

9 1/2

```
# CELL PROVIDED  
  
# %pip install -q japanize-matplotlib-jlite py4macro
```

```
# CELL PROVIDED  
  
import japanize_matplotlib_jlite  
import numpy as np  
import matplotlib.pyplot as plt  
import py4macro  
import random  
  
plt.rcParams['figure.figsize'] = (5, 3.75)
```

$$\mu \quad (\quad) \quad (1)$$

$$X_1, X_2 \cdots X_n \quad n$$

$$\bar{X}_n = \frac{X_1 + X_2 + \cdots + X_n}{n} \quad (2)$$

Law of Large Numbers

$$\mu \quad X_1, X_2, \dots, X_n \quad \bar{X}_n \quad n \quad \mu$$

$$\lim_{n \rightarrow \infty} \bar{X}_n = \mu \quad (3)$$

$$\mu = 0.5 \times 1 + 0.5 \times 0 = 0.5$$

9.2.1

```
random.randint(0,1)
```

1

9.2.2

```
n = 30
toss = [random.randint(0,1) for _ in range(n)]
head = sum(toss)
avr = head / n
avr
```

0.4333333333333335

1:

2:

$\frac{1}{3} X_1 + \frac{1}{3} X_2 + \frac{1}{3} X_3 = \frac{(X_1 + X_2 + X_3)}{3}$	$\frac{1}{N} \bar{X}_2 = \frac{(X_1 + X_2)}{2}$	$\frac{1}{N} \bar{X}_3 = \frac{(X_1 + X_2 + X_3)}{3}$	$\frac{1}{N} \bar{X}_N = \frac{(X_1 + X_2 + \dots + X_N)}{N}$
	$\frac{* 1}{2} + \frac{* 1}{3}$	$\frac{1}{2} + \frac{1}{3}$	$\frac{1}{3} + \frac{1}{N}$
	$\frac{1}{2} + \frac{1}{3}$	$\frac{1}{3} + \frac{1}{N}$	$\frac{1}{N} + \frac{1}{N}$
	$\frac{1}{2} + \frac{1}{3}$	$\frac{1}{3} + \frac{1}{N}$	$\frac{1}{N} + \frac{1}{N}$

```
N = 2000
sample = range(1, N+1) # 1 2000
```

2

9.2.8

```
random.seed(123)                      #

head_count = 0                         #
avr_lst2 = []                          #

for i in range(1, N+1):                # 1 2000    for
    coin = random.randint(0, 1)         # i
    head_count = head_count + coin    # 1 0   head_count
    avr = head_count / i              # i
    avr_lst2.append(avr)              # avr_lst2

plt.plot(sample, avr_lst2,            # 1 2000
          linewidth=0.9,             #
          color="black")            #

plt.title("  2",                   #
          size=12)                 #

plt.xlabel(" ", size=10)           #
plt.ylabel(" ", size=10)           #
plt.show()
```



