

Q1. Sigmoid Classification with New Values

You are given a feature vector $x = [2, 4]$, weight vector $w = [0.5, -0.3]$, and bias $b = 0.2$.

Tasks:

- (a) Compute the linear combination: $z = w \cdot x + b$

Compute the linear combination

$$z = w \cdot x + b$$

$$z = (0.5)(2) + (-0.3)(4) + 0.2 = 1.0 - 1.2 + 0.2 = 0.0$$

$$\mathbf{z = 0.0}$$

- (b) Apply the sigmoid function: $\sigma(z) = \frac{1}{1+e^{-z}}$

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$$\sigma(0) = 1/1+e^0 = 0.5$$

$$\mathbf{\text{Sigmoid output} = 0.5}$$

- (c) Predict the class label using threshold 0.5

If $\sigma(z) \geq 0.5 \Rightarrow \text{class} = 1$; else 0.

$$0.5 \geq 0.5 \Rightarrow \text{Predicted class} = 1$$

$$\mathbf{\text{Predicted class label} = 1}$$