

Q5. PMI vs PPMI

Given:

- $P(\text{word, context})=0.015$
- $P(\text{word})=0.1$
- $P(\text{context})=0.2$

Tasks:

- (a) Compute PMI

$$\begin{aligned} \text{PMI} &= \log_2 [P(\text{word, context}) / (P(\text{word}) \times P(\text{context}))] \\ &= \log_2 [0.015 / (0.1 \times 0.2)] \\ &= \log_2 [0.015 / 0.02] \\ &= \log_2 (0.75) \\ &= -0.415 \end{aligned}$$

$$\mathbf{PMI = -0.415}$$

- (b) Compute PPMI by thresholding negatives at 0

$$\begin{aligned} \text{PPMI} &= \max(\text{PMI}, 0) \\ &= \max(-0.415, 0) \\ &= 0 \end{aligned}$$

$$\mathbf{PPMI = 0}$$