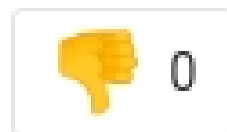
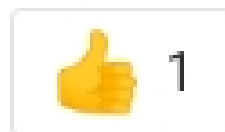
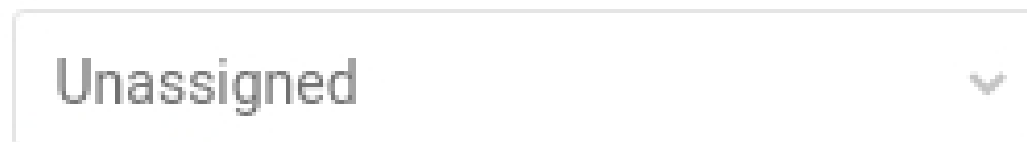


- Writing peer feedback
  - Copy/paste code you're talking about
  - Offer code alternatives
- Responding to feedback
  - Discuss the code review
  - Is there anything contentious in the review?
  - Ask in the comments if anything unclear
  - ***Thank the reviewer!***



Assignee



Software Development 3 (F27SG)

## Lecture 8

# Dynamic Stacks

Rob Stewart



# Outline

- we implemented a stack using an array (lecture 4)
- Today: **pictorially** implement stack with linked list
- **You will then implement this in the lab**
- First.. let's revise the stack ADT

# The Stack ADT

- The data is the type of elements stored
- Main operations
  - **push(object)** - adds object to the top of the stack
  - **pop()** - remove and returns element at the top
- Auxiliary operations
  - **top()** - return element at top (also called **peek()**)
  - **size()** - return number of elements
  - **isEmpty()** - check if empty
- Error conditions: pop/top of empty stack

# Advantages

- Linked lists
  - It can change size dynamically
  - Allocated only the space you need
- Arrays
  - Random access
  - Can be faster
  - More efficient representation of arrays in memory

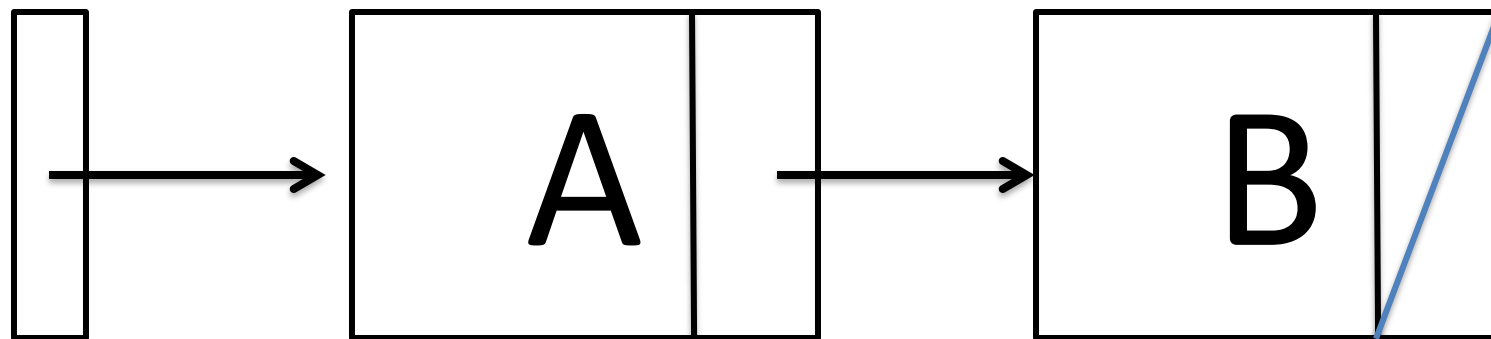
# The Stack ADT as a Java Interface

- We can represent the Stack ADT as a Java interface
- Elements are of type **Object**
- We need to create a **StackException** for error conditions

```
public interface StackI {  
    public int size();  
    public boolean isEmpty();  
    public Object top() throws StackException;  
    public void push(Object element);  
    public Object pop() throws StackException;  
}
```

# Linked Lists revision

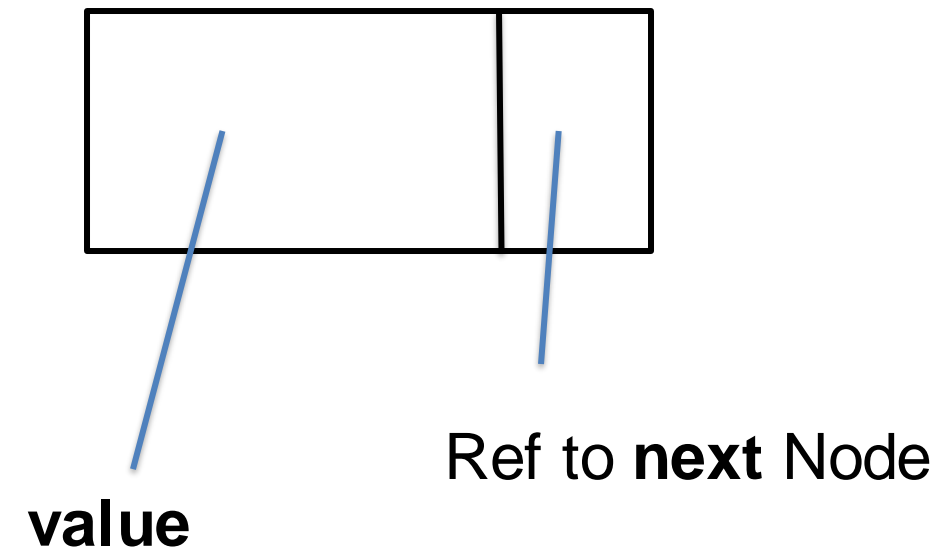
- A Linked List is a **Linear** ordered sequence of **Nodes**
- Each **Node** contains
  - a data item
  - a reference to another Node of the same type (Class)
- We have a reference (**head**) to the first element
- Traverse through the chain of nodes to visit each one





# Stacked as linked structure - data

```
class Node{  
    Object value;  
    Node next;  
  
    public Node(Object e, Node n){  
        element = e;  
        next = n;  
    }  
}
```



- The stack has to contain a **node**
  - Contains the data
  - We will call this **top**
  - This should initially be a **null** pointer
- This will be incremented/decremented by push and pop



# First a linked list exercise...

Assume a LinkedList Class where the following operations can be performed:

- void addAtTail(int i);
  - adds the given value to the end of the linked-list;
- void removeValueAtIndex(int i);
  - removes the value at the index specified in i
- void addAtHead(int i);
  - adds the given value to the beginning of the linked-list

```
LinkedList l1 = new LinkedList();
```

```
l1.addAtTail(34);
```

```
l1.addAtTail(22);
```

```
l1.addAtHead(33);
```



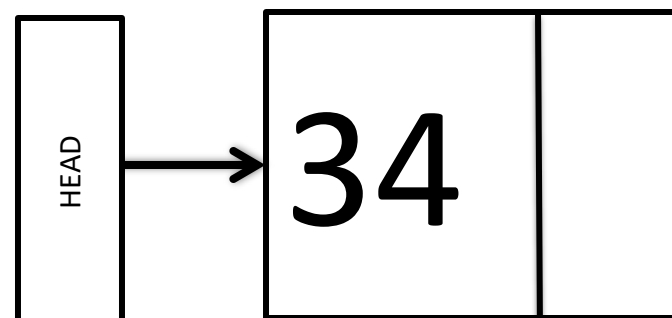


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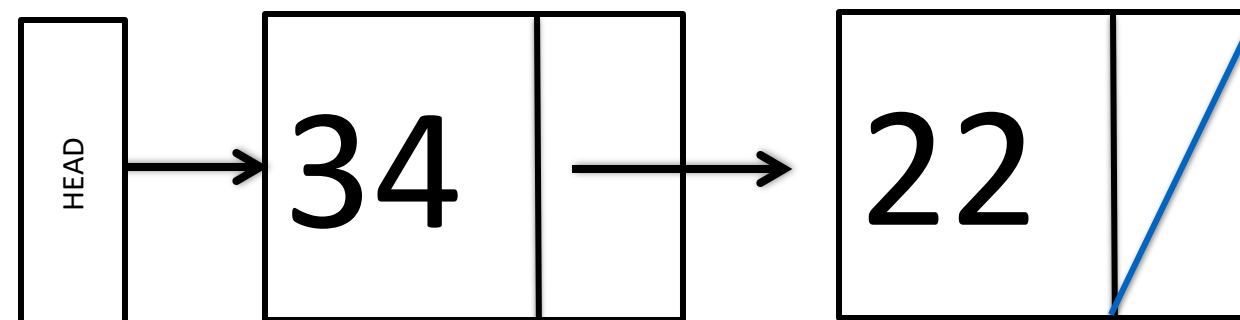


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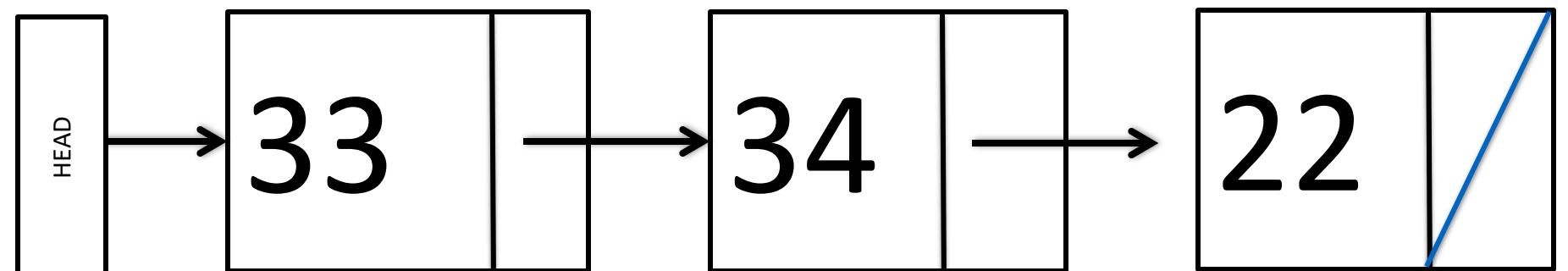


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```
LinkedList ll = new LinkedList();  
ll.addAtTail(34);  
ll.addAtTail(22);  
ll.addAtHead(33);
```



# Stack as a linked list

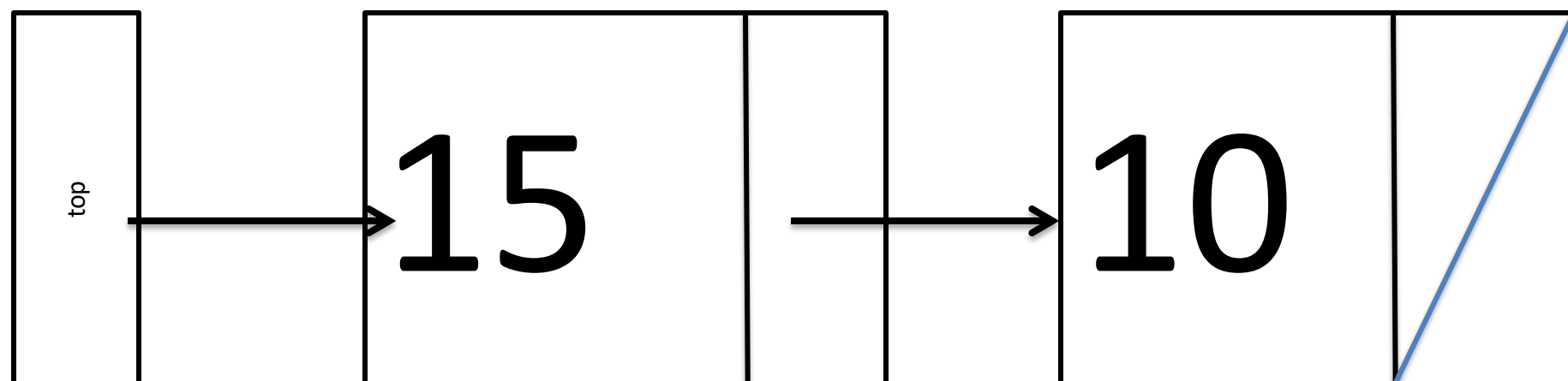
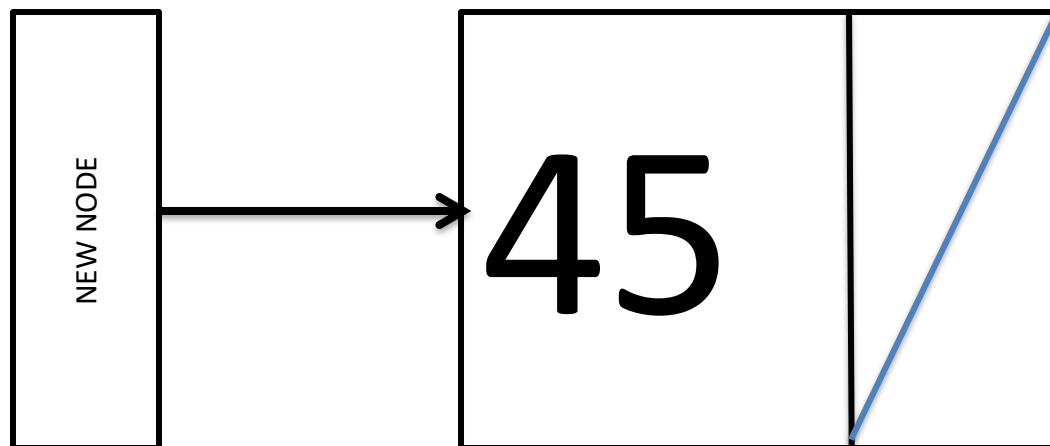
- We always aim for  $O(1)$  constant complexity
  - push, pop, size, isEmpty, top
  - We achieved this with **array** based implementation
- **Push**: create new node, add it to linked list
- **Pop**: remove node from linked list
- When we are using a **linked list** data structure
  - `push()`    add at tail, or head of linked list?
  - `pop()`        remove from tail, or head of linked list?

# Pushing an element

- Solution:
  - **Add to the front**
- Why?
  - This is a constant operation
  - Adding to the rear will force us to traverse the list
    - i.e. linear time operation
- How to push
  - Create the New Node
  - Set its reference to be the existing **top**
  - Set the New Node to be the **top** Node

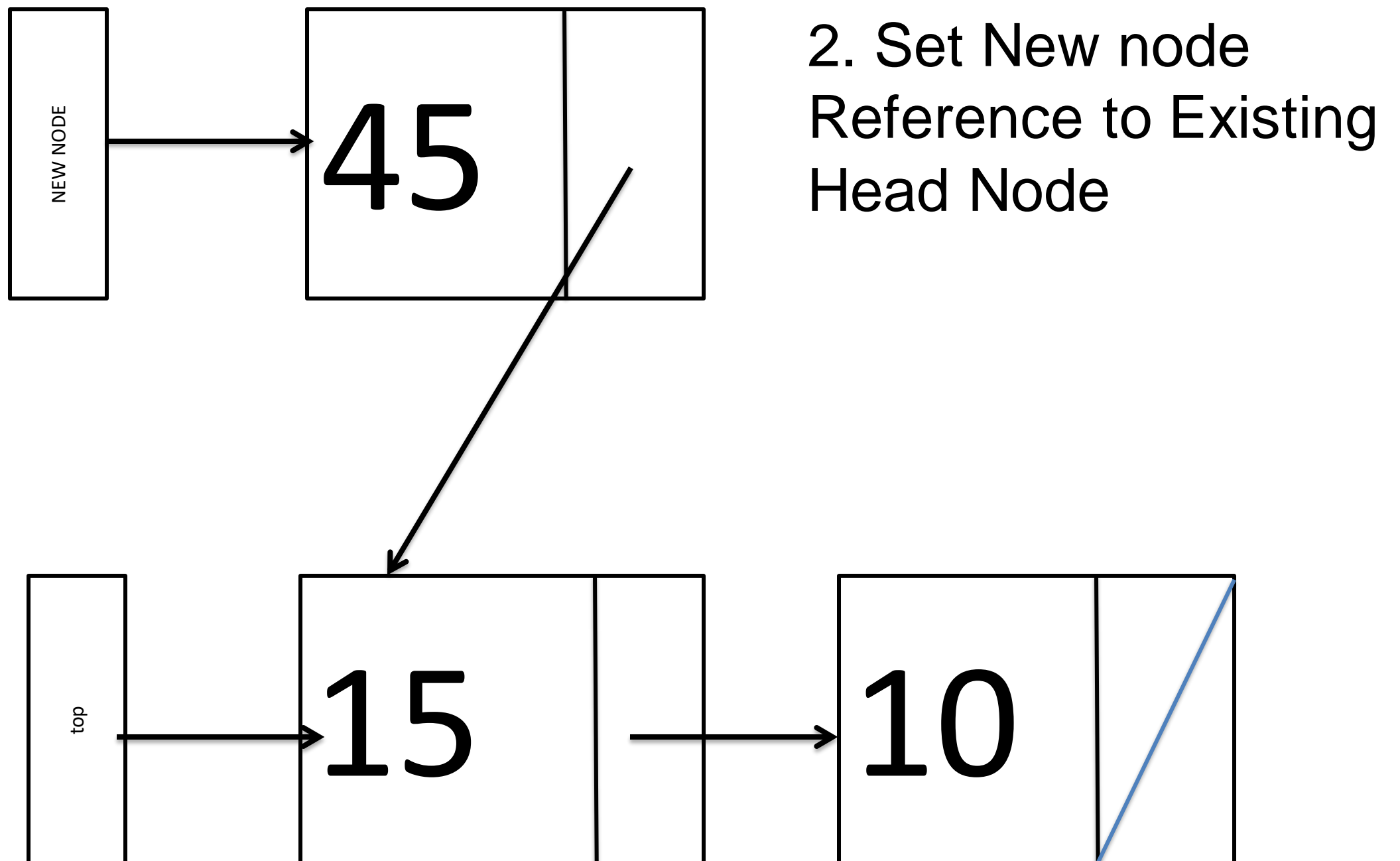
# Pushing an element

1. Create the new node

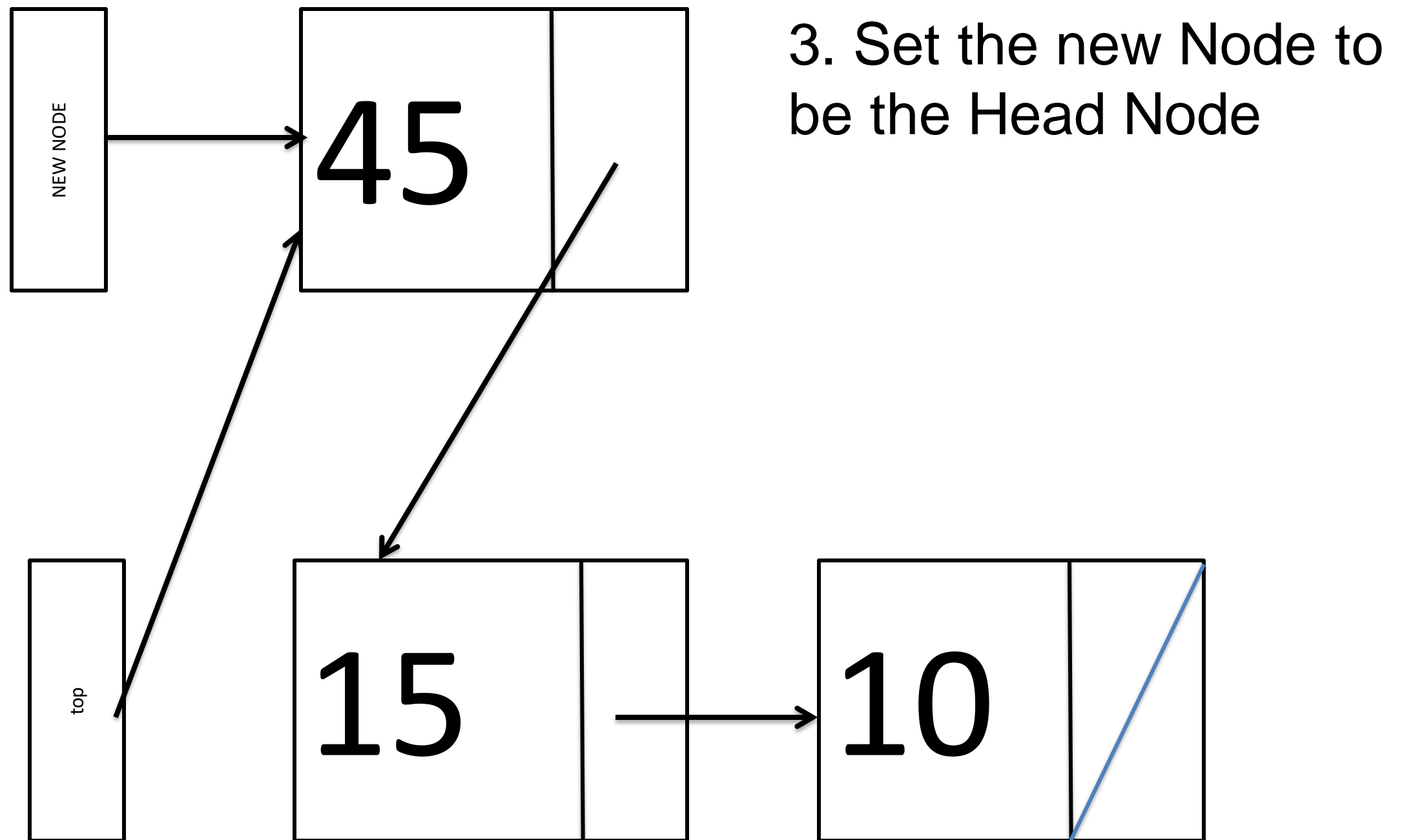




# Pushing an element



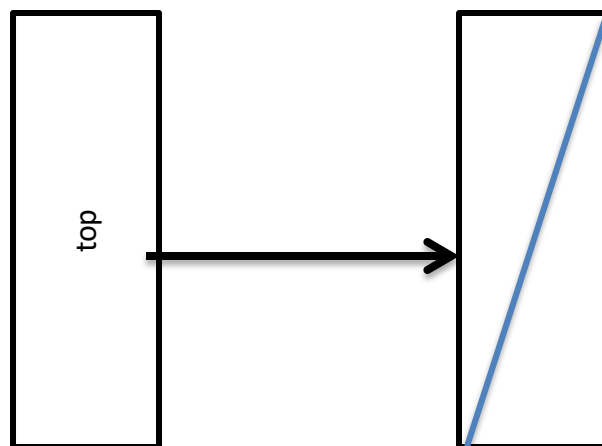
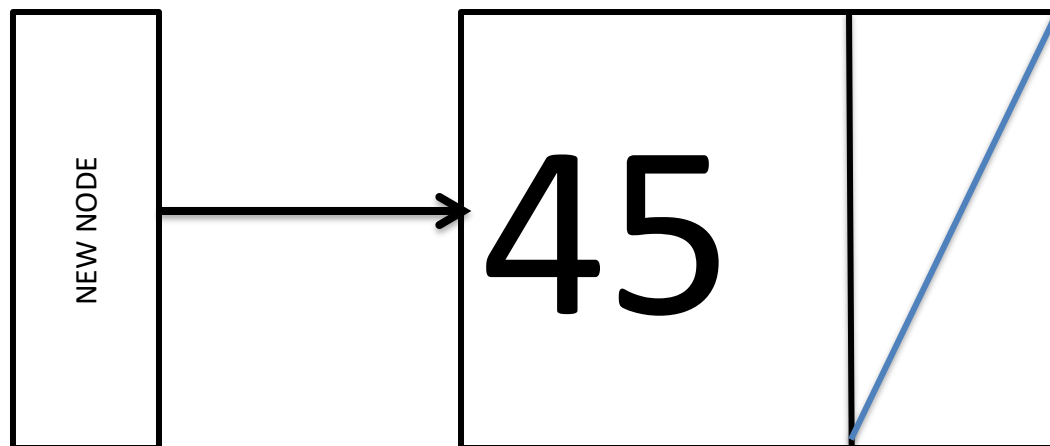
# Pushing an element



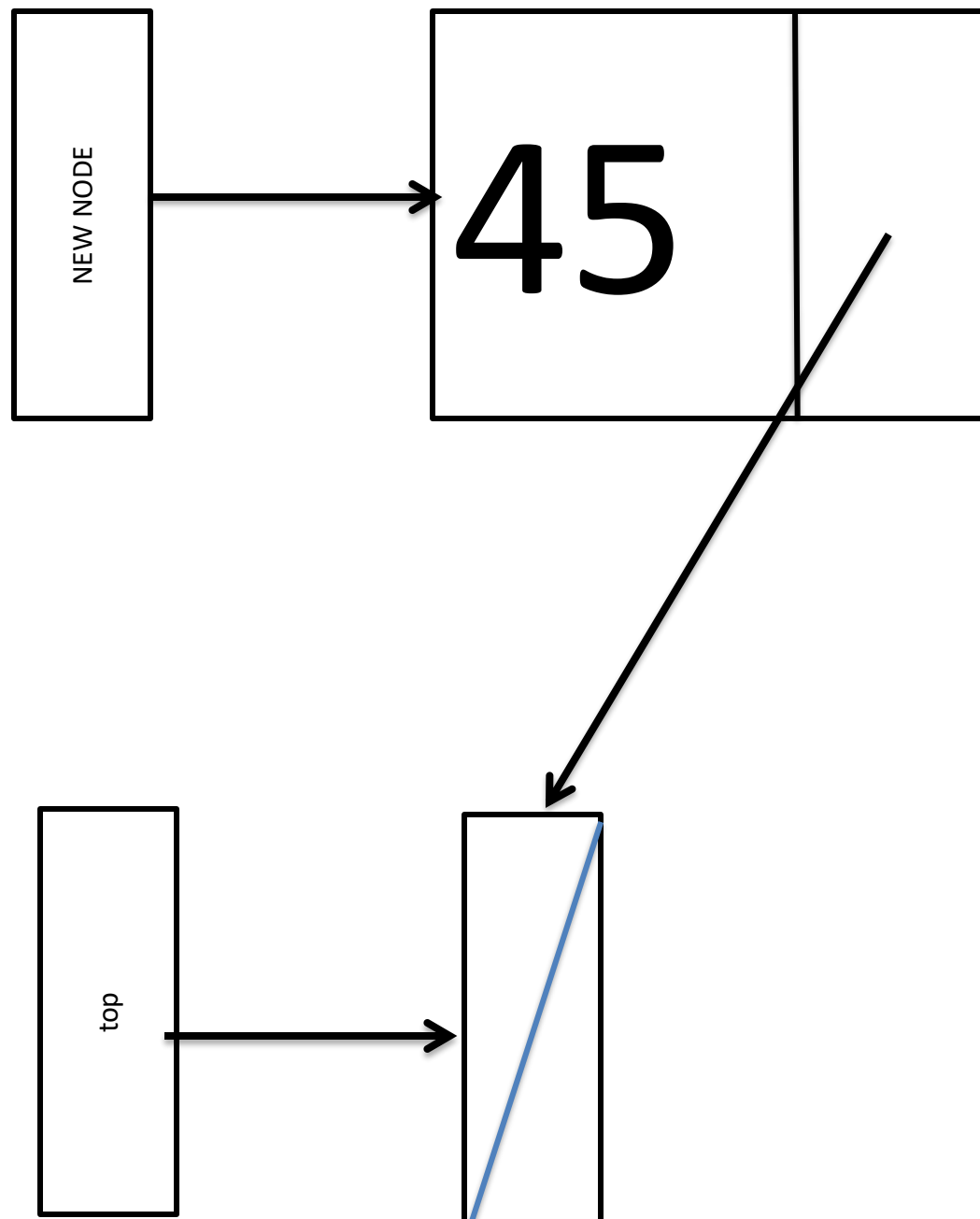
What if the stack is Empty?

# Pushing an element (Empty stack)

1. Create the new node

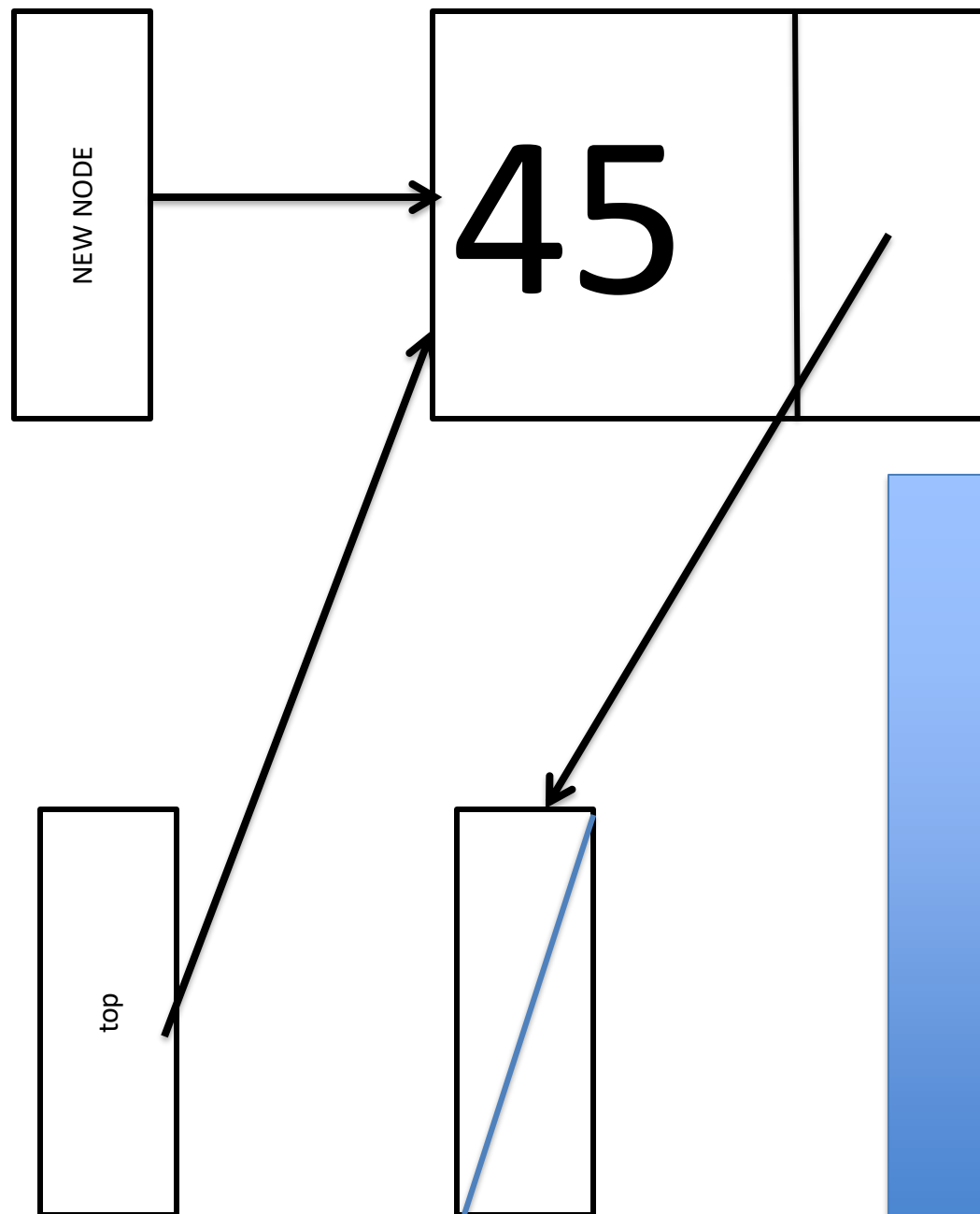


# Pushing an element



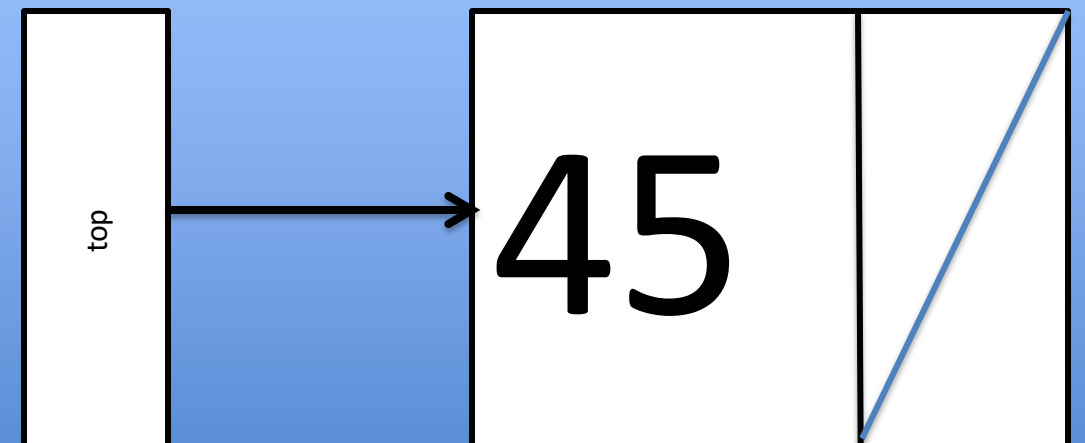
2. Set New node  
Reference to Existing  
Head Node

# Pushing an element



3. Set the new Node to be the Head Node

Which is the same as:





# Popping an element

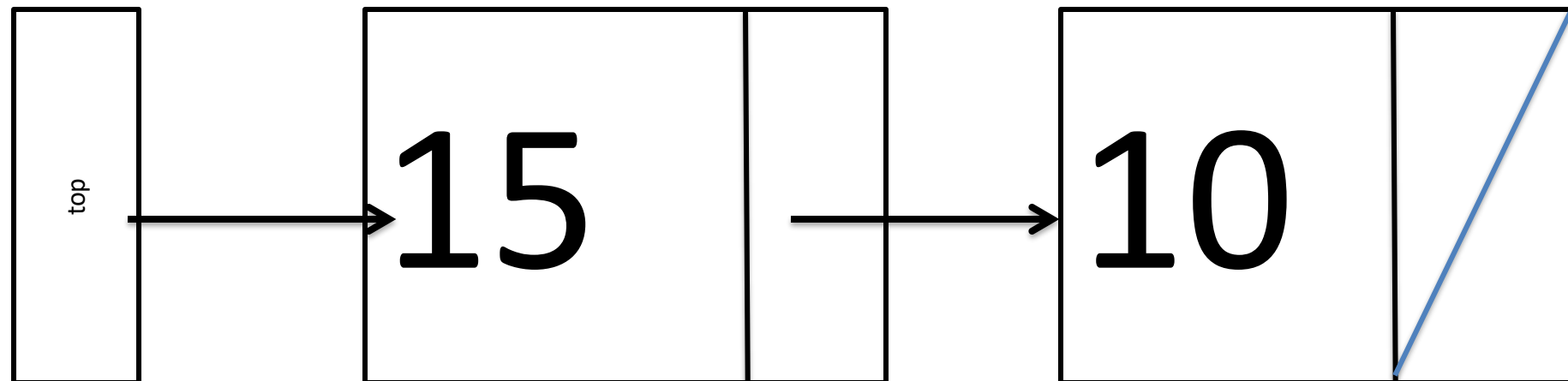
- Again, this should be constant time
- Q: should we remove the first or last element?

# Popping an element

- Solution
  - Remove the first
- Why?
  - Firstly, as we are adding to the first we also have to remove it
    - If not this will not be a stack!
  - As with push, removing the last element will be require that we traverse the list
    - This operation is linear
- Solution:
  - Check that the stack is not empty
    - Can't remove something if it isn't there
    - In this case raise an **StackException**
  - Get the element of the current top list
  - Make the top's next Node the new top node
  - Return the element

# Popping

1. Check the List isn't Null

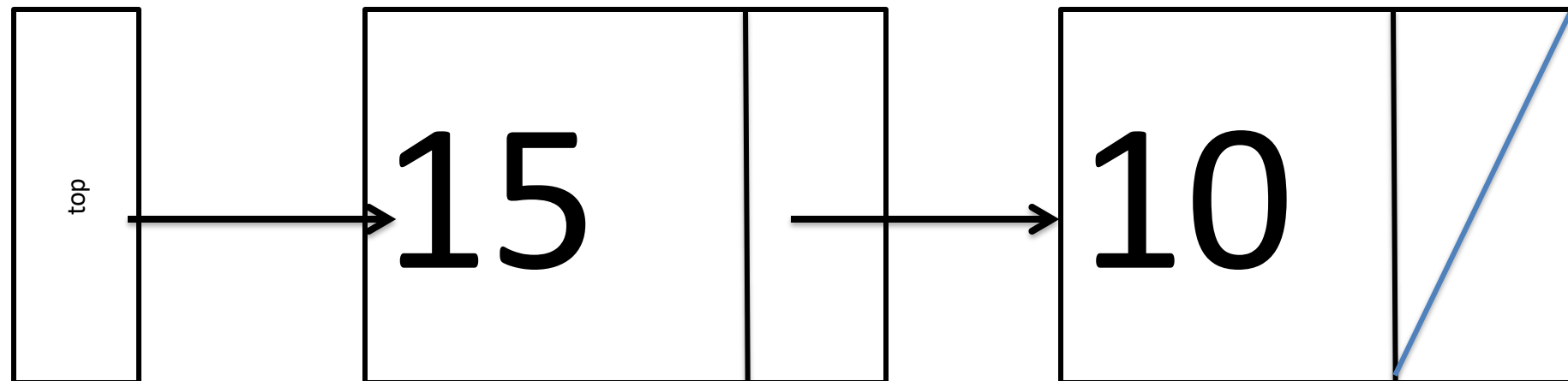


HEAD == NULL throws a **StackException**



# Popping

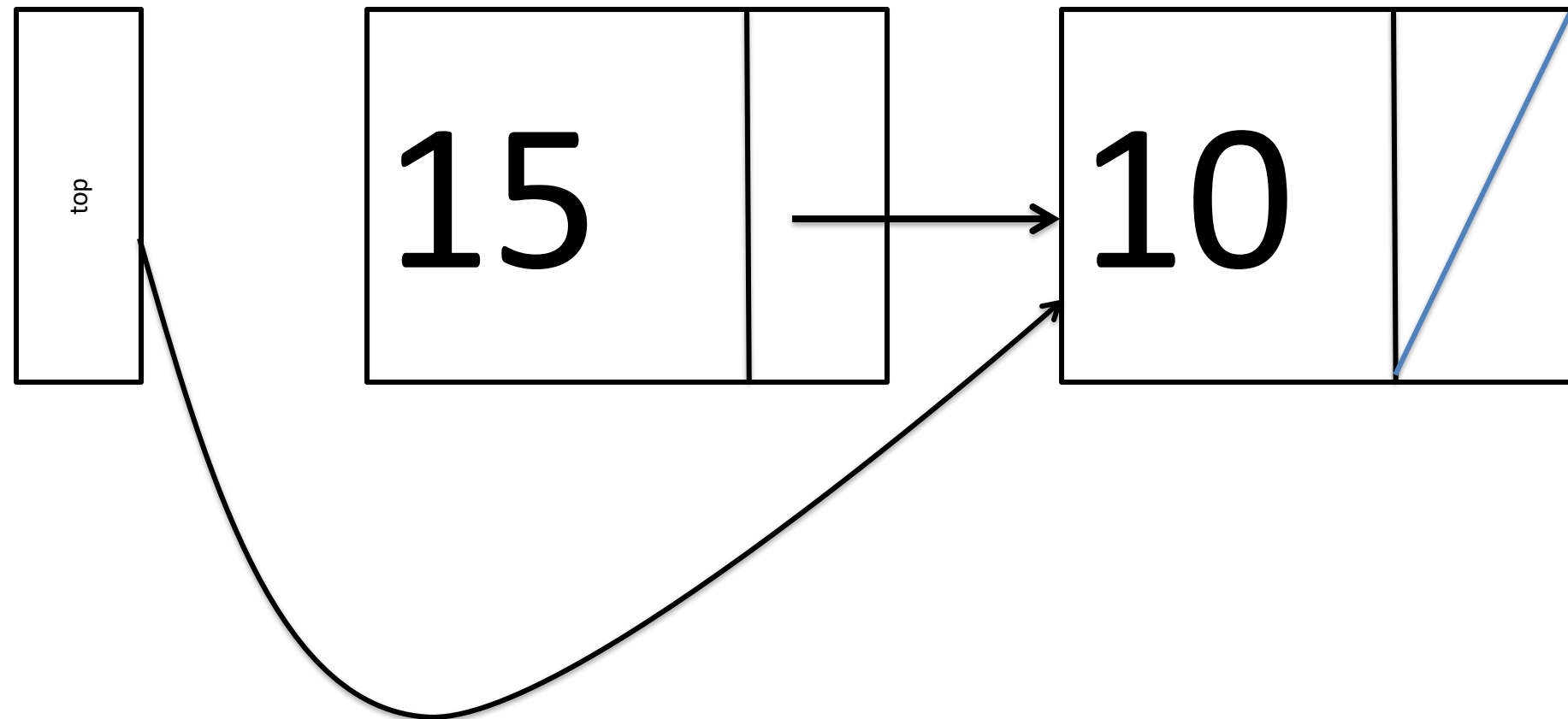
2. Get the first element



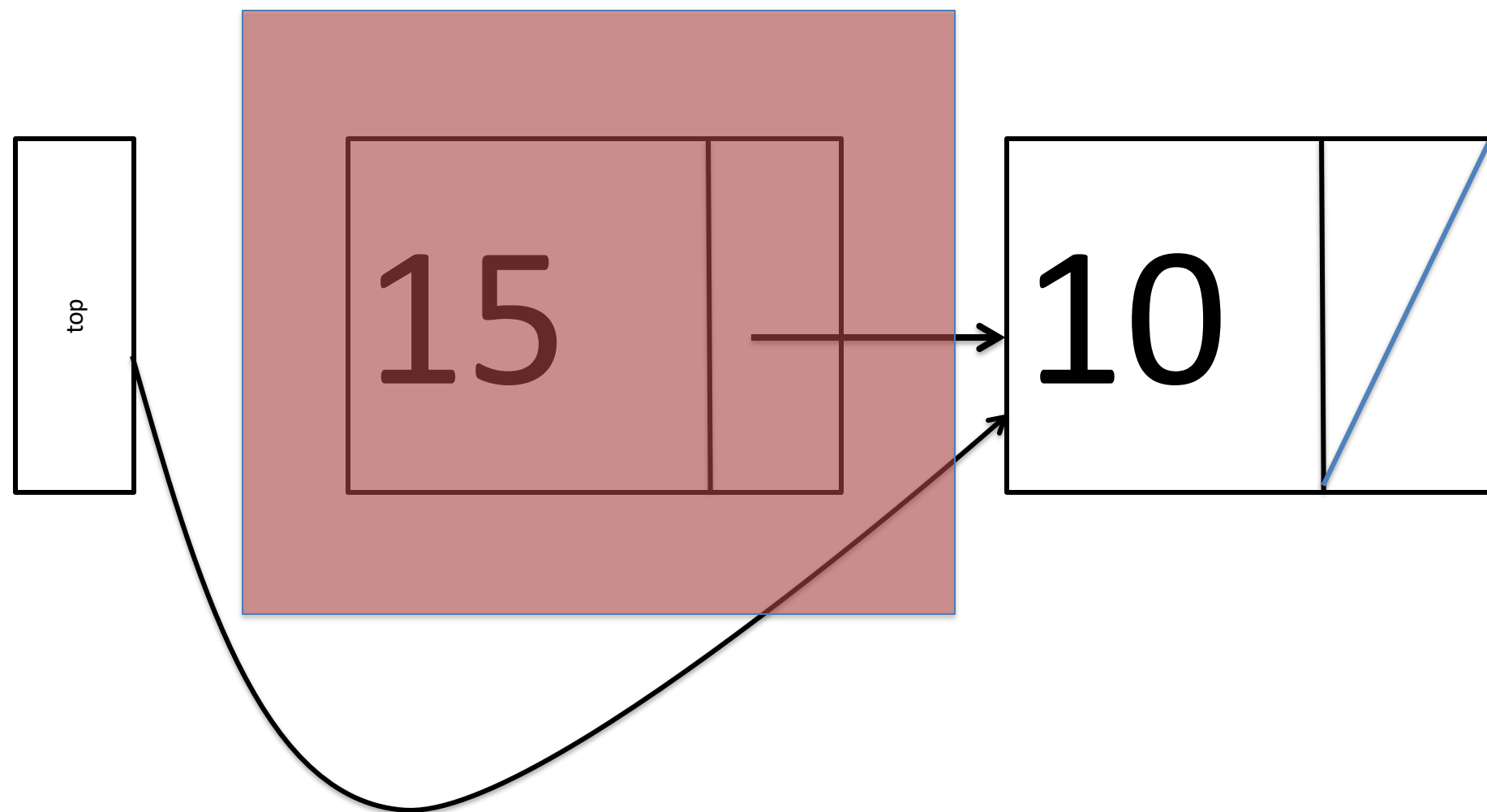
**tmp = 15;**

# Popping

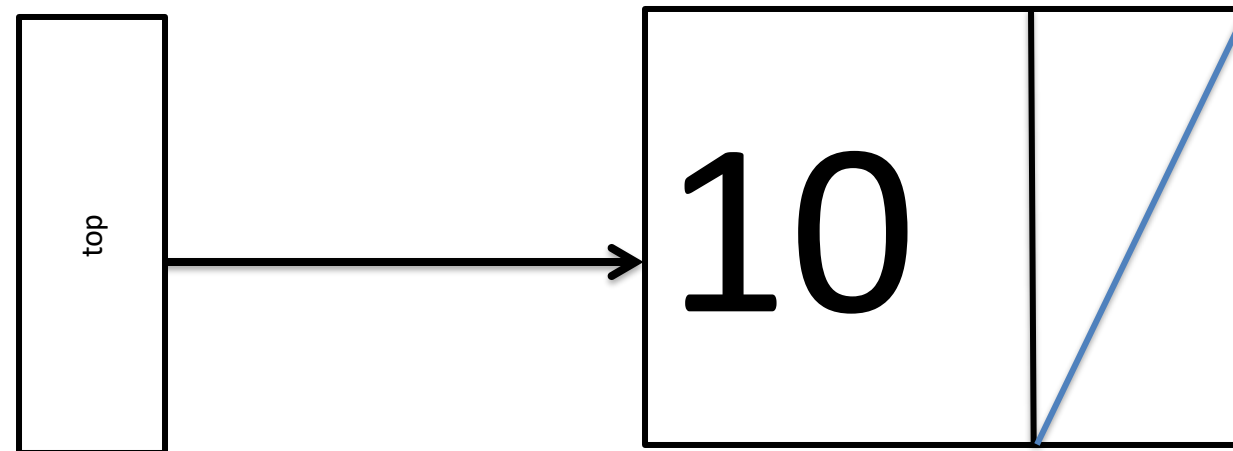
3. Set top to the next element of top



# Popping



# Popping



4. Return the tmp  
element (15 in this  
case)

# The **top** operation

- Here we only return the element of top
- This is trivially constant time

# The **isEmpty** operation

- When is the stack empty?
- Solution
  - When **top == null**
- Why is this  $O(1)$

# The **size** operation

- Can we do this in  **$O(1)$** ?
  - Not using current representation
  - Need to iterate the full lists  $\sim O(N)$
- Solution
  - We add a size field to our stack
  - Should be incremented by a push
  - Should be decrement by a pop

# Summary

- Representing a stack as a linked list
- Advantage over array representation is:
  - it can grow dynamically
  - while all operations are constant time  $O(1)$
- You will implement today's pictures in Java (lab 4)
- Attendance sheet
- Next lecture: **Queues**