

04/02/2026
Wednesday

first wrong
one
So for answer we can return high also

Find Nth root of a number

$$\sqrt[3]{27} \quad m=27 \quad N=3 \quad \sqrt[3]{27} = 3 \\ \text{ans} = 3 \quad 3 \times 3 \times 3$$

$$\sqrt[4]{69} \quad m=69 \quad N=4 \quad \text{ans} = -1$$

if ans not found we return -1

Generally we can do in $O(n)$ but we do binary search on answers

Given

$$n=3 \quad m=27$$

$$\text{low} = 1$$

$$\text{mid} = 14$$

$$\text{high} = 27$$

Now I will check

$$14 \times 14 \times 14 > 27$$

so we move left side

$$\text{high} = \text{mid} = 13$$

$$\text{high} = 13$$

$$\text{low} = 1 \quad \text{mid} = 7 \quad \text{high} = 13$$

$$7 \times 7 \times 7 <= 27 \quad \text{false}$$

we move left side

$$\text{high} = \text{mid} - 1$$

$$\text{high} = 6$$

$$\text{low} = 1 \quad \text{mid} = 3 \quad \text{high} = 6$$

$$3 \times 3 \times 3 = 27$$

$$27 < 69 \rightarrow \text{true}$$

so we return 3

take 3 another one as example

$$\sqrt[4]{69}$$

$$m = 69 \quad n = 4$$

$$\text{low} = 1 \quad \text{mid} = 35$$

$$\text{high} = 69$$

$$35 \times 35 \times 35 \times 35 < 69 \rightarrow \text{false}$$

$$\begin{aligned} \text{high} &= \text{mid} - 1 \\ &= 34 \end{aligned}$$

$$\text{low} = 1 \quad \text{mid} = 17 \quad \text{high} = 34$$

$$17 \times 17 \times 17 \times 17 < 34 \rightarrow \text{false}$$

$$\begin{aligned} \text{high} &= \text{mid} - 1 \\ &= 16 \end{aligned}$$

$$\text{low} = 1 \quad \text{mid} = 8 \quad \text{high} = 16$$

$$8 \times 8 \times 8 \times 8 < 69 \rightarrow \text{false}$$

$$\begin{aligned} \text{high} &= \text{mid} - 1 \\ &= 7 \end{aligned}$$

$$\text{low} = 1 \quad \text{mid} = 4 \quad \text{high} = 7$$

$$4 \times 4 \times 4 \times 4 < 69 \rightarrow \text{false}$$

$$\begin{aligned} \text{high} &= \text{mid} - 1 \\ &= 3 \end{aligned}$$

$$\text{low} = 1 \quad \text{mid} = 2$$

$$2 \times 2 \times 2 \times 2 < 69 \rightarrow \text{true}$$

$$\text{low} = \text{mid} + 1$$

low=3 mid=3 high=3

$2 \times 3 \times 3 \times 3 < 69$ false

high = mid - 1
= 2

Search space does not exist
So we does not found.
return -1

public int findNthroot (int n, int m) {

int low = 1

int high = m

while (low <= high)

{

int mid = low + (high - low) / 2;

int midN = findpower (mid, m)

these will give values

like 0, 1, 2

If mid == m return 1

else return 2

if ans > m return 2

if ans < m return 0

if (midN == 1)

return mid;

else if (midN == 2)

high = mid - 1;

else

low = mid + 1;

return -1;

```

int findPower (int mid, int m)
{
    int ans = 1;
    for (int i=1; i<=m; i++)
    {
        ans *= mid;
        if (ans > m)
            return -1;
        if (ans == m)
            return i;
    }
    else
        return 0;
}

```

we do this approach becz when m is 10^9

$$\text{low} = 1 \quad \text{high} = 10^9$$

$$\text{mid} = \frac{10^9}{2}$$

then when calculate power

$$\left[\frac{10^9}{2} \times \frac{10^9}{2} \times \frac{10^9}{2} \times \frac{10^9}{2} \right] \text{ it overflows}$$

so instead of mid when it crosses

10^9 or given m return -1 like go

left side

$$[1 + a \cdot s]$$

$$a = \text{constant} \quad s = \text{constant}$$

$$a = \text{constant} \quad s = \text{constant}$$

$$[1 + a \cdot s]$$

$$s = \text{constant} \quad s = \text{constant}$$

Koko eating Bananas

→ Return the min integers k such that Koko can eat all bananas within h hours

$\text{piles}[] = [3 \ 6 \ 7 \ 11]$ h=8 $\text{k} \rightarrow \text{bananas/hr}$

\downarrow \downarrow
1 pile 1 pile

for this we can do $\text{brute force } O(n)$
but we need to do in $\log n$

Here take
 $k=1$ 1 banana/hr

$3 \ 6 \ 7 \ 11 \ 27 \text{ hrs}$

$k=2$ 2 bananas/hr

Total time spent used depends on k
we take ceil of array element/k

1st ele 2 bananas 1 hr
remaining 1 banana 1 hr
total 2 hrs actual 3 hrs

$[3 \ 6 \ 7 \ 11]$

second ele 2 hrs total hrs = 15

OR 5th ele
take $k=3$ 3 bananas/hr

$[3 \ 6 \ 7 \ 11]$

1 2 3 4 total hrs = 10

take $k=4$ 4 bananas/hr

$[3 \ 6 \ 7 \ 11]$

1 2 2 3 total hrs = 8

$h=8$

we want min right so answer is 4

Here for binary search on answers

we take max element from array has
high and low as 1

low=1

mid=6

high=11

6 bananas/hr

we send this to a function

(it takes time) and check the time if it is less than
or equal

1 1 2 2 (1 = 6 hrs)

6 < 8

high=mid-1

high=5 hrs

low=1

mid=3

3 bananas/hr

1 2 3 4 5 hrs

so we go to right side

bcoz hrs are increasing

low=mid+1

by mistake

low=4

mid=4

high=5

4 bananas/hr

1 2 2 3 hrs

hrs

1 will store it in ans

ans=8 and go left side

high=mid-1

low=4 high=3

so search space does not exist

```
public int totattime (int[] a, int m) {  
    int total = 0;  
    for (int i = 0; i < a.length; i++)  
        total += Math.ceil (a[i]/m);  
    return total;
```

```
public int find min less bananas (int[] a, int h)
```

```
{  
    int low = 1; // low is 1  
    int high = max(a); // high is max  
    int ans = 1;  
    while (low <= high) {  
        int mid = low + (high - low)/2;  
        int totaltime = totattime(a, mid);  
        if (totaltime <= h) {  
            ans = mid; // ans is mid  
            high = mid - 1; // high is mid - 1  
        } else {  
            low = mid + 1; // low is mid + 1  
        }  
    }  
    return low;
```

Time complexity we are doing is on $\max(a, \text{max})$

and each time calculating time by taking mid
 $O(n * \log_2(m))$