

Marmara University, 2015

Probability and Statistics

Chapter 1
Describing Data with Graphs

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Contents



- Variables and Data
- Types of Variables
- Graphs for Categorical Data
- Graphs for Quantitative Data
- Relative Frequency Histograms
- Most parts of the slides are derived from the textbook: "Mendenhall, Beaver, Beaver, Introduction to Probability and Statistics, 14th Ed., Brooks/Cole, Cengage Learning, 2013"
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Variables and Data



- A **variable** is a characteristic that changes or varies over time and/or for different individuals or objects under consideration.
- Examples: Hair color, white blood cell count, time to failure of a computer component.

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Definitions



- An **experimental unit** is the individual or object on which a variable is measured.
- A measurement results when a variable is actually measured on an experimental unit.
- A set of measurements, called **data**, can be either a **sample** or a **population**.

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- Variable
 - -Hair color
- Experimental unit
 - -Person



- Typical Measurements
 - -Brown, black, blonde, etc.

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Example



- Variable
 - -Time until a light bulb burns out
- Experimental unit
 - -Light bulb
- Typical Measurements
 - -1500 hours, 1535.5 hours, etc.

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How many variables have you measured?



- Univariate data: One variable is measured on a single experimental unit.
- **Bivariate data:** Two variables are measured on a single experimental unit.
- Multivariate data: More than two variables are measured on a single experimental unit.

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Types of Variables Qualitative Quantitative Discrete Continuous 1-8 Mujdat Soyturk, Probability and Statistics, Spring 2015, Marmara University

Types of Variables



- Qualitative variables measure a quality or characteristic on each experimental unit.
- Specifies the similarities or differences in kind
 → categorical data
- •Examples:
 - •Hair color (black, brown, blonde...)
 - •Make of car (Fiat, Opel, Honda, Ford...)
 - •Gender (male, female)
 - •City of birth (Istanbul, Ankara,....)

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Types of Variables



- •Quantitative variables measure a numerical quantity on each experimental unit.
 - Discrete if it can assume only a finite or countable number of values.
 - Continuous if it can assume the infinitely many values corresponding to the points on a line interval.

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- For each orange tree in a grove, the number of oranges is measured.
 - Quantitative discrete
- For a particular day, the number of cars entering the Goztepe campus is measured.
 - Quantitative discrete
- Time until a light bulb burns out
 - Quantitative continuous

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Graphing Qualitative Variables

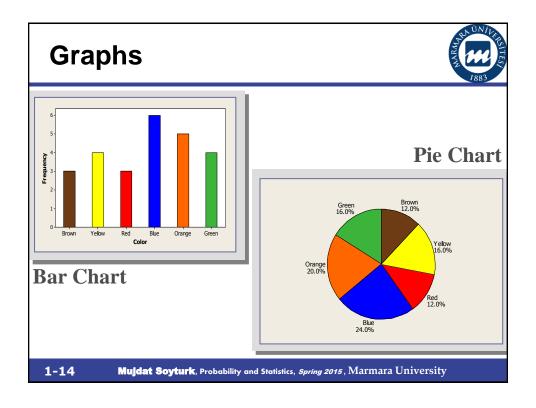


- Use a **data distribution** to describe:
 - What values of the variable have been measured
 - How often each value has occurred
- "How often" can be measured 3 ways:
 - Frequency
 - Relative frequency = Frequency/n
 - Percent = 100 x Relative frequency
- Three steps to a data distribution:
 - 1. Raw data →
 - 2. Statistical Table →
 - 3. Graph



- A bag of candies that contains 25 candies:
- Raw Data:
- Statistical Table:

Color	Tally	Frequency	Relative Frequency	Percent
Red	m m m	3	3/25 = .12	12%
Blue		6	6/25 = .24	24%
Green		4	4/25 = .16	16%
Orange		5	5/25 = .20	20%
Brown	m m m	3	3/25 = .12	12%
Yellow	m m m	4	4/25 = .16	16%

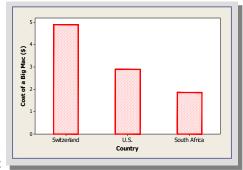


Graphing Quantitative Variables



A single quantitative variable measured for different population segments or for different categories of classification can be graphed using a **pie** or **bar chart**.

A Big Mac hamburger costs \$4.90 in Switzerland, \$2.90 in the U.S. and \$1.86 in South Africa.



Pareto chart: →

bars ordered from largest to smallest

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Graphing Quantitative Variables



A single quantitative variable measured over time is called a **time series.** It can be graphed using a **line** or **bar chart.**

CPI: All Urban Consumers-Seasonally Adjusted

Sept	Oct	Nov	Dec	Jan	Feb	Mar
178.10	177.60	177.50	177.30	177.60	178.00	178.60
178.5 — Xapu a Jud 178.0 — Lauring 100 O 177.5 —					BUREAU OF LAB	OR STATISTICS

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Dotplots



- The simplest graph for quantitative data
- Plots the measurements as points on a horizontal axis, stacking the points that duplicate existing points.
- **Example:** The set 4, 5, 5, 7, 6





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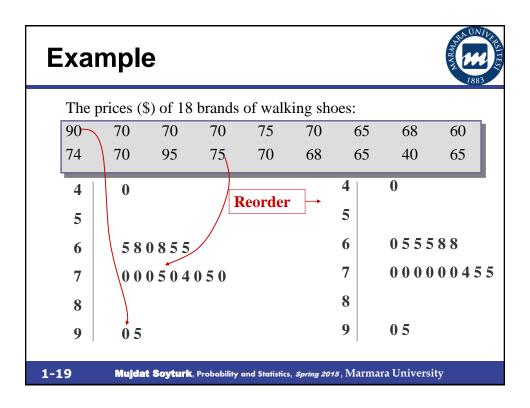
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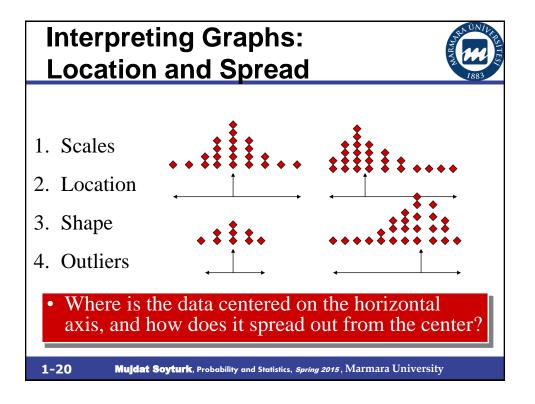
Stem and Leaf Plots



- A simple graph for quantitative data
- Uses the actual numerical values of each data point.
 - -Divide each measurement into two parts: the **stem** and the **leaf.**
 - -List the stems in a column, with a **vertical line** to their right.
 - -For each measurement, record the leaf portion in the **same row** as its matching stem.
 - **-Order** the leaves from lowest to highest in each stem.
 - -Provide a **key** to your coding.

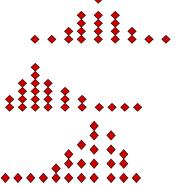
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Interpreting Graphs: Shapes





Mound shaped and symmetric (mirror images)

Skewed right: a few unusually large measurements

Skewed left: a few unusually small measurements

Bimodal: two local peaks

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Interpreting Graphs: Outliers



• Are there any strange or unusual measurements that stand out in the data set?

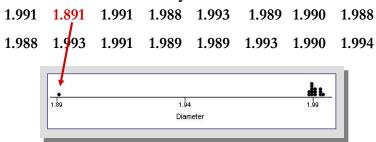




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• A quality control process measures the diameter of a gear being made by a machine (cm). The technician records 15 diameters, but inadvertently makes a typing mistake on the second entry.



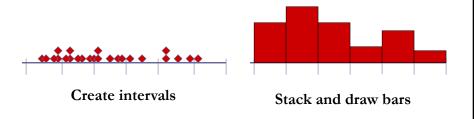
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Relative Frequency Histograms



A **relative frequency histogram** for a quantitative data set is a bar graph in which the height of the bar shows "how often" (measured as a proportion or relative frequency) measurements fall in a particular class or subinterval.



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Relative Frequency Histograms



- Divide the range of the data into **5-12 subintervals** of equal length.
- Calculate the **approximate width** of the subinterval as Range/number of subintervals.
- Round the approximate width up to a convenient value.
- Use the method of **left inclusion** including the left endpoint, but not the right in your tally.
- Create a **statistical table** including the subintervals, their frequencies and relative frequencies.

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Relative Frequency Histograms



- Draw the **relative frequency histogram** plotting the subintervals on the horizontal axis and the relative frequencies on the vertical axis.
- The height of the bar represents
 - The **proportion** of measurements falling in that class or subinterval.
 - The **probability** that a single measurement, drawn at random from the set, will belong to that class or subinterval.

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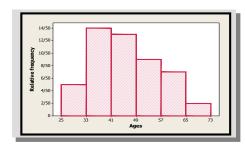
The ages of 50 tenured faculty at a state university.

- 34 48 **70** 63 52 52 35 50 37 43 53 43 52 44
- 42 31 36 48 43 **26** 58 62 49 34 48 53 39 45
- 34 59 34 66 40 59 36 41 35 36 62 34 38 28
- 43 50 30 43 32 44 58 53
 - We choose to use **6** intervals.
 - Minimum class width = (70 26)/6 = 7.33
 - Convenient class width = 8
 - Use 6 classes of length 8, starting at 25.

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Age	Tally	Frequency	Relative Frequency	Percent
25 to < 33	1411	5	5/50 = .10	10%
33 to < 41	1111 1111 1111	14	14/50 = .28	28%
41 to < 49	1111 1111 1111	13	13/50 = .26	26%
49 to < 57	1111 1111	9	9/50 = .18	18%
57 to < 65	JH1 11	7	7/50 = .14	14%
65 to < 73	11	2	2/50 = .04	4%



Describing the Distribution



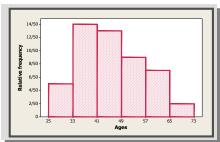
Shape? Skewed right

Outliers? No.

What proportion of the tenured faculty are younger than 41?

What is the probability that a randomly selected faculty

member is 49 or older?



$$(14 + 5)/50 = 19/50 = .38$$

(9+7+2)/50 = 18/50 = .36

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Key Concepts



I. How Data Are Generated

- 1. Experimental units, variables, measurements
- 2. Samples and populations
- 3. Univariate, bivariate, and multivariate data

II. Types of Variables

- 1. Qualitative or categorical
- 2. Quantitative
 - a. Discrete
 - b. Continuous

III. Graphs for Univariate Data Distributions

- 1. Qualitative or categorical data
 - a. Pie charts
 - b. Bar charts

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Key Concepts



- 2. Quantitative data
 - a. Pie and bar charts
 - b. Line charts
 - c. Dotplots
 - d. Stem and leaf plots
 - e. Relative frequency histograms
 - 3. Describing data distributions
 - a. Shapes—symmetric, skewed left, skewed right, unimodal, bimodal
 - b. Proportion of measurements in certain intervals
 - c. Outliers