

Extension of the Homomorphic Cryptosystem BGV by Fixed-Point Number Arithmetic: Insights and Pitfalls

Bachelor Proposal Presentation

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01.02.2024

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Overview

Introduction



Related Work



Approach



Evaluation



Conclusion

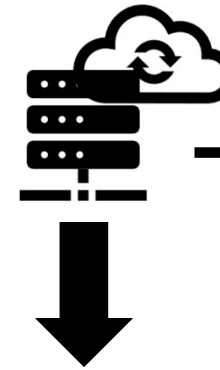
1. Encryption: data to ciphertext



2. Ciphertext sent to provider

4. Resulting ciphertext send to user

3. Computation on ciphertext



Sharing of
User Data?



- Library: OpenFHE
- Implements: BGV, BFV and CKKS scheme
- Different support for each scheme

1. What are the capabilities of step 3?
2. Are there different approaches to step 3?
3. How performend is step 3?

Answers from related work

Introduction



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<p>Theoretical Capabilities?</p> <ul style="list-style-type: none"> ➤ Features of the scheme ➤ Choice of parameters ➤ Mathematical boundaries ➤ Mathematical capabilities <p>=> no mention of real world performance and difference</p> <p>=> comparison of features or types only (FHE, SWHE)</p> <p>[2,3,4,7]</p>	<p>Different Approaches?</p> <ul style="list-style-type: none"> ➤ Comparison of multiple self implemented schemes ➤ Multitude of languages ➤ Limited capabilities <p>=> evaluation difficult</p> <p>=> niche usecases</p> <p>[5,6,9,10,11]</p>	<p>Performance?</p> <ul style="list-style-type: none"> ➤ Mostly built-in functions ➤ Measurement of completion time only ➤ Different libraries <p>=> no high level functions using the capabilities</p> <p>=> no depth in evaluation</p> <p>[1,9]</p>
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Approach to Implementation

Introduction



Related Work



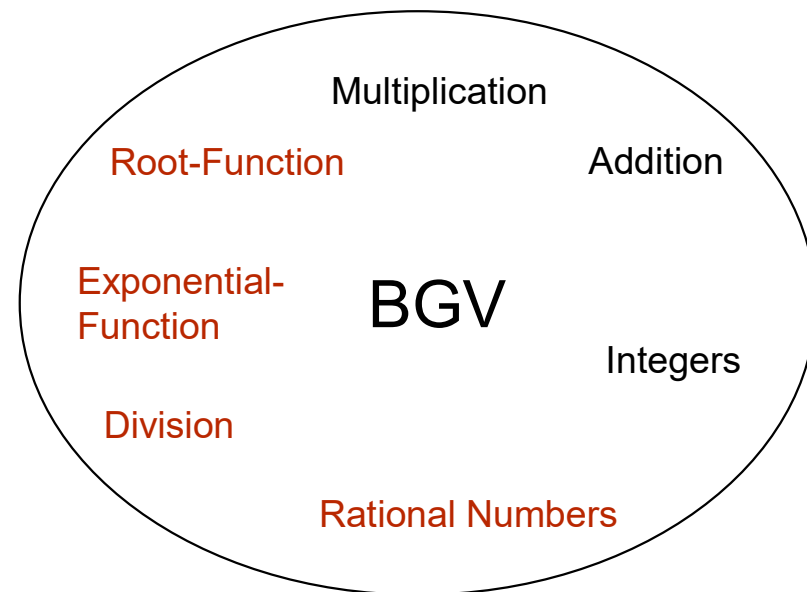
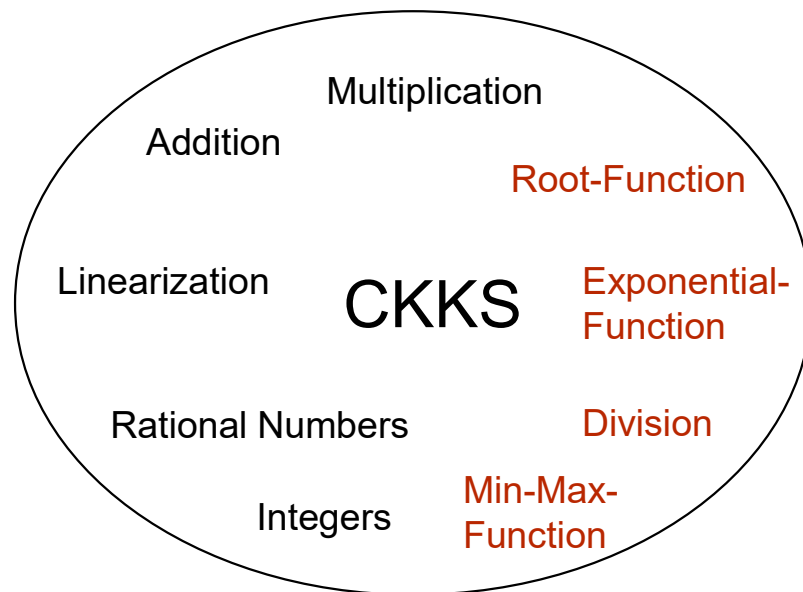
Approach



Evaluation



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Performance Testing

Introduction



Related Work



Approach



Evaluation



Conclusion

Test Cases:

- Every number representation
- Every function (Division ...)

Test Subject:

- Completion time
- Accuracy
- RAM usage
- CPU usage

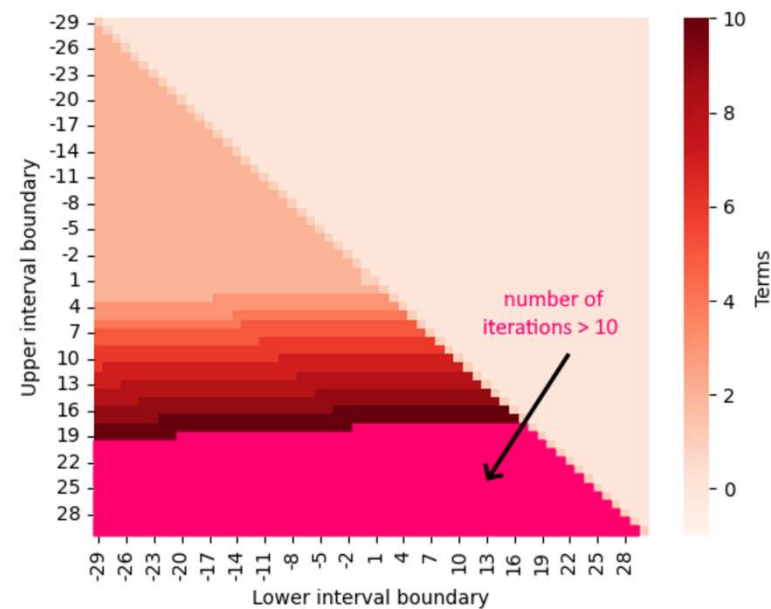
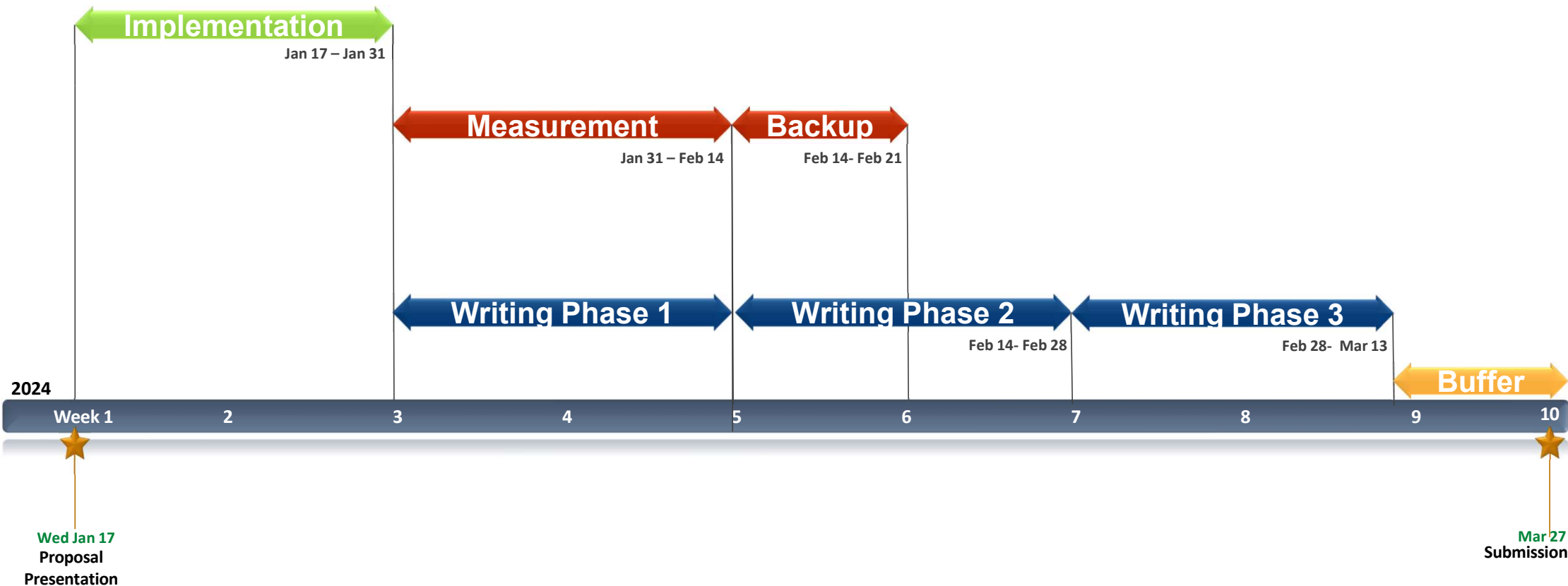


Fig. 5: Visualization of the required iterations to compute the exponential function for values from different intervals with an accuracy of 0.1.
[9]

Time Management



Risk Management



Risks:

- Mathematical bounds/ parameters
- Testing
 - Time for test suite
 - Values invalid
- Results inconclusive due to variance



Solutions:

- Evaluating with disclosed errors
- Multiple test cases
 - Reduced number of intervals
 - Multitude of parameters
- General information

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Problem

- Limited functions in BGV scheme
- Insufficient data on performance

Idea

- Implementing missing capabilities
- Evaluation of BGV compared to CKKS

Benefit

- Versatility of the library
- Performance numbers

Action

- Different number representations
- Evaluation cases

Sources:

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Number Representation

➤ Example: 6.453

➤ 1. Expand to fraction with power of ten

$$6.453 = \frac{6.453 \times 1000}{1000} = \frac{6453}{1000}$$

➤ 2. Encode as vector

$$\begin{pmatrix} 6453 \\ 1000 \end{pmatrix}$$

➤ 3. Encrypt to ciphertext

➤ Example: 6.453 – but different

➤ What if the vector is extended?

$$\begin{pmatrix} 6453 \\ 1000 \\ 6453 \\ 0 \end{pmatrix}$$

➤ What if the nominator and denominator are different vectors?

$$\begin{pmatrix} 6 \\ 4 \\ 5 \\ 3 \end{pmatrix} \quad \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$