

Homework 4

1.

```

1  import math
2  def main():
3      # days = pow(2, 16)
4      days = 356
5      not_sharing = 1
6      for i in range(1, days):
7          print("{0} - {1:.16f}".format(i+1, (1-(1-(i/days))))))
8          if (i == 1000):
9              break
10
11 if __name__ == "__main__":
12     main()

```

days = 356 for question A, days = pow(2, 16) for question B.

A) $\min(q \mid \text{BirthdayProb}(q, 356) \geq 0.99) = 57$

B) $\min(q \mid \text{BirthdayProb}(q, 2^{16}) \geq 0.99) = 776$

2.

```

1  import random
2
3  def main():
4      guesses = [] #stores the strings already generated
5      iterations = 0 #number of guesses so far
6      num = 0 #initialize byte value
7      while (True):
8          num = random.getrandbits(16) #random 16 bits
9          if (num not in guesses): #check if num has already been generated
10             guesses.append(num) #if not, append to guesses
11             iterations += 1 #increment number of guesses
12         else:
13             break #break when collision occurs
14     print(iterations)
15     return
16
17 if __name__ == "__main__":
18     main()

```

A) The rule of thumb for the expected samples before seeing a collision is \sqrt{N} . This is because collisions tend to become much more likely when q (the number of guesses) gets close to \sqrt{N} . Since we are randomly choosing 16-bit values, a collision is likely after $2^8 = 256$

guesses.

B) Average of 20 runs: 274.65 fetches. $\text{Sqrt}(65536) = 256 = 2^8$. This is close to the average that I got.

3.

```
1  import math
2  def main():
3      cSet = 100 # change to match number of characters in charset
4      numPass = pow(2, 128) # number of passwords needed
5      i = 0 #represents the power that our charset is taken to in order to surpass numPass
6      while (pow(cSet, i) <= numPass):
7          i += 1
8          print(i)
9      return i
10
11 if __name__ == "__main__":
12     main()
```

A) 28 characters w/ charset of 26 characters

B) 23 characters w/ charset of 52 characters

C) 22 characters w/ charset of 62 characters

D) 20 characters w/ charset of 100 characters