Jutorial 4:-

$$\frac{\text{dol1:}}{\text{T(n)}} = 3T(n/2) + n^2$$

$$c = \log_{1.58}^{0}$$

= $\log_{2.3} = 1.58$.

$$\Rightarrow n^{c} = n^{1.58}$$
Which is $n^{2} \times h^{1.58}$

$$\Rightarrow$$
 $T(n) = O(n^2)$

$$\pm 012$$
: $T(n) = 4T(n/2) + n^2$

$$a=4$$
 $b=2$ $f(n)=n^2$

... a quater's theorem is applicable.

$$c = \log_6 a$$
 $= \log_2 4 = \log_2 2^2 = 2 \log_2 2 = 2$.

$$n^c = n^2$$

$$n^{c} = \beta(n)$$

$$\Rightarrow T(n) = O(n^2 \log n)$$

$$\frac{443 - T(n) - T(n/2) + 2^n}{a = 1}$$

$$a = 1$$

$$b = 2$$

$$f(n) = 2$$

a=1 b=2 $f(n)=2^n$ is a & b are constant and fin) is a +we function

.. Master's theorem is applicable.

$$C = \log_b a = \log_2 1$$

$$\Rightarrow$$
 $n^c = n^o = 1$.

.. can 3 is applied here.

$$\Rightarrow T(n) = O(2^n)$$

$$4014:-T(n)=2^{n}T(n/2)+n^{n}$$

$$a=2^{n} b=2 F(n)=n^{n}$$

« à u not constant, its value dépends en n.

=: Master's unessem i not applicable here.

$$a = 16 = 6 = 4$$
 f(n) = n.

or a è b are constant and fin) is a +u function

$$\Rightarrow n^c = n^2$$

: case I is applied here.

$$T(n) = \theta(n^2)$$

Sol6: Tin) = 2 Tin/2) + n log n a=2 b=2 $f(n)=n\log n$ a, b are constant and fin) is a +us function & c= logs a = log_2 2 - 1. n'= h!= n "; f(n) > h" : case 3 is applied. > T(n) = 0 (n logn) 10/7: T(n) = 2 T(n/2) + n/logn. $a = 2 b = 2 f(n) = n/\log n$: a and b are constant & fent is a + ne function c= logba = lag 2 = 1. " Jusp : de non-polynomial difference b/w fin) à n° .. Master's theorem is not applicable. 8018:-T(n) = 2 T(n/4) + n0.51. $f(n) = n^{0.51}$ a=2 b=4" a & b are constant & f(n) is a +re function .. Master's theorem is applicable. C = logs a = log42 = 0.50. if(n) > nc

· · case 3 is applicable Tin) = 0 (n0.51) 5019:- T(n) = 0.5 T(n/2) + /n a a = 0.15 b = 2 f(n) = yn. " a ia < 1 : Master's theorem is not applicable. Lelso: - T(n) = 16 T(n/4) + h! a = 16 b = 4 f(n) = n!i a à b are const à f(n) is a tre function. .. Master's theorem is applicable $= \log_4 16 = \log_4 4^2 = 2 \log_4 4 = 2$ New C = logga n = n2. : f(n) > h : case 3 is applied here. $\sqrt{T(n)} = O(n!)$ \$0111:- T(n) = 4T(n/2) + logn. a=4 b=2 f(n)= lign. : a è b are constant è fin) is a tre function :. Master's theorem is applicable c = logga = log2 4 = leg222 = 2 log22 = 2.

": f(n) < n' $\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}$ in case I is applied Sol 12 - In Tinge + Logn $a = \sqrt{n}$ b = 2 $f(n) - \log n$ " a fi b we constant of find is a the function in Master & theorem is applicable c-logha - log : a is not constant .. Master's theorem is not applicable 10/14:- T(n) = 3T(n/3) + In $a = 3 \quad b = 3 \quad f(n) = \sqrt{n}$ "a q b are constant à for) is a + re function · " Master's theorem is applicable $c = \log_{6} a = \log_{3} 3 = 1$. $n^c = n^t = n$ " f(n) < nc .. case I is applicable 1=) Th) = 0(n) 1 10/13:- T(n) = 3T(n/2)+n a = 3 b = 2 f(n) = n« a à bare constant & f(n) is a +ue function " Master's theorem is applicable c = logba = log23 = 01.58

Solf:
$$T(n) = 3T(n/3) + n/2$$
 $a = 3$ $b = 3$ $f(n) = n/3$
 $a = 3$ $b = 3$ $f(n) = n/3$
 $a = 4$ a

$$50125 - T(n) = 7T(n/3) + n^2$$

 $a = 7 b = 3 f(n) = n^2$

$$c = \log_{1} 6a = \log_{3} 7 = 177$$
 $n = n^{177}$

$$\Rightarrow T(n) = O(n^2)$$

$$\frac{20122}{T(n)} = \frac{T(n|_2) + n(2 - (0sn))}{1 - (0sn)}$$