## Lesture 5

· Twin pillors of statistical inference

Classical traventist

Probabilities refer to

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the frequency of

outcomes in repeated belief conditioned
experiments

on data and

PRIORS in Bayasian obdistics act as boundaries on our inference,

Prior Knowledge.

- Maximum Likelihood Estimation

  (7) Formulate a model with a
  - (9) Formulate a model with some parameters, 0, that best fit the doserved data.
  - 3) Estinate he uncertainty on those poometars.
- (4) Try other models, and see which fits best.

· hikelihood -> filting/abjective function. eg let's assume the noise in our data data = Signal + noise  $p(n_i) = N(0, \sigma_i)$   $p(d_i) = N(S_i, \sigma_i)$   $p(d_i) = N(S_i, \sigma_i)$   $p(d_i) = \sqrt{2\pi\sigma_i^2}$   $p(d_i) = \sqrt{2\pi\sigma_i^2$ 

PROBABILITY OF DATA GIVEN PARAMETERS

LIKELIHOD OF = The p(d;)  $= \text{The p(d;)$ 

o MLE Horoscovic  $\frac{1}{N}$ · Quantifying Unartainty on Model Parameters \* With > 1 parameter, you can have correlated measurement uncertainties, Jik = ([F-1]ik)/2 where  $F_{jk} = -\frac{\partial^2 I_n L}{\partial o_j \partial o_k}\Big|_{o = o_{MLE}}$ FISHER INFORMATION MATRIX e.g. Measuring the mean  $\mu$  of Gaussian-distributed total with homoscedastic uncertainties. On =  $\frac{\sigma}{M}$