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import cv2
import numpy as np
import os
import matplotlib.pyplot as plt
import tifffile as tiff
from pathlib import Path
import os
import scipy.io
import numpy as np
from google.colab import drive
drive.mount('/content/drive')
import os
import shutil
import scipy.io as sio
# Define directories
original dir = '/content/drive/My Drive/Croppedimages'
new dir = '/content/drive/My Drive/Croppedimageswithrgb'
# Create new directory
os.makedirs(new dir, exist ok=True)
def save_channel_as_mat(channel_data, save_path):
    sio.savemat(save_path, {'croppedImg': channel_data})
# Iterate over the original directory
for folder in os.listdir(original_dir):
    folder_path = os.path.join(original_dir, folder)
    new folder path = os.path.join(new dir, folder)
    os.makedirs(new_folder_path, exist_ok=True)
    for subfolder in os.listdir(folder_path):
         subfolder_path = os.path.join(folder_path, subfolder)
new_subfolder_path = os.path.join(new_folder_path, subfolder)
         os.makedirs(new_subfolder_path, exist_ok=True)
         for file in os.listdir(subfolder_path):
             file_path = os.path.join(subfolder_path, file)
             new_file_path = os.path.join(new_subfolder_path, file)
             if 'RGB cropped.mat' in file:
                  mat_contents = sio.loadmat(file_path)
                  rgb_image = mat_contents['croppedImg']
                  # Extract R, G, B channels
                  R_channel = rgb_image[:, :, 0]
G_channel = rgb_image[:, :, 1]
B_channel = rgb_image[:, :, 2]
                  # Save R, G, B channels as separate .mat files
                  save_channel_as_mat(R_channel, new_file_path.replace('RGB_cropped.mat', 'R_cropped.mat'))
save_channel_as_mat(G_channel, new_file_path.replace('RGB_cropped.mat', 'G_cropped.mat'))
save_channel_as_mat(B_channel, new_file_path.replace('RGB_cropped.mat', 'B_cropped.mat'))
                  # Copy other files as they are
                  shutil.copy(file_path, new_file_path)
print ("Processing completed and files copied to the new directory.")
def create subblocks(image, block size=100, num subblocks=10, overlap ratio=0.9):
    h, w = image.shape
    step_size = int(block_size * (1 - overlap_ratio))
    subblocks = []
    # Start from the center
    center_x, center_y = h // 2, w // 2
    for i in range(-int(np.sqrt(num subblocks))//2, int(np.sqrt(num subblocks))//2 + 1):
         for j in range(-int(np.sqrt(num subblocks))//2, int(np.sqrt(num subblocks))//2 + 1):
             start_x = center_x + i * step_size - block_size //
             start_y = center_y + j * step_size - block_size // 2
if start_x >= 0 and start_x + block_size <= h and start_y >= 0 and start_y + block_size <= w:</pre>
                  subblock = image[start_x:start_x + block_size, start_y:start_y + block_size]
                  subblocks.append(subblock)
             if len(subblocks) >= num_subblocks:
                  return subblocks
    return subblocks
def process directory(input directory, output directory):
    if not os.path.exists(output_directory):
         os.makedirs(output directory)
    for folder in sorted(os.listdir(input directory)):
         folder_path = os.path.join(input_directory, folder)
         if os.path.isdir(folder_path):
             output_folder_path = os.path.join(output_directory, folder)
             if not os.path.exists(output_folder_path):
                  os.makedirs(output folder path)
             for subfolder in sorted(os.listdir(folder path)):
                  subfolder path = os.path.join(folder path, subfolder)
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if os.path.isdir(subfolder_path):
    output_subfolder_path = os.path.join(output_folder_path, subfolder)
                       if not os.path.exists(output_subfolder_path):
                           os.makedirs(output subfolder path)
                       for mat_file in sorted(os.listdir(subfolder_path)):
                           if mat file.endswith('.mat'):
                               mat_file_path = os.path.join(subfolder path, mat file)
                                mat_contents = scipy.io.loadmat(mat_file_path)
                                if 'croppedImg' in mat contents:
                                    image_data = mat_contents['croppedImg']
                                    if image data.ndim == 3:
                                         image_data = np.mean(image_data, axis=2)
                                    subblocks = create_subblocks(image_data)
                                    band_folder = os.path.join(output_subfolder_path, os.path.splitext(mat_file)[0])
                                    if not os.path.exists(band folder):
                                        os.makedirs(band folder)
                                    for i, subblock in enumerate(subblocks):
                                         subblock filename = f"{os.path.splitext(mat file)[0]} subblock {i+1}.mat"
                                         subblock_path = os.path.join(band_folder, subblock_filename)
scipy.io.savemat(subblock_path, {'subblock': subblock})
                                         print(f"Saved subblock: {subblock_path}")
input_directory = "/content/drive/My Drive/Croppedimageswithrgb"
output_directory = "/content/drive/My Drive/Subblocks10"
process directory(input_directory, output_directory)
import numpy as np
import os
import scipv.io
def create column vector(subblocks, total size=10000):
    vectors = []
    for subblock in subblocks:
         if subblock is not None:
             vectors.append(subblock.flatten())
         else:
             vectors.append(np.zeros(total_size))
    combined vector = np.concatenate(vectors)
    return combined vector
def process_directory_in_chunks(input_directory, chunk_size=10):
    subfolders = sorted(os.listdir(input_directory))
    num_subfolders = len(subfolders)
    gram matrix chunks = []
    for chunk_start in range(0, num_subfolders, chunk_size):
         chunk_end = min(chunk_start + chunk_size, num_subfolders)
         gram matrix chunk = []
         for folder in subfolders[chunk start:chunk end]:
              folder_path = os.path.join(input_directory, folder)
             samples = sorted(os.listdir(folder path))
              for sample in samples:
                  sample_path = os.path.join(folder_path, sample)
bands = sorted(os.listdir(sample_path))
                  subblocks_dict = {band: [] for band in bands}
                  for band in bands:
                       band path = os.path.join(sample path, band)
                       subblock_files = sorted([os.path.join(band_path, f) for f in os.listdir(band_path) if f.endswith('.mat')])
                       for subblock_file in subblock_files:
                           try:
                               mat_contents = scipy.io.loadmat(subblock_file)
                               subblock_data = mat_contents.get('subblock', None)
if subblock data is not None:
                                    subblocks_dict[band].append(subblock_data)
                                else:
                                    subblocks dict[band].append(None)
                           except Exception as e:
                               subblocks dict[band].append(None)
                               print(f"Error loading {subblock_file}: {e}")
                  for subblock idx in range(10):
                       subblocks = [subblocks_dict[band][subblock_idx] if len(subblocks_dict[band]) > subblock_idx else None for band in bands]
                       # If a whole band is missing, replace it with zeros
                       for i, subblock in enumerate(subblocks):
    if subblock is None:
                               subblocks[i] = np.zeros((100, 100))
                       column_vector = create_column_vector(subblocks)
                       if column vector.size == 70000: # Ensure the column vector is the correct size
                           gram matrix chunk.append(column vector)
         if gram_matrix_chunk: # Ensure chunk is not empty before converting to array
             gram_matrix_chunk = np.array(gram_matrix_chunk).T
chunk_file = f'gram_matrix_chunk_{chunk_start}_{chunk_end}.npy'
             np.save(chunk_file, gram_matrix_chunk)
gram_matrix_chunks.append(chunk_file)
             print(f'Saved chunk: {chunk file}')
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return gram matrix chunks
def merge chunks (chunk files, output file):
    gram_matrix = []
    for chunk_file in chunk_files:
       chunk = np.load(chunk file)
        gram_matrix.append(chunk)
    gram matrix = np.concatenate(gram matrix, axis=1)
    np.save(output_file, gram_matrix)
    print(f'Final gram matrix saved to {output_file}')
def make_gram_matrix_downloadable(output_file):
    import shutil
    from google.colab import files
    shutil.move(output_file, "/content/gram_matrix.npy")
    files.download("/content/gram matrix.npy")
# Define input and output paths
input directory = "/content/drive/My Drive/Subblocks10"
output file = "gram matrix.npy"
# Process directory in chunks
chunk_files = process_directory_in_chunks(input_directory)
# Merge all chunks into a final gram matrix
merge_chunks(chunk_files, output_file)
# Make the final gram matrix downloadable
make gram matrix downloadable(output file)
import numpy as np
import pandas as pd
# Load the numpy file from Google Drive
npy_file_path = "/content/drive/My Drive/gram_matrix.npy"
gram_matrix = np.load(npy_file_path)
# Convert the numpy array to a DataFrame
df = pd.DataFrame(gram_matrix)
# Save the DataFrame to a CSV file
csv_file_path = "/content/gram_matrix.csv"
df.to_csv(csv_file_path, index=False)
# Create a download link for the CSV file
from google.colab import files
files.download(csv_file_path)
import numpy as np
# Load the Gram matrix from the .npy file
file_path = '/content/drive/My Drive/gram_matrix.npy'
M = np.load(file path)
# Check the shape of the loaded matrix to confirm
print("Shape of Gram matrix:", M.shape)
# Step 1: Calculate I = M^T M M_T = M.T
I = np.dot(M T, M)
# Step 2: Compute the Covariance Matrix of I
I_centered = I - np.mean(I, axis=0)
cov_I = np.cov(I_centered, rowvar=False)
# Step 3: Compute the Pseudoinverse of I
I pinv = np.linalg.pinv(I)
# Step 4: Calculate the Eigenvectors and Eigenvalues of I pinv * cov I
eigvals, eigvecs = np.linalg.eig(np.dot(I pinv, cov I))
# Sorting eigenvalues and eigenvectors
sorted_indices = np.argsort(eigvals)[::-1]
eigvals = eigvals[sorted_indices]
eigvecs = eigvecs[:, sorted_indices]
# Print the results
print("Eigenvalues:")
print(eigvals)
print("\nEigenvectors:")
print(eigvecs)
# Save the results
np.save('eigvals.npy', eigvals)
np.save('eigvecs.npy', eigvecs)
# Plot the Cumulative Normalized Eigenvalues
def plot_cumulative_normalized_eigenvalues(eigenvalues, threshold=0.80):
    sorted eigenvalues = np.sort(np.abs(eigenvalues))[::-1] # Sort in descending order
    cumulative_sum = np.cumsum(sorted_eigenvalues)
total sum = cumulative sum[-1]
    normalized cumulative sum = cumulative sum / total sum
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plt.figure(figsize=(10, 6))
    plt.plot(normalized_cumulative_sum, marker='o')
    plt.title('Cumulative Normalized Eigenvalues')
    plt.xlabel('Number of Eigenvalues')
    plt.ylabel('Cumulative Normalized Sum')
    plt.grid(True)
    plt.show()
    num eigenvalues = np.searchsorted(normalized cumulative sum, threshold) + 1
    return num_eigenvalues
print(f'Number of eigenvalues needed to reach 80% variance: {num_eigenvalues_for_80}')
# Select Eigenvectors Corresponding to Top Eigenvalues
top_eigenvectors = eigvecs[:, :num_eigenvalues_for_80]
# Step 5: Compute New Basis Vectors
V = np.dot(gram_matrix, top_eigenvectors)
# Step 6: Construct the Dimensionally Reduced Data
def construct reduced data(V, gram matrix):
    V T = V.T
    reduced_data = np.dot(V_T, gram_matrix)
    return reduced_data
reduced_data = construct_reduced_data(V, gram_matrix)
# Save the reduced data and make it downloadable
np.save('/content/reduced_data.npy', reduced_data)
# Create a link to download the reduced data
from google.colab import files
files.download('/content/reduced data.npy')
print('Shape of reduced data:', reduced_data.shape)
import numpy as np
from sklearn.preprocessing import MinMaxScaler
from google.colab import files
# Load the reduced data from the drive
reduced_data_path = '/content/drive/My Drive/reduced_data.npy'
reduced data = np.load(reduced data path)
# Normalize the reduced data
scaler = MinMaxScaler()
normalized reduced data = scaler.fit transform(reduced data)
# Check the shape and range of the normalized data
print("Normalized reduced data shape:", normalized_reduced_data.shape)
print("Min value:", normalized_reduced_data.min())
print("Max value:", normalized_reduced_data.max())
# Save the normalized reduced data to a CSV file
normalized reduced data path = 'normalized reduced data.csv'
np.savetxt(normalized_reduced_data_path, normalized_reduced_data, delimiter=',')
# Automatically download the file
files.download(normalized_reduced_data_path)
# Save the normalized reduced data to a Numpy file
normalized_reduced_data_npy_path = 'normalized_reduced_data.npy'
np.save(normalized_reduced_data_npy_path, normalized_reduced_data)
# Automatically download the Numpy file
files.download(normalized_reduced_data_npy_path)
import pandas as pd
import numpy as np
# Load the target soil data from the Excel file
file path = '/content/drive/My Drive/Targetsoil.xlsx'
df = pd.read excel(file path)
\label{eq:extract}  \mbox{\# Extract the proportions of sand, silt, and clay} \\ \mbox{proportions} = \mbox{df[['Sand_N', 'Silt_N', 'Clay_N']].values}
# Initialize the target matrix with zeros
num_proportions = proportions.shape[0]
num_subblocks_per_sample = 10
num\_samples\_per\_proportion = 3
total_columns_ideal = num_proportions * num_samples_per_proportion * num_subblocks_per_sample
# Adjust the number of columns to match the actual data
total columns actual = 1840
if total_columns_actual < total_columns_ideal:</pre>
    missing columns = total columns ideal - total columns actual
    print(f"Missing columns: {missing columns}")
    missing\_columns = 0
# Initialize the target matrix with zeros
target_matrix = np.zeros((3, total_columns_actual))
# Fill the target matrix with the proportion values
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column_index = 0
for i in range(num_proportions):
    for _ in range(num_samples_per_proportion):
        for
             in range (num subblocks per sample):
            if column_index < total_columns_actual:</pre>
                target_matrix[:, column_index] = proportions[i]
                column_index += 1
# Save the target matrix to a CSV file
target matrix file path = '/content/drive/My Drive/target matrix.csv'
np.savetxt(target_matrix_file_path, target_matrix, delimiter=',')
# Make the target matrix downloadable
from google.colab import files
files.download(target_matrix_file_path)
print(f"Target matrix saved to {target matrix file path}")
print("Download initiated.")
# Check the size of the target matrix
print("Target matrix shape:", target matrix.shape)
import pandas as pd
import numpy as np
\# Load the target matrix from \mathit{CSV}
target_file_path = '/content/drive/My Drive/target_matrix.csv' # Correct file name
target_df = pd.read_csv(target_file_path, header=None)
# Convert to numpy array and transpose to match the expected shape (3, 1840)
target matrix = target df.to numpy()
# Check the shape of the target matrix
print('Shape of target matrix:', target_matrix.shape)
# Ensure the target matrix is of shape (3, 1840)
if target_matrix.shape[0] != 3:
    target matrix = target matrix.T
print('Updated shape of target matrix:', target matrix.shape)
import numpy as np
import pandas as pd
from sklearn.gaussian_process import GaussianProcessRegressor
from sklearn.gaussian_process.kernels import RBF, ConstantKernel as C
from sklearn.model_selection import train_test_split
from sklearn.metrics import mean_squared_error
import matplotlib.pyplot as plt
# Load the normalized reduced data
normalized_reduced_data_path = '/content/drive/My Drive/normalized_reduced_data.csv'
normalized_reduced_data = pd.read_csv(normalized_reduced_data_path, header=None).to_numpy()
# Load the target matrix
target_file_path = '/content/drive/My Drive/target_matrix.csv'
target_df = pd.read_csv(target_file_path, header=None)
target_matrix = target_df.to_numpy()
# Ensure the target matrix is of shape (3, 1840)
if target matrix.shape[0] != 3:
    target matrix = target matrix.T
print('Shape of normalized reduced data:', normalized reduced data.shape)
print('Shape of target matrix:', target_matrix.shape)
# Split the data into training and testing sets
train_ratio = 0.8
X_train, X_test, y_train, y_test = train_test_split(
    normalized_reduced_data.T, target_matrix.T, train_size=train_ratio, random_state=42
# Define the kernel
kernel = C(1.0, (1e-4, 1e1)) * RBF(1.0, (1e-4, 1e1))
# Train the Gaussian Process model for each target variable
models = []
for i in range(y_train.shape[1]):
   gpr = GaussianProcessRegressor(kernel=kernel, n restarts optimizer=10, random state=42)
    gpr.fit(X_train, y_train[:, i])
    models.append(gpr)
# Predict and evaluate the model
y_pred = np.zeros_like(y_test)
for i, gpr in enumerate(models):
    y_pred[:, i] = gpr.predict(X_test)
mse = mean squared error(y test, y pred)
print(f'Mean Squared Error: {mse}')
# Plot the results
plt.figure(figsize=(12, 6))
plt.plot(y_test[:, 0], label='True Sand')
plt.plot(y_pred[:, 0], label='Predicted Sand')
plt.legend()
plt.title('Sand Prediction')
plt.show()
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plt.figure(figsize=(12, 6))
plt.plot(y_test[:, 1], label='True Silt')
plt.plot(y_pred[:, 1], label='Predicted Silt')
plt.legend()
plt.title('Silt Prediction')
plt.show()
plt.figure(figsize=(12, 6))
plt.plot(y_test[:, 2], label='True Clay')
plt.plot(y_pred[:, 2], label='Predicted Clay')
plt.legend()
plt.title('Clay Prediction')
plt.show()
import pandas as pd
# Predict the values for the test set
for i, gpr in enumerate(models):
    y_pred[:, i] = gpr.predict(X_test)
# Create a DataFrame to display actual and predicted values side by side
results df = pd.DataFrame({
   'Sample': range(1, len(y_test) + 1),
   'Actual Clay': y_test[:, 0],
      'Predicted Clay': y_pred[:, 0],
'Actual Silt': y_test[:, 1],
'Predicted Silt': y_pred[:, 1],
'Actual Sand': y_test[:, 2],
'Predicted Sand': y_pred[:, 2]
})
# Display the results
print(results_df)
\mbox{\# Optionally, save the results to a CSV file}
results\_df.to\_csv('gpr\_actual\_vs\_predicted.csv', index=\textbf{False})
# Automatically download the CSV file (for Google Colab)
from google.colab import files
files.download('gpr_actual_vs_predicted.csv')
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