

Homework 14

1. Let g^{ab} be the key derived from the second DHKA instance.

Eve can learn the keys used in the first and third DHKA instances by computing the following:

First instance key: $(g^{a-1})^{b-1}$

Third instance key: $(g^{a+1})^{b+1}$

Eve knows g^a, g^b, g, p, g^{ab}

Let the first instance key = g^w and the third instance key = g^z , where $w = (a-1)(b-1)$ and $z = (a+1)(b+1)$

$$w = (a-1)(b-1) = ab - a - b + 1$$

$$\text{So } g^w = g^{ab - a - b + 1} = g^{ab} * 1/g^a * 1/g^b * g$$

$$z = (a+1)(b+1) = ab + a + b + 1$$

$$\text{so } g^z = g^{ab + a + b + 1} = g^{ab} * g^a * g^b * g$$