Birla Institute of Applied Sciences
बिरला इंस्टिट्यूट ऑफ़ अप्लाइड साइंसेस
Bhimtal, Distt: Nainital, Uttarakhand- 263136

Pattern Recognition

- S. S. Samant

Classification-oriented measures

Cluster	Enter-tainment	Financial	Foreign	Metro	National	Sports	Entropy	Purity
1	3	5	40	506	96	27		
2	4	7	280	29	39	2		
3	1	1	1	7	4	671		
4	10	162	3	119	73	2		
5	331	22	5	70	13	23		
6	5	358	12	212	48	13		
Total	354	555	341	943	273	738		

Calculate Entropy, purity, precision, recall, F-score of each of the clusters above.

Classification-oriented measures

Cluster	Enter-tainment	Financial	Foreign	Metro	National	Sports	Entropy	Purity
1	3	5	40	506	96	27	1.2270	0.7474
2	4	7	280	29	39	2	1.1472	0.7756
3	1	1	1	7	4	671	0.1813	0.9796
4	10	162	3	119	73	2	1.7487	0.4390
5	331	22	5	70	13	23	1.3976	0.7134
6	5	358	12	212	48	13	1.5523	0.5525
Total	354	555	341	943	273	738	1.1450	0.7203

Classification-oriented measures

Cluster	Entertainment	Financial	Foreign	Metro	National	Sports	Entropy	Purity
1	3	5	40	506	96	27	1.2270	0.7474
2	4	7	280	29	39	2	1.1472	0.7756
3	1	1	1	7	4	671	0.1813	0.9796
4	10	162	3	119	73	2	1.7487	0.4390
5	331	22	5	70	13	23	1.3976	0.7134
6	5	358	12	212	48	13	1.5523	0.5525
Total	354	555	341	943	273	738	1.1450	0.7203

What is the precision and recall of Cluster-1 *wrt* Metro class

Classification-oriented measures

Cluster	Entertainment	Financial	Foreign	Metro	National	Sports	Entropy	Purity
1	3	5	40	506	96	27	1.2270	0.7474
2	4	7	280	29	39	2	1.1472	0.7756
3	1	1	1	7	4	671	0.1813	0.9796
4	10	162	3	119	73	2	1.7487	0.4390
5	331	22	5	70	13	23	1.3976	0.7134
6	5	358	12	212	48	13	1.5523	0.5525
Total	354	555	341	943	273	738	1.1450	0.7203

What is the precision and recall of Cluster-1 *wrt* Metro class

Precision = 0.74

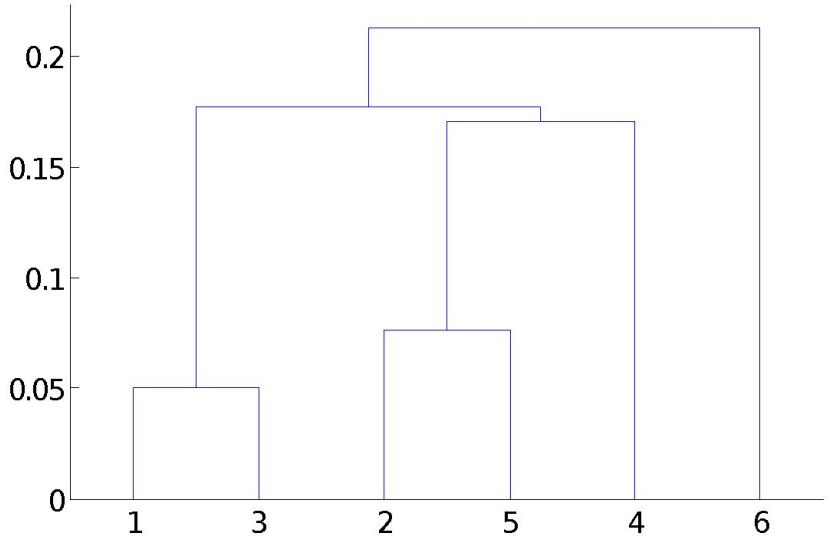
Recall = 0.53

Agglomerative Hierarchical Clustering

- Starts with each point being a cluster, and at each step, merge the *closest* pair of clusters
- Displayed graphically using a **dendrogram – a tree like structure**

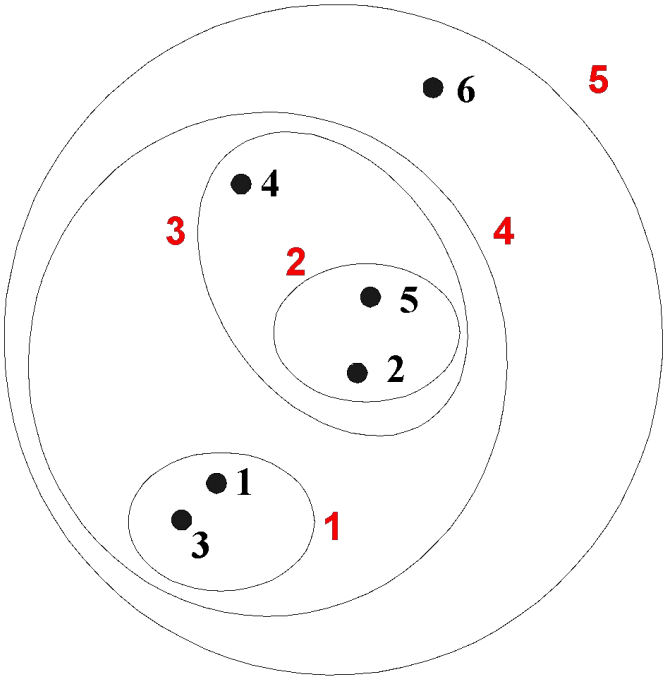
Agglomerative Hierarchical Clustering

- Starts with each point being a cluster, and at each step, merge the *closest* pair of clusters
- Displayed graphically using a **dendrogram – a tree like structure** (*dendro* "tree", *gramma* "drawing")



Agglomerative Hierarchical Clustering

- Starts with each point being a cluster, and at each step, merge the *closest* pair of clusters
- Can also be displayed graphically using a **nested cluster diagram**



Agglomerative Hierarchical Clustering

Basic algorithm

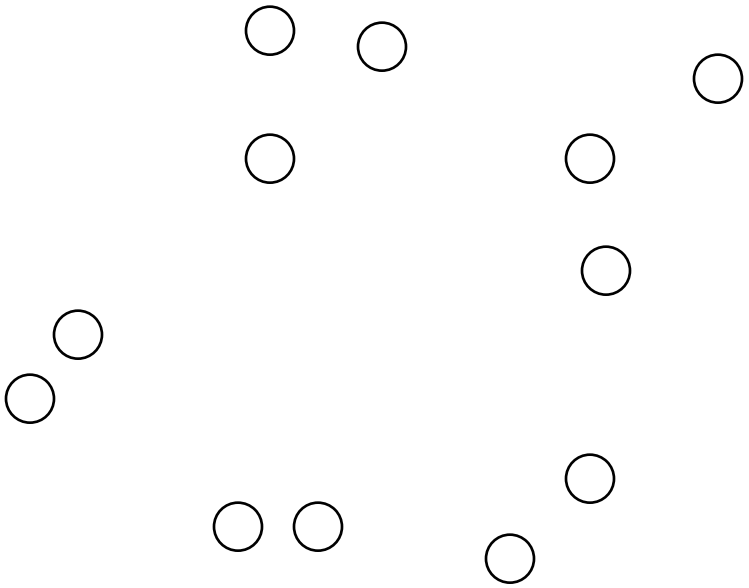
1. Compute the proximity matrix
2. Let each data point be a cluster
3. **Repeat**
4. Merge the two closest clusters
5. Update the proximity matrix
6. **Until** only a single cluster remains

Key operation is the computation of the proximity of two clusters

- Different approaches to defining the distance between clusters distinguish the different algorithms

Starting Situation

- Start with clusters of individual points and a proximity matrix

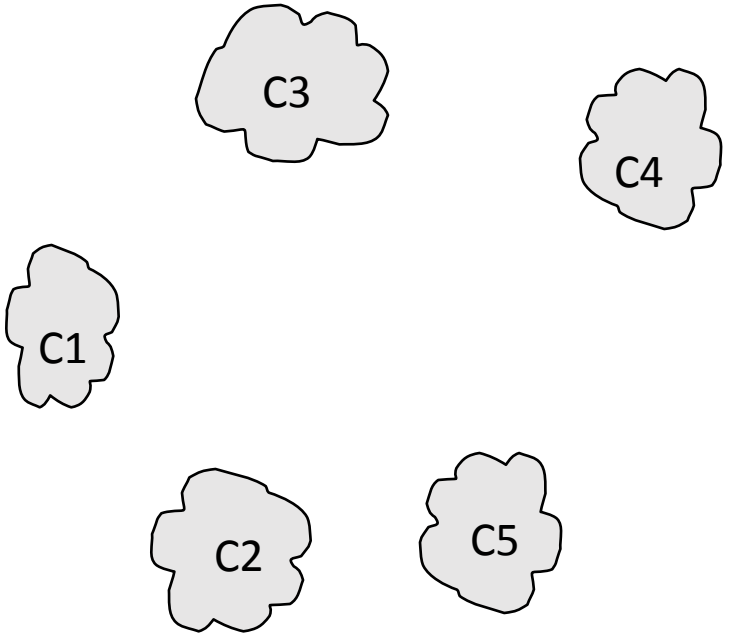


	p1	p2	p3	p4	p5	. . .
p1						
p2						
p3						
p4						
p5						
.						
.						
.						

Proximity Matrix

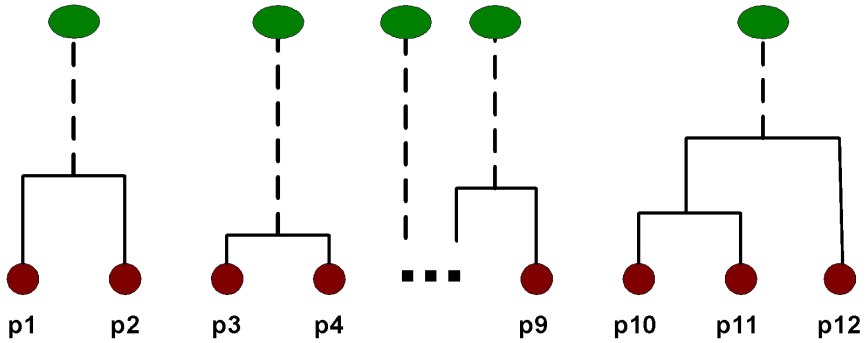
Intermediate Situation

- After some merging steps, we have some clusters



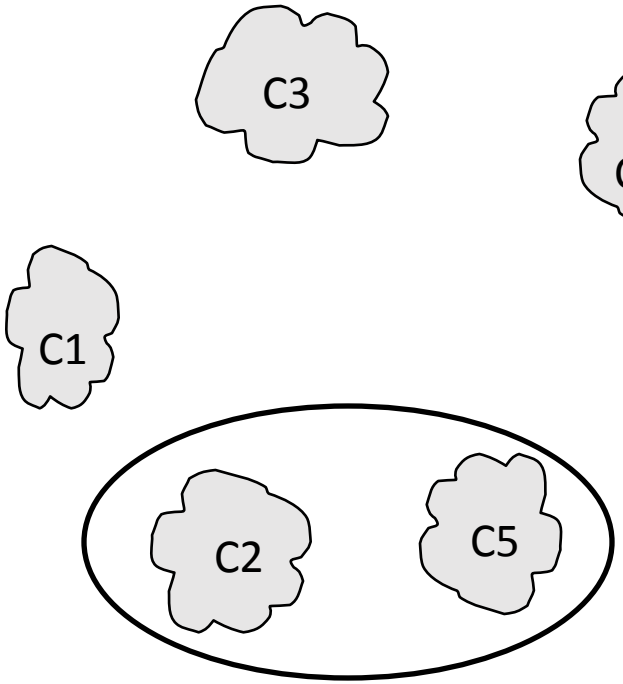
	C1	C2	C3	C4	C5
C1					
C2					
C3					
C4					
C5					

Proximity Matrix



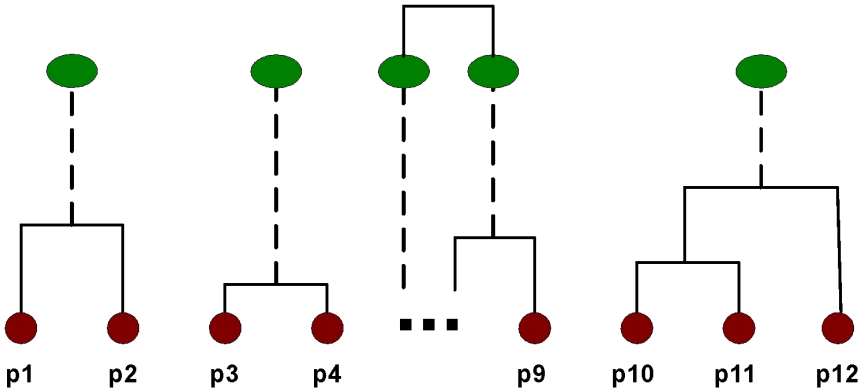
Intermediate Situation

- We want to merge the two closest clusters (C2 and C5) and update the proximity matrix.



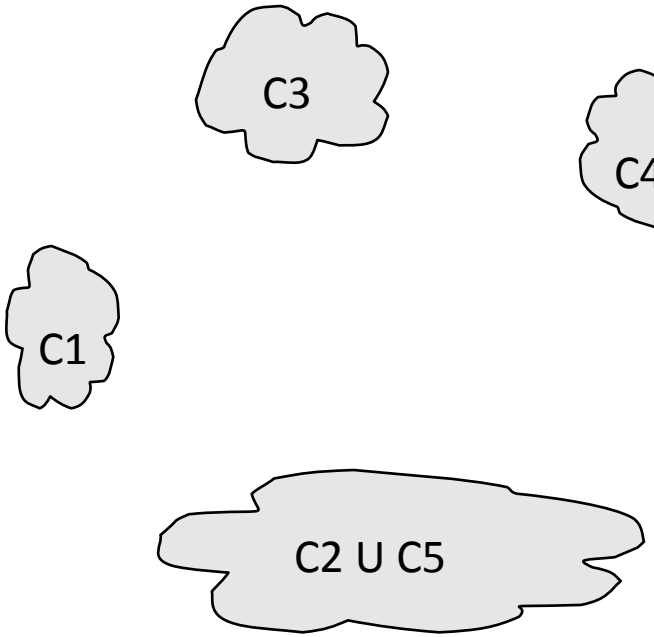
	C1	C2	C3	C4	C5
C1					
C2					
C3					
C4					
C5					

Proximity Matrix



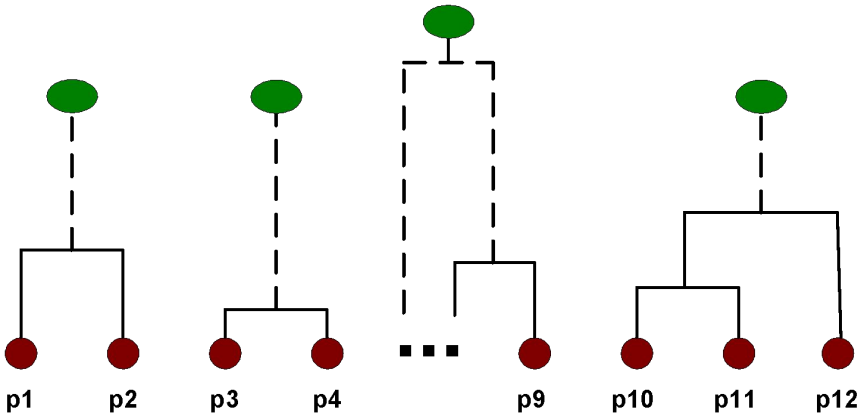
After Merging

- The question is “How do we update the proximity matrix?”

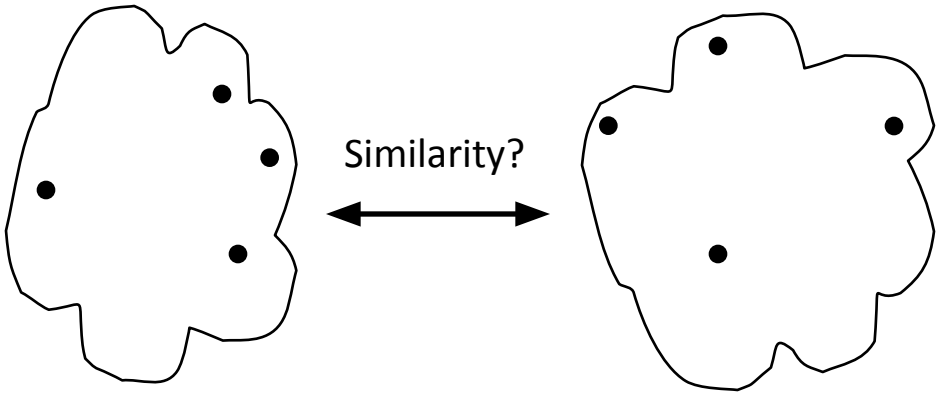


	C1	C2 U C5	C3	C4
C1		?		
C2 U C5	?	?	?	?
C3		?		
C4		?		

Proximity Matrix



How to Define Inter-Cluster Similarity



- MIN
- MAX
- Group Average
- Distance Between Centroids

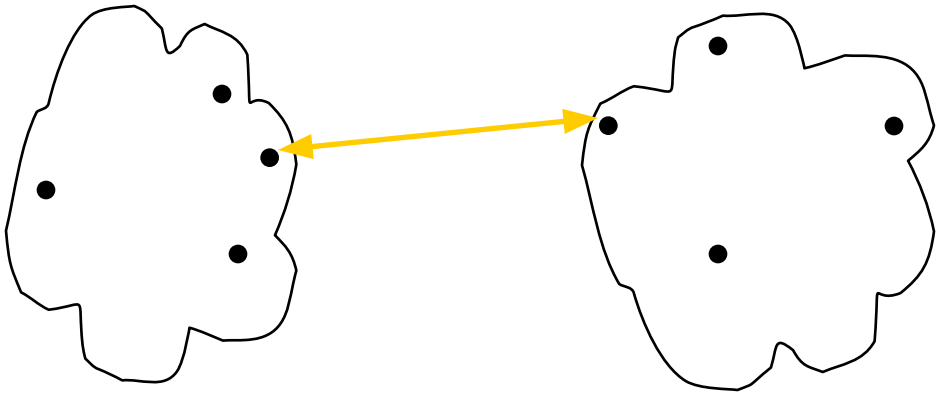
	p1	p2	p3	p4	p5	. . .
p1						
p2						
p3						
p4						
p5						
.						

.

.

Proximity Matrix

How to Define Inter-Cluster Similarity



- MIN
- MAX
- Group Average
- Distance Between Centroids

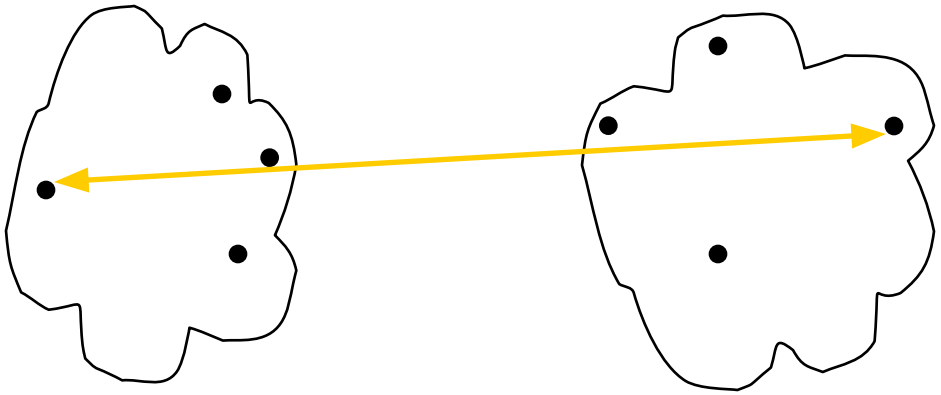
	p1	p2	p3	p4	p5	. . .
p1						
p2						
p3						
p4						
p5						
.						

.

.

Proximity Matrix

How to Define Inter-Cluster Similarity



- MIN
- MAX
- Group Average
- Distance Between Centroids

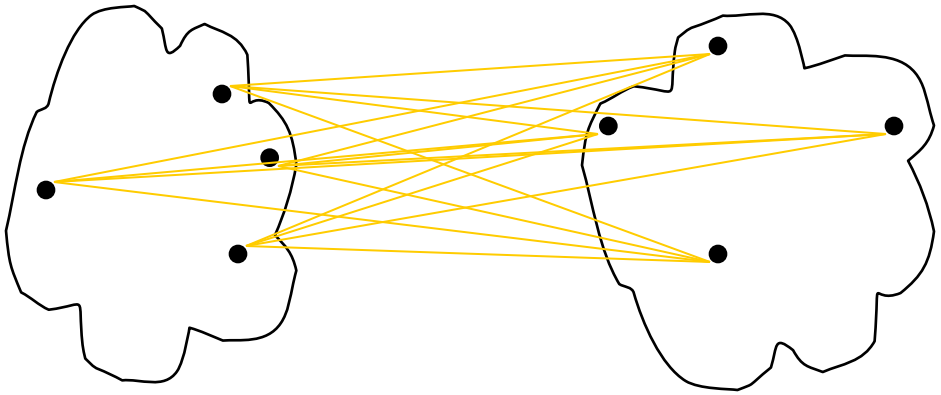
	p1	p2	p3	p4	p5	. . .
p1						
p2						
p3						
p4						
p5						
.						

.

.

Proximity Matrix

How to Define Inter-Cluster Similarity

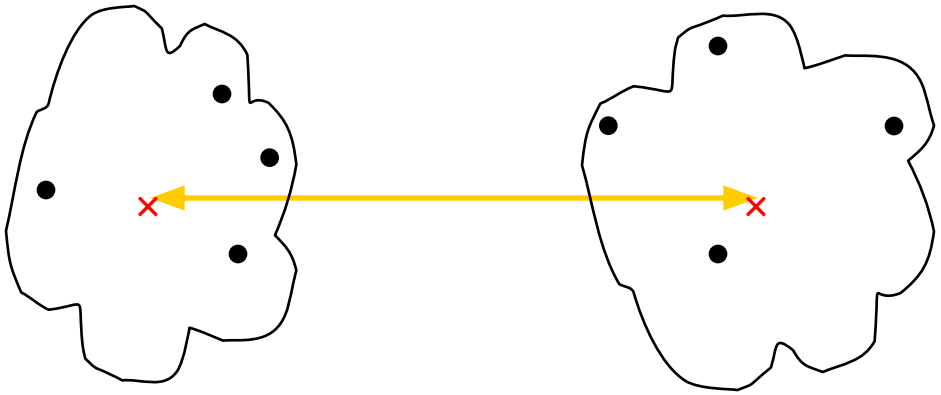


- MIN
- MAX
- Group Average
- Distance Between Centroids

	p1	p2	p3	p4	p5	. . .
p1						
p2						
p3						
p4						
p5						
.						
.						
.						

Proximity Matrix

How to Define Inter-Cluster Similarity



- MIN
- MAX
- Group Average
- Distance Between Centroids

	p1	p2	p3	p4	p5	. . .
p1						
p2						
p3						
p4						
p5						
.						

.

.

Proximity Matrix

Cluster Similarity: MIN or Single Link

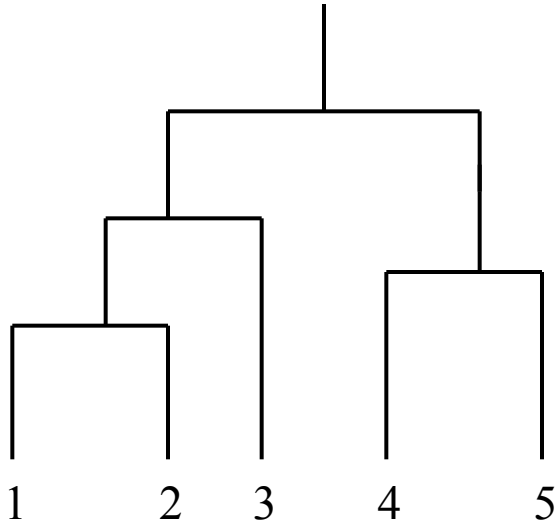
- Similarity of two clusters is based on the two closest points in the different clusters

	I1	I2	I3	I4	I5
I1	1.00	0.90	0.10	0.65	0.20
I2	0.90	1.00	0.70	0.60	0.50
I3	0.10	0.70	1.00	0.40	0.30
I4	0.65	0.60	0.40	1.00	0.80
I5	0.20	0.50	0.30	0.80	1.00

Cluster Similarity: MIN or Single Link

- Similarity of two clusters is based on the two closest points in the different clusters

	I1	I2	I3	I4	I5
I1	1.00	0.90	0.10	0.65	0.20
I2	0.90	1.00	0.70	0.60	0.50
I3	0.10	0.70	1.00	0.40	0.30
I4	0.65	0.60	0.40	1.00	0.80
I5	0.20	0.50	0.30	0.80	1.00



Cluster Similarity: MAX or Complete Linkage

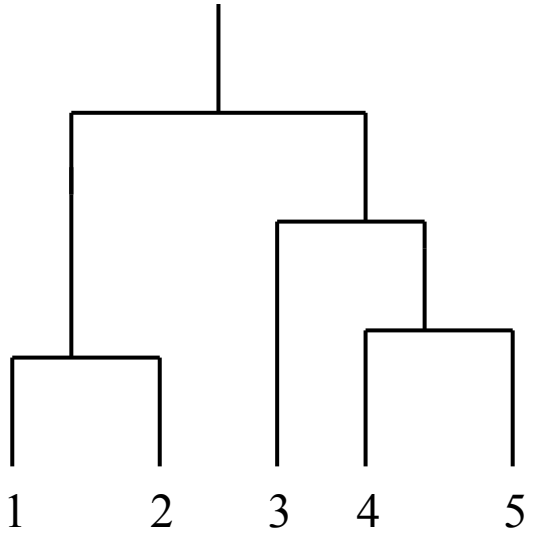
- Similarity of two clusters is based on the two farthest points in the different clusters

	I1	I2	I3	I4	I5
I1	1.00	0.90	0.10	0.65	0.20
I2	0.90	1.00	0.70	0.60	0.50
I3	0.10	0.70	1.00	0.40	0.30
I4	0.65	0.60	0.40	1.00	0.80
I5	0.20	0.50	0.30	0.80	1.00

Cluster Similarity: MAX or Complete Linkage

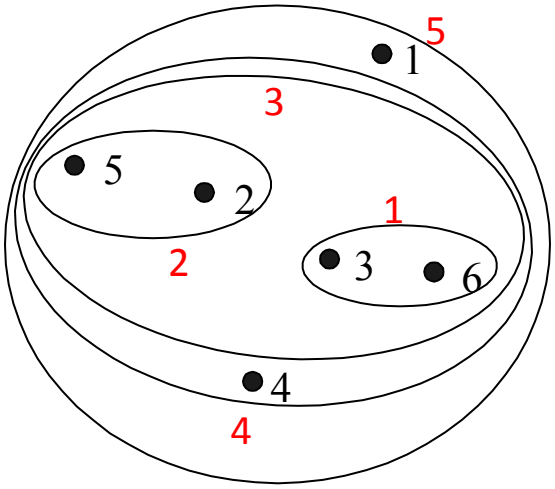
- Similarity of two clusters is based on the two farthest points in the different clusters

	I1	I2	I3	I4	I5
I1	1.00	0.90	0.10	0.65	0.20
I2	0.90	1.00	0.70	0.60	0.50
I3	0.10	0.70	1.00	0.40	0.30
I4	0.65	0.60	0.40	1.00	0.80
I5	0.20	0.50	0.30	0.80	1.00

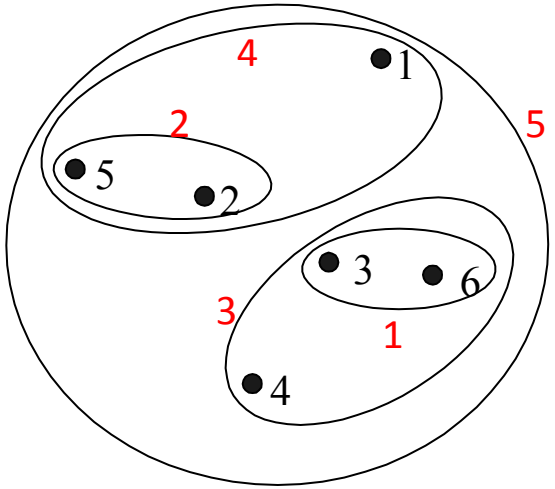


Hierarchical Clustering: Comparison

MIN



MAX



Examples

	p1	p2	p3	p4	p5
p1	1.00	0.10	0.41	0.55	0.35
p2	0.10	1.00	0.64	0.47	0.98
p3	0.41	0.64	1.00	0.44	0.85
p4	0.55	0.47	0.44	1.00	0.76
p5	0.35	0.98	0.85	0.76	1.00

Given the data above, perform single link and complete link hierarchical clustering. Draw dendrogram of your results.

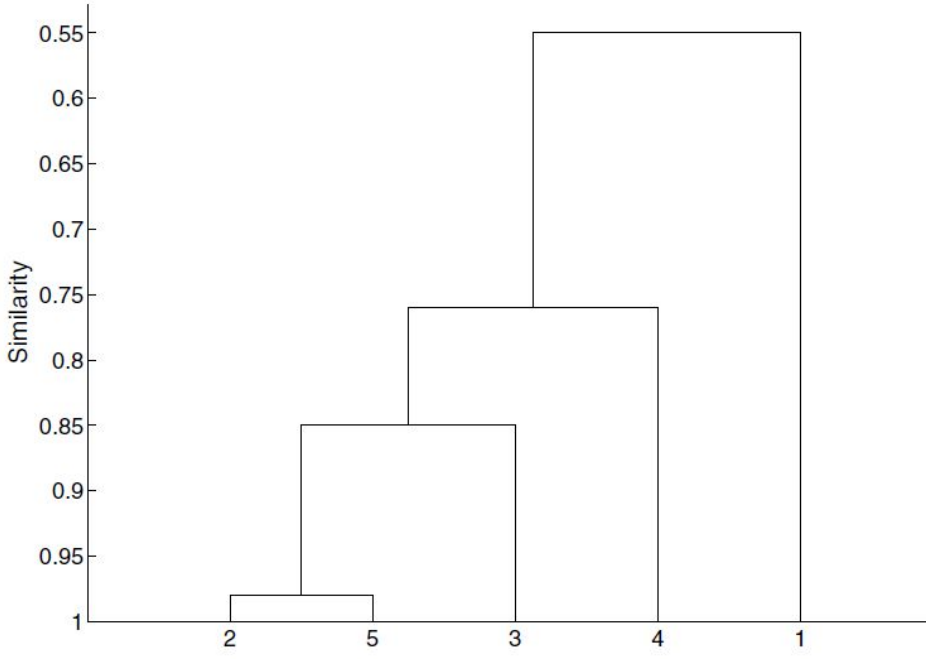
Single Link:

Examples

	p1	p2	p3	p4	p5
p1	1.00	0.10	0.41	0.55	0.35
p2	0.10	1.00	0.64	0.47	0.98
p3	0.41	0.64	1.00	0.44	0.85
p4	0.55	0.47	0.44	1.00	0.76
p5	0.35	0.98	0.85	0.76	1.00

Given the data above, perform single link and complete link hierarchical clustering. Draw dendrogram of your results.

Single Link:

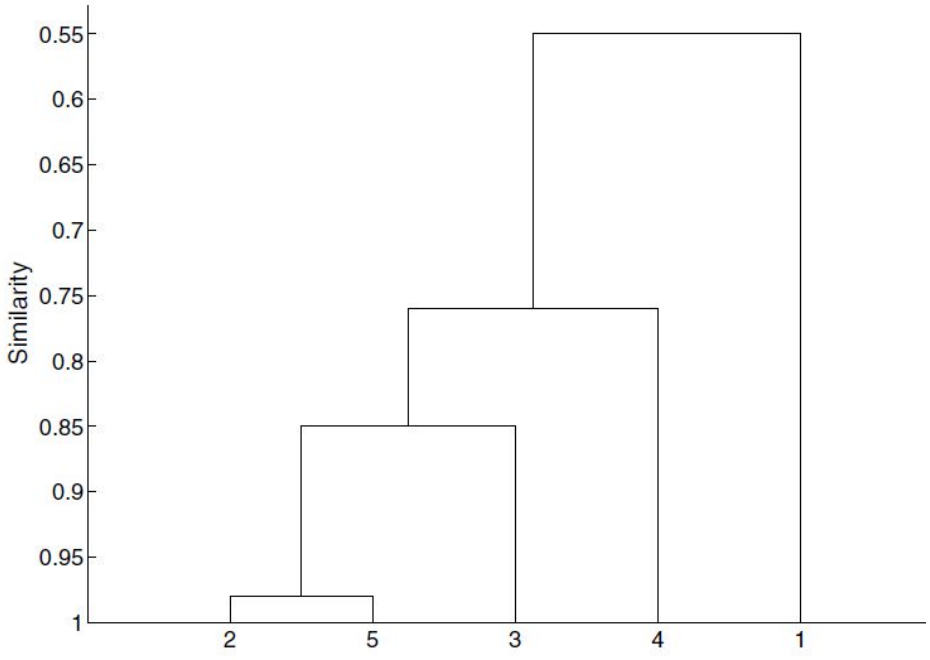


Examples

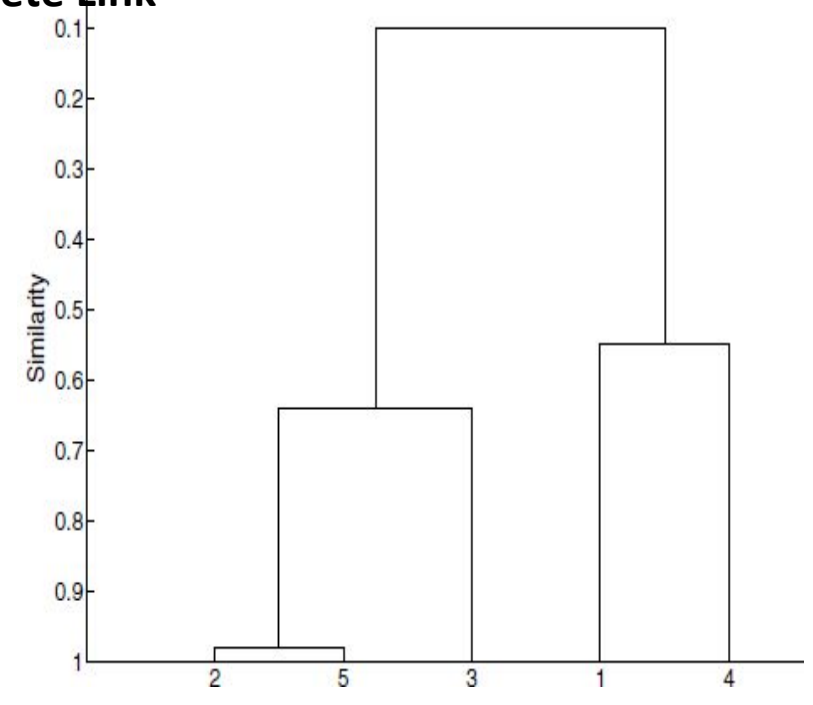
	p1	p2	p3	p4	p5
p1	1.00	0.10	0.41	0.55	0.35
p2	0.10	1.00	0.64	0.47	0.98
p3	0.41	0.64	1.00	0.44	0.85
p4	0.55	0.47	0.44	1.00	0.76
p5	0.35	0.98	0.85	0.76	1.00

Given the data above, perform single link and complete link hierarchical clustering. Draw dendrogram of your results.

Single Link:



Complete Link



Example - HAC on Iris dataset

```
from sklearn import datasets
import matplotlib.pyplot as plt
from sklearn.cluster import AgglomerativeClustering
from sklearn import metrics

iris = datasets.load_iris()
X = iris.data
y = iris.target
plt.scatter(X[:,0], X[:,1], c=y, cmap='rainbow', s=10)
plt.title('Actual',fontsize=15, fontweight='bold')
plt.xlabel('Sepal Length',fontsize=15)
plt.ylabel('Petal Length',fontsize=15)
plt.figure()

cls = AgglomerativeClustering(n_clusters = 3, linkage='average')
cls.fit(X)

hac_labels = cls.labels_
print (metrics.silhouette_score(X, hac_labels))
plt.scatter(X[:,0], X[:,1],c=hac_labels, cmap='rainbow', s=10)
plt.xlabel('Sepal Length',fontsize=15)
plt.ylabel('Petal Length',fontsize=15)
plt.title('Predicted clusters',fontsize=15, fontweight='bold')
plt.show()
```

Thank You!