

# Analysis and Forecasting of Carbon Emission in SAARC Countries using Attention-based LSTM

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**Abstract**—Climate change and global warming are urgent environmental issues demanding immediate action to safeguard future generations. The major contributor to the greenhouse effect, carbon dioxide (CO<sub>2</sub>), primarily originates from industrial and transportation fossil fuel combustion. International agreements, like the Paris Agreement, call for a 30-35% reduction in CO<sub>2</sub> emissions compared to 2005 levels. This research aims to predict CO<sub>2</sub> emissions and raise awareness among SAARC nations and governments about the increasing trend. We introduce a novel predictive framework using Attention-based Long Short-Term Memory (A-LSTM) for CO<sub>2</sub> emissions analysis. The Attention mechanism assigns variable weights to input data, facilitating indirect connections between LSTM outputs and pertinent inputs. This enhances resource allocation in the A-LSTM model, overcoming computational constraints. We integrate input parameters encompassing CO<sub>2</sub> emissions from land-use changes, oil, natural gas, and coal combustion to forecast CO<sub>2</sub> emissions and correlate them with population and per capita GDP. Our comparative analysis conclusively demonstrates the superior performance of A-LSTM models over baseline LSTM models when applied to the CO<sub>2</sub> emission dataset sourced from Our World in Data (OWID) and World Bank Indicator database. Specifically, the LSTM model registers a MAPE of 24.968 and an RMSE of 0.34, whereas the Attention-based LSTM model showcases a marked improvement of 57% with a considerably lower MAPE of 10.5902 and an RMSE of 0.107.

**Index Terms**—Climate Change, Green House Gas, Long Short Term Memory, Attention, CO<sub>2</sub> Emission

## I. INTRODUCTION

### A. Background

Similar to other emerging nations, the member states of the South Asian Association for Regional Cooperation (SAARC) are confronted with various challenges linked to climate change. Mitigating these challenges necessitates coordinated global efforts. Accurate predictions of CO<sub>2</sub> emissions are essential to combat climate change, guide policy-making, improve air quality, fulfil international commitments, support economic development, raise public awareness, and advance environmental research and education. Ensuring precise CO<sub>2</sub>

emission forecasts is imperative for these nations to attain a sustainable and resilient future. In 2015, a worldwide summit on climate change took place in France, with participation from representatives of 196 nations, including the United States [1]. This gathering led to an accord to incorporate nationally determined contributions (NDCs) into the framework of the Paris Agreement.

Developing countries, characterised by significant landmass, population, and expanding economies, possess substantial potential for carbon reduction [2]. However, they require substantial financial and technical support to leverage their physical assets for a global cause, as emphasized in the Paris Agreement. Numerous economic factors, such as foreign investment, population growth, land use changes, economic growth (EG), energy consumption (EC), labour force (LF), urban population (UP), inflation (INF), tourism, and transportation contribute to carbon emissions. Many scholars have conducted extensive analyses of the literature on the relationships between CO<sub>2</sub> emissions, environmental factors, and energy usage [3]. Due to the heavy reliance of SAARC nations on coal, cement, land use alterations, and oil, a significant increase in carbon emissions from these countries is anticipated in the future. This paper evaluates carbon emissions and their Granger causality correlations with population changes, GDP, energy consumption, and income for each SAARC nation (Afghanistan, Bangladesh, Bhutan, India, Nepal, Pakistan, and Sri Lanka), excluding Maldives due to data limitations. Whenever time-series data is available and there is a requirement for forecasting future trends, machine learning presents itself as a valuable and effective tool.

Traditional ML approaches have inherent drawbacks, including prolonged processing times and often inadequate forecasting capabilities [14], [15]. Therefore, this work creates time-series forecast models based on robust and efficient ML algorithms. The outcome is the attention-based long short-term memory (A-LSTM) network, which integrates the attention

mechanism into the long short-term memory network. This A-LSTM network addresses the issue of poor predictive power by offering speed and precision. Like other developing nations, South Asian Association for Regional Cooperation (SAARC) nations face a variety of climate change-related difficulties, and addressing those challenges will need coordinated global action. To combat climate change, inform policy making, enhance air quality, fulfil international obligations, assist economic development, increase public awareness, and advance environmental research and education, CO<sub>2</sub> emissions ought to be predicted. For the nations to have a sustainable and resilient future, accurate CO<sub>2</sub> emission forecasts are crucial. Significant opportunity for carbon reduction exists in emerging economies that are characterised by huge landmasses, sizable people, and growing economic activity. As emphasized in the Paris Agreement, these developing countries need a lot of financial and technical support in order to utilise their physical resources for a greater good [2].

A number of economic factors contribute to Carbon emission, including foreign investment, population growth, changes in land use, economic growth (EG), energy consumption (EC), labour force (LF), urban population (UP), inflation (INF), tourism, and transportation, among others. Numerous scholars have conducted analyses and evaluations of the body of literature concerning the correlation between CO<sub>2</sub> emissions, environmental variables, and various energy consumption patterns [5]. Machine learning can be used to tackle any problem involving time-series data and a need to foresee the future. Traditional and conventional ML approaches have the primary flaw that they take a lot of time and frequently have poor forecasting ability. In order to forecast production using historical data, time-series forecast models based on effective and powerful ML algorithms are created in this work. The attention-based long short-term memory (A-LSTM) network is the result of integrating the attention mechanism into the long short-term memory network. Since the A-LSTM network is quick and precise, it can address the issue of poor predicting power.

The paper is structured as follows: Section 2 outlines the research gap and presents the contributions made by this work. In Section 3, the methodology is detailed, which includes an in-depth description of the deep learning models used and the performance metrics employed. Section 4 elaborates on the experimental setup, covering model configurations, performance metrics, and the results of the experiments. Section 5 is dedicated to a discussion of the findings and offers insights into potential research directions. It also outlines the conclusions drawn from the study and discusses policy implications.

Numerous variables might affect CO<sub>2</sub> emissions, thus forecasting is important. Because of this, new models to predict CO<sub>2</sub> emissions have recently been developed and some are in the works. The study [4] underscores the pivotal role of feature engineering and selection in improving the accuracy of ML and deep learning algorithms for CO<sub>2</sub> emission prediction. The superior performance of hybrid deep learning algorithms,

as evidenced by lower RMSE, rRMSE, and MAPE values, offers promising prospects for effectively addressing the challenges associated with CO<sub>2</sub> emission forecasting, ultimately contributing to our efforts to combat climate change. In the study titled "Predicting the Environmental Change of Carbon Emission Patterns in South Asia," researchers employed a Bi-LSTM deep learning approach. Their analysis revealed that carbon emissions pose a substantial concern, with projections indicating that the problem is likely to exacerbate in the coming years [5]. This escalation is attributed primarily to the high levels of emissions from China and India, especially within the next decade.

The CO<sub>2</sub> emissions in Bangladesh are predicted using the logarithmic mean division index (LMDI) decomposition method, and the results show that while globalisation, foreign direct investment, and innovation have a negative impact on CO<sub>2</sub> emissions in terms of improving environmental quality, economic growth, trade, energy consumption, and urbanisation have a positive impact on CO<sub>2</sub> emissions and thereby promote environmental degradation both in the long run and the short term [6].

To assess the impact of GDP and different forms of energy consumption—comprising total, non-renewable, renewable, industrial, and residential energy—on CO<sub>2</sub> emissions at the state level, various quantitative methodologies have been employed. These approaches encompass both static models and dynamic models [7].

To determine the CO<sub>2</sub> emission trends in Iran, Canada, and Italy, The results demonstrate that the proposed method is more accurate in long-term CO<sub>2</sub> emissions forecasting when using a general regression neural network (GRNN) and grey wolf optimisation (GWO) [8]. By using a linear and nonlinear time series modelling approach, specifically ARIMA, naive, TBATS, ETS, NNAR, and MLP, an accurate estimate of future CO<sub>2</sub> emissions in Pakistan was shown [9].

Four deep learning algorithms—Convolution neural network (CNN), CNN long short-term memory (CNN-LSTM), long short-term memory (LSTM), and dense neural network (DNN)—are examined for formulating the multivariate time series CO<sub>2</sub> emissions forecasting. A statistically significant long-term cointegrating relationship between CO<sub>2</sub> emissions, electrical energy consumption, and GDP is presented [10].

## II. RESEARCH GAPS AND CONTRIBUTIONS

Numerous empirical inquiries have delved into multifaceted aspects of carbon dioxide (CO<sub>2</sub>) emissions, encompassing examinations of the causal linkages between CO<sub>2</sub> emissions and their determinants. Nevertheless, these endeavours have left several research lacunae that necessitate further investigation. The impetuses for pursuing this research endeavour are grounded in several considerations. Firstly, limitations inherent in the scale of datasets employed have constrained the comprehensiveness of prior studies. Secondly, certain pivotal determinants of CO<sub>2</sub> emissions have been omitted from prior investigations. Lastly, the South Asian Association for Regional Cooperation (SAARC) nations have not received

adequate scrutiny within this context. Additionally, the conventional machine learning models employed in this domain have confronted formidable challenges related to overfitting due to the scarcity of data points available for training and testing.

The prevailing literature has centered on time series forecasting in the domain of CO<sub>2</sub> emissions, leveraging machine learning, regression methodologies, and the extensive adoption of deep learning techniques. This research, in particular, focuses on evaluating the efficacy of Attention-based Long Short-Term Memory (A-LSTM) in forecasting, with the objective of addressing gaps in prior research efforts. This research contributes to the body of knowledge in the following ways:

- Sheding light on the low level of environmental awareness, particularly regarding CO<sub>2</sub> emissions, in SAARC countries. The study investigates the intricate dynamics and causal relationships between CO<sub>2</sub> emissions and cement production, illuminating critical insights.
- While similar indicators have been explored in previous studies, minimal attention has been devoted to analyzing SAARC data using machine learning techniques. This research endeavours to enrich the literature by applying deep learning methodologies to forecast CO<sub>2</sub> emissions, particularly within the unique context of SAARC nations.
- Significantly, this research emphasizes the importance of forecasting CO<sub>2</sub> emissions using A-LSTM, demonstrating its practical advantages in terms of enhanced accuracy compared to traditional LSTM models.

### III. METHODOLOGY

#### A. Data and Variables

The data used in this research are collected from the year 1858 to 2021 from datasets in our world in data and world bank indicators of the world bank, which is the most comprehensive and includes all the sectors along with gases [13]. The major influencing carbon monitor categories considered in this work are Power (Oil Power plants, Coal Power Plants, Gas Power Plants), Industry( Oil combustion and use for Manufacturing, Gas combustion and use for Manufacturing, Coal combustion use for Manufacturing, Cement and other) including GDP per capita and population. The cumulative CO<sub>2</sub> emission data was collected from Kaggle. In this work, multivariate time series data of SAARC Countries (including Afganistan, Bangladesh, Bhutan, India, Nepal, Pakistan and Srilanka, excluding Maldives) have been used, having an increasing CO<sub>2</sub> emission trend. Table 1 depicts the descriptive analysis of the dataset CO<sub>2</sub> emission data. The upward trend in CO<sub>2</sub> levels becomes evident upon examining the minimum, median, and maximum values presented in Table I. This study primarily focuses on monitoring carbon emissions across critical categories such as Power, Industry, Residential Consumption, Ground Transport, and Land Use Change. Our analysis centres on understanding the growing trend in CO<sub>2</sub> emissions in relation to two key factors: GDP Per Capita and Population, within the SAARC countries. This approach

Variable	Year	CO <sub>2</sub> Emission
Mean	5347.84137548842	1944.35294117647
Standard Error	79.5731157532357	3.67292915087126
Median	3258.583479	1945
Standard Deviation	6630.40330990176	45.4316245333571
Sample Variance	43962248.0519562	2064.03250773994
Kurtosis	4.77203074137582	-1.08436364978744
Skewness	2.03347130343245	-0.0838680587457871
Range	40568.739095459	163
Minimum	1.630634541	1858
Maximum	40570.36973	2021
Sum	37130062.6700161	297486
Count	6943	153

TABLE I  
DESCRIPTIVE ANALYSIS OF DATA

not only provides insights into both short-term and long-term dynamics but also helps uncover the causal connections between industrial development, energy consumption, and carbon emissions.

To gain a deeper understanding of the evolving relationships between these variables and to make more informed predictions about their future trends, we express them in a growth form. This form allows us to track changes over time relative to the previous period, offering valuable insights into potential future movements. In contrast, a straightforward ratio form only provides data for the current period.

Our research employs time series-based models to forecast CO<sub>2</sub> emissions for the upcoming years in all SAARC nations. The dataset exhibits stationarity with a clear upward trend. In this study, we implement advanced deep learning models, including LSTM and attention-based LSTM, tailored to the unique characteristics of this dataset.

#### B. Data Preprocessing

The datasets encompass 26 factors such as GDP, population, cement-related CO<sub>2</sub> emissions, gas production, and land use changes, along with per-capita CO<sub>2</sub> production trends over time. We conducted data cleaning by removing values with missing data points exceeding 50 per cent, primarily those before 1950. For the remaining missing data, we utilised interpolation and next-value fill methods from the pandas library. To enhance the data for LSTM training, we upsampled it and converted it into monthly data using the 'M' keyword within the pandas resample() library. This transformation ensured the data's consistency and suitability for LSTM modelling. To predict next year's per capita CO<sub>2</sub> production, we utilised data from the preceding three years, converting it into training samples. Furthermore, we partitioned the data by country, introducing a separation between adjacent data elements. This approach resulted in a multivariate time series dataset, on which we meticulously applied LSTM and LSTMs, as elaborated in the subsequent sections. During our analysis of carbon emissions across SAARC countries, we observed a consistent upward trend in carbon emissions across all countries within the SAARC region. However, it's important to note that these emission trends are not uniform across the region, which poses a significant challenge in developing a suitable model for joint

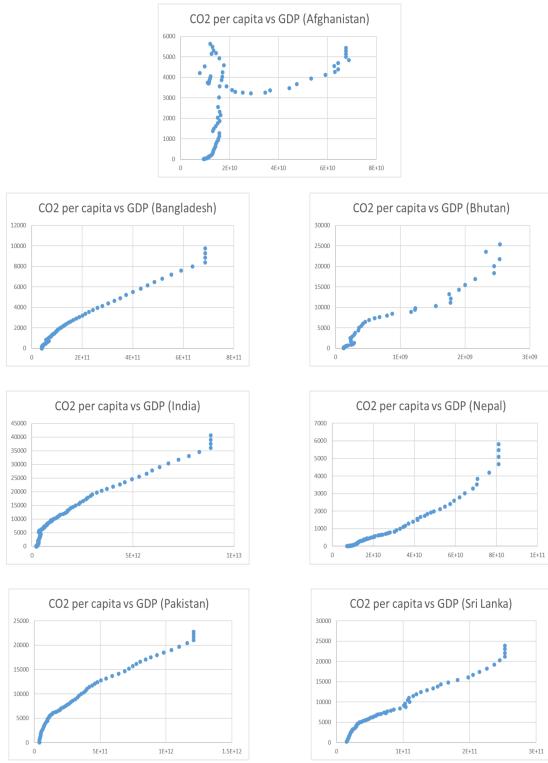


Fig. 1. Country wise GDP vs CO<sub>2</sub> emission per capita

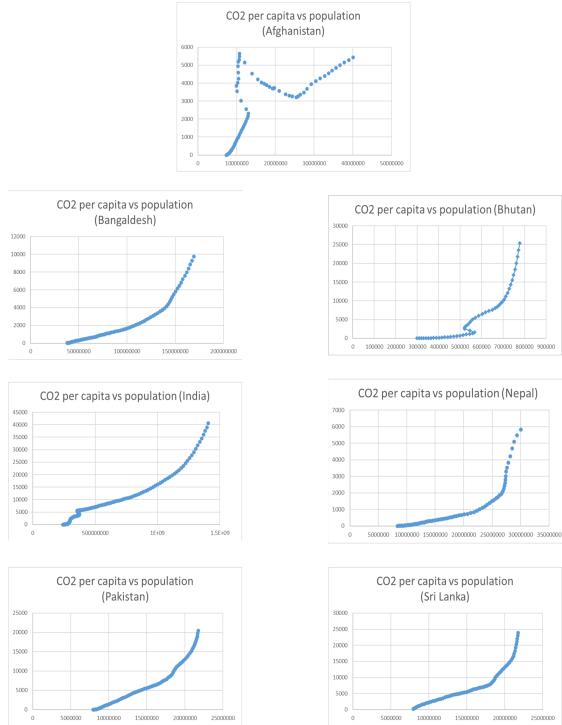


Fig. 2. Country wise Population vs CO<sub>2</sub> emission per capita

analysis and forecasting of carbon emissions for these diverse nations.

Figures 1 and 2 depict the correlation between carbon emissions and GDP per capita as well as population growth for the seven major SAARC countries.

Table 1 offers a descriptive analysis of the preprocessed CO<sub>2</sub> emission dataset. By examining the minimum, maximum, and median values, it becomes evident that carbon emissions are consistently increasing.

### C. Long Short Term Memory

Recurrent neural networks (RNNs) are a class of artificial neural networks that are particularly good at processing time series data because the nodes between the hidden layers are connected. Although RNN may potentially capture long-distance dependence, when the time step is increased, it is simple to produce gradient explosion or disappearance when the backpropagation method updates the weights. Gradient explosion may hinder network convergence during training and may potentially result in network failure, and the gradient's removal will make it more challenging for networks to learn long-distance dependence. Gradient clipping can prevent gradient explosion, which is a pretty simple problem to manage. The key to understanding RNN and nearly all other deep learning techniques is understanding how to minimise gradient vanishing. Hochreiter and Schmidhuber (1997) first proposed the LSTM, and Alex Graves most recently made improvements to it. The gradient disappearance issue is resolved by LSTM by creating a complex network structure. Figure 3 illustrates the

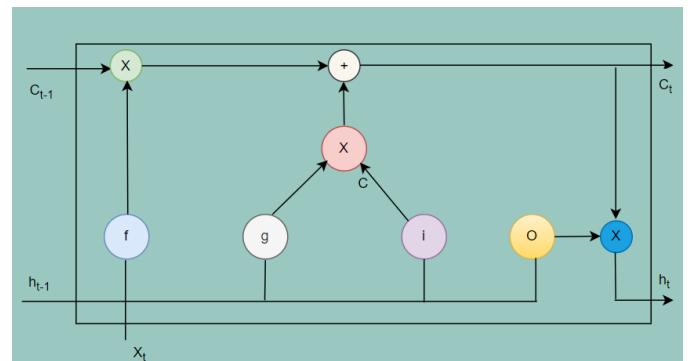


Fig. 3. LSTM architecture

fundamental architectural arrangement of an LSTM. Within the LSTM cell, it receives inputs: the current variable  $x_t$ , the preceding output  $h_{t-1}$ , and the prior cell state  $C_{t-1}$ . The components, namely the input gate ( $i_t$ ), forget gate ( $f_t$ ), output gate ( $o_t$ ), and memory cell ( $C_t$ ), are represented as small boxes [3]. These components are computed utilizing equations 1 through 5.

$$f_t = \sigma_g (W_f \cdot x_t + U_f \cdot h_{t-1} + b_f) \quad (1)$$

$$i_t = \sigma_g (W_i \cdot x_t + U_i \cdot h_{t-1} + b_i) \quad (2)$$

$$o_t = \sigma_g (W_o \cdot x_t + U_o \cdot h_{t-1} + b_o) \quad (3)$$

$$\tilde{C}_t = \tanh(W_C \cdot x_t + U_C \cdot h_t - 1 + b_C) \quad (4)$$

In this context, the symbol  $\cdot$  signifies the matrix multiplication operation, while  $b_f$ ,  $b_i$ ,  $b_o$ , and  $b_C$  correspond to four bias vectors. The weight matrices  $U_f$ ,  $U_i$ ,  $U_o$ , and  $U_C$  establish connections between the previous output and the three gates as well as the memory cell. Similarly, the weight matrices  $W_f$ ,  $W_i$ ,  $W_o$ , and  $W_C$  are associated with these gates. The gate activation function denoted as  $\sigma_g$ , is specifically a sigmoid function, and the function  $\tanh()$  refers to the hyperbolic tangent function, as indicated in reference [3] and demonstrated in equations 5 and 6.

$$C_t = (f_t \oplus C_{t-1}) + i_t \oplus \tilde{C}_t \quad (5)$$

$$h_t = o_t \oplus \tanh(C_t) \quad (6)$$

where  $\oplus$  denotes the element-wise matrix/vector, multiplication operator.

#### D. Proposed Framework

The task of predicting CO<sub>2</sub> emissions is a formidable challenge that engages climate change experts and meteorological departments worldwide. In recent years, a multitude of strategies has evolved to anticipate CO<sub>2</sub> output, and our research framework, depicted in Figure 4, encapsulates these endeavours. We commence with data collection from sources such as OWID and World Bank indicators, followed by a meticulous data preprocessing phase. This encompasses handling missing values, selecting relevant features, normalizing data, and implementing resampling techniques. Subsequently, we partition the dataset into an 80:20 split for training and testing purposes. The heart of our study lies in the development of predictive models, employing both LSTM and Attention-based LSTM architectures. These models undergo rigorous training and fine-tuning, culminating in a meticulous assessment of their performance through a range of performance evaluation metrics. Our overarching goal is to leverage the predictive capabilities of these models to forecast CO<sub>2</sub> emissions, an imperative facet of environmental research with far-reaching implications.

#### E. Proposed Model

Human perception is unique in that it prioritises the relevant aspects of the environment in order to get the information they require rather than dealing with all external stimuli at once. Likewise, within financial markets, the significance of different trading information varies significantly. While certain information may be redundant, other data points could be of paramount importance [11]. In order to anticipate CO<sub>2</sub> emissions, we also need to prioritise important features over less important ones. "Hence, we propose an Attention Mechanism-based Long Short-Term Memory model as a predictive tool capable of synthesizing and utilizing valuable information from multiple temporal contexts to inform decision-making." The data suggests using an attention model to improve input sequences for CO<sub>2</sub> emission predictions. This mechanism maps queries and key-value pairs to outputs, all represented

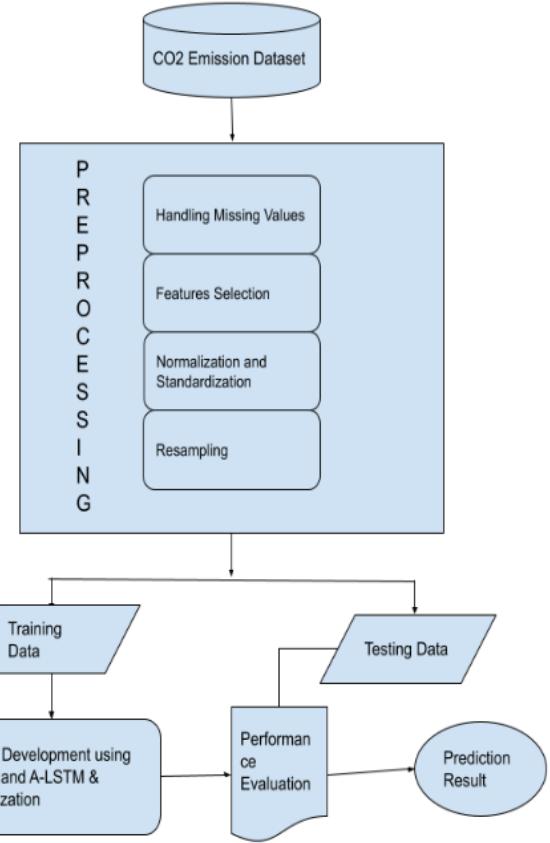


Fig. 4. Framework for CO<sub>2</sub> emission forecasting

as vectors. [11]. The result is calculated as a weighted sum of the values, with each value's weight determined by the query's compatibility function with its corresponding key. The attention weight generation and attention-based new input features are summarised in Figures 5 and 6. In the initial step, we establish a mapping from  $x_t$  to  $f_t$  as follows:  $h_t = f_1(f_{t-1}, x_t)$ . Here,  $f_t$  represents a non-linear activation function, and  $h_t \in \mathbf{R}^s$  denotes the hidden state at time t, where ' $s$ ' signifies the size of the hidden state. In this context, we employ LSTM as the function  $f_1$  to mitigate the long-term dependence issue often encountered in time series prediction. Subsequently, we construct an attention mechanism utilizing a deterministic attention model. For a given feature sequence  $\mathbf{x}^k = (x_1^k, x_2^k, \dots, x_m^k)^T \in \mathbf{R}^m$ , we define the input feature sequence using equation 7, while the attention weight is established in equation 8 by referencing the preceding hidden state  $h_{t-1}$  and cell state  $C_{t-1}$  within the LSTM unit.

$$\alpha_t^k = \mathbf{v}^T \tanh(\mathbf{W}_1 \cdot [h_{t-1}, C_{t-1}] + \mathbf{W}_2 \mathbf{x}^k) \quad (7)$$

$$\beta_t^k = \text{softmax}(\alpha_t^k) = \frac{\exp(\alpha_t^k)}{\sum_{i=1}^n \exp(\alpha_t^k)} \quad (8)$$

"The vector  $\mathbf{v}$  and the matrices  $\mathbf{W}_1$  and  $\mathbf{W}_2$  are adjustable parameters within the model. The vector  $\alpha^k$  consists of 'm' elements, where each 'i'-th element quantifies the significance

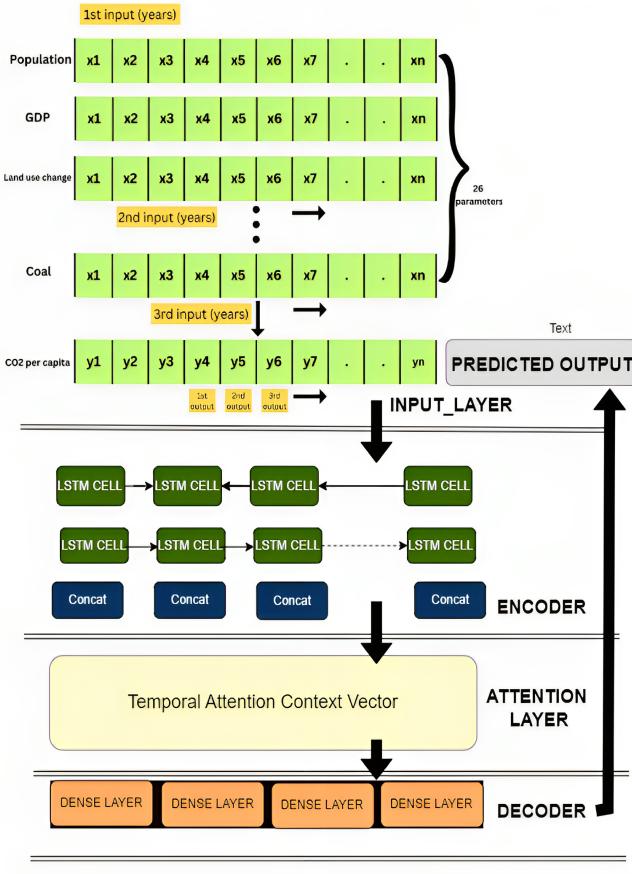


Fig. 5. Proposed Attention-based Long Short Term Memory

of the ' $k$ '-th input feature sequence at time ' $t$ '. These values are normalised using softmax [12]. Additionally,  $\beta_t^k$  serves as an attention weight, encapsulating a score that determines the degree of attention directed towards the ' $k$ '-th feature sequence. Equation 9 provides the expression for the weighted input feature sequence  $z_t$ , at time ' $t$ ', which represents the output of the attention model.

$$z_t = (\beta_t^1 x_t^1, \beta_t^2 x_t^2, \dots, \beta_t^n x_t^n)^T \quad (9)$$

Now  $x_t$  is replaced by the newly computed  $z_t$  to update the attention model and finally raw time series is converted into attention-based time series.

#### F. Performance metrics

In this section, the performance metrics are used to determine the effectiveness of the proposed model. There are many evaluation metrics; we have used four to evaluate the models' effectiveness. Training and test sets of the data are created where the Training set (80 per cent of the data set) was used to train all models and the remaining 20 per cent was used to test the model. The MSE, RMSE, MSLE, MAPE and R-2 score values for the training and test sets have been assessed. We have also showcased a comparative analysis

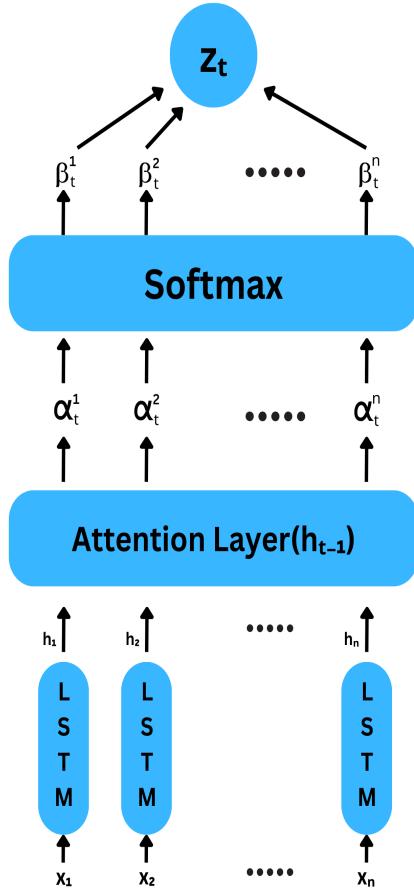


Fig. 6. Attention-based Long Short Term Memory

between the performance evaluation metrics of the proposed A-LSTM model and those of the baseline LSTM model.

1) *Mean Absolute Error (MAE)*: MAE is the average of the absolute difference between forecasted values and true values. The MAE shows us how much inaccuracy we should expect from the forecast on average. The model with the lowest MAE is superior when comparing many models. MAE can be calculated by using equation 10.

$$\text{MAE} = \frac{\sum_{i=1}^n |y_i - \hat{y}_i|}{n} \quad (10)$$

Where  $\hat{y}$  is the predicted value and  $y_i$  is the actual value. The letter n represents the total number of values in the test set.

2) *Mean Squared Error (MSE)*: Mean squared error is the average of the square of the difference between the predicted values and true values. It has the same units as the true and predicted values squared and is always positive. MSE can be calculated by using Equation 11.

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 \quad (11)$$

Where  $\hat{y}$  is the predicted value,  $y_i$  is the actual value, and n is the total number of values in the data sets.

3) *Mean Absolute Percentage Error(MAPE)*: The calculation of MAPE (Mean Absolute Percentage Error) plays a crucial role in enhancing the precision of forecasts for future projects. When a MAPE calculation indicates that the existing forecasting is inaccurate, it prompts the possibility of revising strategies or even adopting entirely new methods. Furthermore, MAPE calculations are valuable for pinpointing when forecasting is accurate, enabling more effective communication of forecasting results and the implementation of sound strategies. MAPE can be calculated by using equation 12.

$$MPE(y, \hat{y}) = \frac{100\%}{N} \sum_{i=0}^{N-1} \frac{|y_i - \hat{y}_i|}{y_i}. \quad (12)$$

4) *Root Mean Square Error(RMSE)*: RMSE (Root Mean Square Error) is a widely utilised metric in fields such as climatology, forecasting, and regression analysis to validate experimental findings. It quantifies the standard deviation of prediction errors or residuals. These residuals represent the extent to which data points deviate from the regression line. RMSE, in essence, provides insight into how these residuals are distributed, indicating how closely the data points cluster around the line of best fit. RMSE can be calculated by using equation 13.

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (f_i - o_i)^2} \quad (13)$$

#### IV. EXPERIMENTS AND RESULTS

##### A. Implementation Architecture

The experiments are carried out in Jupyter Notebook using Python 3.7.13. Open-source libraries like Pandas 2.1.1, Numpy 1.19.3, Keras and Tensorflow 2.0+ are used for experimentation. The experimental setup is based on a working environment having a Ryzen 7 5800-H processor with 16 GB RAM under a 64-bit Windows 11 Operating system. Time series forecasting of the CO<sub>2</sub> emissions dataset is modelled using two deep learning models, namely, LSTM and LSTM with Attention (referred to as A-LSTM). The optimum results are considered from each model's ten unique runs. The chosen architecture of both the models is briefed as follows:

The model architecture relies on LSTM units for sequence modelling. It consists of two fully connected layers, each with 64 neurons, followed by a dense layer. The ReLU activation function is used for each layer. Optimisation is done using ADAM with a learning rate of 1e-4 and a decay of 1e6. Training employs the MAE loss metric and a 20% validation split. To combat overfitting, a 0.1 dropout rate is applied after the second fully connected layer. Batch size 32 is found to be optimal for performance and robustness.

In the proposed A-LSTM model, we introduce a 64-unit attention layer between the LSTM layer and the dense layer. Hence, we have a 64-neuron LSTM layer followed by the attention layer and the dense layer. The learning rate, loss metric, optimiser, decay rate and batch size are the same as LSTM for a comparative study.

##### B. Performance Analysis

Table II displays the experimental outcomes achieved through the application of both the LSTM model and the proposed A-LSTM model. The results unmistakably indicate substantial enhancements in the proposed model compared to the baseline. Table III illustrates a comparison between the

	MAE	MSE	MAPE	RMSE
LSTM	0.227	0.0246	24.968	0.34
<b>A-LSTM</b>	<b>0.056</b>	<b>0.0115</b>	<b>10.5902</b>	<b>0.107</b>

TABLE II  
EXPERIMENTAL RESULTS

experimental results obtained and those acquired in [5]. The findings indicate that A-LSTM surpasses LSTM, GRU, and Bi-LSTM in both Mean Squared Error (MSE) and Mean Absolute Percentage Error (MAPE).

Fine-tuning was performed on both LSTM and A-LSTM

Models	Performance Parameters	
	MSE	MAPE
LSTM	0.0246	24.968
GRU [5]	0.027	26.11
Bi-LSTM [5]	0.0242	24.72
<b>A-LSTM [proposed]</b>	<b>0.0115</b>	<b>10.5902</b>

TABLE III  
COMPARISON OF EXPERIMENTAL RESULTS

models, given that their performance is highly dependent on parameter adjustments. Particular attention has been given to calibrating the parameters of the LSTM forecasting model due to its more intricate structure compared to other deep learning models. We manually adjusted all hyperparameters through trial and error, optimizing the number of hidden layers and neurons for both deep learning models to achieve the best results. Across all models, a learning rate of 0.0001 consistently yields higher accuracy. To prevent over-fitting and enhance model efficiency, we've implemented an early stopping strategy.

We gave importance to dropout due to the over-fitting nature of the data. We tried different dropout settings in the LSTM architecture. We found out that a dropout of 0.1 after the second layer was the optimum setting with the loss metric as MAE as shown in Table 3. Hence, we used this in our final model architecture. In comparing the performance of

Dropout configuration	Training MAE	Validation MAE
Two dropouts (0.6 each)	0.148	0.244
Two dropouts (0.2 each)	0.1	0.23
Dropout of 0.2 after first layer	0.03	0.31
Dropout of 0.1 after first layer	0.06	0.27
Dropout of 0.1 after second layer	0.05	0.24
No Dropout	0.01	0.32

TABLE IV  
LOSS METRIC (MAE) EVALUATION IN DIFFERENT DROPOUTS

the LSTM and A-LSTM models, we observed significant differences across multiple evaluation metrics. The LSTM model exhibited a Mean Absolute Error (MAE) of 0.227, a Mean Squared Error (MSE) of 0.0246, a Mean Absolute

Percentage Error (MAPE) of 43.6, and a Root Mean Squared Error (RMSE) of 0.34. In contrast, the A-LSTM model displayed notably superior results, with a substantially lower MAE of 0.056, a significantly reduced MSE of 0.0115, a remarkably improved MAPE of 10.5902, and a substantially lower RMSE of 0.107. These metrics collectively demonstrate that the A-LSTM model outperforms the LSTM model in terms of accuracy and precision, showcasing its superior predictive capabilities in forecasting CO<sub>2</sub> per capita across various countries over multiple years.

In Figure 7, 8, we presented the validation and training loss values for both LSTM and A-LSTM models. Furthermore, we evaluate the predictive proficiency of the models by analyzing how effectively they forecast CO<sub>2</sub> emissions per capita across the countries specified in the dataset over various years. The superior performance of the A-LSTM model is evident in the results illustrated in Figure 8,9. Furthermore, we provide a comprehensive comparison of the training and testing loss for both the LSTM and A-LSTM models in Figure 9,10 to evaluate their overall performance. Figure 11 displays the final predicted CO<sub>2</sub> emission outcomes for each of the seven SAARC nations.

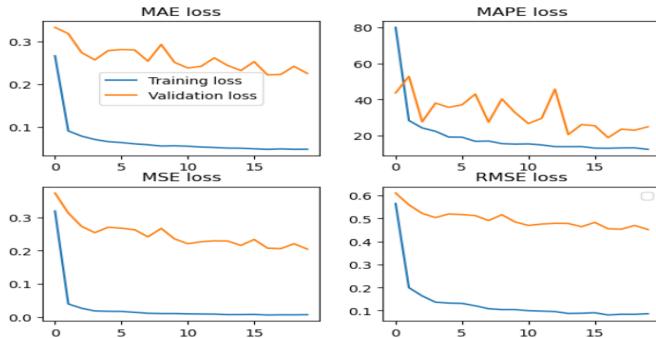


Fig. 7. LSTM Loss

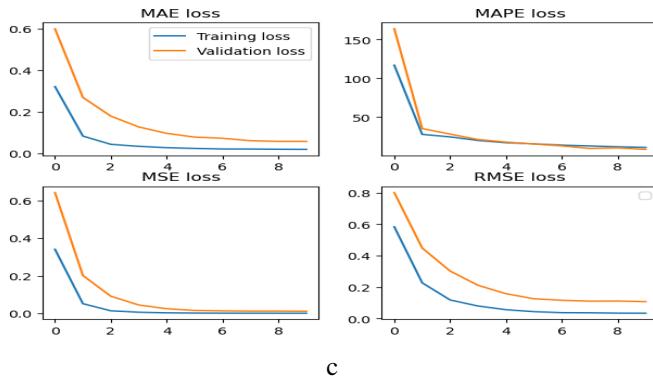


Fig. 8. A-LSTM LOSS

## V. CONCLUSION AND FUTURE RESEARCH DIRECTIONS

In conclusion, our study delved into the critical task of forecasting carbon dioxide (CO<sub>2</sub>) emissions, an imperative endeavour to address the pressing issue of climate change and global

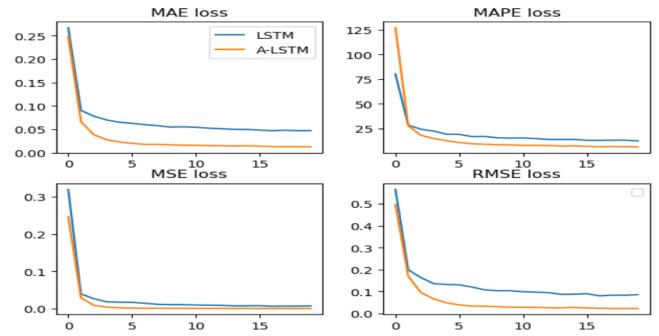


Fig. 9. Training loss comparison of LSTM and A-LSTM

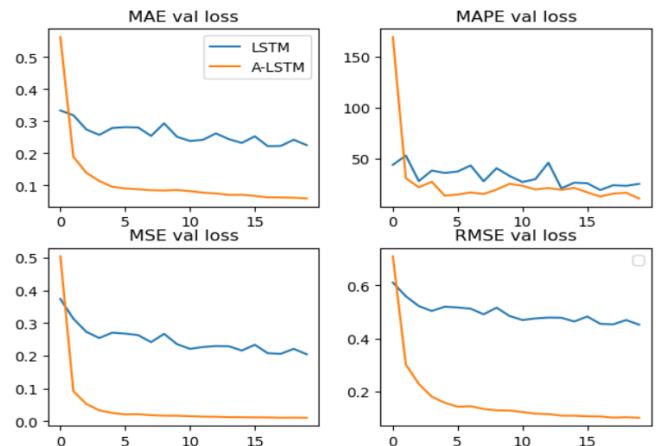


Fig. 10. Validation loss comparison of LSTM and A-LSTM

warming. With international commitments calling for substantial reductions in CO<sub>2</sub> emissions, our research introduced an innovative predictive framework leveraging an Attention-based Long Short-Term Memory (A-LSTM) architecture. This A-LSTM model, which incorporates an attention mechanism to allocate computational resources efficiently, outperformed the baseline LSTM model across various evaluation metrics. The LSTM model had limitations, with a MAPE of 24.968 and an RMSE of 0.34, while the A-LSTM model demonstrated superior performance with a lower MAPE of 10.5902 and RMSE of 0.107 with 57% improvement in MAPE loss. These results highlight a notable enhancement in predictive accuracy when compared with the existing models LSTM, GRU and Bi-LSTM [5], accomplished through the application of attention mechanisms within the context of the carbon emission dataset examined in this research. This outcome bears noteworthy implications and provides valuable insights, particularly for a diverse set of predictive modelling applications, with a strong focus on forecasting CO<sub>2</sub> emissions and understanding their impact on sustainable development.

While our study primarily centres on SAARC countries, its implications extend far beyond this region. The discoveries made herein can serve as a viable blueprint for reshaping energy consumption practices globally, ultimately leading to

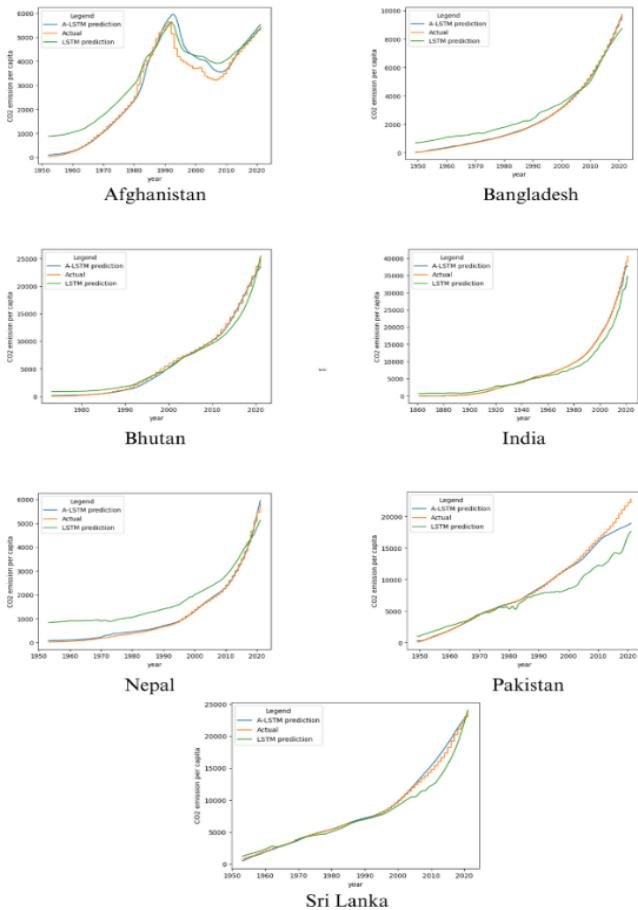


Fig. 11. Country wise prediction of CO<sub>2</sub> via LSTM and A-LSTM

a reduction in CO<sub>2</sub> emissions worldwide. In the future, this study has the potential for expansion, exploring the benefits and practical applications of quantum-enhanced LSTM and A-LSTM models for multivariate time series prediction.

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