```
fun append (xs,ys) =
    if xs=[]
    then ys
    else (hd xs)::append(tl xs,ys)

fun map (f,xs) =
    case xs of
    [] => []
    | x::xs' => (f x)::(map(f,xs'))

val a = map (increment, [4,8,12,16])
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages Dan Grossman

Another Closure Idiom: Callbacks

Callbacks

A common idiom: Library takes functions to apply later, when an event occurs – examples:

- When a key is pressed, mouse moves, data arrives
- When the program enters some state (e.g., turns in a game)

A library may accept multiple callbacks

- Different callbacks may need different private data with different types
- Fortunately, a function's type does not include the types of bindings in its environment
- (In OOP, objects and private fields are used similarly, e.g., Java Swing's event-listeners)

Mutable state

While it's not absolutely necessary, mutable state is reasonably appropriate here

 We really do want the "callbacks registered" to change when a function to register a callback is called

Example call-back library

Library maintains mutable state for "what callbacks are there" and provides a function for accepting new ones

- A real library would all support removing them, etc.
- In example, callbacks have type int->unit

So the entire public library interface would be the function for registering new callbacks:

```
val onKeyEvent : (int -> unit) -> unit
```

(Because callbacks are executed for side-effect, they may also need mutable state)

Library implementation

```
val cbs : (int -> unit) list ref = ref []

fun onKeyEvent f = cbs := f :: (!cbs)

fun onEvent i =
   let fun loop fs =
        case fs of
        [] => ()
        | f::fs' => (f i; loop fs')
   in loop (!cbs) end
```

Clients

Can only register an int -> unit, so if any other data is needed, must be in closure's environment

And if need to "remember" something, need mutable state

Examples: