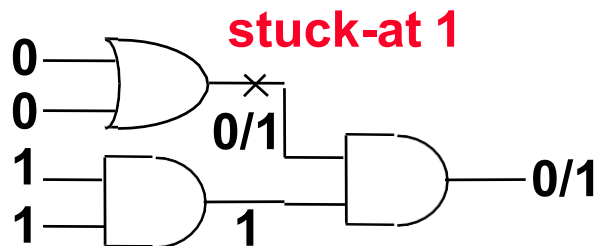


Combinational Test Generation

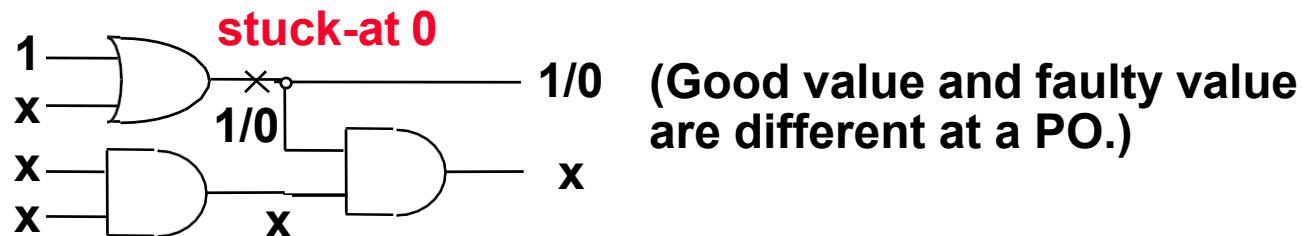
- **Test Generation (TG) Methods**
 - (1) From truth table (2) Using Boolean equation (3) Using Boolean difference (4) From circuit structure
- **TG from Circuit Structure**
 - Common Concepts
 - ATPG Algorithms : D-Algorithm

A Test Pattern

- A test pattern



- A test pattern with don't cares

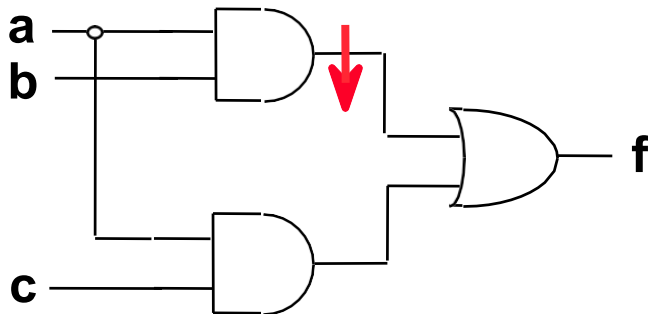


- Test generation: generates a test for a target fault.

Test Generation Methods

(From Truth Table)

Ex: How to generate tests for the stuck-at 0 fault (fault α)?



| abc | f | f_{α} |
|-------|---|--------------|
| 000 | 0 | 0 |
| 001 | 0 | 0 |
| 010 | 0 | 0 |
| 011 | 0 | 0 |
| 100 | 0 | 0 |
| 101 | 1 | 1 |
| ✓ 110 | 1 | 0 |
| 111 | 1 | 1 |

Impractical !!

Test Generation Methods

(Using Boolean Equation)

Since $f = ab+ac$, $f_\alpha = ac \Rightarrow$

T_α = the set of all tests for fault α

$$= \text{ON_set}(f) * \text{OFF_set}(f_\alpha) + \text{OFF_set}(f) * \text{ON_set}(f_\alpha)$$

$$= \{(a,b,c) \mid (ab+ac)(ac)' + (ab+ac)'(ac) = 1\}$$

$$= \{(a,b,c) \mid abc'=1\}$$

$$= \{(110)\}.$$

High complexity !!

Since it needs to compute the faulty function for each fault.

- *ON_set(f): All input combinations that make f have value 1.*
OFF_set(f): All input combinations that make f have value 0.

Boolean Difference

- **Physical Meaning of Boolean Difference**

- For a logic function $F(X)=F(x_1, \dots, x_i, \dots, x_n)$, find all the input combinations that make the change of value in x_i also cause the change of value in F .

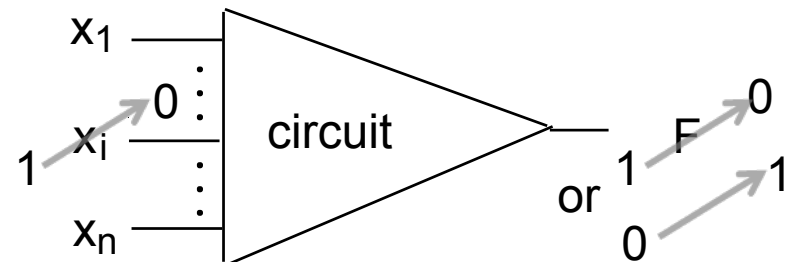
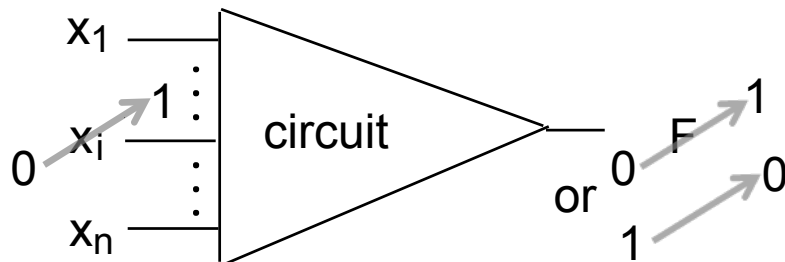
- **Logic Operation of Boolean Difference**

- The Boolean difference of $F(X)$ w.r.t. input x_i is

$$\frac{dF(X)}{dx_i} = F_i(0) \oplus F_i(1) = \overline{F_i(0)} \cdot F_i(1) + F_i(0) \cdot \overline{F_i(1)},$$

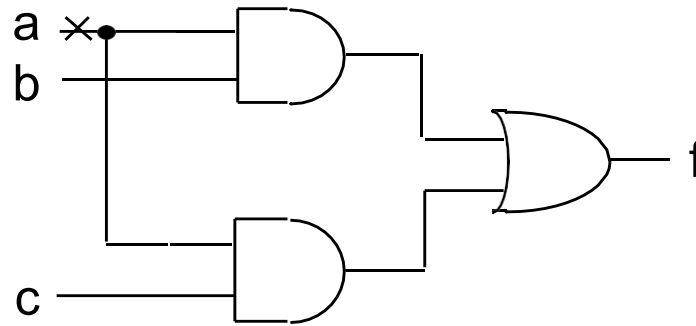
where $F_i(0) = F(x_1, \dots, 0, \dots, x_n)$ and $F_i(1) = F(x_1, \dots, 1, \dots, x_n)$.

- **Relationship between TG and Boolean Difference**



Applying Boolean Difference to Test Generation (1/2)

Case 1: Faults are present at PIs.



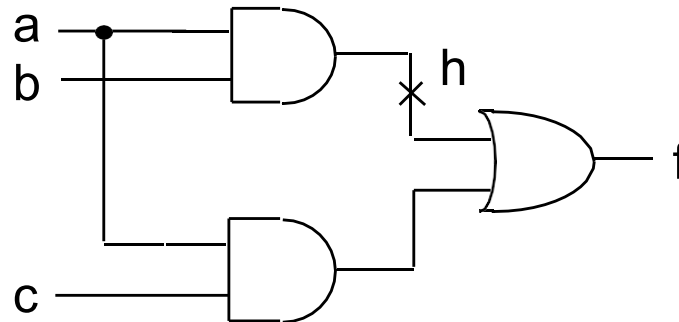
$$f = ab + ac \Rightarrow \frac{df}{da} = f_a(0) \oplus f_a(1) = 1 \cdot (b+c) + 0 = b+c$$

The set of all tests for line **a s-a-1** is $\{(a,b,c) \mid a' \cdot (b+c)=1\} = \{(01x), (0x1)\}$.

The set of all tests for line **a s-a-0** is $\{(a,b,c) \mid a \cdot (b+c)=1\} = \{(11x), (1x1)\}$.

Applying Boolean Difference to Test Generation (2/2)

Case 2: Faults are present at internal lines.



$$f = h + ac, h = ab \Rightarrow \frac{df}{dh} = f_h(0) \oplus f_h(1) = \overline{ac} \cdot 1 + ac \cdot \overline{1} = \overline{a} + \overline{c}$$

The set of all tests for line h s-a-1 is

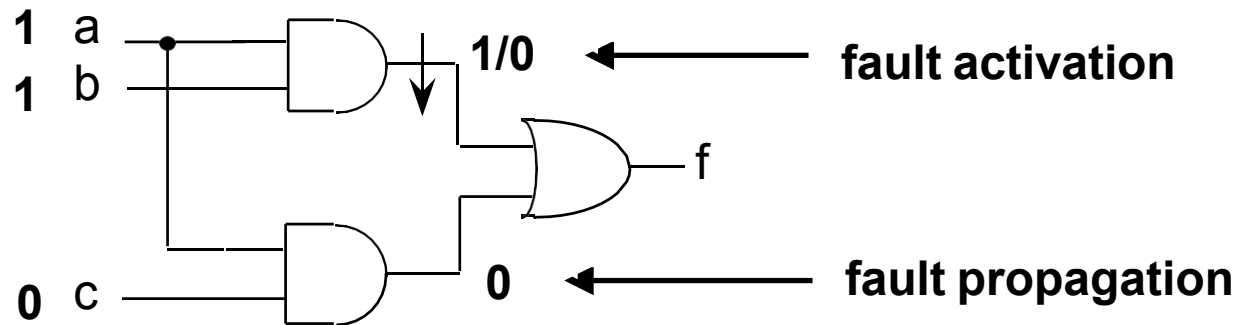
$$\{ (a,b,c) | h' \cdot (a' + c') = 1 \} = \{ (a,b,c) | (a' + b') \cdot (a' + c') = 1 \} = \{ (0xx), (x00) \}.$$

The set of all tests for line h s-a-0 is

$$\{ (a,b,c) | h \cdot (a' + c') = 1 \} = \{ (110) \}.$$

Test Generation Methods

(From Circuit Structure)



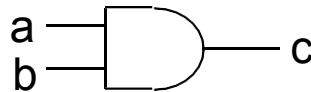
- Two basic goals:
- Fault activation(FA) \Rightarrow Line justification (LJ)
- Fault propagation(FP)

where **1/0** means that the good value is 1 and the faulty value is 0 and is denoted as D. Similarly, 0/1 is denoted as D'. D and D' are called fault effects (FE).

Common Concepts for Structural TG

- The FA problem \Rightarrow a LJ problem.
- The FP problem \Rightarrow
 - (1) Select a FP path to a PO \Rightarrow decisions.
 - (2) Once the path is selected \Rightarrow a set of LJ problems.
- The LJ problems \Rightarrow decisions or implications.

ex:

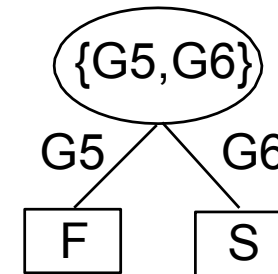
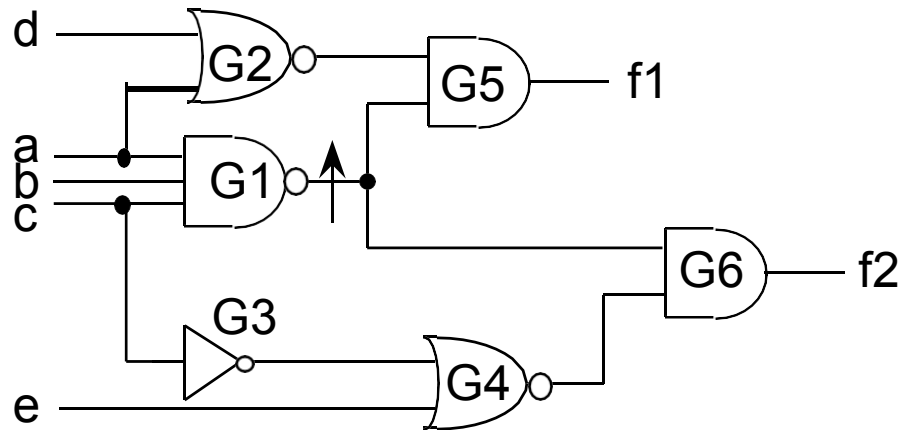


To justify $c=1 \Rightarrow a=1$ and $b=1$. (implication)

To justify $c=0 \Rightarrow a=0$ or $b=0$. (need make decisions)

- **Incorrect decision \Rightarrow Backtracking \Rightarrow Another decision.**
- Once the fault effect is propagated to a PO and all line values to be justified are justified, the test is generated. Otherwise, the decision process must be continued repeatedly until all possible decisions have been tried.

Ex: Decisions When Fault Propagation



The corresponding decision tree

FA $\Rightarrow a=1, b=1, c=1 \Rightarrow G1 = D', G3=0$; FP \Rightarrow through $G5$ or $G6$.

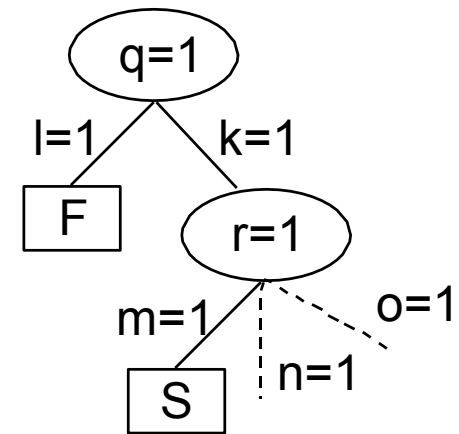
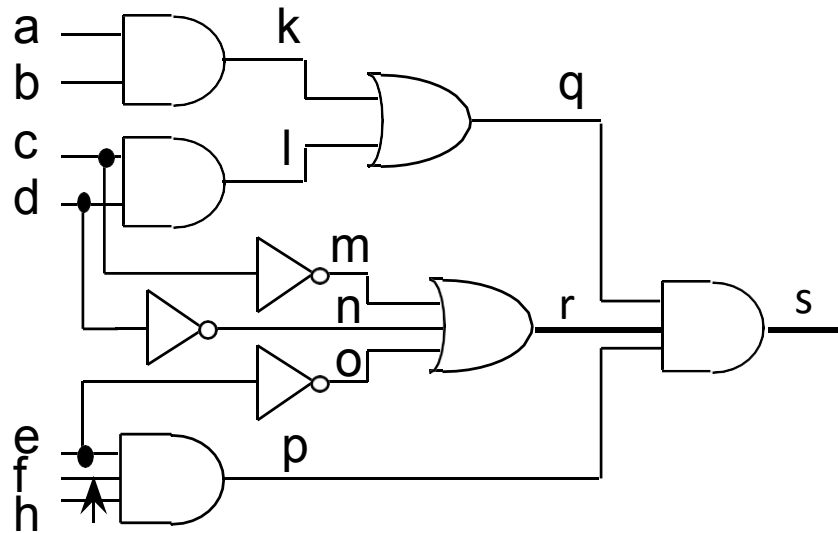
Decision: through $G5 \Rightarrow G2=1 \Rightarrow d=0, a=0. \Rightarrow$ inconsistency \Rightarrow backtracking!!

Decision: through $G6 \Rightarrow G4=1 \Rightarrow e=0. \Rightarrow$ done!!

The resulting test is 111x0.

D-frontier: The set of all gates whose output value is currently x but have one or more fault signals on their inputs. Ex: Initially, the D-frontier of this example is $\{G5, G6\}$.

Ex: Decisions When Line Justification



The corresponding decision tree

FA $\Rightarrow h=D'$; FP $\Rightarrow e=1, f=1 (\Rightarrow o=0)$; FP $\Rightarrow q=1, r=1$.

To justify $q=1 \Rightarrow l=1$ or $k=1$.

Decision: $l=1 \Rightarrow c=1, d=1 \Rightarrow m=0, n=0 \Rightarrow r=0. \Rightarrow$ inconsistency \Rightarrow backtracking!!

Decision: $k=1 \Rightarrow a=1, b=1$.

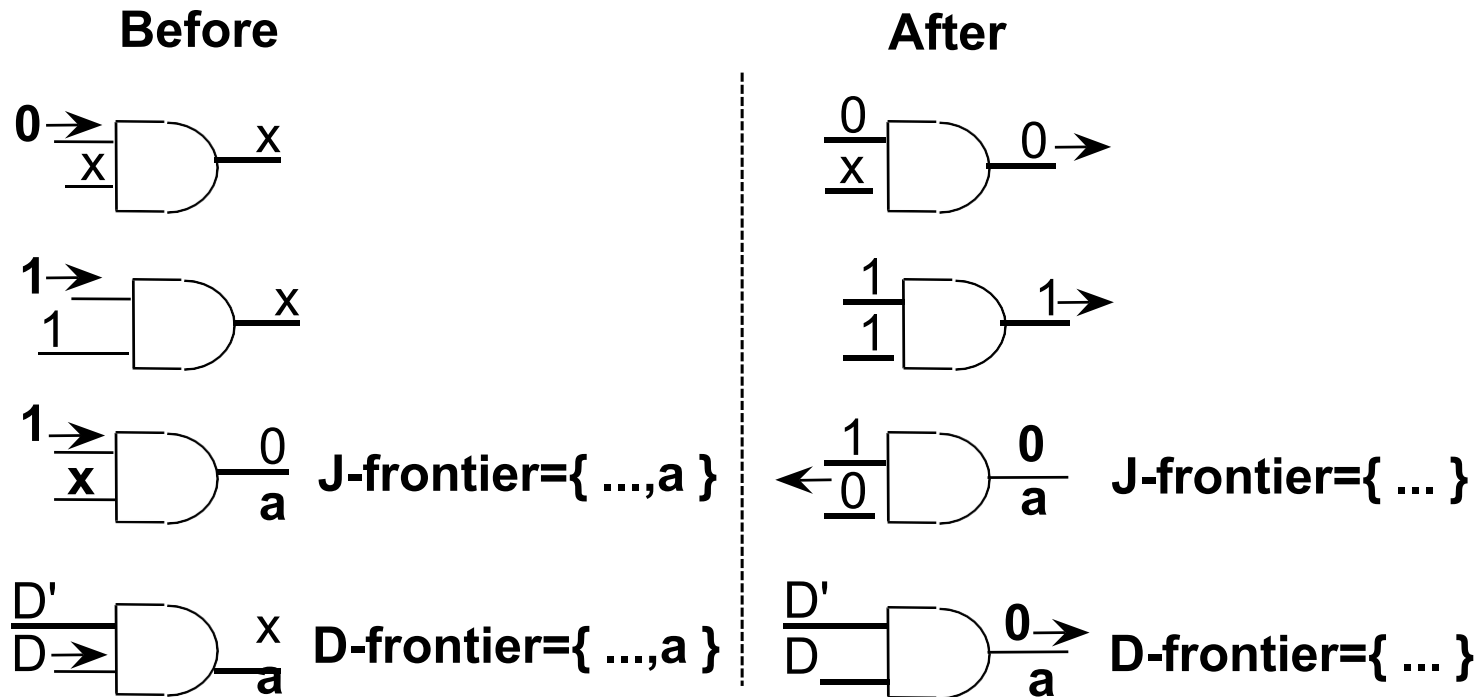
To justify $r=1 \Rightarrow m=1$ or $n=1 (\Rightarrow c=0$ or $d=0). \Rightarrow$ done!!

J-frontier: The set of all gates whose output value is known but is not implied by its input values. Ex: Initially, the J-frontier of the example is $\{q=1, r=1\}$.

Implications

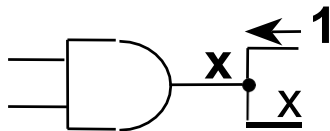
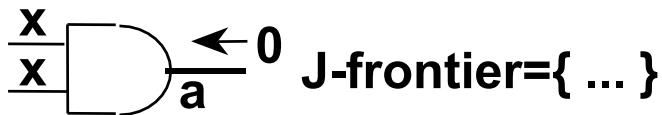
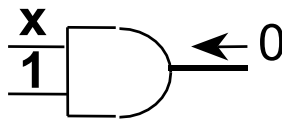
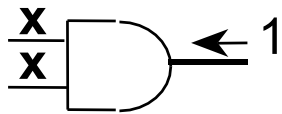
- **Implication: computation of the values that can be uniquely determined.**
 - Local implication: propagation of values from one line to its immediate successors or predecessors.
 - Global implication: the propagation involving a larger area of the circuit and reconvergent fanout.
- **Maximum implication principle: perform as many implications as possible.**
- **Maximum implications help us to either reduce the number of problems that need decisions or to reach an inconsistency sooner.**

Local Implications (Forward)

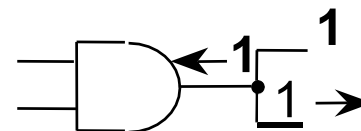
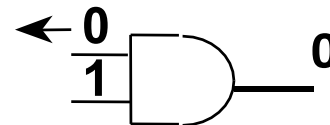
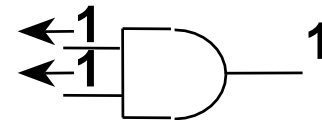


Local Implications (Backward)

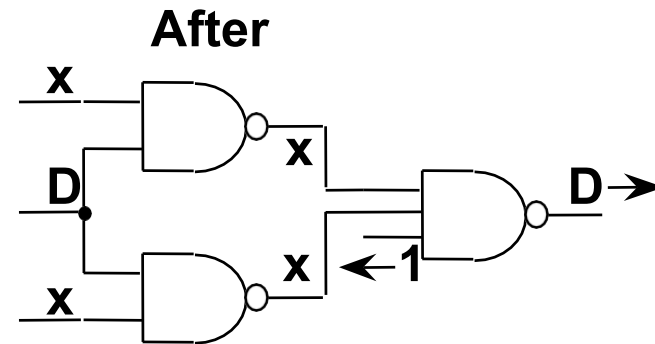
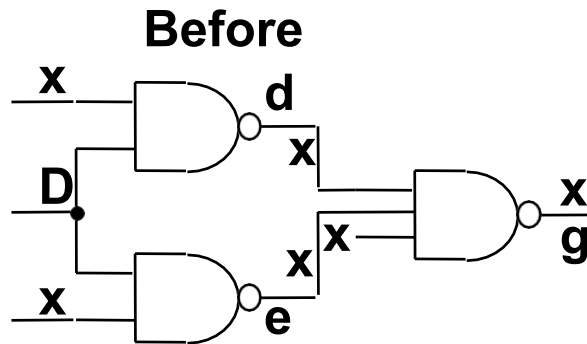
Before



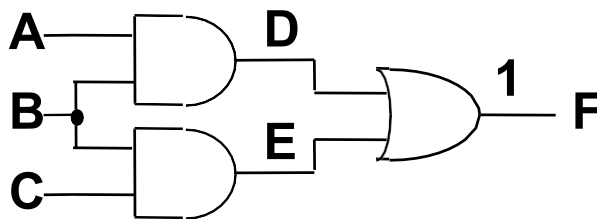
After



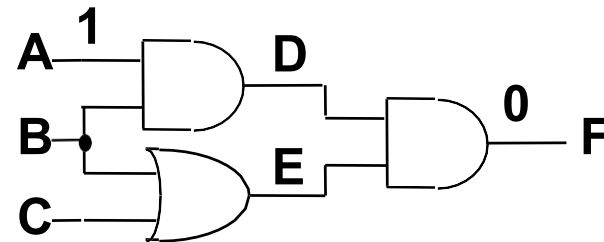
Global Implications



(1) **Future unique D-drive.**



(2) **F=1 implies B=1.**
(Static learning)

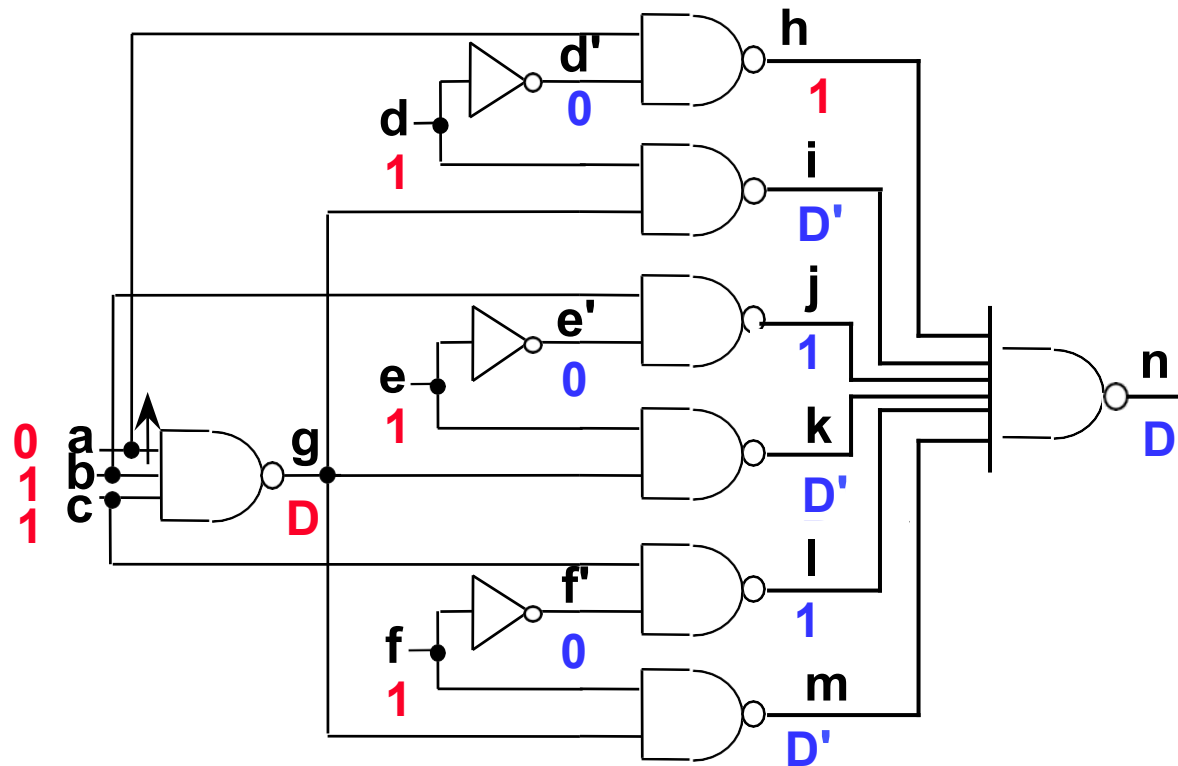


(3) **F=0 implies B=0 when A=1.**
(Dynamic learning)

(2), (3) are based on contraposition law: $(A \Rightarrow B) \Leftrightarrow (!B \Rightarrow !A)$.

D-Algorithm: Example

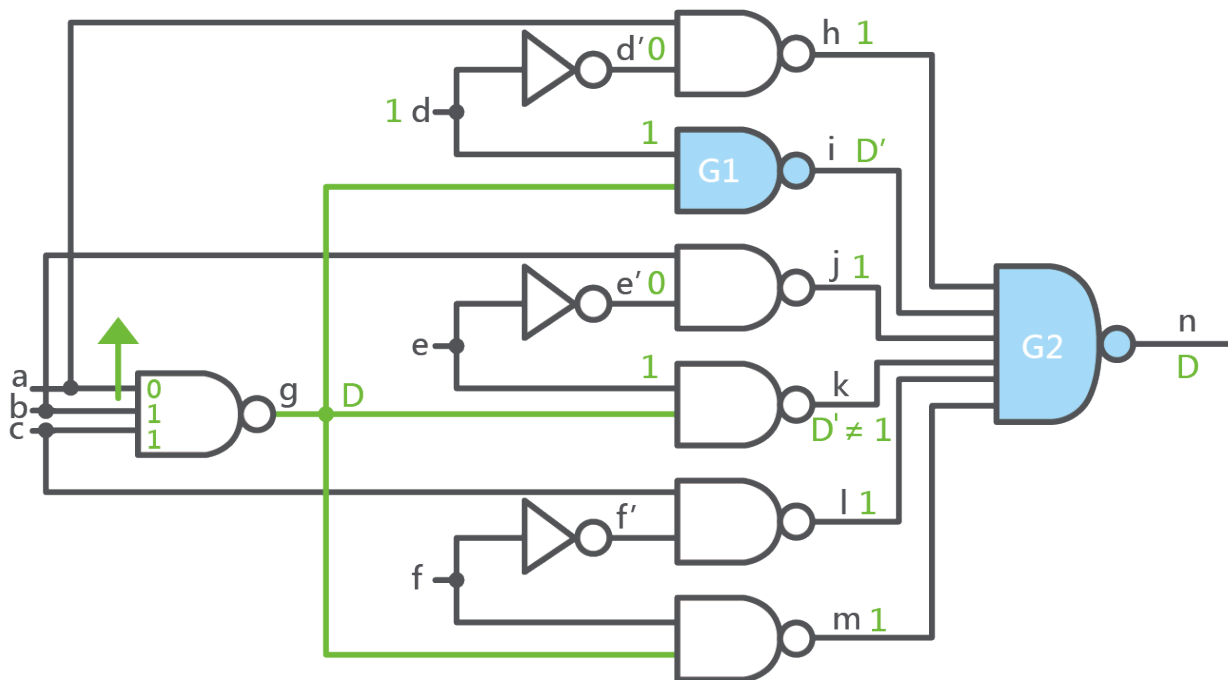
- Logic values = $\{0, 1, D, D', x\}$.



Assignment
Implication

D-Algorithm: Example

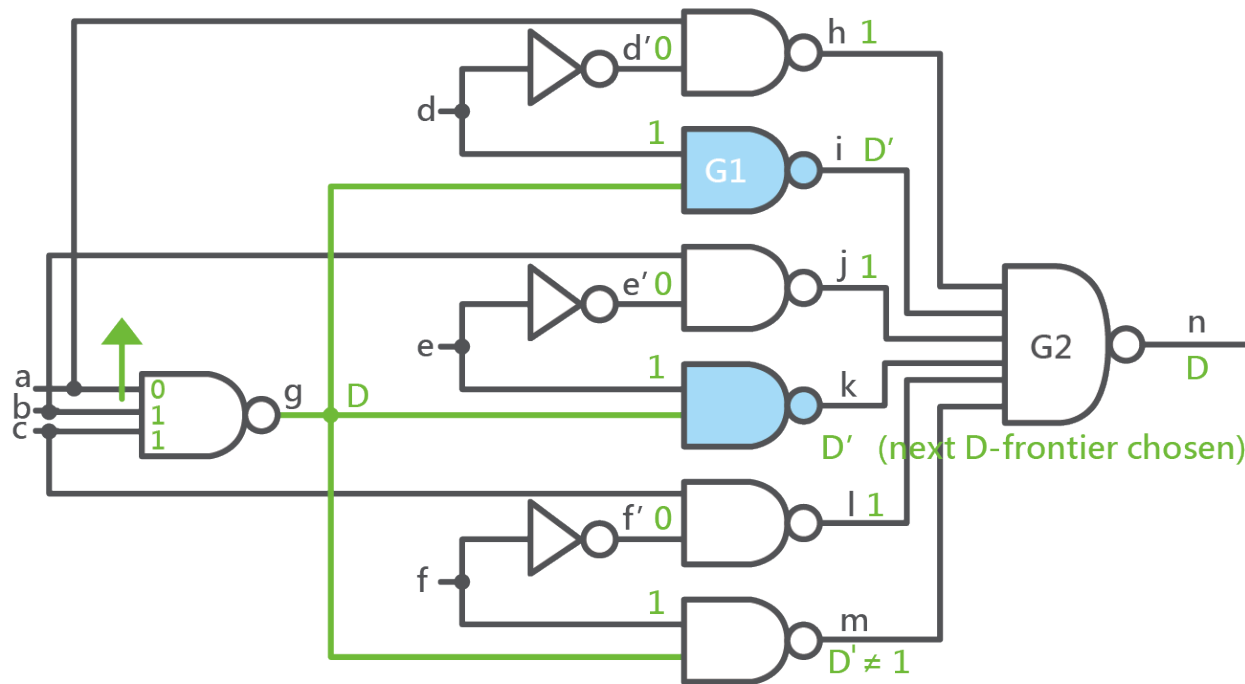
- Logic values = $\{0, 1, D, D', x\}$.



1. Propagate fault effect through G1 → Set d to 1
2. Propagate fault effect through G2 → Set j,k,l,m to 1
3. Conflict occurred at k → Backtrack

D-Algorithm: Example

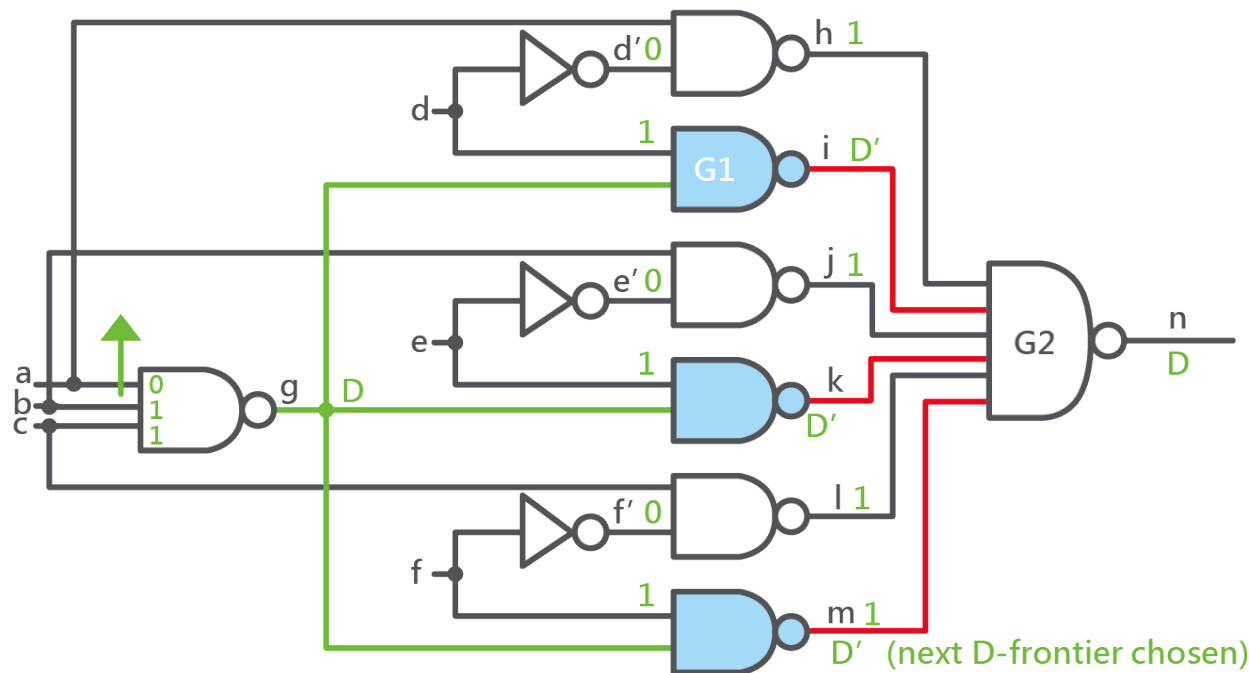
- Logic values = $\{0, 1, D, D', x\}$.



1. Propagate fault effect through G2 → Set j, l, m to 1
2. Conflict occurred at m → Backtrack

D-Algorithm: Example

- Logic values = $\{0, 1, D, D', x\}$.

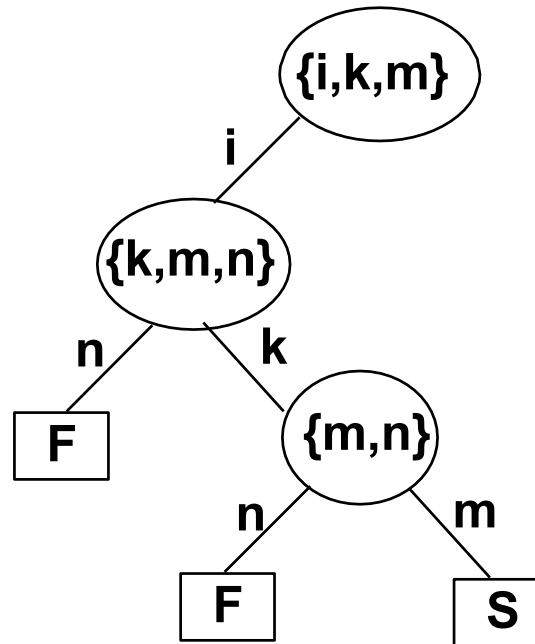


1. Propagate fault effect through G2 → Set j,l to 1
2. Fault propagation and line justification finish

D-Algorithm: Value Computation

| Decision | Implication | Comments |
|--|---|---|
| | $a = 0$ $h = 1$ $b = 1$ $c = 1$ $g = D$ | Active the fault Unique D-drive |
| | | $e = 1$ $k = D'$ $e' = 0$ $j = 1$ Propagate via k |
| $d = 1$ | $i = D'$ $d' = 0$ | Propagate via i $l = 1$ $m = 1$ $n = D$ $f' = 0$ $f = 1$ $m = D'$ Propagate via n |
| $j = 1$ $k = 1$ $l = 1$ $m = 1$ | $n = D$ $e' = 0$ $e = 1$ $k = D'$ | Propagate via n Contradiction $f = 1$ $m = D'$ $f' = 0$ $l = 1$ $n = D$ Propagate via m |

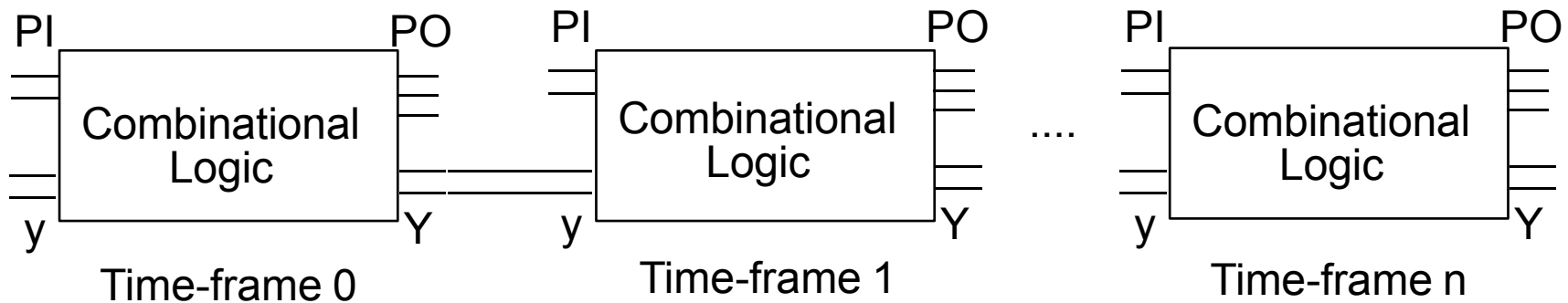
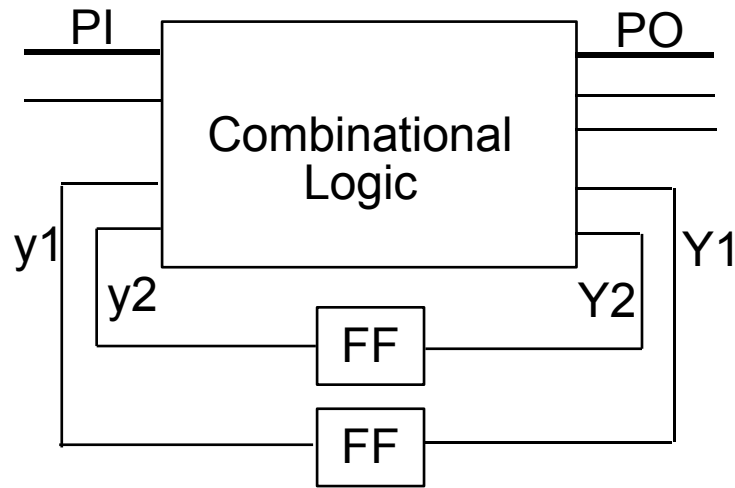
D-Algorithm: Decision Tree



Two times of backtracking!!

- **Decision node:** the associated D-frontier.
branch: the decision taken, i.e., the gate selected from the D-frontier.
- The D-algorithm first tried to propagate the fault solely through i , then through both i and k , and eventually succeeded when all three paths were simultaneously sensitized.

Iterative Logic Array (ILA) Model for Sequential Circuits

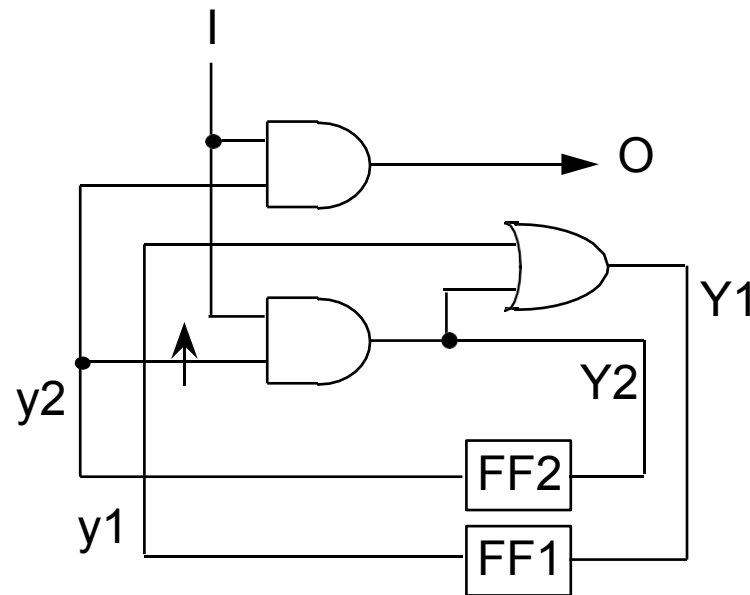


Sequential Test Generation

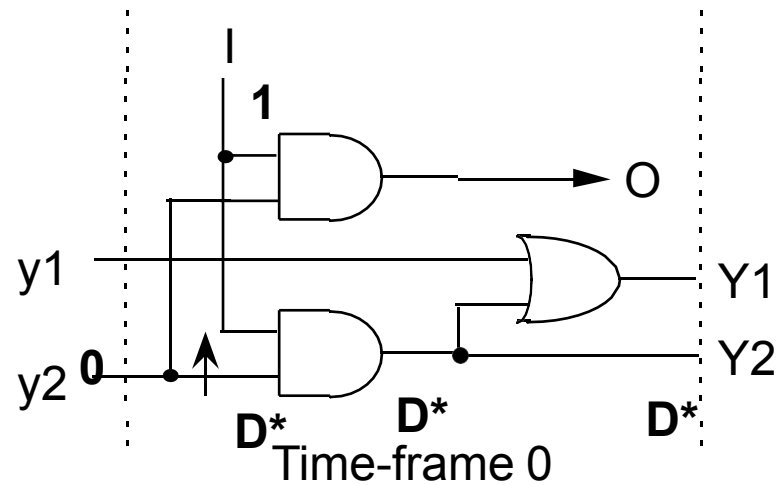
Extended D-Algorithm

- 1. Pick up a target fault f .**
- 2. Create a copy of a combinational logic, set it time-frame 0.**
- 3. Generate a test for f using D-algorithm for time-frame 0.**
- 4. When the fault effect is propagate to the DFFs, continue fault propagation in the next time-frame.**
- 5. When there are values required in the DFFs, continue the justification in the previous time-frame.**

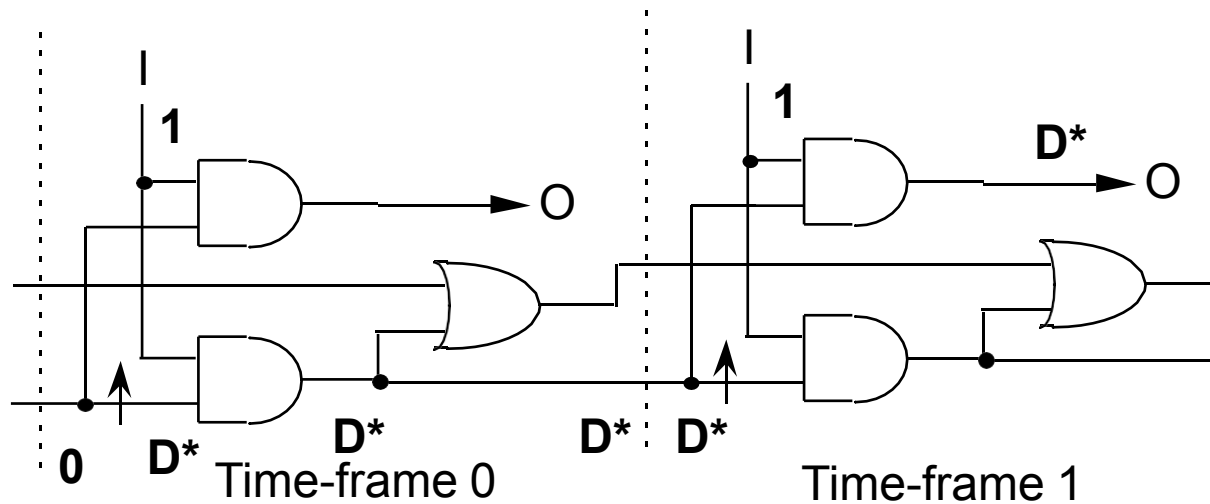
Example for Extended D-Algorithm



Example: Step 1



Example: Step 2



Example: Step 3

