Lecture 9: Models Compression Techniques

AC215

Pavlos Protopapas SEAS/Harvard



Motivation

We want to process data (ideally a lot) and we do not have enough computing resources. For example:

- 1. Your phone can't run GoogleNet to assist you in some tasks
- 2. You can't compress enormous number of images coming from space (8Kx8K pixels from 3K satellites)
- 3. You cannot run "big" LLMs locally.

Using machine learning is resource intensive:

- Computing power to train millions/billions of parameters or predict for many observations
- ii. Limited bandwidth

So what? Model compression techniques

Hannah Peterson and George Williams, <u>An Overview of Model</u>

<u>Compression Techniques for Deep Learning in Space</u>, August 2020

What is Model Compression?

The main idea is to simplify the model without diminishing accuracy. A simplified model means reduced in size and/or latency from the original. Both types of reduction are desirable.

- Size reduction can be achieved by reducing the model parameters and thus using less RAM.
- Latency reduction can be achieved by decreasing the time it takes for the model to make a prediction, and thus lowering energy consumption at runtime (and carbon footprint).

Karen Hao, <u>Training a single AI model can emit as much carbon as five</u> <u>cars in their lifetimes</u>, June 2019

Compression Techniques

- Knowledge distillation
- Pruning

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Problem:

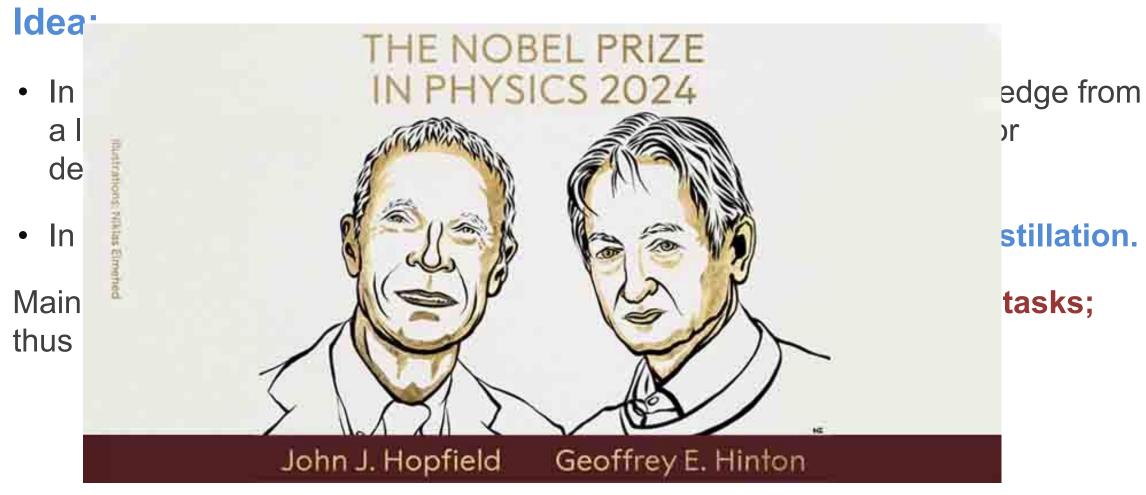
- During training, a model does not have to operate in real time and does not necessarily face restrictions on computational resources, as its primary goal is simply to extract as much structure from the given data as possible.
- But latency and resource consumption do become of concern if it is to be deployed for inference.

So what? we must develop ways to compress model for inference.

Idea:

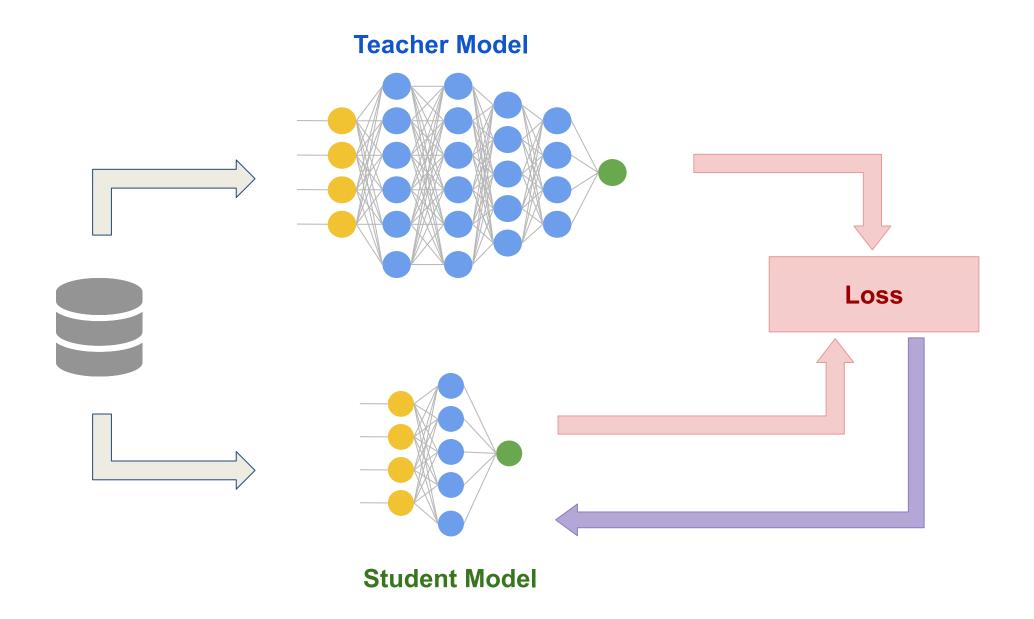
- In 2006, Buciluă et al. showed that it was possible to transfer knowledge from a large trained model (or ensemble of models) to a smaller model for deployment by training it to mimic the larger model's output.
- In 2014 Hinton et al generalized the process and gave the name Distillation.

Main idea of distillation is that training and inference are 2 different tasks; thus a different model should be used.



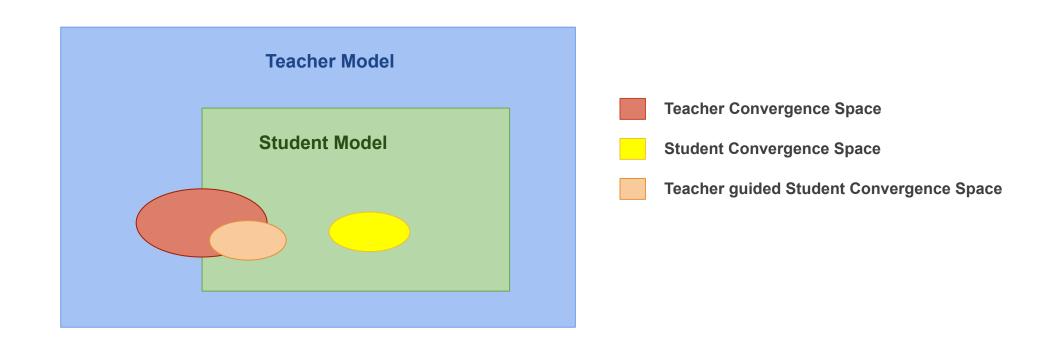
Buciluă et al., <u>Model Compression</u>, 2006 Hinton et al., <u>Distilling the Knowledge in a Neural Network</u>, 2014

Distillation: Teacher Student



Distillation: Teacher Student

Assumption: if we can achieve similar convergence using a smaller network, then the convergence space of the Teacher Network should overlap with the solution space of the Student Network.



Training on one-hot encoded labels only give information about a specific class with complete certainty.

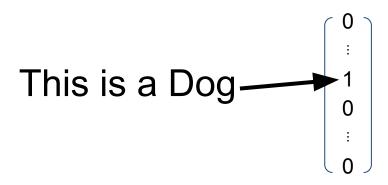
This ignores the rich taxonomy that might exist on a dataset.

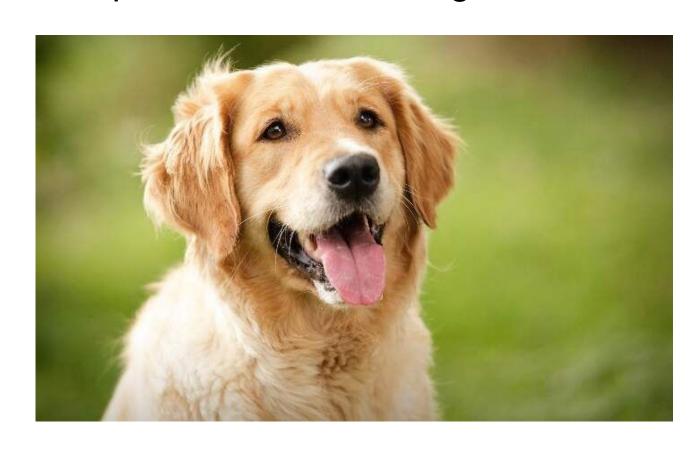
Models trained in this setting, will be overconfident in the predictions, hurting the prediction on unseen data.



While training, our confidence in the labels must be high.

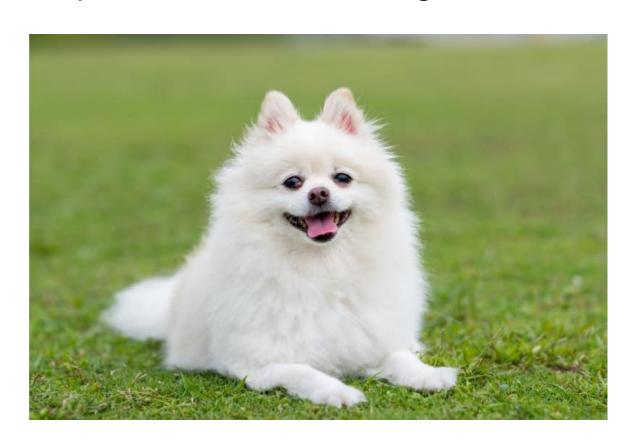
Otherwise the data would not be present in the training set.





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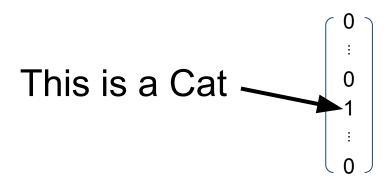
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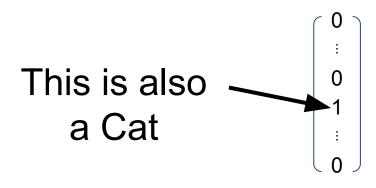
Otherwise the data would not be present in the training set.





While training, our confidence in the labels must be high.

Otherwise the data would not be present in the training set.





What about this example?

This is a ...
$$\begin{bmatrix} 0 \\ \vdots \\ 0.5 \\ 0.5 \\ \vdots \\ 0 \end{bmatrix}$$
?



In the real world, the distinction is never that clear.

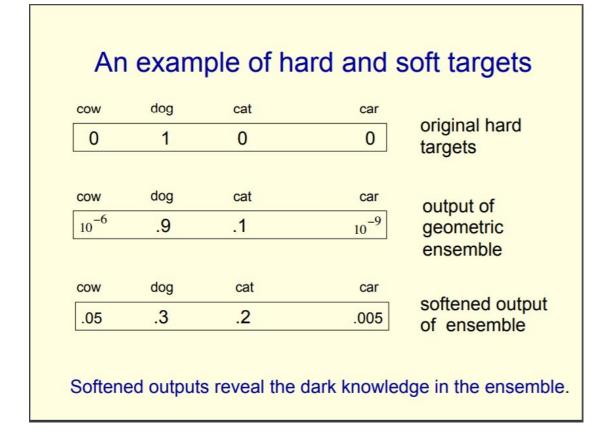
Ideally, the training labels must be soft, to learn about the nuanced relations across the elements of the dataset.



Distillation: Teacher Student Loss

Modified softmax function with Temperature:

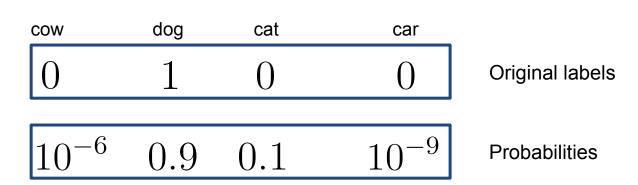
$$q_i = \frac{exp(\frac{z_i}{T})}{\sum_j exp(\frac{z_j}{T})}$$



Distillation: Teacher - Student

The teacher shows the student the relations between the different classes, based on what it learned during its training stage.

From a dataset containing the original categories, the teaching outputs the normalized probabilities for each example.



Adapted from:

Distillation: Teacher - Student

To enhance the student's learning, the teacher softens its output *z* even more.

To do this, introduces the softmax function with temperature *T*:

$$q_i = \frac{exp(\frac{z_i}{T})}{\sum_j exp(\frac{z_j}{T})}$$

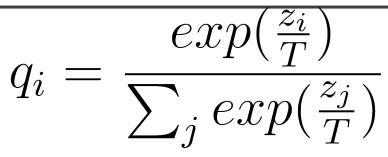
cow	dog	cat	car	
0	1	0	0	Original labels
10^{-6}	0.9	0.1	10^{-9}	Softmax probabilities
0.05	0.3	0.2	0.005	Softened probabilities

Adapted from:

Distillation: Teacher - Student

A high value of T will dilute the information contained in the probabilities.

- The standard softmax is recovered for *T*=1.
- For T>1, the probabilities are softened. Typical values range between 2 and 5.
- For T<1, it approaches to the original one-hot labels.



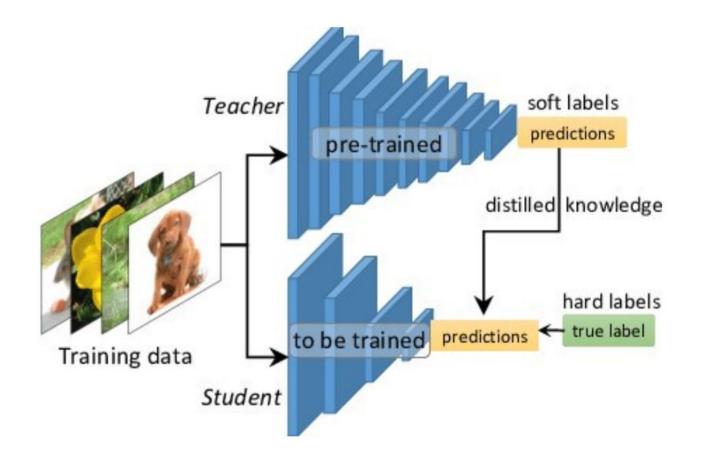
COW	dog	cat	car	
0	1	0	0	Original labels
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Adapted from:

Temperature explanation



The student is trained to solve the original problem, and to replicate the softened probabilities from the teacher.



Scenario 1:

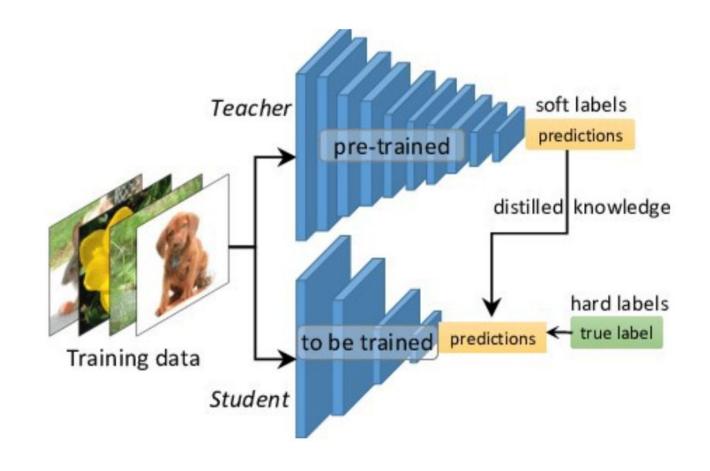
Train on the same data as the teacher model. DistilBert was trained on this example.

Scenario 2:

Train on a reduce dataset. This is usually done when you have the model but not the original dataset or resources.

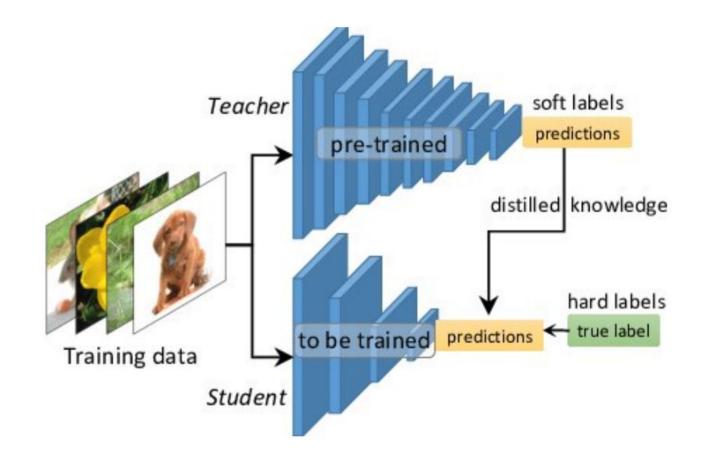
It minimizes the sum of two different cross entropy functions:

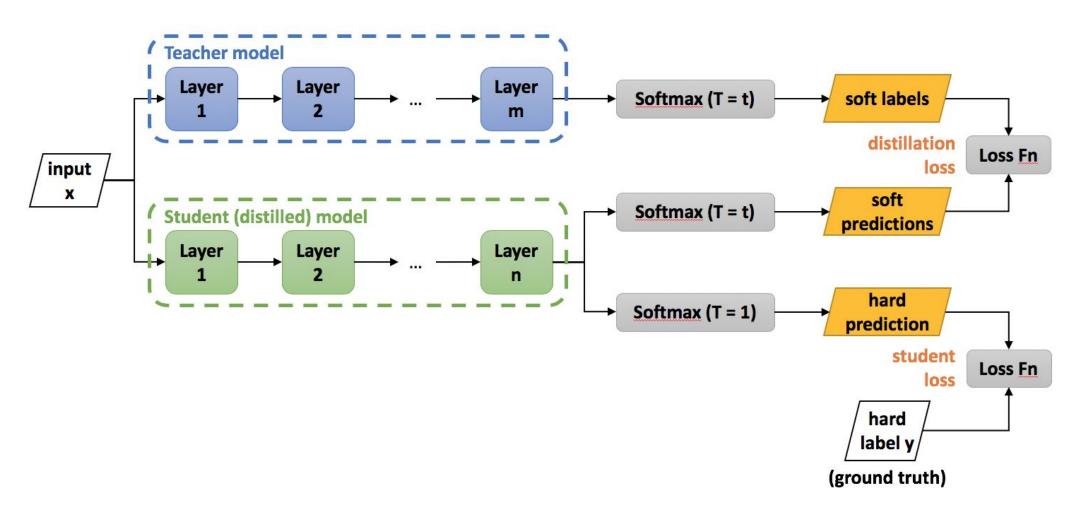
- one involving the original hard labels obtained using a softmax with *T*=1
- one involving the softened probabilities with T>1



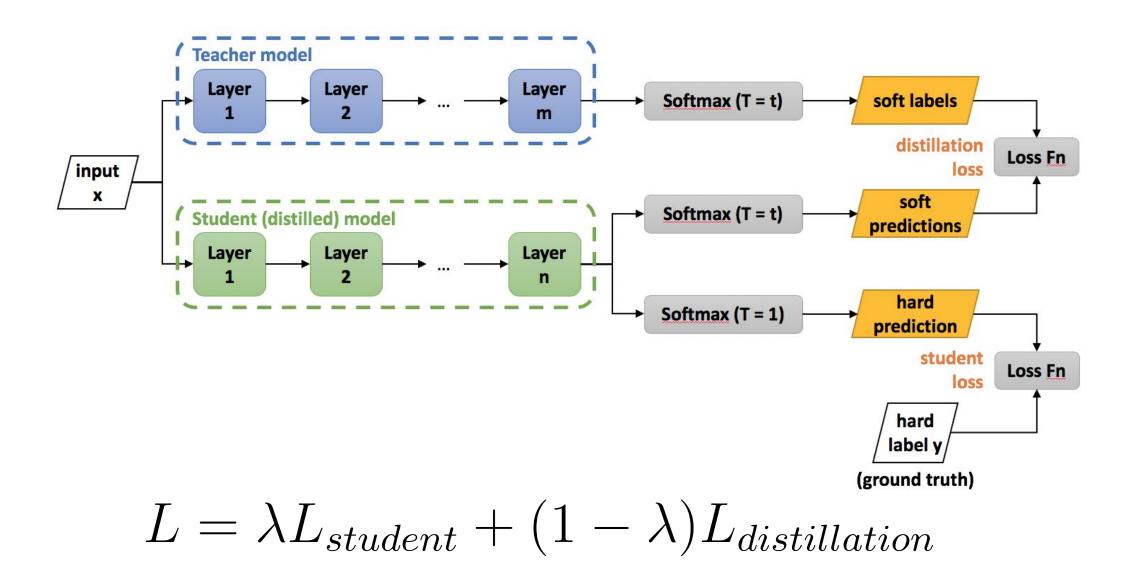
Trained to minimize the sum of two different cross entropy functions:

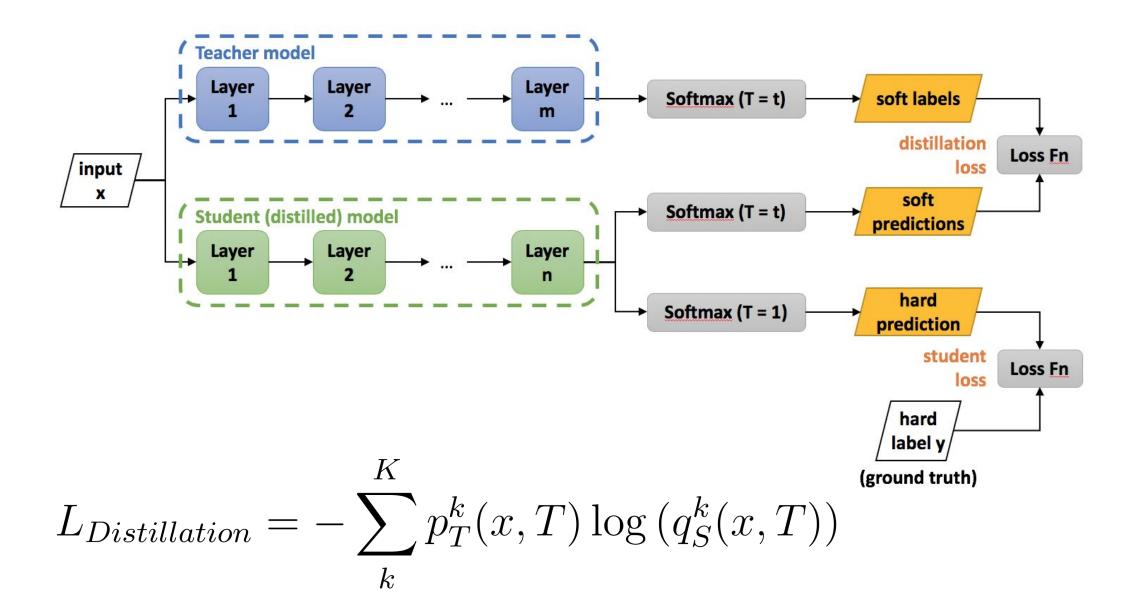
- one involving the original hard labels obtained using a softmax with T=1
- one involving the softened targets, T>1





$$L = \lambda L_{\text{student}} + (1 - \lambda) L_{\text{distillation}}$$





$$L_{Distillation} = -\sum_{k}^{K} p_{T}^{k}(x, T) \log (q_{S}^{k}(x, T))$$

In our example, for the example *n* in the dataset.

$$p_T(x,T) = [0.05, 0.3, 0.2, 0.005]$$

And our predictions

$$q_T(x,T) = [0.1, 0.45, 0.30, 0.15]$$

The resulting loss value for this example is:

$$-[0.05 \cdot \log (0.1) + 0.3 \cdot \log (0.45) + 0.2 \cdot \log (0.30) + 0.005 \cdot \log (0.15)]$$

Tutorial: Model Distillation

Colab Notebook



What is next in Distillation?

- 1: Multiple teachers (i.e. converting an ensemble into a single network).
- 2: Introducing a teaching assistant (the teacher first teaches the TA, who then in turn teaches the student) etc.
- 3: Learning not only the output, but the intermediate representations.
- 4: Quite a young field

A drawback of knowledge distillation as a compression technique, therefore, is that there are many decisions that must be made up-front by the user to implement it (student network doesn't even need to have a similar structure to the teacher).

What is next in Distillation?

- 1: Multiple teachers (i.e. converting an ensemble into a single network).
- 2: Introducing a teaching assistant (the teacher first teaches the TA, who then in turn teaches the student) etc.
- 3: Quite young field

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Compression Techniques

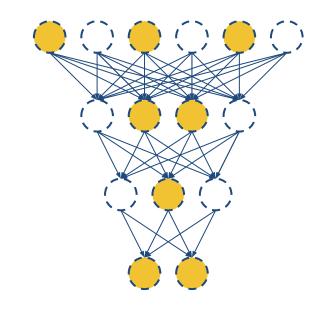
- Knowledge distillation
- Pruning

Pruning is based on the idea of the Lottery Ticket Hypothesis.

A randomly-initialized neural network contains a subnetwork that is initialized such that - when trained in isolation- it can match the test accuracy of the original network after training for at most the same number of iterations.

Inside each network, we might find a winning ticket where a small subset of the neurons are non-zero.

In principle, this network will be use less memory, perform faster during inference without losing performance.

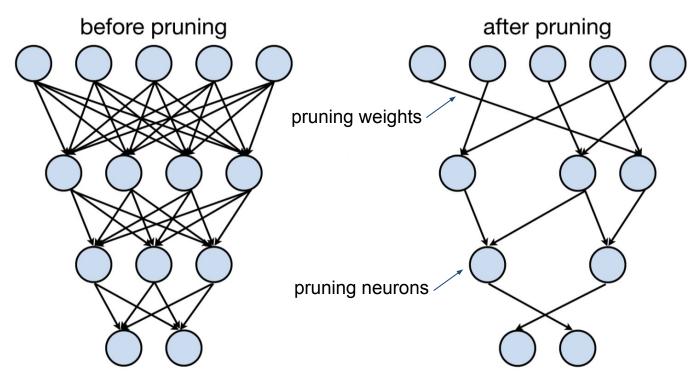


The main idea is to remove less impactful features of the neural network.

Pruning involves removing connections between neurons, and neurons from a trained network. To prune a connection, we set a weight in the matrix to zero.

Two types of pruning:

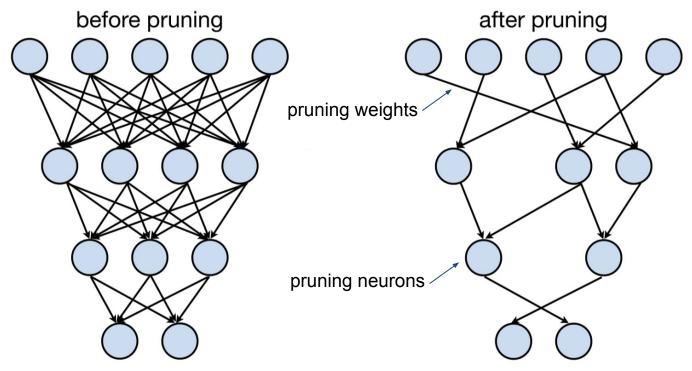
- Pruning weights
- Pruning structure



<u>Learning Both Weights and Connections for Efficient Neural Network</u> [Han et al., NeurlIPS 2015]

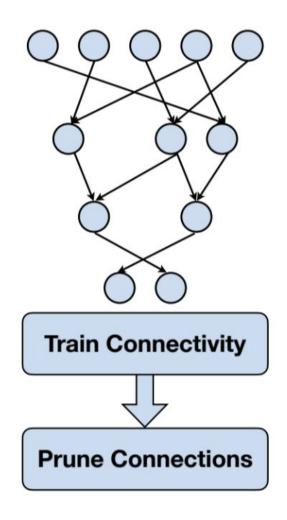
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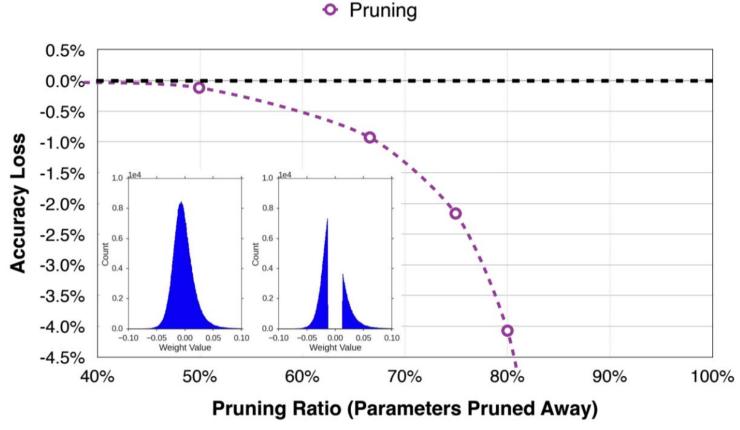
The criteria to select the rank the relevant features might depend on the weights absolute value, on the activations magnitudes, among other values.



<u>Learning Both Weights and Connections for Efficient Neural Network</u> [Han et al., NeurlIPS 2015]

Make neural networks smaller by removing weights and neurons

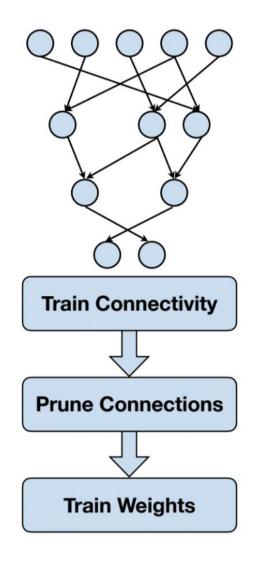


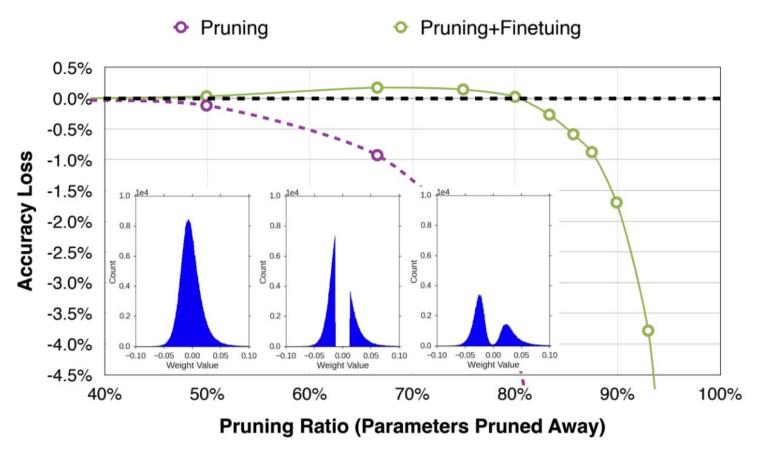


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MIT EfficientML.ai: Pruning and Sparsity

Make neural networks smaller by removing weights and neurons

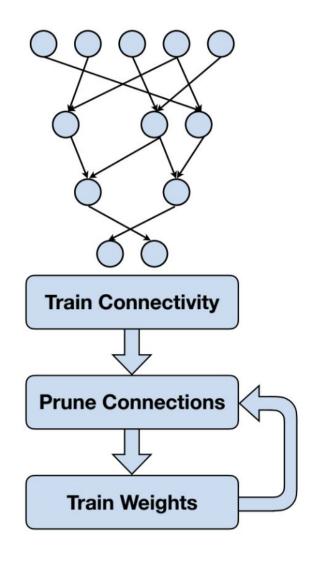


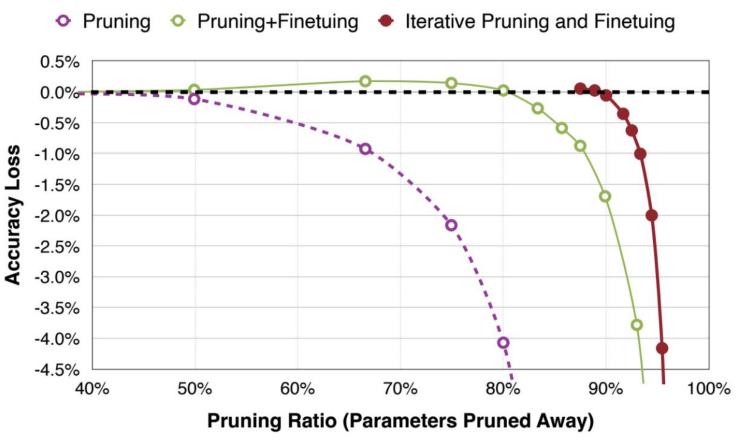


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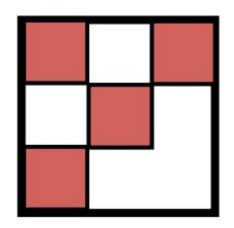


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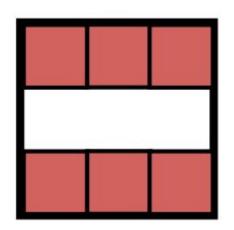
Pruning Granularities

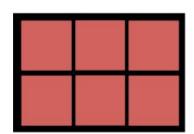
Simple 2-D weight matrix example



Fine-grained/Unstructured

- More flexible pruning index choice
- Hard to accelerate (hardware limitations)





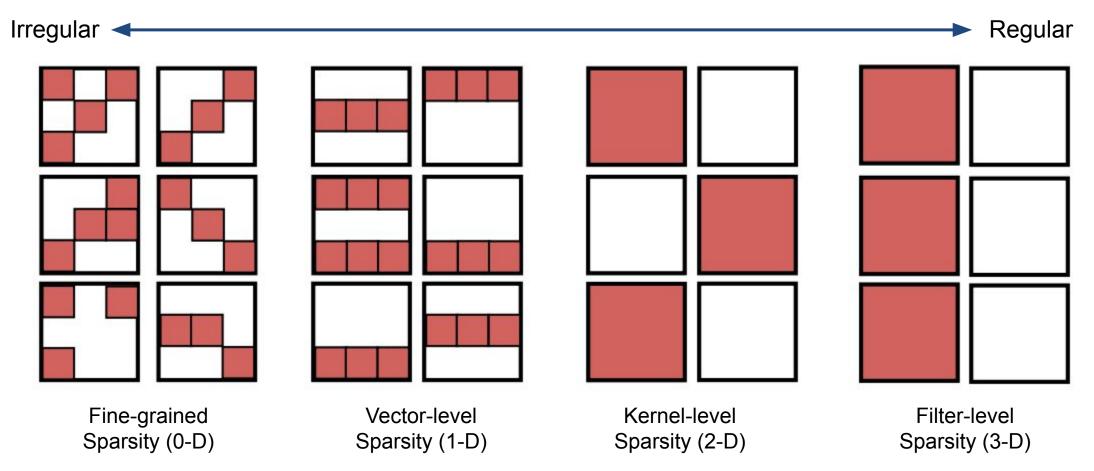
Coarse-grained/Structured

- Less flexible pruning idex choice (a subset of the fine-grained case)
- Easy to accelerate (just a smaller matrix!)

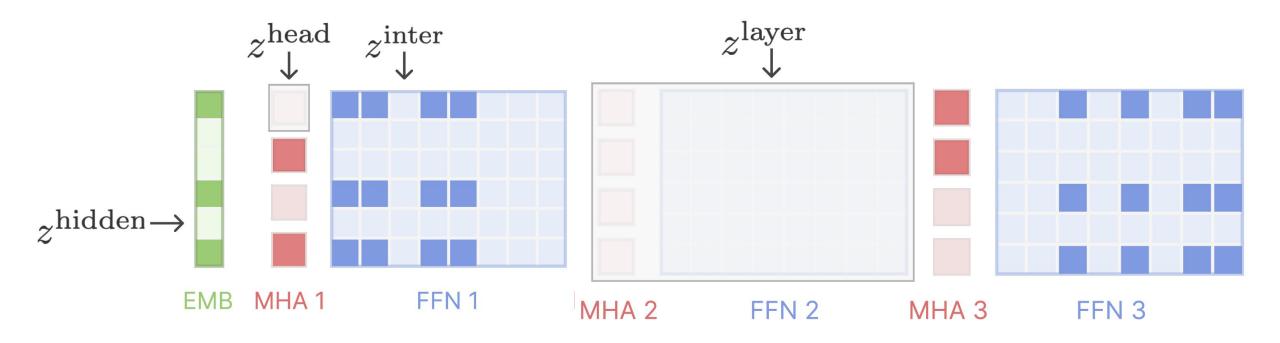
Exploring the Regularity of Sparse Structure in Convolutional Neural Networks [Mao et al., CVPR-W]

Example using convolutional layers

- Commonly used pruning granularities



Pruning on transformers can be applied at different levels



Drawbacks of neural network pruning:

- Optimal Pruning Challenge: determining the optimal neurons or weights to prune
 without detrimentally impacting model performance can be complex and time consuming
 in practise.
- Fine-Tuning Requirement: after pruning, models typically require additional fine-tuning to recover potential losses in predictive accuracy, which might consume additional training resources and time.
- Hardware Dependency: pruned models might not always translate to proportional computational or energy savings due to hardware inefficiencies or dependencies in exploiting sparsity.
- Model Robustness: excessive or imprecise pruning may lead to a substantial decrease in model accuracy or robustness, especially when encountering unseen or out-of-distribution data.

Compression Technique: Next steps

Things to consider:

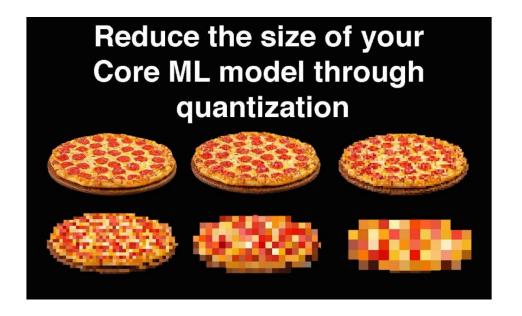
- Quantization, distillation and pruning applied alone can reduce the models complexity.
- But together, these techniques achieve state-of-the-art performance while keeping a "reduced size".
- Distilled LLMs can still be huge, with ~7 billion parameters.
- The choice of methodology depends on the dataset, tasks and models.
- Finetuning is always necessary to regain performance losses. LoRA is extremely relevant.
- There is no general methodology that will work out of the box. Experiment!



Tutorial: Model Pruning

Colab Notebook

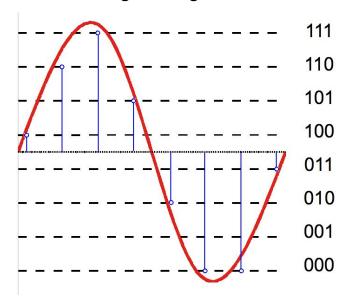
Main idea is to map values from a large set to values in a smaller set without losing too much information in the process. So by reducing the number of pixels, the image below should still be clear.



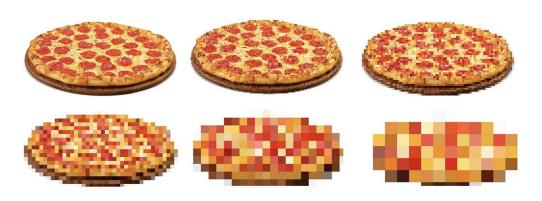
To implement quantization with Tensorflow: MC.AI, *Quantization in Deep Learning using TensorFlow 2.X*, May 2020

Main idea is to map values from a continuous or a large discrete set to values in a smaller discrete set without losing too much information in the process.

Reducing a continuous signal, while maintaining the signal information.



Reducing the number of pixels, while maintaining the image content.



<u>Image</u> is in the public domain. "Analog to digital converter"

To implement quantization with Tensorflow: MC.AI, *Quantization in Deep Learning using TensorFlow 2.X*, May 2020

Size of a Deep Neural Network (in bytes)

deep_nn_size ~ num_parameters * parameter_size

num_parameters = total number of weights and biases of NN
parameter_size = size of parameter in bytes (e.g. 4 bytes for float32)

Bottlenecks in Training and Inference of Deep Neural Networks

Memory Limitations: Memory demands for training large models, storing parameters, and handling intermediary computations challenge available GPU memory, restricting model complexity, and training efficiency.

Data Transfer Bottlenecks: Substantial data movement between storage (e.g., disks), CPUs, and GPUs, generates bottlenecks that slow down training and make real-time processing strenuous.

I/O Constraints: Input/output operations, involving reading and preprocessing data, often become bottlenecks, affecting GPU utilization and elongating training times, especially with voluminous and complex datasets.

Weight Quantization Techniques

- K-Means-based Quantization

2.09	-0.98	1.48	0.09
0.05	-0.14	-1.08	2.12
-0.91	1.92	0	-1.03
1.87	0	1.53	1.49

3	0	2	1	3:	2.00
1	1	0	3	2:	1.50
0	3	1	0	1:	0.00
3	1	2	2	0:	-1.00

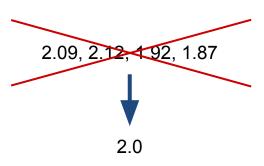
	Full Model	K-Means Quantized Model
Storage	Floating-Point Weights	Integer Weights; Floating-Point Codebook
Computation	Floating-Point Arithmetic	Floating-Point Arithmetic

- Linear Quantization
- Binary/Ternary Quantization

Weight Quantization

weights 32-bit float

2.09	-0.98	1.48	0.09
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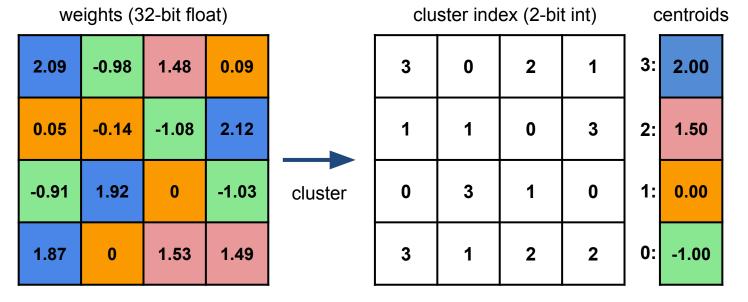


K-Means-based Weight Quantization

weights 32-bit float

2.09	-0.98	1.48	0.09
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K-Means-based Weight Quantization



Assume N-bit quantization, and num_parameters = $M >> 2^N$.

reconstructed weights (32-bit float)

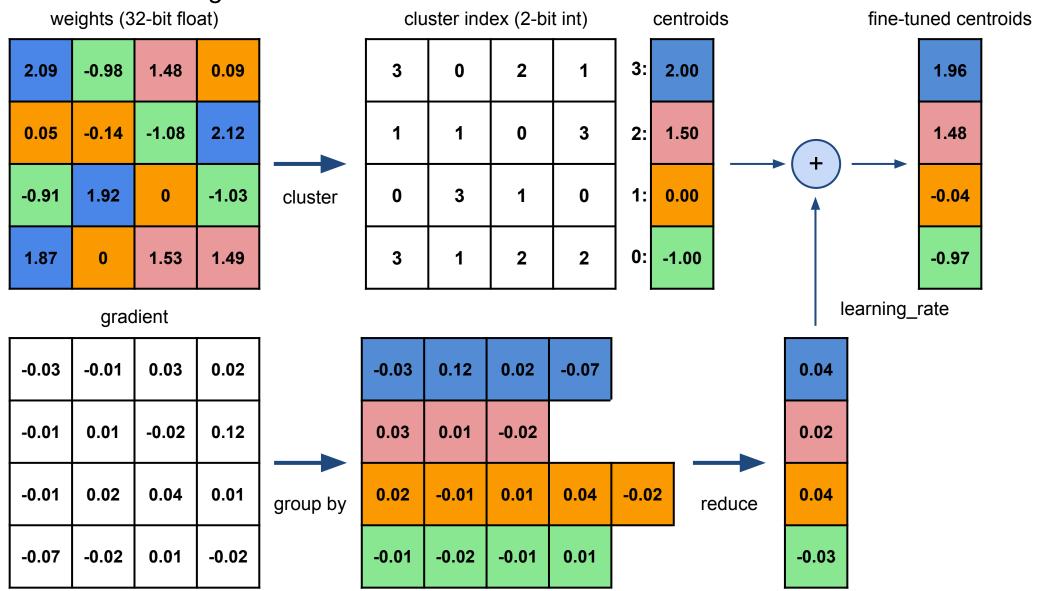
2.00	-1.00	1.50	0.00
0.00	0.00	-1.00	2.00
-1.00	2.00	0.00	-1.00
2.00	0.00	1.50	1.50

quantization error

0.09	0.02	0.02	0.09
0.05	0.14	0.08	0.12
0.09	0.08	0	0.03
0.13	0	0.03	0.01

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K-Means-based Weight Quantization



K-Means-based Weight Quantization: Centroids Initialization

Centroid initialization impacts the quality of clustering and thus the network's prediction accuracy.

Three types of initialization:

Forgy (random): Randomly choose k observations from the data set and use these as initial centroids.

- Tends to concentrate around the highest mass of the weights' PDF

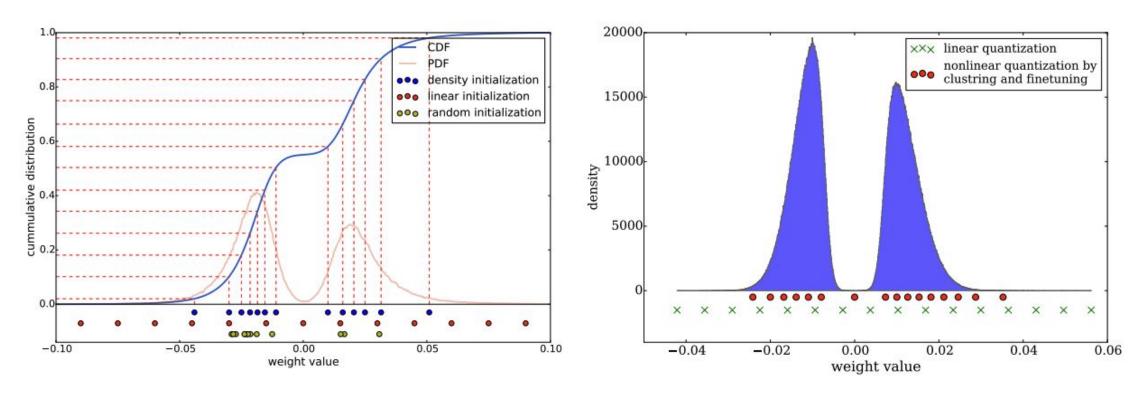
Density-based: Space points linearly on the range of CDF values [0, 1]. Then finds horizontal intersection with the CDF of the weights' distribution.

- Makes the centroids dense around the highest mass, but more scattered than Forgy

Linear: Space points linearly on the range of weights' values [min_weight_val, max_weight_val].

- This method is invariant to the distribution of the weights - most scattered

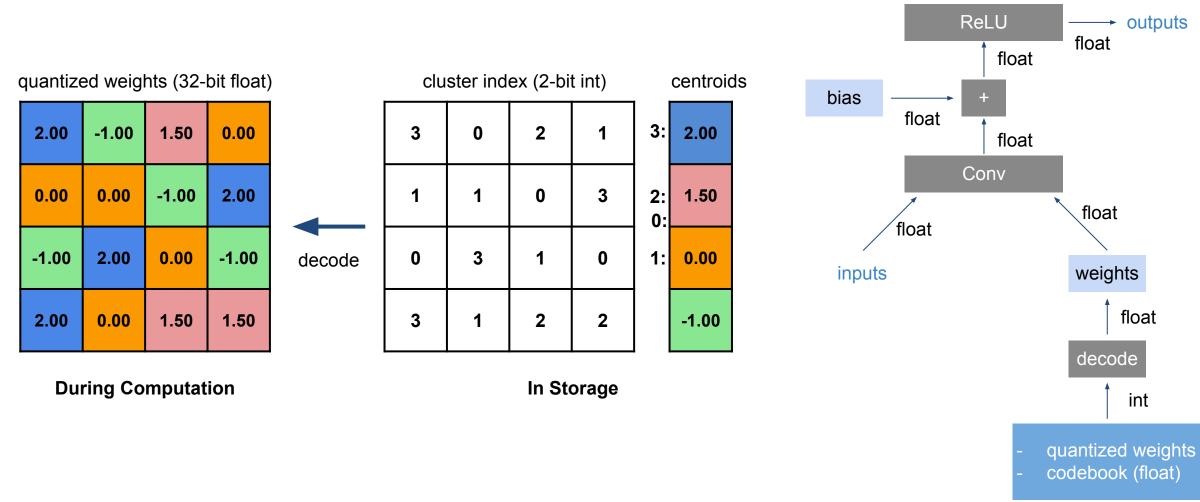
K-Means-based Weight Quantization: Centroids Initialization



Three different methods for centroids initialization

Initial distribution of weights, distribution of codebook before fine-tuning (greencross), and after fine-tuning (red dot)

K-Means-based Weight Quantization



<u>Deep Compression: Compressing Deep Neural Networks with Pruning, Trained Quantization and Huffman Coding</u> [Han et al., ICLR 2016]

Drawbacks of neural network quantization:

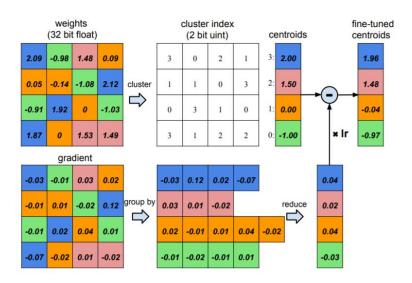
- Proficiency in Hardware Architecture: Necessitates a in-depth understanding of hardware intricacies and bitwise computations.
- Hardware Limitations: Efficiency gains are intrinsically linked to the characteristics and capabilities of the utilized hardware.
- Optimization Difficulties: Maintaining balance between reducing model size through quantization and preserving predictive capabilities could be tricky requiring careful management of the trade-off between model size and accuracy.

Quantization-Aware Training:

There could be an accuracy loss in a post-training model quantization and to avoid this and if you don't want to compromise the model accuracy we do quantization aware training.

This technique ensures that the forward pass matches precision for both training and inference.

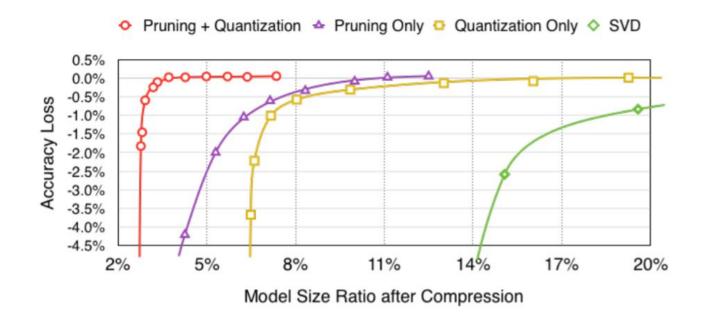
https://www.tensorflow.org/model_optimization/guide/quantization/training



Han S. et al, <u>Deep compression: compressing deep neural networks</u> with pruning, trained quantization and huffman coding, 2016

Quantization can be tricky:

- Requires having a decent understanding of hardware and bitwise computations
- Savings are tied to the features of the hardware being used



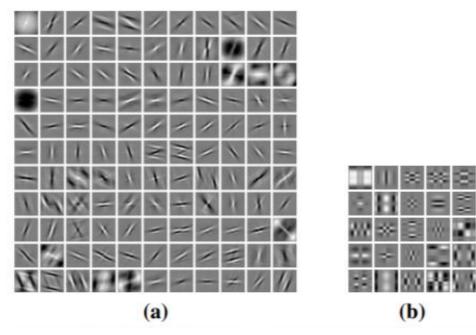
Han S. et al, <u>Deep compression: compressing deep neural networks</u> with pruning, trained quantization and huffman coding, 2016

Compression Technique: Low Rank Approximation

Main idea is to approximate the redundant filters of a layer using a linear combination of fewer filters. Compressing layers in this way reduces the network's memory footprint, the computational complexity of convolutional operations and can yield significant **speedups**.

Examples:

- Singular Value Decomposition
- Tucker decomposition
- Canonical Polyadic decomposition



Rigamonti R. et al., *Learning Separable Filters*, 2013

Compression Technique: Low Rank Approximation

Kim et al. use Tucker decomposition to determine the ranks that the compressed layers should have. They apply the compression to various models for image classification tasks and run them on both a Titan X and Samsung Galaxy S6 phone*:

- Low-rank approximation achieve significant size and latency reductions
- Prove potential deployment on mobile devices
- Reduce parameters simplifying model structure
- Does not require specialized hardware to implement

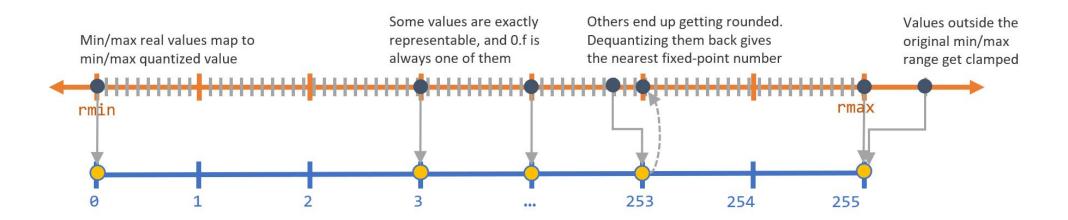
Model	Top-5	Weights	FLOPs	FLOPs S6		Titan X
AlexNet	80.03	61M	725M	117ms	245mJ	0.54ms
AlexNet*	78.33	11M	272M	43ms	72mJ	0.30ms
(imp.)	(-1.70)	$(\times 5.46)$	$(\times 2.67)$	$(\times 2.72)$	$(\times 3.41)$	(×1.81)
VGG-S	84.60	103M	2640M	357ms	825mJ	1.86ms
VGG-S*	84.05	14M	549M	97ms	193mJ	0.92ms
(imp.)	(-0.55)	$(\times 7.40)$	$(\times 4.80)$	$(\times 3.68)$	$(\times 4.26)$	$(\times 2.01)$
GoogLeNet	88.90	6.9M	1566M	273ms	473mJ	1.83ms
GoogLeNet*	88.66	4.7M	760M	192ms	296mJ	1.48ms
(imp.)	(-0.24)	$(\times 1.28)$	$(\times 2.06)$	(×1.42)	$(\times 1.60)$	(×1.23)
VGG-16	89.90	138M	15484M	1926ms	4757mJ	10.67ms
VGG-16*	89.40	127M	3139M	576ms	1346mJ	4.58ms
(imp.)	(-0.50)	$(\times 1.09)$	$(\times 4.93)$	$(\times 3.34)$	$(\times 3.53)$	$(\times 2.33)$

^{*} S6 has a GPU with 35× lower computing ability and 13× smaller memory bandwidth than Titan

Kim et al, <u>Compression of deep convolutional neural networks for fast</u> <u>and low power mobile applications</u>, 2016

Quantization can be achieved by changing the output or NN architecture:

 Post Training Quantization: reducing the size of the weights stored (e.g. from 32-bit floating point numbers to 8-bit)



To implement quantization with Tensorflow: MC.AI, *Quantization in Deep Learning using TensorFlow 2.X*, May 2020

Announcements / Reminders

Milestone 2 Due - 10/18 9PM EST

Please add Staff GitHub Account - @ac2152024 (or ac215.2024@gmail.com) as collaborator (<u>See Ed post</u>)

Upcoming -

Guest Lecture - Modal Labs 10/24

 Milestone 3 - Midterm Presentations - 10/31 (Note: For some groups, presentations may begin and end 15-30 minutes later due to room availability.)