

Lecture 8

Lots of definitions today!

$$p(x, y) = p(x|y)p(y) = p(y|x)p(x)$$

$$\hookrightarrow p(y|x) = \frac{p(x|y)p(y)}{p(x)}$$

reverses
what is
being inferred \Rightarrow

$$p(y|x) = \frac{p(x|y)p(y)}{\int p(x|y)p(y)dy}$$

BAYES'
RULE

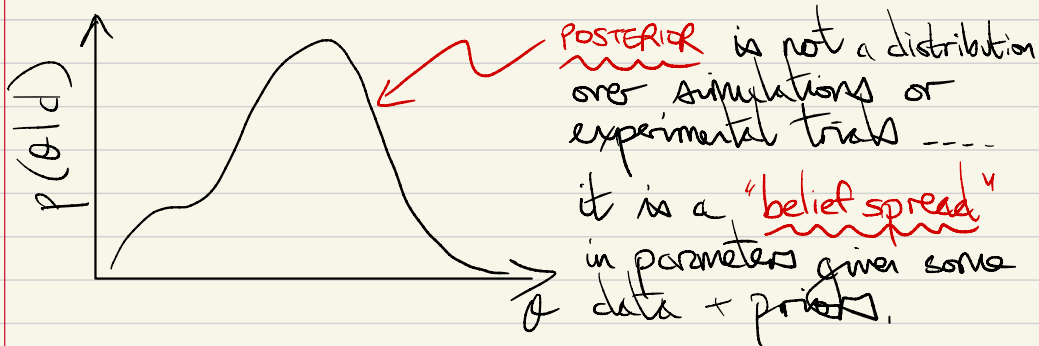


$$\text{Prob}(\text{Parameters} | \text{Data}) = \frac{\text{Prob}(\text{Data} | \text{Parameters}) \times \text{Prob}(\text{Parameters})}{\text{Prob}(\text{Data})}$$

$$p(\theta | d) = \frac{p(d | \theta) \times p(\theta)}{p(d)}$$

$$\text{Posterior Probability} = \frac{\text{Likelihood} \times \text{Prior}}{\text{Evidence}}$$

- Likelihood = fitting function (as before)
- Prior = constraints on parameters
- Evidence = does not depend on model parameters, so not important for parameter estimation.

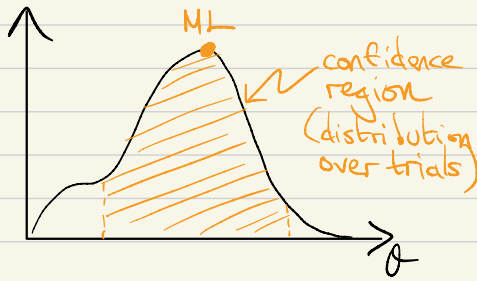


- Priors — we want the posterior to be **DATA DOMINATED**
priors should be **weakly informative**.

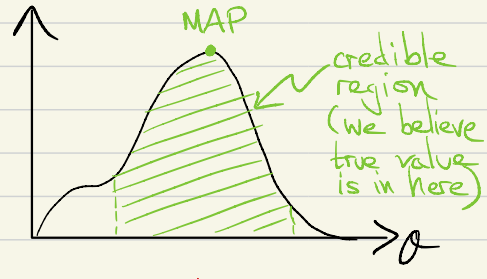
- uniform over a range
- gaussian
- scale-invariant $\Rightarrow p(\theta) \propto 1/\theta$
- conjugate \Rightarrow posterior belongs to the same family of distributions as the prior.

⇒ priors can be physical constraints, or the outcome of previous experiments.

◦ Credible Regions

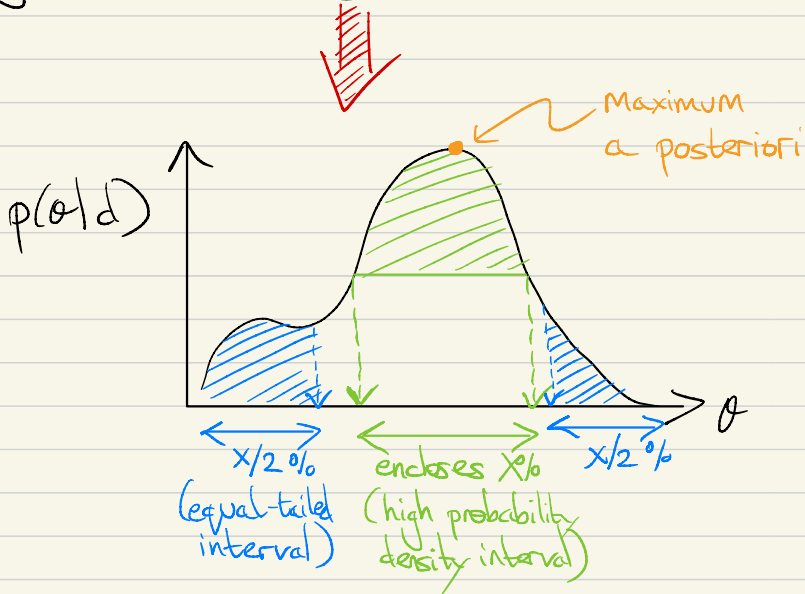


CLASSICAL STATISTICS



BAYESIAN STATISTICS

Bayesian credible regions are not unique



➡ we usually use equal-tailed intervals.