



Birla Institute of Applied Sciences

विरला इंस्टिट्यूट ऑफ़ अप्लाइड साइंसेस

Bhimtal, Distt: Nainital, Uttarakhand- 263136

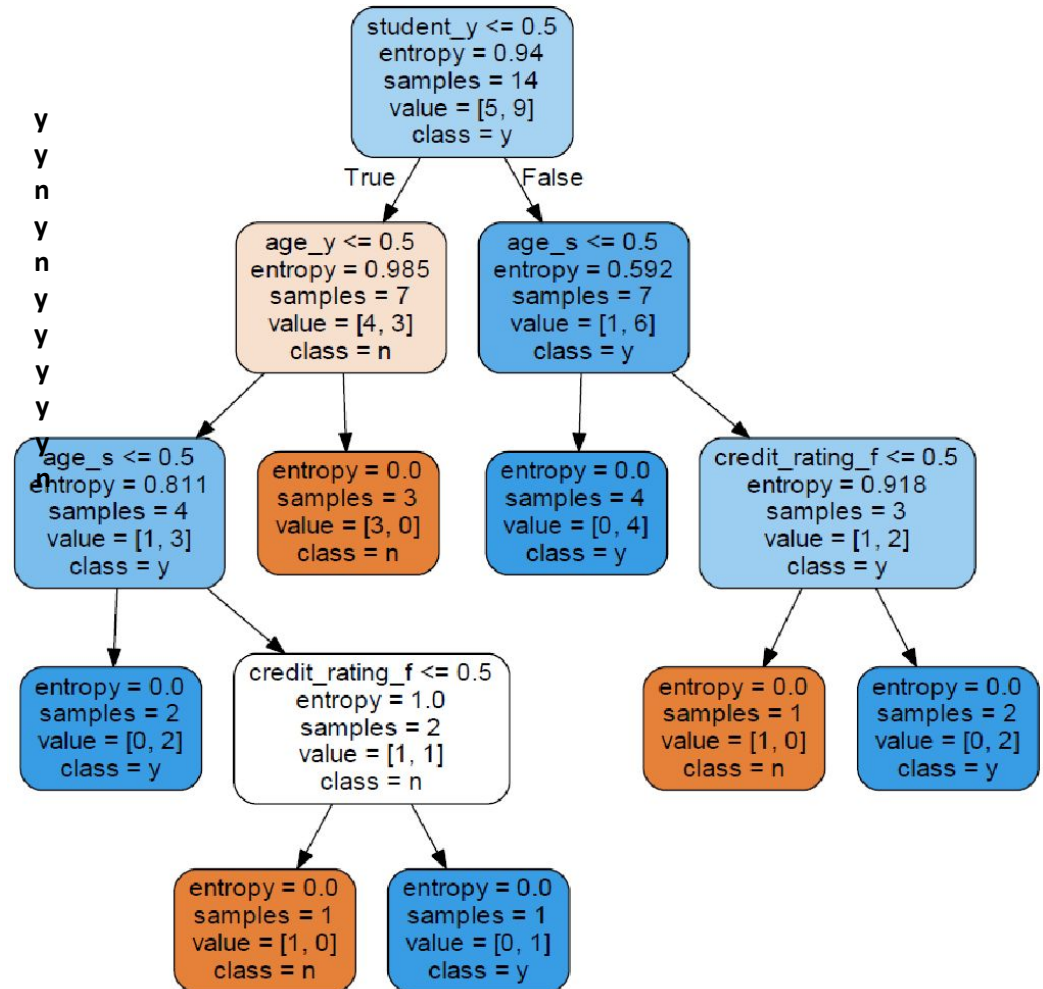
Pattern Recognition

- S. S. Samant

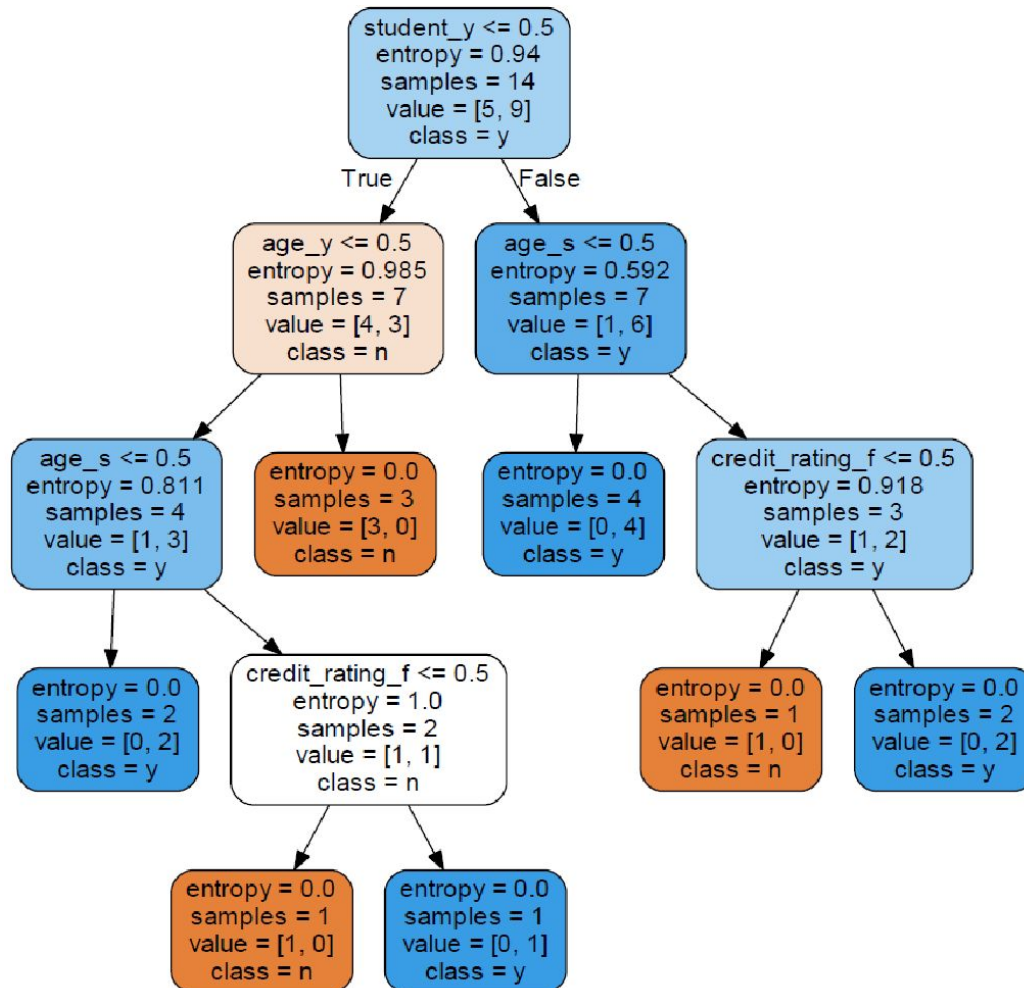
Attribute Selection Measures

	age_s	age_y	credit_rating_f	income_l	income_m	student_y	Class
0	0	1	1	0	0	0	n
1	0	1	0	0	0	0	
2	0	0	1	0	0	0	
3	1	0	1	0	1	0	y
4	1	0	1	1	0	1	y
5	1	0	0	1	0	1	n
6	0	0	0	1	0	1	y
7	0	1	1	0	1	0	n
8	0	1	1	1	0	1	y
9	1	0	1	0	1	1	y
10	0	1	0	0	1	1	y
11	0	0	0	0	1	0	y
12	0	0	1	0	0	1	

RID	age	income	student	credit_rating	Class: buys_computer
1	youth	high	no	fair	no
2	youth	high	no	excellent	no
3	middle_aged	high	no	fair	yes
4	senior	medium	no	fair	yes
5	senior	low	yes	fair	yes
6	senior	low	yes	excellent	no
7	middle_aged	low	yes	excellent	yes
8	youth	medium	no	fair	no
9	youth	low	yes	fair	yes
10	senior	medium	yes	fair	yes
11	youth	medium	yes	excellent	yes
12	middle_aged	medium	no	excellent	yes
13	middle_aged	high	yes	fair	yes
14	senior	medium	no	excellent	no



Decision Tree Pruning

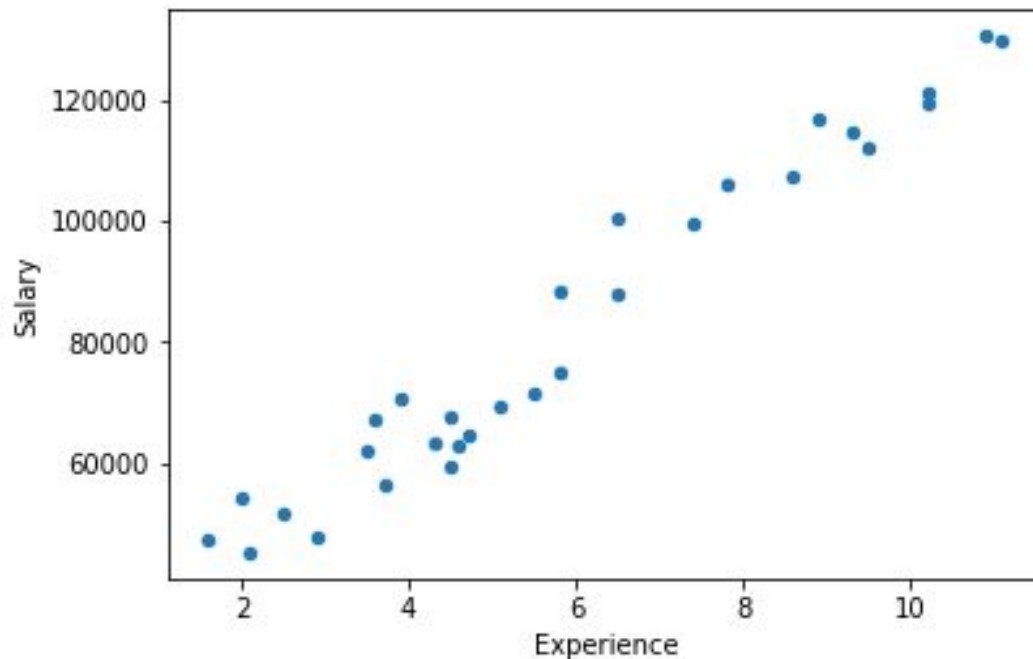


Logistic Regression

Let us briefly look at linear regression

In linear regression, we want to predict a number.

Ex. Given a training set containing *years of experience* and *salary*, fit a line and use it to predict the *salary* of a person given his/her years of experience. In this case, salary is the *dependent* variable and *years of experience* is *independent* variable.

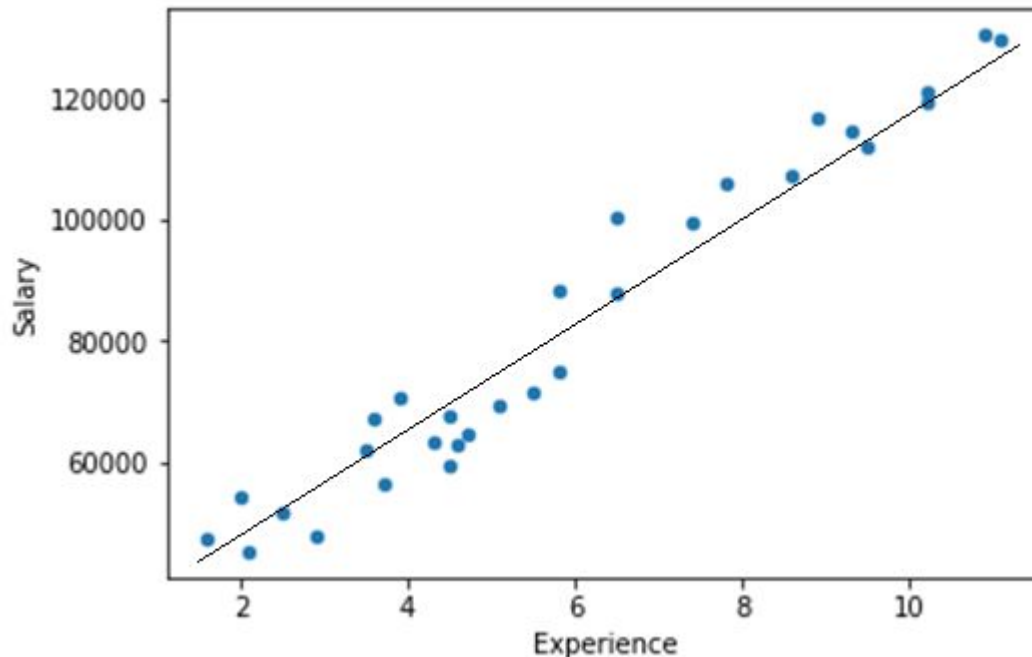


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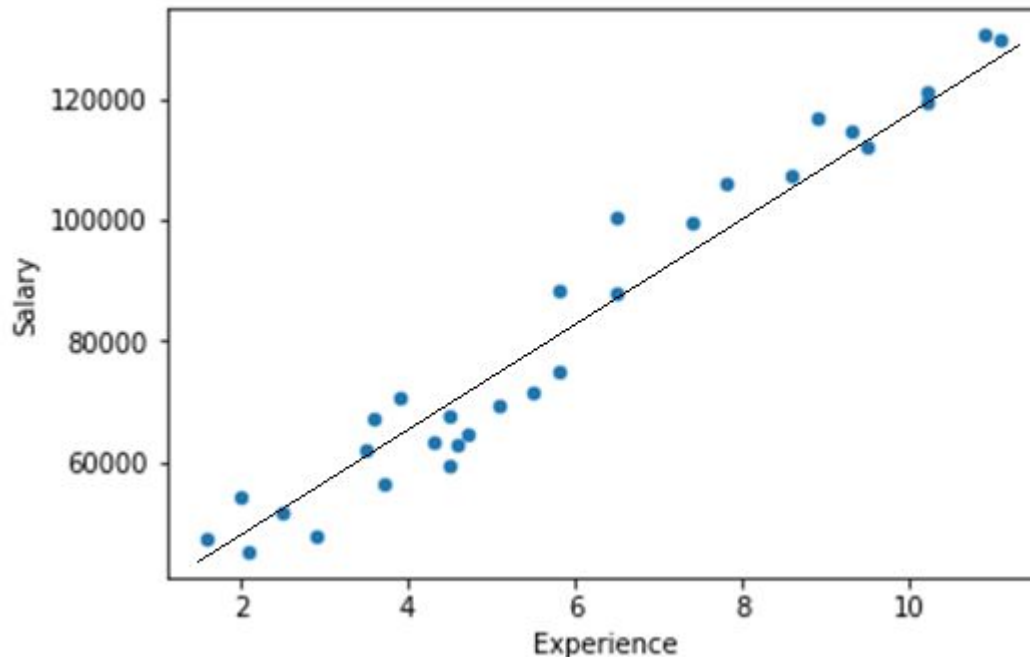


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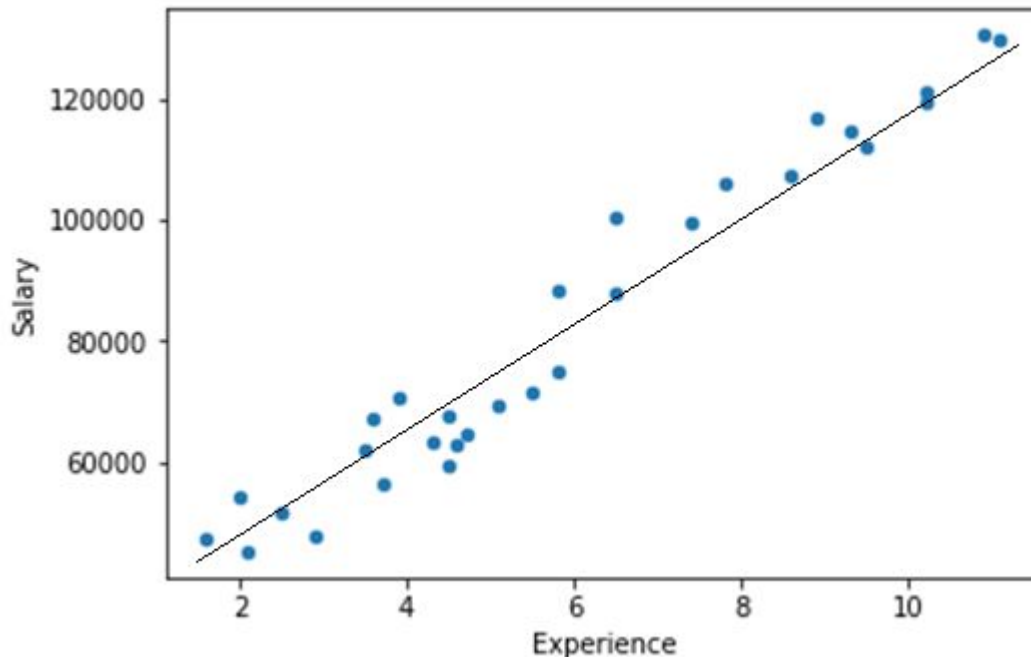
$$y = \beta_0 + \beta_1 x_1$$

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$$y = \beta_0 + \beta_1 x_1$$

Can we use linear regression for classification?

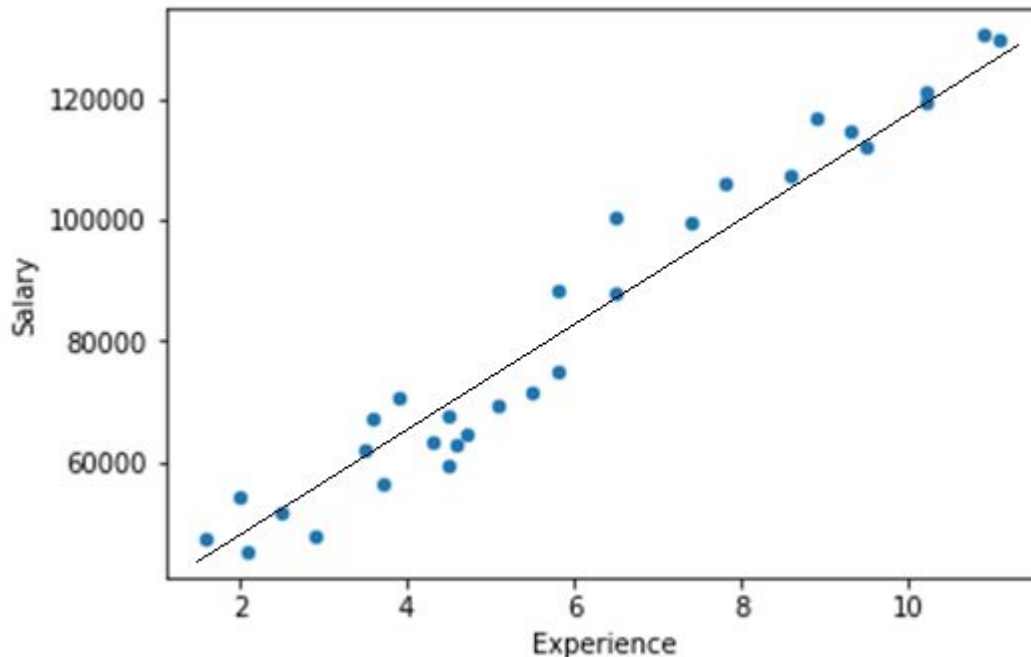
Problem: y has values greater than 1 or less than 0. For ex. we cannot use the above for binary classification

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$$y = \beta_0 + \beta_1 x_1$$

Can we use linear regression for classification?

Solution: Use a function that can bring any number to range (0,1). Then we can use the function to classification.

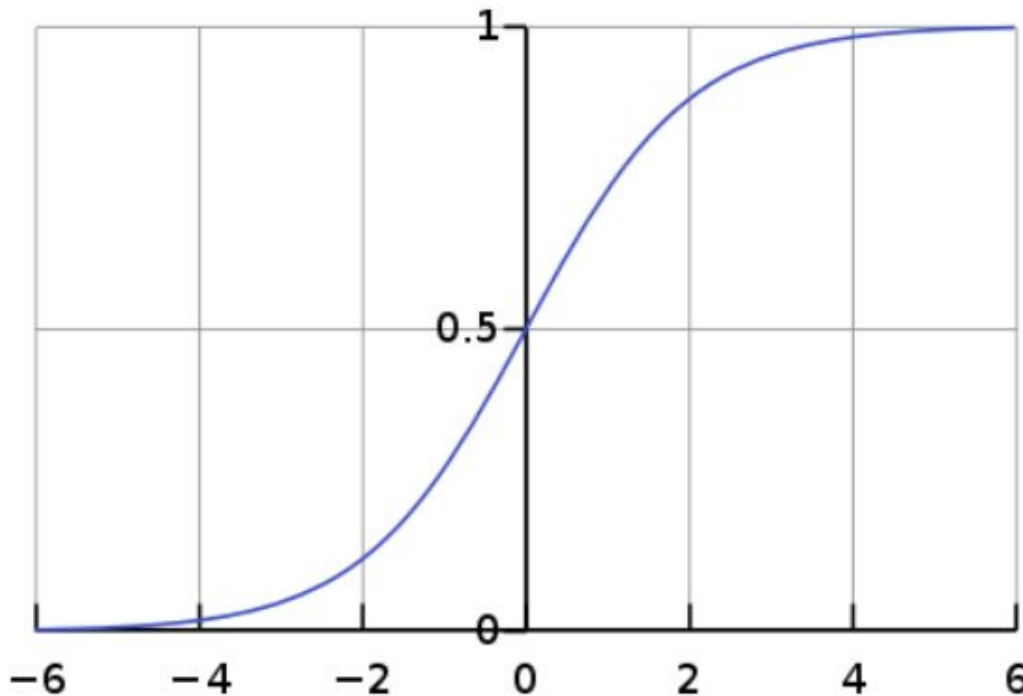
Logistic Regression

The function is called *logistic* function or *sigmoid* function.

$$\sigma(t) = \frac{e^t}{e^t + 1} = \frac{1}{1 + e^{-t}}$$

Here, $y = t = \beta_0 + \beta_1 x_1$

$$\sigma(t) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x)}}$$



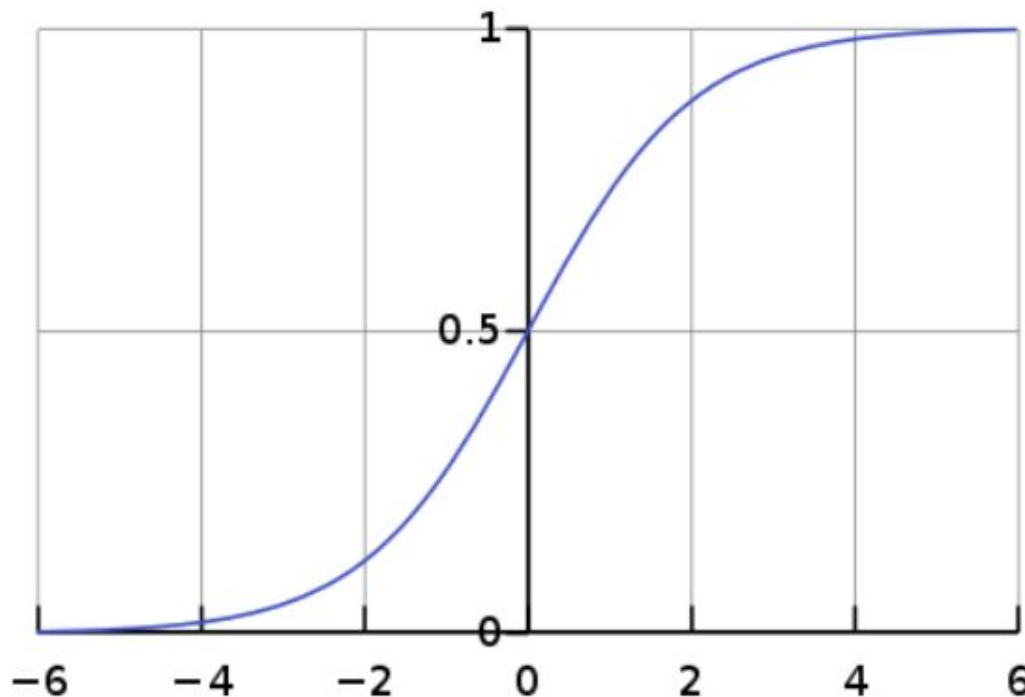
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The function is called logistic function or sigmoid function.

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How do you classify using the above function?

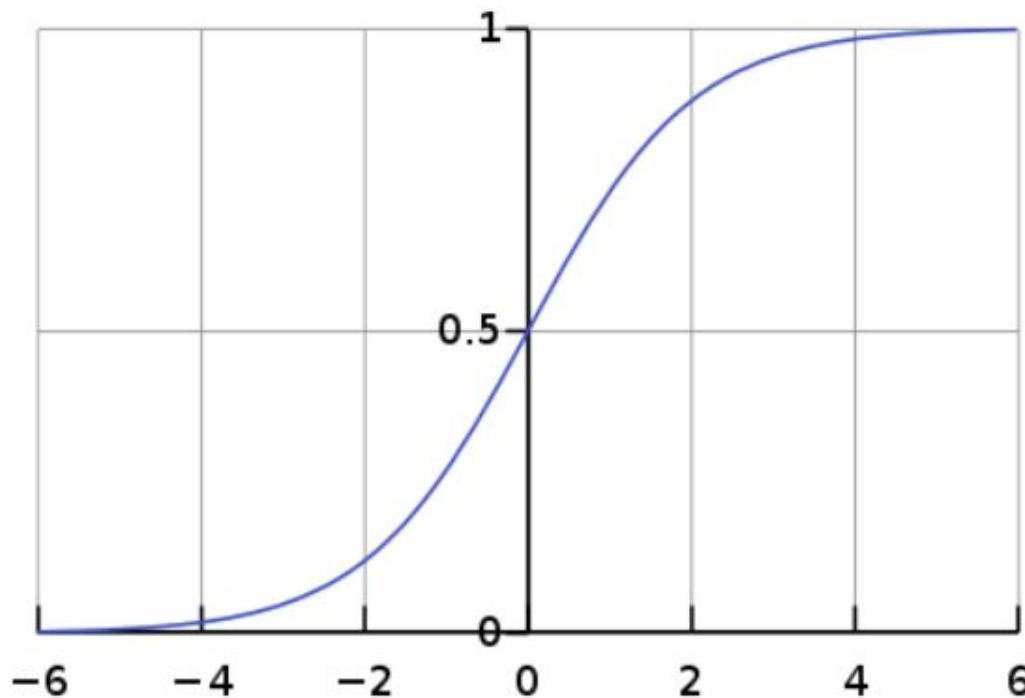
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Here, $y = t = \beta_0 + \beta_1 x_1$

$$\sigma(t) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x)}}$$



How do you classify using the above function?

We will use the value of $\sigma(t)$ as probability of $y=1$ given input x , OR in other words:

$$P(y=1 | \beta; x)$$

Logistic Regression

The function is called logistic function or sigmoid function.

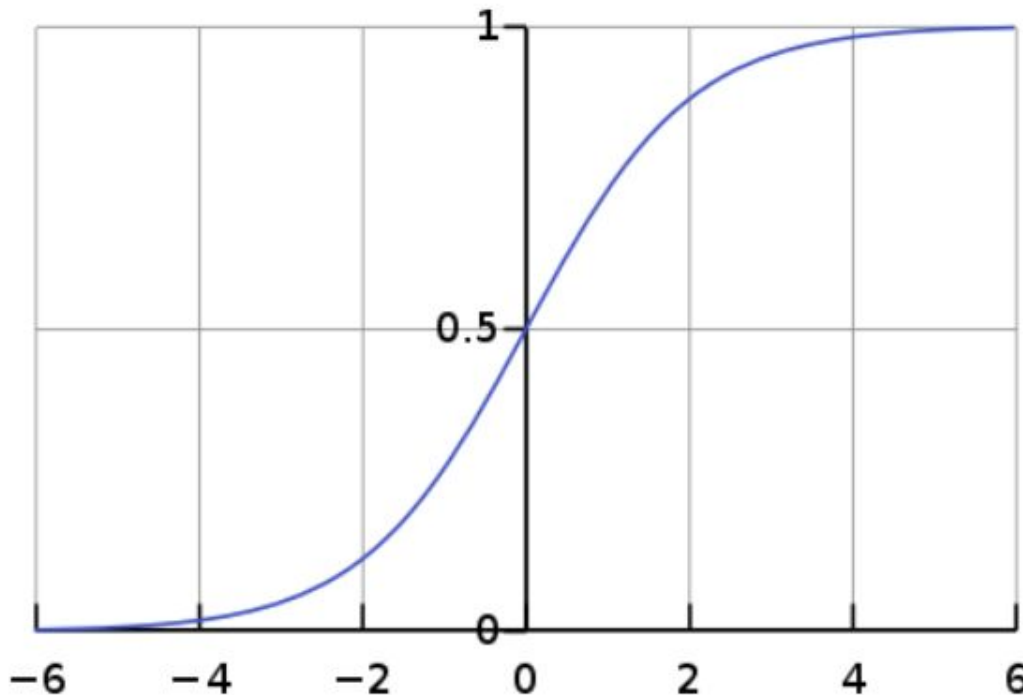
$$\sigma(t) = \frac{e^t}{e^t + 1} = \frac{1}{1 + e^{-t}}$$

Here, $y = t = \beta_0 + \beta_1 x_1$

$$\sigma(t) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x)}}$$

How do you classify using the above function?

We can predict like:
 $y=1$, when $\sigma(t) \geq 0.5$
 $y=0$, when $\sigma(t) < 0.5$



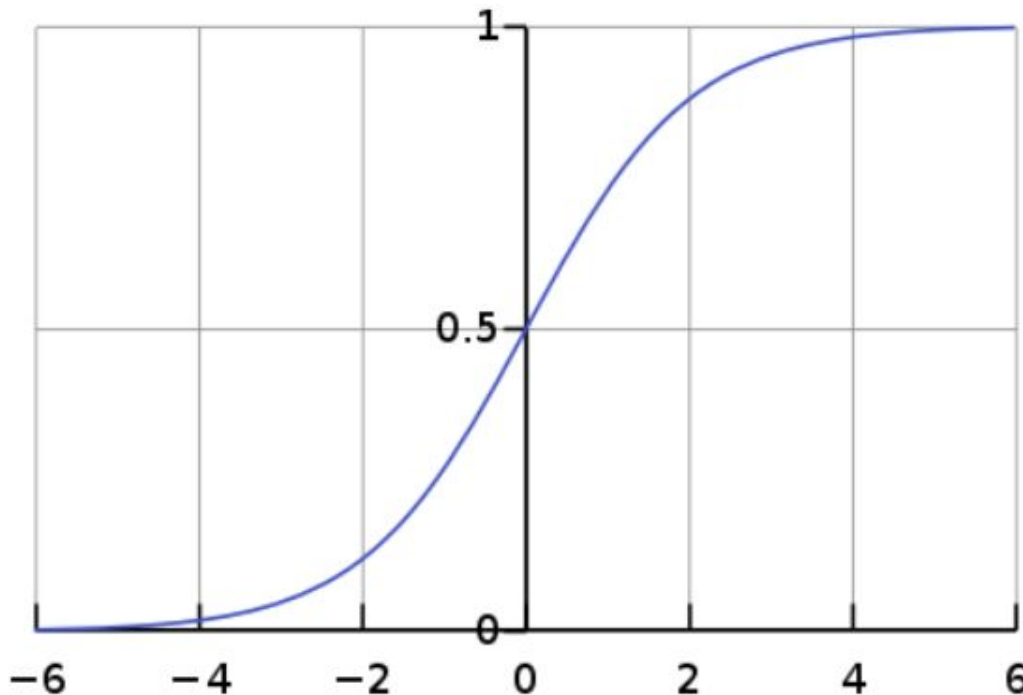
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How do you classify using the above function?

We can predict like:

$y=1$, when $\sigma(t) \geq 0.5$ ($y \geq 0$)

$y=0$, when $\sigma(t) < 0.5$ ($y < 0$)

Logistic Regression

The function is called logistic function or sigmoid function.

$$\sigma(t) = \frac{e^t}{e^t + 1} = \frac{1}{1 + e^{-t}}$$

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$$\sigma(t) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x)}}$$

How do you classify using the above function?

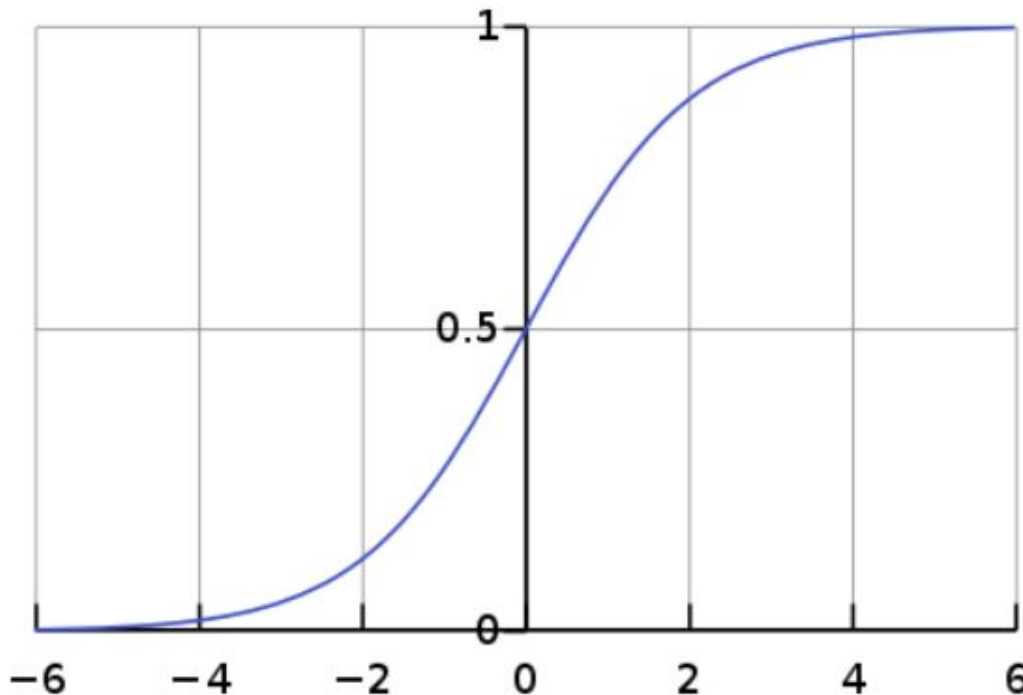
We can predict like:

$y=1$, when $\sigma(t) \geq 0.5$ ($y \geq 0$)

$y=0$, when $\sigma(t) < 0.5$ ($y < 0$)

OR, $y=1$, when $\beta_0 + \beta_1 x_1 \geq 0$

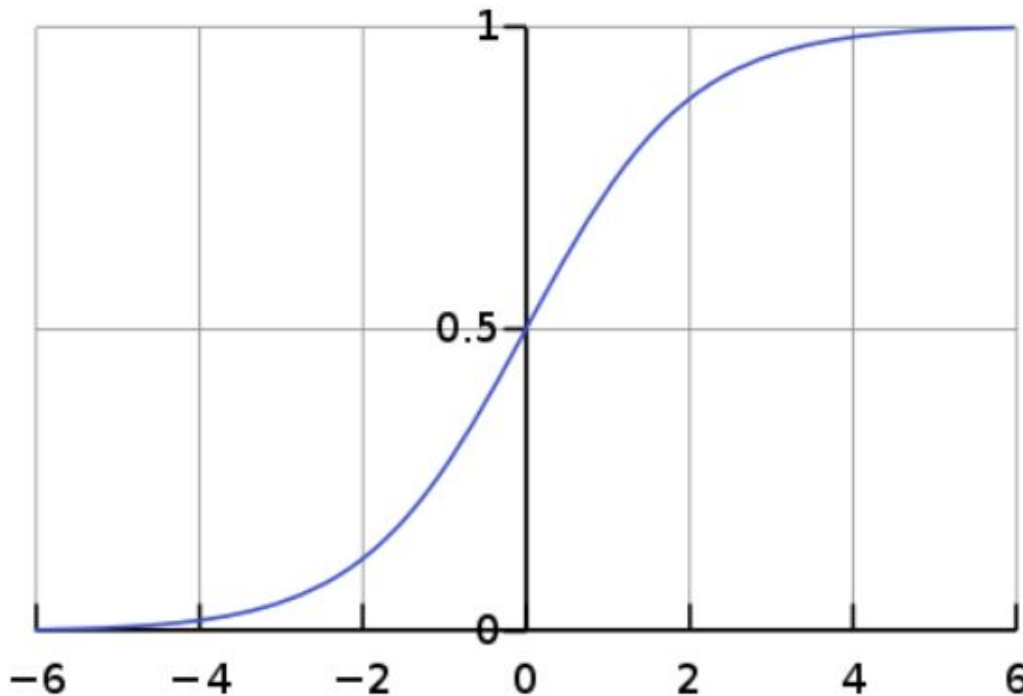
$y=0$, when $\beta_0 + \beta_1 x_1 < 0$



Logistic Regression

The function is called logistic function or sigmoid function.

$$\sigma(t) = \frac{e^t}{e^t + 1} = \frac{1}{1 + e^{-t}} \quad \text{Here, } y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots = \beta^T \mathbf{x}$$



$$y=1 \text{ when } \beta^T \mathbf{x} \geq 0$$

$$y=0 \text{ when } \beta^T \mathbf{x} < 0$$

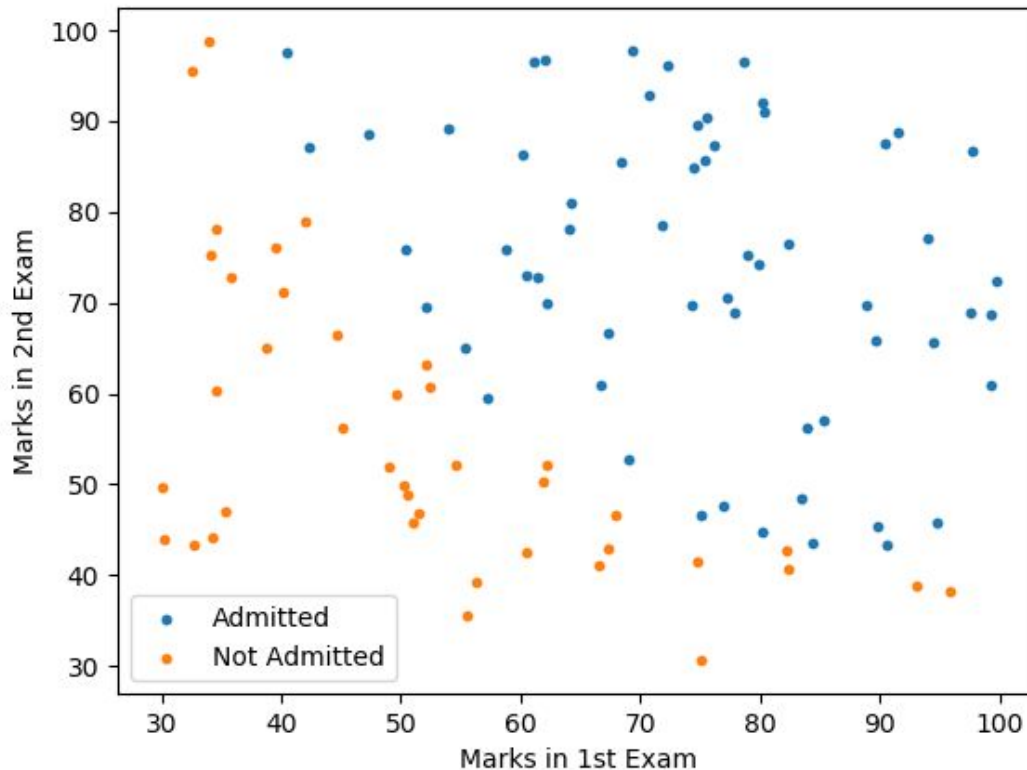
Logistic Regression - Example



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Here, $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2$

$y=1$ when $\beta^T \mathbf{x} \geq 0$

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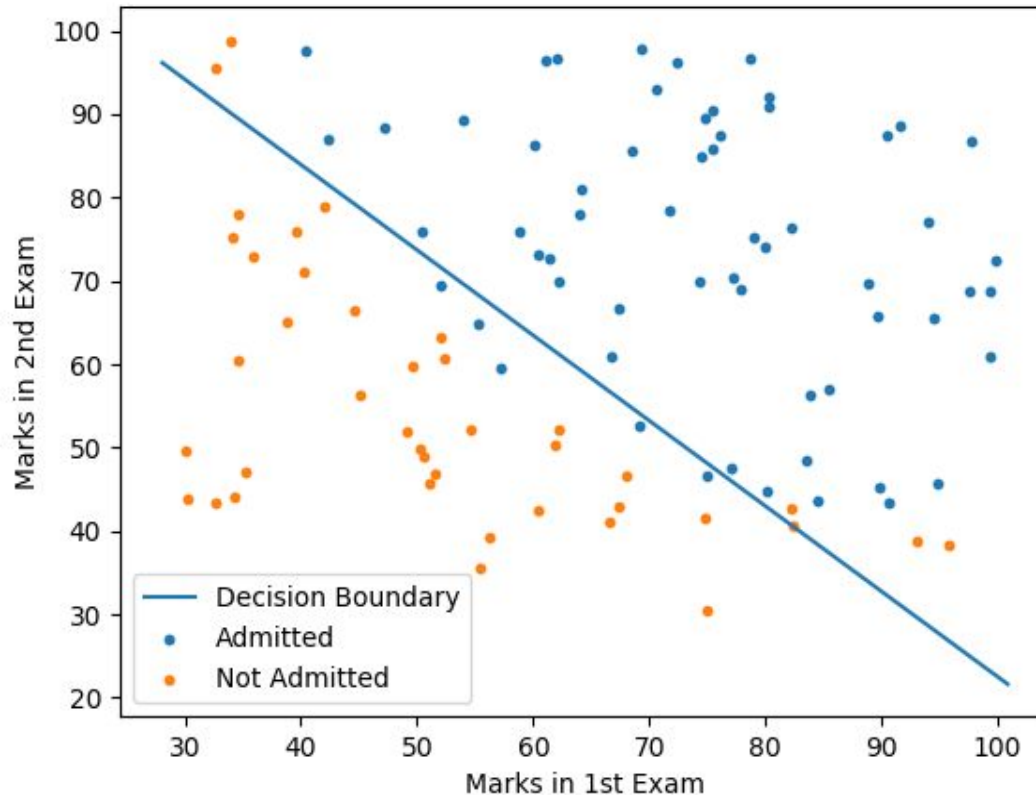
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Here, $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2$

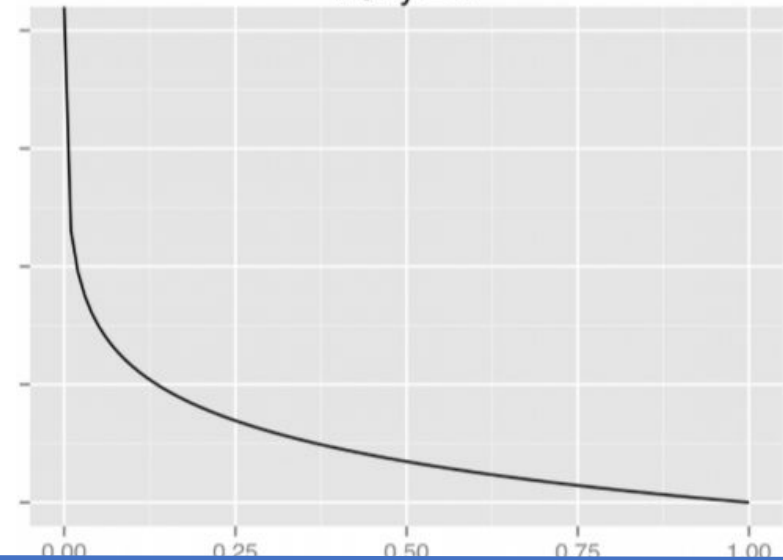
$y=1$ when $\beta^T \mathbf{x} \geq 0$

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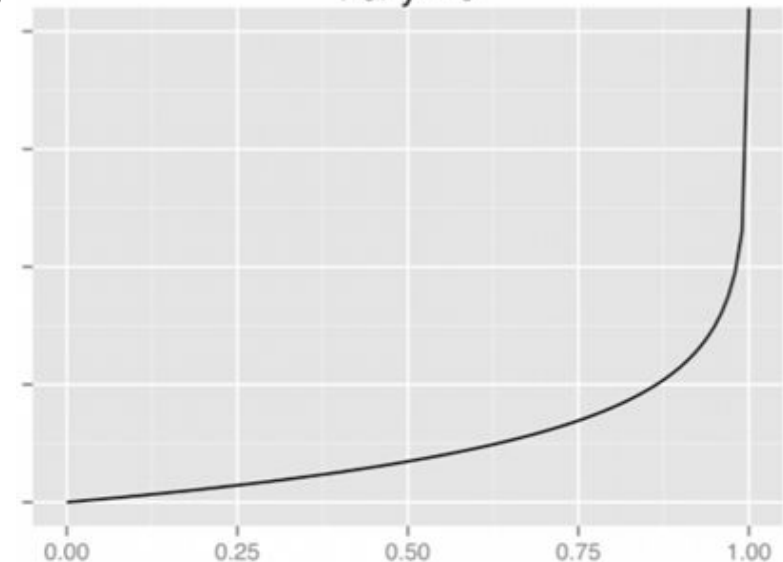
Logistic Regression – Cost function

$$\text{Cost function} = \begin{cases} -\log(\sigma(t)) & \text{if } y = 1 \\ -\log(1-\sigma(t)) & \text{if } y = 0 \end{cases}$$

For $y = 1$



For $y = 0$





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Thank You!