Risk Aware Agent for Bidding in Second-Price Sealed-Bid Auctions and variants

This technical report introduces two forms of a risk aware agent for bidding in Simultaneous Second-Price Sealed-Bid Auctions but who's heuristics are general enough to be used in other auction settings. The main idea of the risk aware agent is the computation of a utility score that given predictions of prices over bundles of goods, considers the risk associated with the distribution of prices over each good contained in a given bundle. This utility is a generalization of the classic acquisition problem described in and used by every agent in .

As a baseline, all agents from were implemented to test the efficacy of the proposed risk-aware agent as well as parallel implementations of both point price predicting and distribution predicting algorithms in order to maximize the number of auction simulations executed in minimal time. The implementation language is Python and all code and documentation can be found in the github repository:

<git://github.com/bam593/bmProjects.git>

The contents can be viewed with a web browser at the address:

<https://github.com/bam593/bmProjects/tree/master/courses/fall2011/csci2951>

Risk Aware Agent

Every strategy profile described in assumes the bidding process can be decomposed into two independent modules:

1. Identify a set of goods that if won would maximize the agent's surplus, defined as valuation less cost (this step is known as the acquisition problem).
2. Compute bids to place on the goods in the bundle that solves that the acquisition problem.

That is we first define a bundle as a collection of goods that we can potentially procure at auction.

If there are goods available, we define the set of all possible bundles, , available for purchase as

where represents the power set of m items. For example, lets' assume , we can enumerate every possible bundle using bit vectors of length , representing the set of all bundles as:

If the entry is 1 in the bundle bit vector, this indicates the good is purchased in bundle , otherwise the good is not included in the bundle.

The agents' valuation function is then a function that assigns a scalar to each bundle

This function is known to the agent prior to bidding. The function used in this report are described in (Sodomka & Greenwald).

Given a vector of prices representing the price paid for each good in a bundle, we can calculate the cost , , associated with each bundle as the dot product of the bundle and the price vector and thus compute the surplus for each bundle.

Therefore the acquisition problem of step (1) is a matter of solving (Boyan & Greenwald, 2001):

The non-additive valuation function described in (Sodomka & Greenwald) and (Yoon & Wellman, 2011) is used to model complementary goods. Goods A and B are complementary if:

That is if we are able to purchase only part of the bundle that solves the acquisition problem, the valuation of the bundle may be zero exposing the agent to a possible negative surplus as he will still be obligated to pay for the items he wins. Therefore, given , (Yoon & Wellman, 2011) describe different strategy profiles that bid differently on this bundle, using techniques based on marginal value calculations shade the bids up to make sure the agent obtains the necessary goods in the target bundle. They also describe a profile bidEvaluator, that uses multiple base strategy profiles to generate candidate bids then evaluate the confidence in each bid against a price distribution and choose the bid by evaluating the candidate bids against the probability distribution over prices of goods.

There are two versions of the risk aware strategy profile, riskAware1 and riskAware2.

riskAware1 attempts to solve a more general form of the acquisition problem, thus modifying the first step above. Given this alternative target bundle, we can use any strategy described in (Yoon & Wellman, 2011) to produce a bid vector.

From economics we define the mean-variance utility function for returns on investments:

<http://en.wikipedia.org/wiki/Modern_portfolio_theory>

The free parameter defines how risk-adverse a particular investor is, defines the expected rate of return of an investment portfolio given a probability distribution and defines the variance associated with the rate of return of the investment and serves as a measure of risk.

Though this function is used in the context of identifying optimal investments for an investor given the investors' level of risk aversion, we can modify this function to conform to our problem.

Let us define:

Using the following property of variance:

we write the mean-variance utility as:

Let us assume as in (Yoon & Wellman, 2011) that prices are independent over goods ,

Given the function and a distribution over prices, we easily calculate and . The intuition behind this heuristic is that we still want to pick the bundle that maximizes the expected surplus for the agent, however, there may be "safer" bundles to bid on quantifying the risk by the variance in the closing prices for that particular good.