



The National University of Computer and Emerging Sciences

Assignment 04: Database Systems

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Question 01:

Consider a scenario where you're tasked with designing an ERD for a bus ticketing system. This system facilitates the sale of tickets for bus transportation services.

Entities:

- **Customer:** Represents individuals who purchase tickets. Attributes may include CustomerID, Name, Email, Phone, etc.
- **Ticket:** Represents the ticket purchased by a customer for a bus journey. Attributes may include TicketID, Price, DepartureDateTime, ArrivalDateTime, SeatNumber, etc.
- **Bus Route:** Represents the specific route for bus journeys. Attributes may include RouteID, DepartureLocation, ArrivalLocation, Distance, etc.
- **Bus:** Represents the individual buses available for booking. Attributes may include BusID, BusNumber, Model, Capacity, etc.
- **Payment:** Represents the payment details for each ticket transaction. Attributes may include PaymentID, Amount, PaymentMethod, etc.

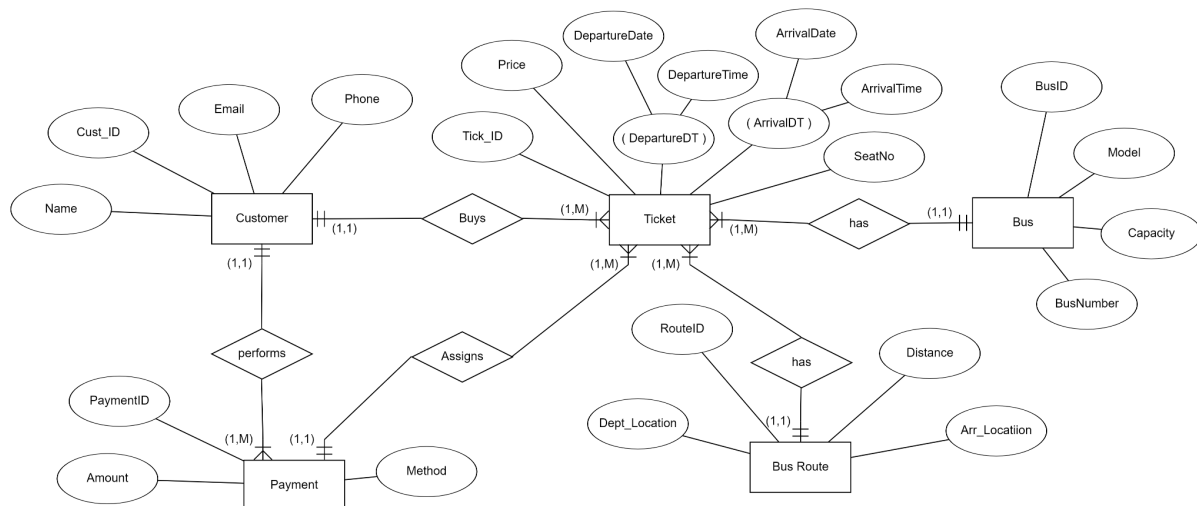
Relationships:

- **Customer - Ticket (1:M):** A customer can purchase multiple tickets, but each ticket is associated with only one customer.
- **Ticket - Bus Route (M:1):** Each ticket corresponds to a specific bus route, but a bus route can have multiple tickets associated with it.
- **Ticket - Bus (M:1):** Each ticket is for a specific bus, but each bus can have multiple tickets associated with it.
- **Customer - Payment (1:M):** A customer can make multiple payments, but each payment is associated with only one customer.
- **Payment - Ticket (1:1 or 1:M):** Each payment is associated with one or more tickets, depending on whether a customer purchases multiple tickets in a single transaction or not. I'm going to assume it is (1:M).

Functional Dependencies:

- CustomerID → Name, Email, Phone
- Email → CustomerID
- Phone → CustomerID
- TicketID → Price, DepartureDateTime, ArrivalDateTime, SeatNumber, CustomerID, RouteID, BusID
- RouteID → DepartureLocation, ArrivalLocation, Distance
- BusID → BusNumber, Model, Capacity
- PaymentID → Amount, PaymentMethod, CustomerID, TicketID

The ER Diagram for this scenario is given as under:



Now for normalization of the FDs, we first find all Candidate keys. First we separate RHS into multiple parts and then find the closure for all Combinations of keys. We get:

- **[DepartureLocation, ArrivalLocation, Distance, BusNumber, Model, Capacity, PaymentID].**

Now the current form is in 1NF. To convert to 2NF, find the minimal cover of the FDs, which includes the FDs:

- CustomerID \rightarrow Name
- CustomerID \rightarrow Email
- CustomerID \rightarrow Phone
- Email \rightarrow CustomerID
- Phone \rightarrow CustomerID
- TicketID \rightarrow Price
- TicketID \rightarrow DepartureDateTime
- TicketID \rightarrow ArrivalDateTime
- TicketID \rightarrow SeatNumber
- TicketID \rightarrow CustomerID
- TicketID \rightarrow RouteID
- TicketID \rightarrow BusID
- PaymentID \rightarrow Amount
- PaymentID \rightarrow PaymentMethod
- PaymentID \rightarrow TicketID

The table is not in 2NF. The FD [PaymentID \rightarrow Amount] is a partial dependency (i.e., LHS is a proper subset of some CK), the table is split. Thus we get the Functional Dependencies:

- CustomerID \rightarrow Phone.
- Email \rightarrow Phone.
- Phone \rightarrow Email, CustomerID, Name.
- PaymentID \rightarrow TicketID, Amount, PaymentMethod.

- TicketID \rightarrow CustomerID, Price, DepartureDateTime, ArrivalDateTime, SeatNumber, RouteID, BusID.
- All the other attributes can go to different tables as there are no dependencies between them. For 3NF, we remove the transitive dependencies. So, we get tables:

Relation 01:

- CustomerID \rightarrow Email
- Email \rightarrow Phone
- Phone \rightarrow CustomerID, Name

Relation 02:

- Email \rightarrow CustomerID
- CustomerID \rightarrow Email

Relation 03:

- Phone \rightarrow CustomerID
- CustomerID \rightarrow Phone

Relation 03:

- TicketID \rightarrow CustomerID, BusID, RouteID, SeatNumber, ArrivalDateTime, DepartureDateTime, Price

Relation 04:

- PaymentID \rightarrow TicketID, PaymentMethod, Amount

For conversion into BCNF, find merged minimal cover of FDs, which contains:

- CustomerID \rightarrow Name, Email, Phone.
- Email \rightarrow CustomerID.
- Phone \rightarrow CustomerID.
- TicketID \rightarrow Price, DepartureDateTime, ArrivalDateTime, SeatNumber, CustomerID, RouteID, BusID.
- PaymentID \rightarrow Amount, PaymentMethod, TicketID.

The FD [CustomerID \rightarrow Name, Email, Phone] violates BCNF as the LHS is not superkey.

Table is split into the two below:

- (CustomerID, Name, Email, Phone)
- (CustomerID, TicketID, Price, DepartureDateTime, ArrivalDateTime, SeatNumber, RouteID, BusID, DepartureLocation, ArrivalLocation, Distance, BusNumber, Model, Capacity, PaymentID, Amount, PaymentMethod)

The FD [PaymentID \rightarrow TicketID, Amount, PaymentMethod] violates BCNF as the LHS is not superkey. Table is split into the two below:

- (PaymentID, TicketID, Amount, PaymentMethod, CustomerID, Price, DepartureDateTime, ArrivalDateTime, SeatNumber, RouteID, BusID).
- (DepartureLocation, ArrivalLocation, Distance, BusNumber, Model, Capacity, PaymentID).

The FD [TicketID \rightarrow CustomerID, Price, DepartureDateTime, ArrivalDateTime, SeatNumber, RouteID, BusID] violates BCNF as the LHS is not superkey. Table is split into the two below:

- (TicketID, CustomerID, Price, DepartureDateTime, ArrivalDateTime, SeatNumber, RouteID, BusID)
- (PaymentID, TicketID, Amount, PaymentMethod)

So, for BCNF we get the final tables:

Relation 01:

- CustomerID \rightarrow Phone.
- Email \rightarrow Phone.
- Phone \rightarrow Email, CustomerID, Name.

The attributes DepartureLocation, ArrivalLocation, Distance, BusNumber, Model, Capacity, PaymentID can be put in separate tables.

Relation 02:

- TicketID \rightarrow CustomerID, Price, DepartureDateTime, ArrivalDateTime, SeatNumber, RouteID, BusID.

Relation 03:

- PaymentID \rightarrow TicketID, Amount, PaymentMethod.

This represents the final BCNF form of the FDs.

Question 02:

EMPLOYEE (Entity) has the following attributes:

- **Employee ID (identifier)**
- **Name**
- **Address**
- **Birthdate**

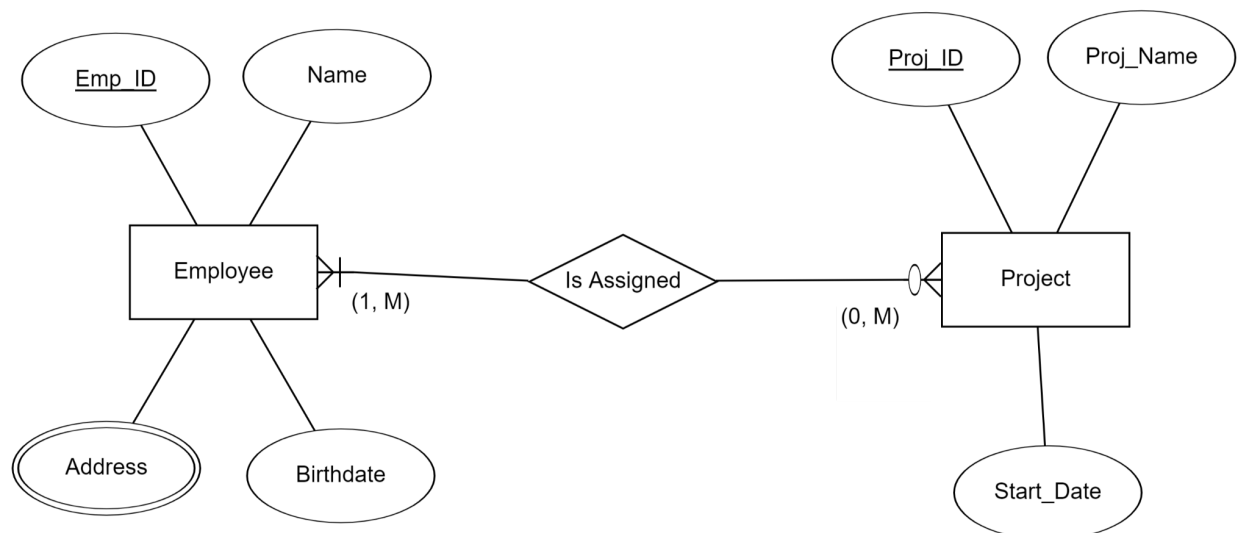
PROJECT (Entity) has the following attributes:

- **Project ID (identifier)**
- **Project Name**
- **Start Date**

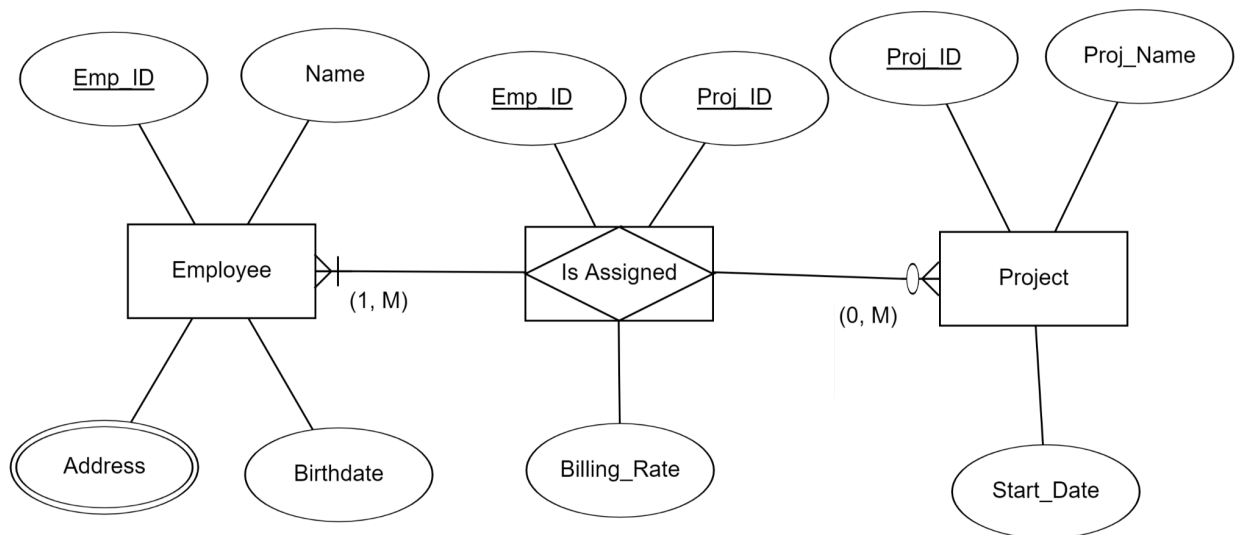
Each project is assigned to one or more Employees and each Employee is assigned to one or more projects. This means the relationship is named as **Assignment**.

- **Each employee may be assigned to one or more projects or may not be assigned to a project:** This means that the cardinality between EMPLOYEE and PROJECT is zero or many because each employee can be assigned to none or many projects.
- **A project must have at least one employee assigned and may have any number of employees assigned:** This means the project and employee have a one or many relationship because a project has one or many employees assigned to it.

Assumption: Address is a multivalued attribute because it has alphanumeric values (i think).



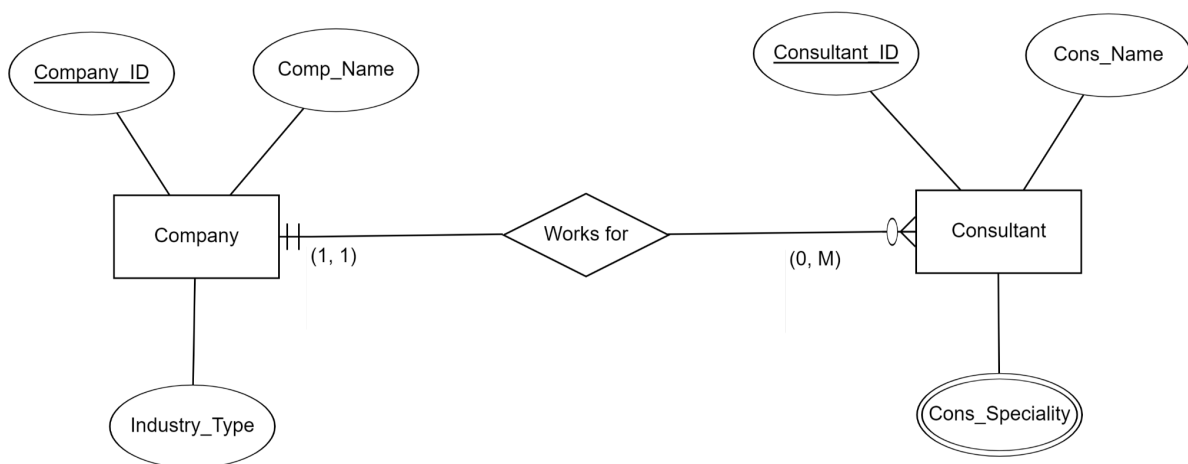
For the Assignment relationship, it is represented as an entity because the company wishes to record the applicable billing rate (Billing_Rate) for each employee when assigned to a particular project. So Billing_Rate becomes an attribute of Assignment.



Question 03:

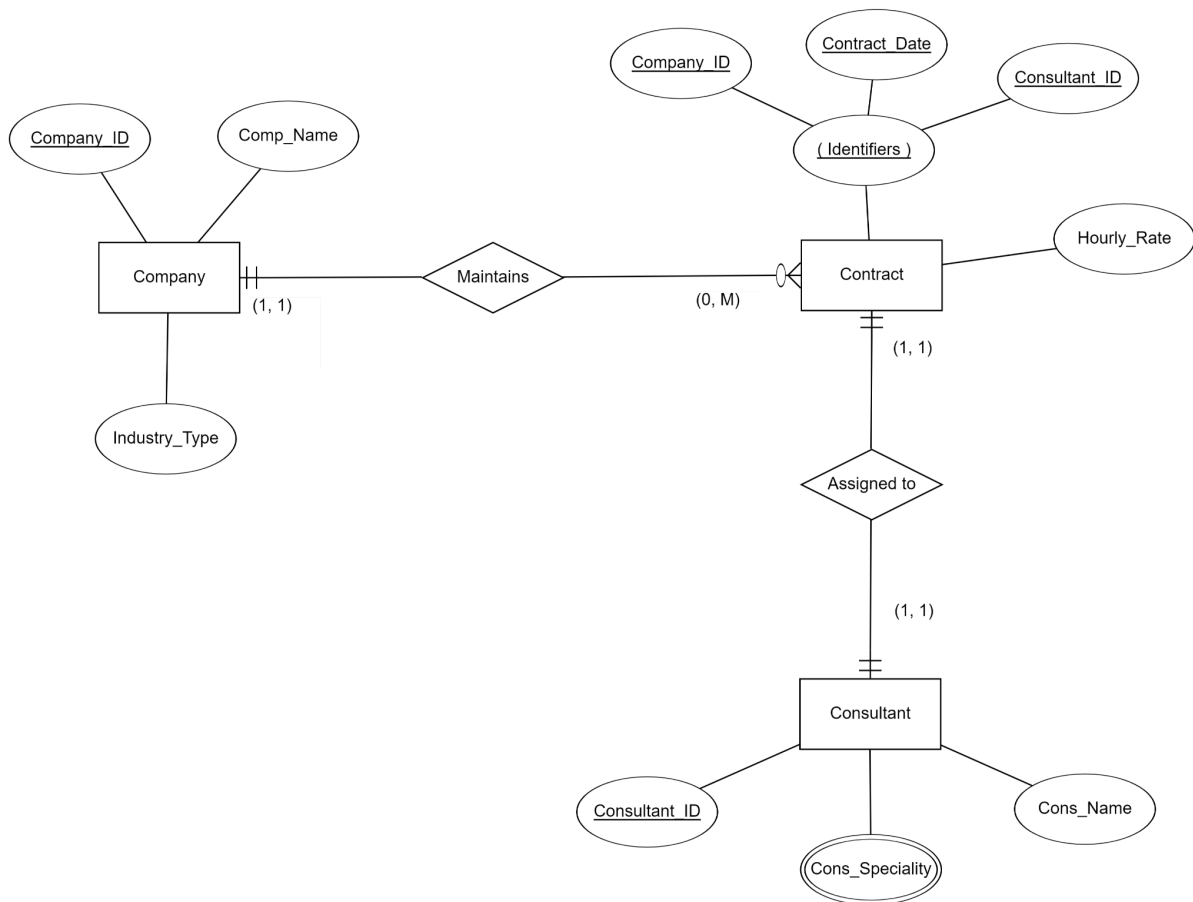
Companies, identified by a Company_ID and described by Company_Name and Industry_Type, hire consultants, identified by Consultant_ID and described by Consultant_Name, Consultant_Speciality, which is multivalued. Assume that a consultant can work for only one company at a time, and we need to track only current consulting engagements. A company can also have multiple consultants working for them, or at times, they have no need of consultants.

(a): Draw an ERD for this Situation:



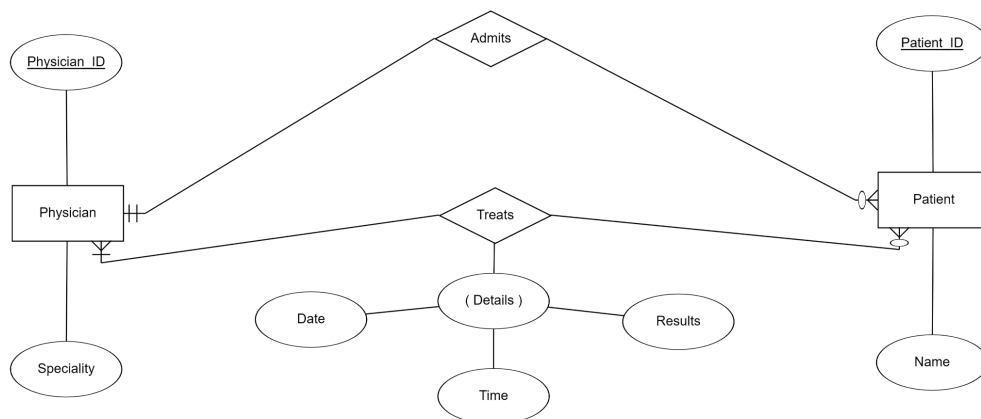
Now, consider that each time a consultant works for a company, a contract is written describing the terms for this consultant engagement. Contract is identified by a composite identifier of Company ID, Consultant ID, and Contract Date. The contract should also include the hourly rate at which the consultant is paid. Assuming the consultant can still work for only one company at a time.

(b): Redraw the ERD for this situation.

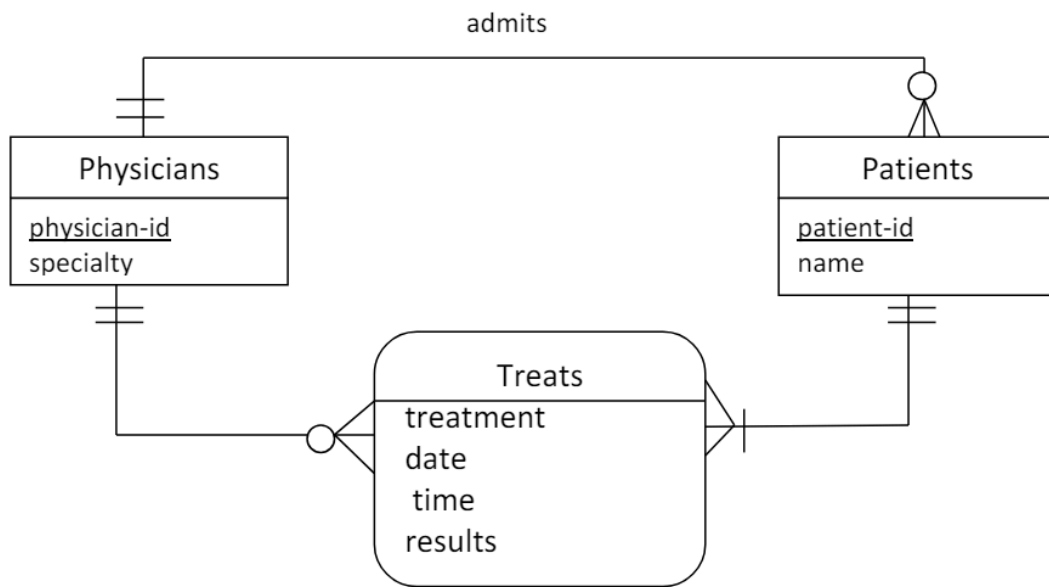


Question 04:

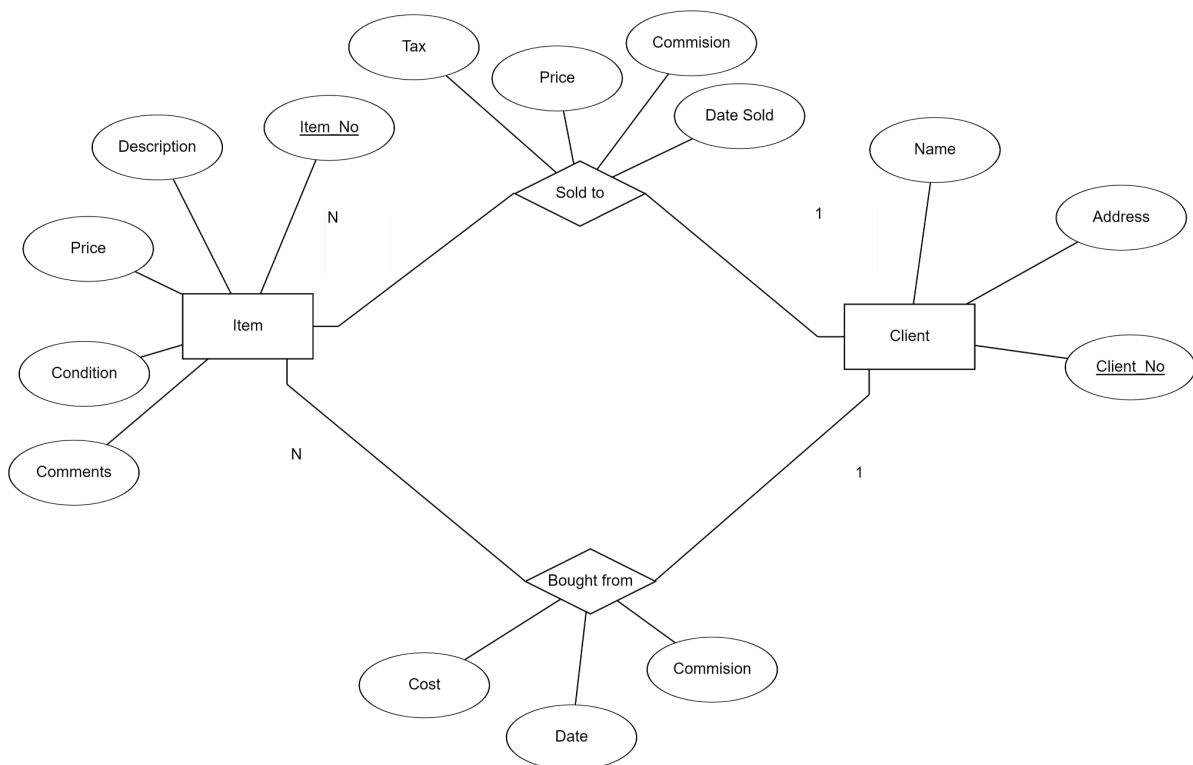
The ERD for the hospital situation consists of three main entity types, PHYSICIAN, PATIENT, and TREATMENT. The relationships between these entities allow for the tracking of multiple admissions and treatments over time. The hospital is not included as an entity as it has no attributes or relationships to be recorded in this model. Moreover, I am assuming that both Physician and Patient have IDs that are Primary Keys (identifiers). Also assuming that, details are Composite



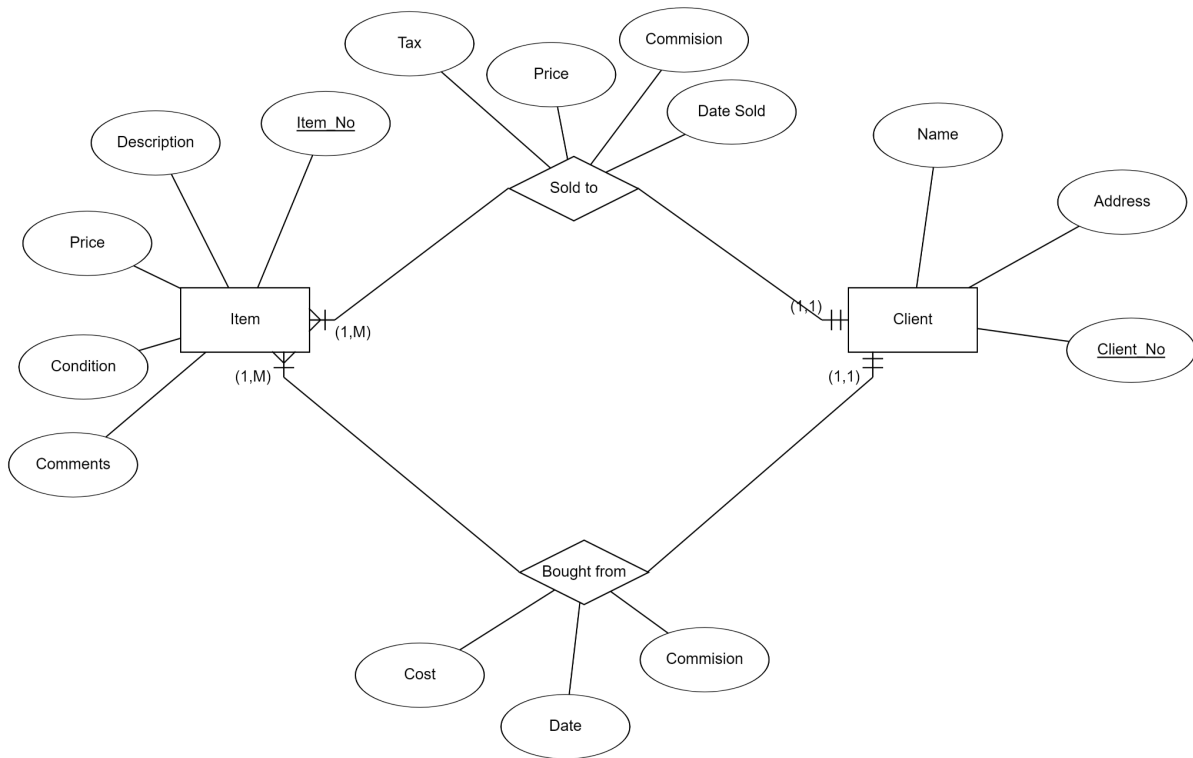
In other Notation we can also draw ERD as:



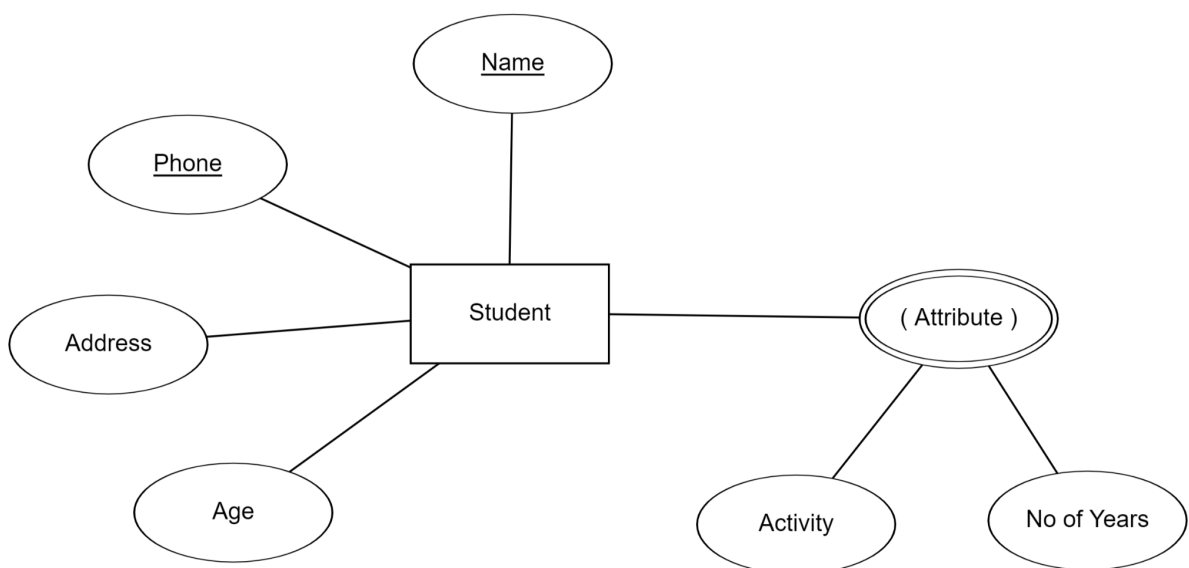
Question 05:



However, if i use the (min, max) notation with the Assumptions that a Client must have a minimum of 1 Item bought or sold and that for Item the minimum is 1 and maximum is M. Then, we can also use the following ERD:



Question 06:



Here I have taken both Name and Phone as a Composite Primary Key (identifier). You can take Name only as an identifier, but then it is possible that 2 people might have the same name. But 2 people with the same Name and Phone (with the same country code) isn't really possible. Moreover, Attribute is both a Multivalued key and Composite satisfying the condition of [Student may engage in more than one activity].

Question 07:

An associative entity is an entity type used for associating one or more entity instances that have a many-to-many relationship. It contains attributes important for all entity instances that are associated with the associative entity.

A good example is an associative entity that associates entity instances of Book and Customer entity types. A new entry is created each time when the Customer borrows a book in the bookstore.

A weak entity is an entity whose existence is dependent on the other (strong) entities. It doesn't have its identifier, ie: it is identified by the primary attribute of the strong entity that is implemented as a foreign key in the weak entity.

So, Associative entities are a type of weak entity because they cannot exist on their own and are dependent on other entities in the many-to-many relationship. The speciality about their weakness is that they are dependent on both entities that are forming the relationship that needed the associative entity to resolve their relationship.

Question 08:

Given Functional Dependencies:

- **StaffID** → **StaffName**
- **CustomerID** → **Cust_Name, Cust_Address**
- **Cust_Address** → **Cust_Phone**
- **OrderID** → **OrderDate, CustomerID, StaffID**
- **FoodDishID** → **FoodDishName, UnitPrice**
- **OrderID, FoodDishID** → **Quantity, QuantityPrice**

The definition of partial dependency is that if a relation has a candidate key that consists of more than one attribute, and if an attribute is dependent on only a part of that candidate key, then such a dependency is referred to as partial dependency. First finding all Candidate Keys:

From above FDs, we can infer that:

- **StaffID** identifies **StaffName**.
- **CustomerID** identifies **Cust_Name** and **Cust_Address**.
- **Cust_Address** identifies **Cust_Phone**.
- **OrderID** identifies **OrderDate, CustomerID** and **StaffID**.
- **FoodDishID** identifies **FoodDishName** and **UnitPrice**.
- Combination of **OrderID** and **FoodDishID** identifies **Quantity, QuantityPrice**.

According to the rules of Partial Dependency:

1. **Left side of the arrow in a functional dependency:** Must be a proper subset of any candidate key.
2. **Right side of the arrow in a functional dependency:** Must be a non-prime attribute.

This way to Convert the given 1NF in the first Step is to find the Candidate Keys, which in this case are **OrderID** and **FoodDishID**. First checking 1NF, as LHS of 6th Dependency LHS is a proper Subset of both Candidate Keys so it is in a 1NF Form. So to convert to 2NF, we divide the table into 3 tables.

Relation 1: OrderID, OrderDate, CustomerID, StaffID, StaffName, Cust_Name, Cust_Address, Cust_Phone.

- CustomerID \rightarrow Cust_Address, Cust_Name
- Cust_Address \rightarrow Cust_Phone
- OrderID \rightarrow StaffID, CustomerID, OrderDate
- StaffID \rightarrow StaffName

Relation 2: FoodDishId, FoodDishName, UnitPrice.

- FoodDishId \rightarrow FoodDishName, UnitPrice

Relation 3: OrderID, FoodDishId, Quantity, QuantityPrice

- FoodDishId, OrderID \rightarrow Quantity, QuantityPrice

These 3 Relations describe the 2NF Form. Now for 3NF, we remove the Transitive Dependencies. Find the minimal cover of FDs, which contains

- StaffID \rightarrow StaffName
- CustomerID \rightarrow Cust_Name
- CustomerID \rightarrow Cust_Address
- Cust_Address \rightarrow Cust_Phone
- OrderID \rightarrow OrderDate
- OrderID \rightarrow CustomerID
- OrderID \rightarrow StaffID
- FoodDishId \rightarrow FoodDishName
- FoodDishId \rightarrow UnitPrice
- OrderID, FoodDishId \rightarrow Quantity
- OrderID, FoodDishId \rightarrow QuantityPrice

Merge FDs with same LHS and whose RHS are non-key attributes, we get the given set which contains:

- StaffID \rightarrow StaffName
- CustomerID \rightarrow Cust_Address, Cust_Name
- Cust_Address \rightarrow Cust_Phone
- OrderID \rightarrow StaffID, CustomerID, OrderDate
- FoodDishId \rightarrow UnitPrice, FoodDishName
- OrderID, FoodDishId \rightarrow QuantityPrice, Quantity

Check each FD in the set F1 for violation of 3NF, and split the table accordingly.

Checking FD [StaffID \rightarrow StaffName]. The FD violates 3NF as its LHS is not a superkey (and RHS is a set of non-key attributes). The following 3NF table is obtained:

- StaffID, StaffName with FDs StaffID \rightarrow StaffName.

Checking FD [CustomerID \rightarrow Cust_Address, Cust_Name]. The FD violates 3NF as its LHS is not a superkey (and RHS is a set of non-key attributes). The following 3NF table is obtained:

- CustomerID, Cust_Address, Cust_Name with FDs CustomerID \rightarrow Cust_Address, Cust_Name.

Checking FD [Cust_Address \rightarrow Cust_Phone]. The FD violates 3NF as its LHS is not a superkey (and RHS is a set of non-key attributes). The following 3NF table is obtained:

- Cust_Address, Cust_Phone with FDs Cust_Address \rightarrow Cust_Phone.

Checking FD [OrderID \rightarrow StaffID, CustomerID, OrderDate]. The FD violates 3NF as its LHS is not a superkey (and RHS is a set of non-key attributes). The following 3NF table is obtained:

- OrderID, StaffID, CustomerID, OrderDate with FDs OrderID \rightarrow CustomerID, StaffID, OrderDate.

Checking FD [FoodDishId \rightarrow UnitPrice, FoodDishName]. The FD violates 3NF as its LHS is not a superkey (and RHS is a set of non-key attributes). The following 3NF table is obtained:

- FoodDishId, UnitPrice, FoodDishName with FDs FoodDishId \rightarrow UnitPrice, FoodDishName.

Checking FD [OrderID, FoodDishId \rightarrow QuantityPrice, Quantity]. FD does not violate 3NF. No change done. Thus the table is now in 3NF. For BCNF, we can check if LHS of the Arrow is a Super Key or not. If it is not, we split the table into 2 or more (only sometimes). The final Relations for BCNF are:

Relation 1: StaffID, StaffName

- StaffID \rightarrow StaffName

Relation 2: Cust_Address, Cust_Phone

- Cust_Address \rightarrow Cust_Phone

Relation 3: CustomerID, Cust_Address, Cust_Name

- CustomerID \rightarrow Cust_Address, Cust_Name

Relation 4: OrderID, CustomerID, StaffID, OrderDate

- OrderID \rightarrow CustomerID, StaffID, OrderDate

Relation 5: FoodDishId, FoodDishName, UnitPrice

- $\text{FoodDishId} \rightarrow \text{FoodDishName, UnitPrice}$

Relation 6: OrderID, FoodDishId, Quantity, QuantityPrice

- $\text{OrderID, FoodDishId} \rightarrow \text{Quantity, QuantityPrice}$

This final table is in BCNF Form. All requirements are satisfied. You can also check the Ruf Work for this Question at the End of the [Document](#).

Question 09:

We are given the relation $R(\text{ABCDEFGH})$, and FDs $\{AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$. Turning the relation into its lowest form by removing its dependencies, we get ABFH.

Taking the closure of ABFH, we get $\{A, B, C, D, E, F, G, H\}$, so it can be called a super key. But, closure of BFH gives $\{B, D, F, H\}$ which means it is not a candidate key. Similarly, the closure of AFH gives $\{A, F, H\}$, thus it is also not a candidate key. Thus, ABFH is one candidate key. Closure of ACFH gives all values in the relation, ie: $\{A, B, C, D, E, F, G, H\}$. While, taking closure of AFH and CFH does not give all values in the Relation. So, ACFH is a Candidate key.

Moreover, the closure of BCFH gives all values in the relation mainly $\{B, C, A, D, E, G, F, H\}$. So, BCFH is a Candidate key. There are 3 candidate keys: **ABFH, ACFH, BCFH**.

Moreover, the Paper written version of this Question is also given at the End of this [Document](#). Moreover, the Diagrams in this Assignment have been created using [ERDPlus](#). The Source Files for each Document have been attached to Google Classroom.

NEXT PAGE

Question 08 (Hand Written):

Question 8

Date: _____ Day: _____

→ Keys : Order ID, Food Dish ID
As

→ Order ID and Food Dish ID⁺ = { All attributes }

→ Prime Attributes : Order ID, Food Dish ID

→ Non-Prime Attributes: All except the prime attributes.

• Checking Highest Normal Form:

i. For BCNF L.H.S must be a superkey.

StaffID → SName CustID →,,, CustAd →,,, OrderID → FoodID (OrderID, FoodID) →

BCNF:	X	X	X	X	X	✓
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ii. For 3NF there should be no transitive Dependency
So either L.H.S is Superkey or R.H.S is Prime attributes

3NF:	X	X	X	X	X	✓
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iii. For 2NF there should be partial Dependency
so L.H.S is proper Subset of candidate key
and R.H.S is Non Prime attribute.

2NF:	✓	✓	✓	X	X	✓
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Therefore, highest Normal form is 1NF.

Date: _____

Day: _____

i Partial Dependency:

a. $\text{OrderID} \rightarrow \text{OrderDate}, \text{CustomerID}, \text{StaffID}$

b. $\text{FoodDishID} \rightarrow \text{FoodDishName}, \text{Unit Price}$

Making Relations

$\text{OrderID}^+ = \{ \text{OrderDate}, \text{CustomerID}, \text{StaffID}, \text{StaffName}, \text{Customer Name}, \text{Cust-}$

$\text{OrderID}, \text{Cust-Phone}, \text{Address} \}$

→ $R_1 = \{ \text{OrderDate}, \text{CustID}, \text{StaffID}, \text{StaffName}, \text{OrderID}, \text{CustomerName}, \text{CustPhone}, \text{CustAddress} \}$

$\text{FoodDishID}^+ = \{ \text{FoodDishName}, \text{Unit Price} \}$

→ $R_2 = \{ \text{FoodDishID}, \text{FoodDishName}, \text{Unit Price} \}$

◦ Remaining attributes in one table with common candidate keys of R_1 and R_2 .

→ $R_3 = \{ \text{Quantity}, \text{Quantity Price}, \text{OrderID}, \text{FoodDishID} \}$

Computing FD's of each Relation:

for R_1

$F_1: \{ \text{OrderID} \xrightarrow{\text{ID}} \text{OrderDate}, \text{StaffID}, \text{StaffName}, \text{CustID}, \text{Customer Name}, \text{CustPhone}, \text{Cust Address} \}$

and $\text{CustID} \rightarrow \text{CustName}, \text{Cust-Address},$

$\text{CustADD} \rightarrow \text{Cust Phone}, \text{StaffID} \rightarrow \text{StaffName} \}$

Date: _____

Day: _____

For R_2 :

$F_2: \{ \text{Food Dish ID} \rightarrow \text{Food Dish Name, Unit Price} \}$

For R_3 :

$F_3: \{ \text{Order ID, Food Dish ID} \rightarrow \text{Quantity, Quantity Price} \}$

So for R_1

CK = OrderID

Checking normal form,

BCNF: \checkmark X X X
3NF: \checkmark X X X
2NF: \checkmark \checkmark \checkmark \checkmark

Successfully Converted into 2NF.

So for R_2

CK: Food Dish ID

BCNF: \checkmark
3NF: \checkmark
2NF: \checkmark

Successfully converted into BCNF

R_3

CK: OrderID, Food Dish ID

BCNF: \checkmark
3NF: \checkmark
2NF: \checkmark

Successfully converted in BCNF

Problem is transitive Dependency in R_1 therefore, FDs causing this Problem are,

$\begin{cases} \text{CustID} \rightarrow \text{Cust Name, Cust-Address} \\ \text{CustAdd} \rightarrow \text{CustPhone} \\ \text{StaffID} \rightarrow \text{Staff Name} \end{cases}$

Making Relations

$\text{CustID}^* = \{ \text{CustName, CustAdd} \}$

$\text{CustAdd}^* = \{ \text{add, Phone} \}$

$\text{StaffID}^* = \{ \text{Staff Name} \}$

$R_1: \{ \text{CustID, CustName, Custadd} \}$

$R_2: \{ \text{Custadd, Phone} \}$

$R_3: \{ \text{StaffID, Name} \}$

Computing FD,

$F_1: \{ \text{CustID} \rightarrow \text{CustName, Custadd} \}$

$F_2: \{ \text{Custadd} \rightarrow \text{Cust, Phone} \}$

$F_3: \{ \text{StaffID} \rightarrow \text{Name} \}$

CK: add BCNF \checkmark

CK: ID BCNF \checkmark

CK: ID

Checking NF

BCNF \checkmark

$R_4: \{ \text{OrderID, Date, Name, CustName, CustPhone, CustID} \}$

$F_4: \{ \text{OrderID} \rightarrow \text{Date, Name, CustName, CustPhone, CustID} \}$

BCNF \checkmark

Question 09 (Handwritten):

Question 9

Date: _____ Day: _____

9. $R(ABCDEFGH)$

→ $F = \{AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$

~~ABCFH~~

$ABFH^+ = \{ABCDEFGFH\}$

→ $BFH = \{B, D, F, H\} \times$

→ $AFH = \{AFH\} \times$

Therefore,

→ $ABFH^+$ is one candidate key

$ACFH^+ = \{ACBDEGFH\}$

→ $AFH^+ \times$

→ $CFH^+ = \{CFH\} \times$

Therefore,

$ACFH$ is another candidate key

$BCFH^+ = \{BCADEGFH\}$

So,

$BCFH^+$ is another candidate key

Therefore there are 3 candidate keys

$ABFH, ACFH, BCFH$