Task2', 'Task4', 'Task6']
81
82
  # Set up the figure and axis
85 fig, ax = plt.subplots(figsize=(10, 2))
86
  # Plot each task segment on the CPU and GPU
  for core_type, core_tasks in tasks.items():
      for i, (start_x, end_x) in enumerate(core_tasks):
          y_position = y_positions[core_type]
90
91
          color = colors[core_type]
          # Draw the rectangle representing the task's execution time
93
          rect = patches.Rectangle((start_x, y_position - 0.4), end_x -
     start_x, 0.8, edgecolor='black', facecolor=color)
          ax.add_patch(rect)
95
          # Add the task name and the execution time range inside the box
97
          task_name = task_names[core_type][i]
          ax.text((start_x + end_x) / 2, y_position + 0.15, task_name, ha='
99
     center', va='center', fontsize=10, color='black')
          ax.text((start_x + end_x) / 2, y_position - 0.15, f'{start_x}-{}
100
     end_x}', ha='center', va='center', fontsize=8, color='black')
102
  # Set y-axis limits and labels
ax.set_ylim(0.5, 2.5) # y-axis to accommodate both CPU and GPU rows
104 ax.set_yticks([1, 2])
ax.set_yticklabels(['GPU', 'CPU']) # Label y-axis as 'CPU' and 'GPU'
107 # Set x-axis limits and labels
108 total_time = max(end for core_tasks in tasks.values() for _, end in
     core_tasks)
109 ax.set_xlim(0, total_time) # Set x-axis limit based on the total time
ax.set_xticks(range(0, total_time + 1, 10)) # Mark every 10 units on the x
     -axis
# Draw a red vertical line at x=103 for the deadline
```

```
ax.axvline(x=103, color='red', linestyle='--', linewidth=2)
ax.text(103, 2.3, 'Deadline=142', color='white', ha='center', va='center',
     fontsize=10, rotation=0, backgroundcolor='red')
115
# Add grid lines for better readability
ax.grid(True, which='both', axis='x', linestyle='--', color='gray', alpha
     =0.7)
118
119 # Add labels and title
120 ax.set_ylabel('Cores')
ax.set_xlabel('Execution Time')
ax.set_title('Ideal Case Task Scheduling - Heterogeneous')
123
plt.savefig('idealcasetaskscheduling.png')
125 # Show the plot
plt.tight_layout()
  plt.show()
127
128
129
     import matplotlib.pyplot as plt
import matplotlib.patches as patches
132 import numpy as np
133
134 # Define the input array
execution_times = [24, 52, 64, 100, 240, 76]
task_names = ['Task1', 'Task5', 'Task3', 'Task2', 'Task4', 'Task6'] # Task
      names corresponding to each segment
138 # Set up the figure and axis
  fig, ax = plt.subplots(figsize=(10, 2))
139
140
141 # Define y-axis position for CPU
142 y_position = 1
143 color = 'orange'
144
145 # Initialize the starting point of the x-axis
146 | current_x = 0
```

```
147
148 # Plot each segment based on the execution times
149 for i, value in enumerate (execution_times):
      start_x = current_x
150
      end_x = current_x + value
      # Draw the rectangle with a height of 0.8 units
      rect = patches.Rectangle((start_x, y_position - 0.4), value, 0.8,
154
      edgecolor='black', facecolor=color)
      ax.add_patch(rect)
155
      # Add task name and execution time inside the box
158
      ax.text((start_x + end_x) / 2, y_position + 0.15, task_names[i], ha='
      center', va='center', fontsize=10, color='black')
      ax.text((start_x + end_x) / 2, y_position - 0.15, f'{start_x}-{end_x}',
159
      ha='center', va='center', fontsize=8, color='black')
160
      # Update current_x to the end_x for the next segment
161
      current_x = end_x
162
163
  # Set y-axis limits and labels
  ax.set_ylim(0.5, 1.5) # y-axis to accommodate CPU row
165
166 ax.set_yticks([1])
  ax.set_yticklabels(['CPU']) # Label y-axis as 'CPU'
168
169 # Set x-axis limits and labels
ax.set_xlim(0, np.sum(execution_times)) # Set x-axis limit based on the
     total value
| ax.set_xticks(range(0, int(np.sum(execution_times)) + 1, 50)) # Mark every
       50 units on the x-axis
172
\# Draw a red vertical line at x=103 for the deadline
ax.axvline(x=103, color='red', linestyle='--', linewidth=2)
ax.text(103, 1.3, 'Deadline', color='white', ha='center', va='center',
     fontsize=10, rotation=0, backgroundcolor='red')
176
177 # Add grid lines for better readability
ax.grid(True, which='both', axis='x', linestyle='--', color='gray', alpha
     =0.7)
```

```
179
  # Add labels and title
180
181 ax.set_ylabel('Cores')
ax.set_xlabel('Execution Time')
ax.set_title('Ideal case - CPU (Homogeneous)')
plt.savefig('idealcasecpu.png')
186 # Show the plot
187 plt.tight_layout()
188 plt.show()
189
     import matplotlib.pyplot as plt
191
  # Define the tasks and their corresponding power factors
  parallel_task_power_factors = [
193
      ('Task1', 13),
194
      ('Task2+Task3', 45),
195
      ('Task2+Task5', 50),
196
      ('Task3+Task4', 36),
197
      ('Task4+Task5', 41),
198
      ('Task6', 12)
199
200
201
  # Separate the tasks and power factors into two lists
  tasks = [task for task, _ in parallel_task_power_factors]
203
  power_factors = [power for _, power in parallel_task_power_factors]
204
205
  # Create the bar chart
206
plt.figure(figsize=(8, 4))
  plt.bar(tasks, power_factors, color='skyblue', edgecolor='black')
208
209
210 # Add labels and title
211 plt.xlabel('Tasks')
212 plt.ylabel('Power Factor')
plt.title('Actual Case Power Factor by Task')
214
215 # Set y-axis limit to 70
```

```
plt.ylim(0, 70)
217
  # Draw a red line at MAX_POWER_FACTOR = 50
218
plt.axhline(y=50, color='red', linestyle='--', linewidth=2, label='
     MAX_POWER_FACTOR = 50')
220
  # Annotate the bars with their power factor values
221
  for i, value in enumerate(power_factors):
      plt.text(i, value + 1, f'{value}', ha='center', va='bottom')
223
224
  # Display the legend
226 plt.legend()
227
228 plt.savefig('actualcasepowerfactorbytask.png')
229
230 # Show the plot
231 plt.tight_layout()
232 plt.show()
234
235
     236 import matplotlib.pyplot as plt
237
  # Define the tasks and their corresponding power factors
239
  parallel_task_power_factors = [
      ('Task1', 13),
240
      ('Task2+Task3', 45),
      ('Task2+Task5', 57),
242
      ('Task3+Task4', 36),
243
      ('Task4+Task5', 48),
244
      ('Task6', 16)
245
246
247
248 # Separate the tasks and power factors into two lists
249 tasks = [task for task, _ in parallel_task_power_factors]
250 power_factors = [power for _, power in parallel_task_power_factors]
251
```

```
252 # Create the bar chart
253 plt.figure(figsize=(8, 4))
plt.bar(tasks, power_factors, color='skyblue', edgecolor='black')
256 # Add labels and title
plt.xlabel('Tasks')
258 plt.ylabel('Power Factor')
  plt.title('Ideal Case Power Factor by Task')
260
261 # Set y-axis limit to 70
  plt.ylim(0, 70)
263
264 # Draw a red line at MAX_POWER_FACTOR = 50
plt.axhline(y=50, color='red', linestyle='--', linewidth=2, label='
     MAX_POWER_FACTOR = 50')
266
  # Annotate the bars with their power factor values
267
  for i, value in enumerate(power_factors):
      plt.text(i, value + 1, f'{value}', ha='center', va='bottom')
269
270
271 # Display the legend
272 plt.legend()
273
274 plt.savefig('idealcasepowerfactorbytask.png')
275
276 # Show the plot
plt.tight_layout()
278 plt.show()
279
280
     281 import matplotlib.pyplot as plt
282
283 # Data for the graph
284 number_of_cores = [2, 3, 4, 5, 6, 7]
  nQ_values = [0.811, 0.9, 0.98, 1, 1.2, 1.5]
286
287 # Create the line plot
```

```
plt.figure(figsize=(5, 4))
  plt.plot(number_of_cores, nQ_values, marker='o', linestyle='-', color='blue
      ')
290
  # Add labels and title
291
292 plt.xlabel('Number of Cores')
plt.ylabel('nQ')
  plt.title('ACCURACY')
295
  \# Draw a horizontal red line at y=1
  plt.axhline(y=1, color='red', linestyle='--', linewidth=2)
298
299
  # Annotate the red line
300 plt.text(2.0, 1.05, 'Actual QoS = Ideal QoS', color='red', ha='left', va='
     center', fontsize=10)
plt.text(2.6, 0.85, 'Actual QoS < Ideal QoS', color='green', ha='left', va=
      'center', fontsize=10)
plt.text(2.0, 1.25, 'Actual QoS > Ideal QoS', color='green', ha='left', va=
     'center', fontsize=10)
303
  # Add grid lines for better readability
  plt.grid(True)
305
306
plt.savefig('Accuracy.png')
308
  # Show the plot
310 plt.tight_layout()
311 plt.show()
```

Listing A.2: Python Program for generating graphs