

## Relational Algebra Solutions

**Q1:**

$$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{SALARY}}(\text{Employee}) - \text{SALARY} \downarrow \\ (\pi_{\text{SALARY}}(\sigma_{\text{LAST\_NAME}='Bull'}(\text{Employee})))$$

**Q2:**

$$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}}(\sigma_{\text{DEPARTMENT\_NAME}='IT'} \\ (\text{Employee} \bowtie_{\text{Employee.DEPARTMENT\_ID} = \text{Departments.DEPARTMENT\_ID}} \text{Departments}))$$

**Q3:**

$$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}}(\sigma_{\text{MANAGER\_ID} \neq \text{NULL} \wedge \text{COUNTRY\_ID}='US'} \\ (\text{Employee} \bowtie_{\text{Employee.DEPARTMENT\_ID} = \text{Departments.DEPARTMENT\_ID}} \\ \text{Departments} \bowtie_{\text{Departments.LOCATION\_ID} = \text{Locations.LOCATION\_ID}} \text{Locations}))$$

**Q4:**

$$\pi_{\text{EMPLOYEE\_ID}, \text{FIRST\_NAME}, \text{LAST\_NAME}}(\text{Employee} - \text{SALARY} \downarrow \\ (\pi_{\text{AVG}(\text{SALARY})}(\text{Employee})))$$

**Q5:**

$$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{EMPLOYEE\_ID}, \text{JOB\_ID}}(\sigma_{\text{CITY}='Toronto'} \\ (\text{Employee} \bowtie_{\text{Employee.DEPARTMENT\_ID} = \text{Departments.DEPARTMENT\_ID}} \\ \text{Departments} \bowtie_{\text{Departments.LOCATION\_ID} = \text{Locations.LOCATION\_ID}} \text{Locations}))$$

**Q6:**

$$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{EMPLOYEE\_ID}, \text{SALARY}}(\sigma_{\text{MANAGER\_ID}=(\pi_{\text{EMPLOYEE\_ID}} \\ (\sigma_{\text{FIRST\_NAME}='Payam'}(\text{Employee})))}(\text{Employee}))$$

**Q7:**

$$\pi_{\text{DEPARTMENT\_NAME}}(\text{Departments} \cap \text{Employee})$$

**Q8:**

$$\text{Employee} - \text{DEPARTMENT\_ID} \text{ NOT IN } (\pi_{\text{DEPARTMENT\_ID}}(\sigma_{\text{MANAGER\_ID} \geq 100 \wedge \text{MANAGER\_ID} \leq 200}(\text{Departments})))$$

**Q9:**

$$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{DEPARTMENT\_ID}}(\sigma_{\text{SALARY}=\text{MIN}(\text{SALARY})}(\text{Employee}))$$

**Q10:**

$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}}(\sigma_{\text{EMPLOYEE\_ID} \in (\pi_{\text{MANAGER\_ID}}(\text{Departments}))}(\text{Employee}))$

**Q11:**

$\pi_{\text{EMPLOYEE\_ID}, \text{FIRST\_NAME}, \text{LAST\_NAME}, \text{JOB\_ID}}(\sigma_{\text{SALARY} < (\pi_{\text{SALARY}}(\sigma_{\text{JOB\_ID} = \text{'MK\_MAN'}}(\text{Employee})))}(\text{Employee}))$

**Q12:**

$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{SALARY}}(\sigma_{\text{SALARY} > \text{AVG}(\text{SALARY})}(\text{Employee}))$

**Q13:**

$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{SALARY}}(\sigma_{\text{SALARY} = (\pi_{\text{MIN\_SALARY}}(\sigma_{\text{Employee.JOB\_ID} = \text{Jobs.JOB\_ID}(\text{Employee}) \times \text{Jobs}}))}(\text{Employee}))$

**Q14:**

$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{SALARY}}(\sigma_{\text{SALARY} > \text{AVG}(\text{SALARY})}(\text{Employee} \bowtie_{\text{Employee.DEPARTMENT\_ID} = \text{Department.DEPARTMENT\_ID}} \text{Department}))$

**Q15:**

$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{SALARY}}(\sigma_{\text{SALARY} > (\pi_{\text{SALARY}}(\sigma_{\text{LAST\_NAME} = \text{'Bell'}}(\text{Employee})))}(\text{Employee}))$

**Q16:**

$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{SALARY}}(\sigma_{\text{SALARY} = \text{MIN}(\text{SALARY})}(\text{Employee}))$

**Q17:**

$\pi_{\text{FIRST\_NAME}, \text{LAST\_NAME}, \text{SALARY}}(\sigma_{\text{SALARY} > \text{AVG}(\text{SALARY})}(\text{Employee}))$

**Q18:**

OFFSET 2(Employee) LIMIT 1