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of Find the builtange sine series for the

- (a) Define random variable. [2]
  - (b) A die is tossed thrice. A success is 'getting 1 or 6' on a toss. Find the mean and variance of the number of success. [7]
  - (c) The probability of a bad reaction from a certain injection is 0.001. Determine the chance that out of 2000 individuals more than two will get a bad reaction.
  - (d). Fit a normal curve to the following [7] distribution:

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in the interest (x) = x = (x) in the interval (0, 1)

BE (3<sup>rd</sup> Semester) Examination, Nov.-Dec., 2018

(New Scheme)

## Mathematics—III

Maximum Marks: 80 Time Allowed: 3 hours

Minimum Pass Marks: 28

- Note: (i) Answer all questions. Part (a) is compulsory from each question. Attempt any two from (b), (c) and (d) of each question.
  - (ii) The figures in the right-hand margin indicate marks.
- 1. (a) Check which function is even or odd:
  - $f(x) = x \sin x$
  - (ii)  $f(x) = x(1-\cos x)$
  - (b) Prove that

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$$x^{2} = \frac{\pi^{2}}{3} + 4\sum_{n=1}^{\infty} \frac{(-1)^{n} \cos nx}{n^{2}}, -\pi < x < \pi$$

Hence show that  $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \cdots = \frac{\pi^2}{6}$ . [7]

[7]

- (c) Find the half-range sine series for the function  $f(x) = x x^2$  in the interval (0, 1). [7]
- (d) Obtain the first three coefficients in the Fourier series for y, where y is given in the following table:

x	0	1.,	2	3	4	5
<i>y</i> :	4	8	15	7	6	2

- 2. (a) Find the Laplace transform of  $f(t) = t \cos 2t$ . [2]
  - (b) Evaluate the integrals by Laplace transform

$$\int_0^\infty te^{-2t}\cos t\,dt \qquad [7]$$

(c) Use convolution theorem to find the inverse Laplace transform of the function

$$L^{-1}\left\{\frac{1}{s^2(s+1)^2}\right\} = \frac{1}{(s+1)^2}$$

- (d) Solve  $ty'' + 2y' + ty = \cos t$ , given that y(0) = 1. [7]
- 3. (a) Find the value of  $\int_{|z|=3}^{\infty} \left(\frac{z}{z-1}\right) dz$  [2]

- (b) Show that the function  $f(z) = \sqrt{|xy|}$  is not analytic at the origin even though C-R equations are satisfied thereof.
  - (c) If f(z) = u + iv is an analytic function of z, find f(z) if  $u - v = (x - y)(x^2 + 4xy + y^2)$ . [7]
  - (d) Find the Laurent series expansion of  $\frac{z^2 1}{z^2 + 5z + 6}$

about 
$$z = 0$$
 in the region  $2 < |z| < 3$ . [7]

4. (a) Form the partial differential equation by eliminating the arbitrary function

$$z = f\left(\frac{xy}{z}\right). ag{2}$$

- (b) Solve: [7]  $4 \frac{\partial^2 z}{\partial x^2} 4 \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial^2 z}{\partial y^2} = 16 \log(x + 2y)$
- (c) Solve: [7]  $x^{2}(y-z)p + y^{2}(z-x)q = z^{2}(x-y)$
- (d) Using the method of separation of variables, solve

$$\frac{\partial u}{\partial x} = 2 \frac{\partial u}{\partial t} + u$$
, where  $u(x, 0) = 6e^{-3x}$ 

[7]

[7]