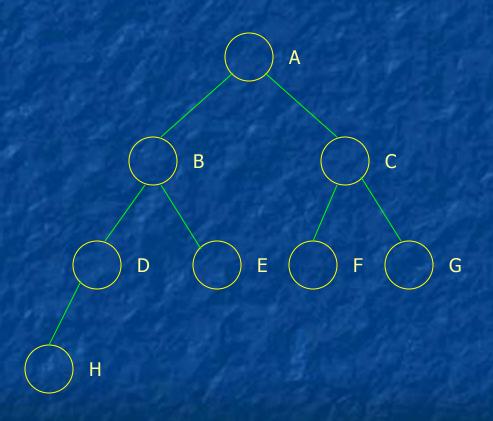
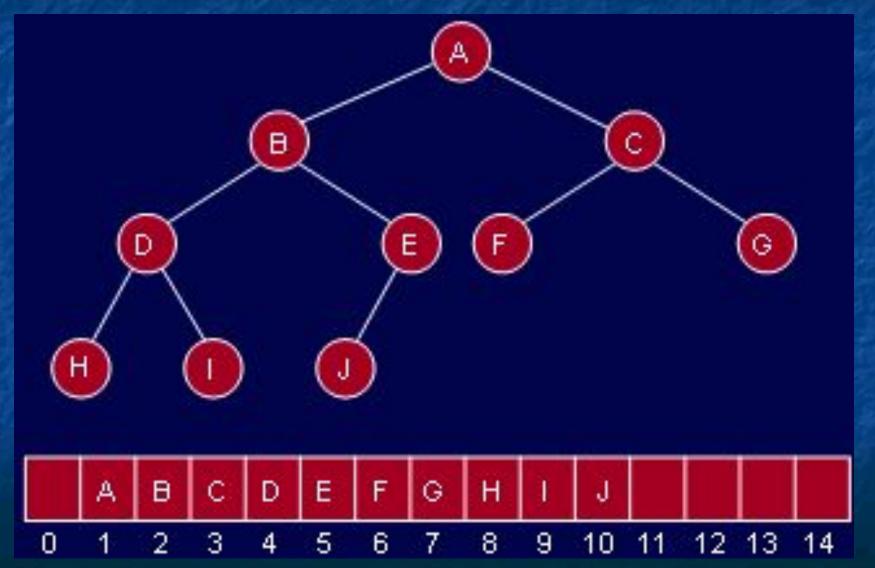
Lecture # 17



Recall that such a tree of height h has between 2^h to $2^{h+1}-1$ nodes.

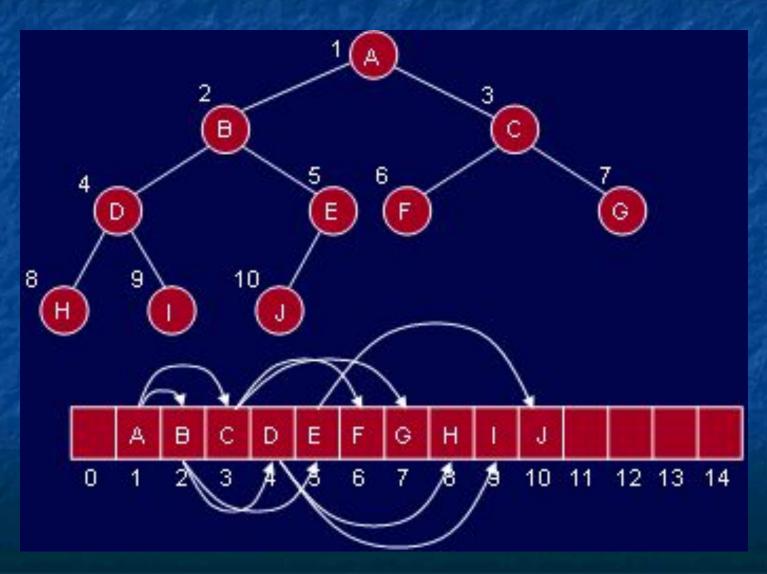
Because the tree is so regular, it can be stored in an array; no pointers are necessary.



For any array element at position i, the left child is at 2i, the right child is at (2i +1) and the parent is at [i/2].







• Question:

why don't we store all binary trees in arrays? Why use pointers?

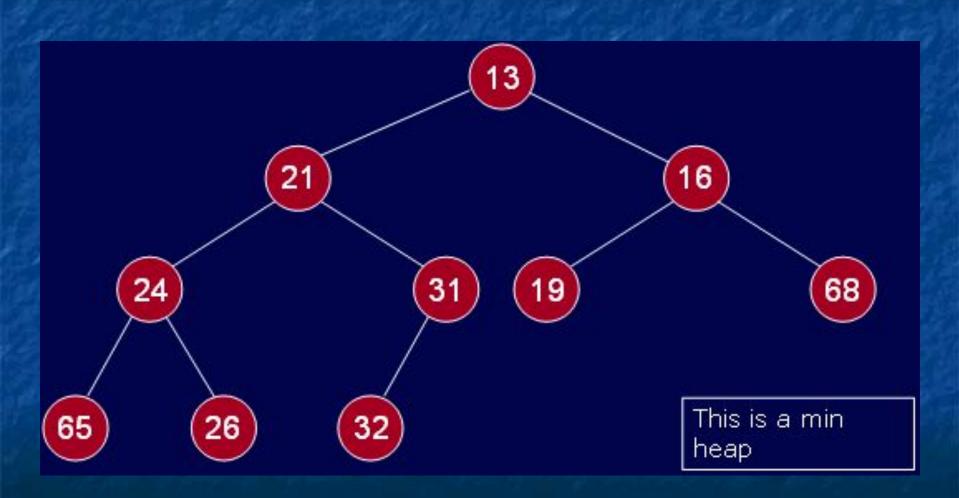
The Heap ADT

 The major usage of heap is in Priority Queues.

Heap

- A heap is a complete binary tree that conforms to the heap order.
- The heap order property: in a (min) heap, for every node X, the key in the parent is smaller than (or equal to) the key in X.
- Or, the parent node has key smaller than or equal to both of its children nodes.

Heap

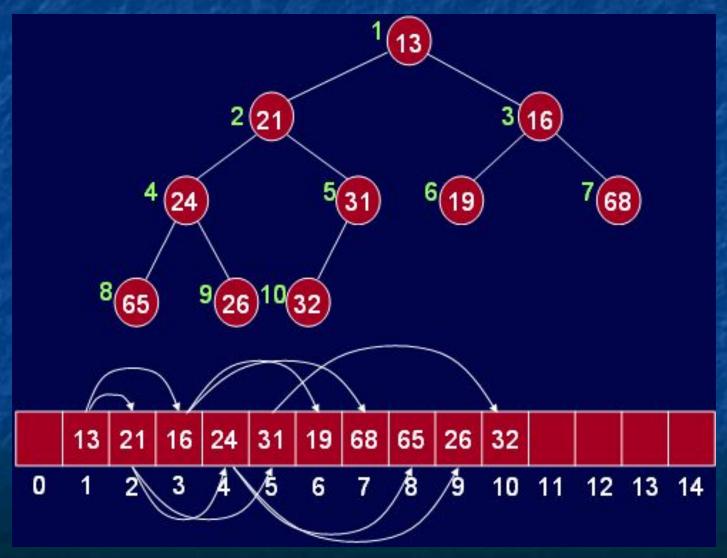


Heap

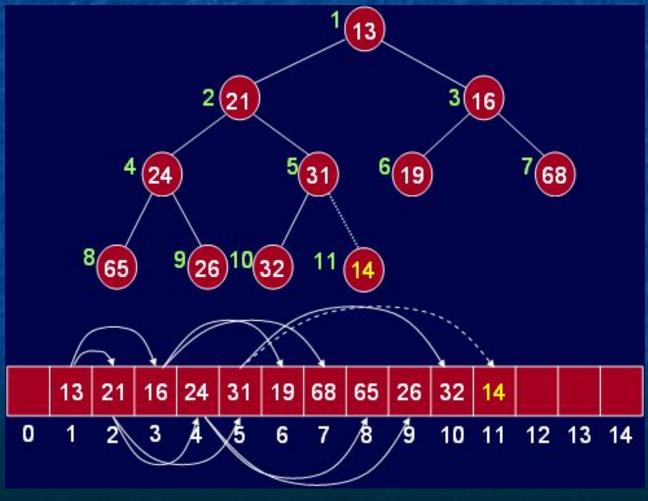
Not a heap: heap property violated



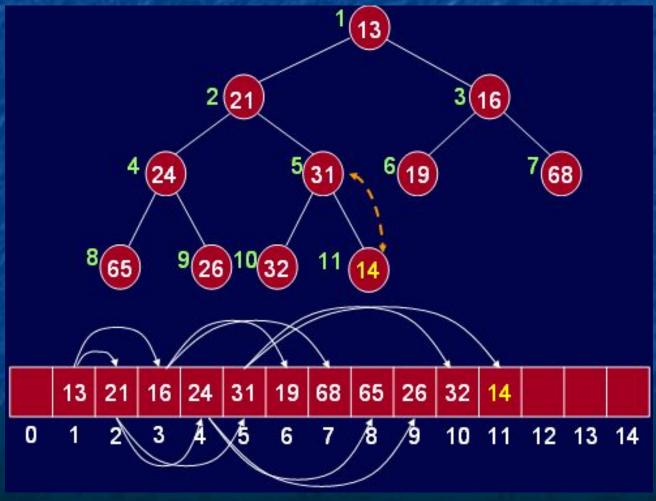
Assume this existing heap

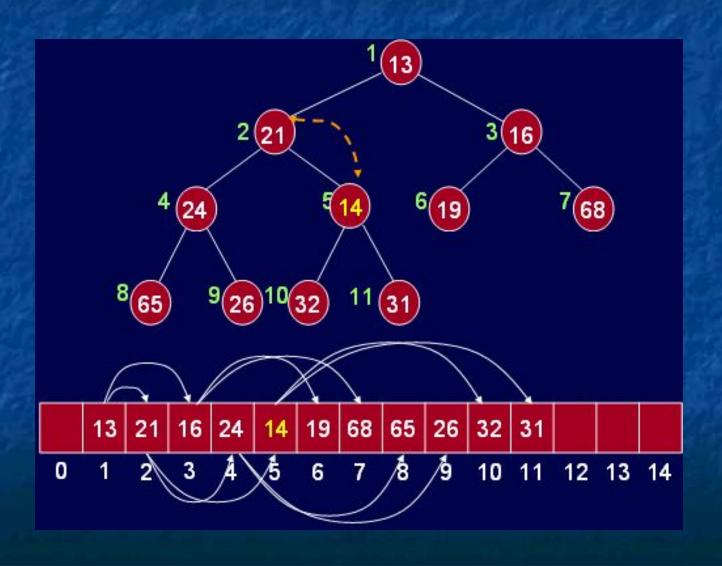


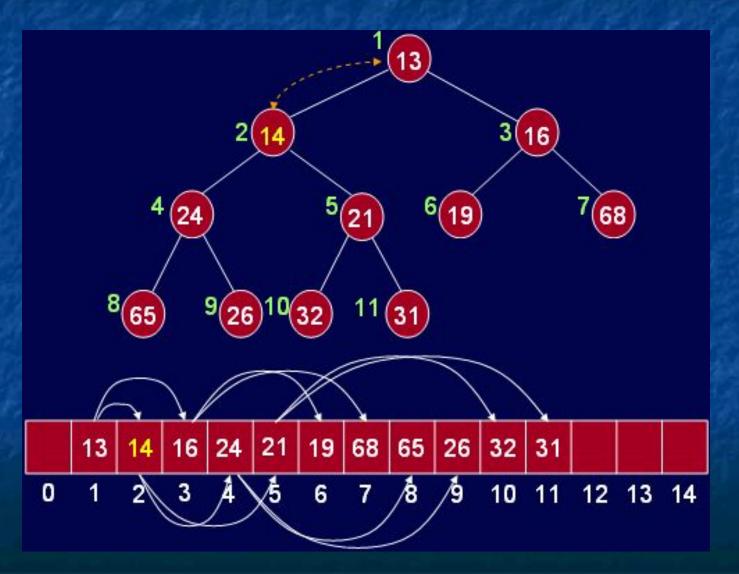
insert(14)



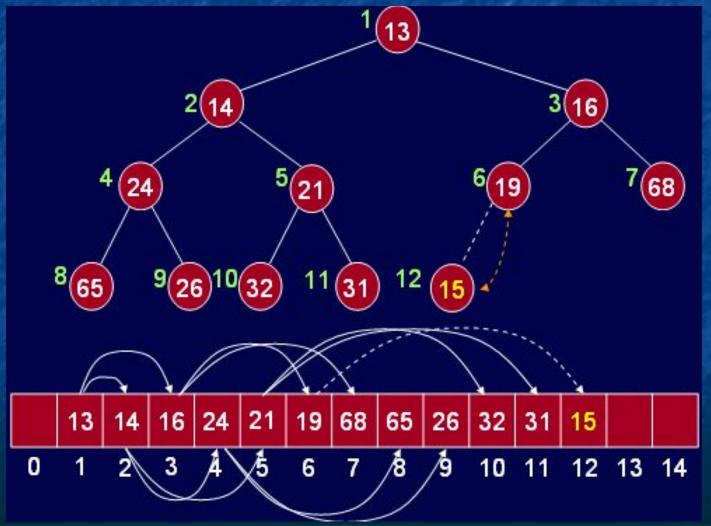
insert(14) with exchange

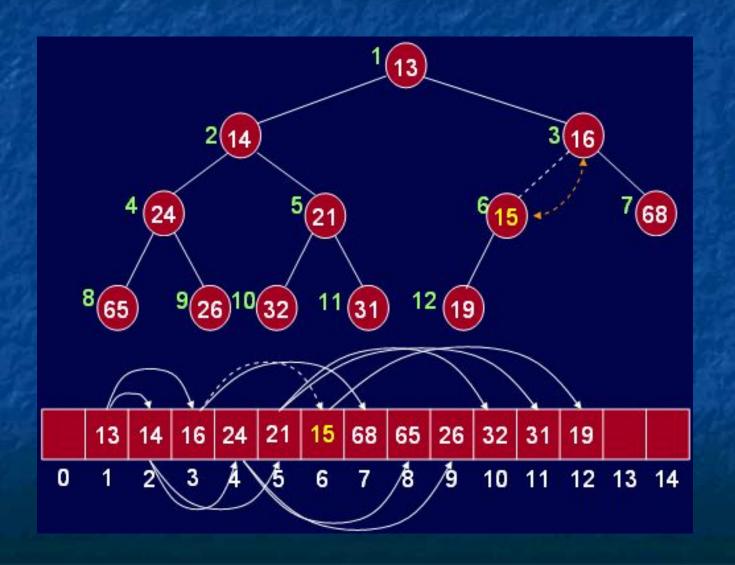


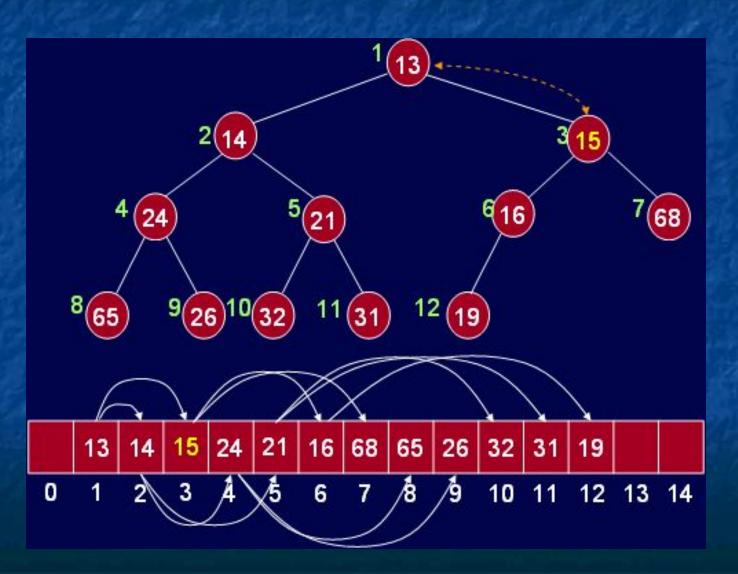


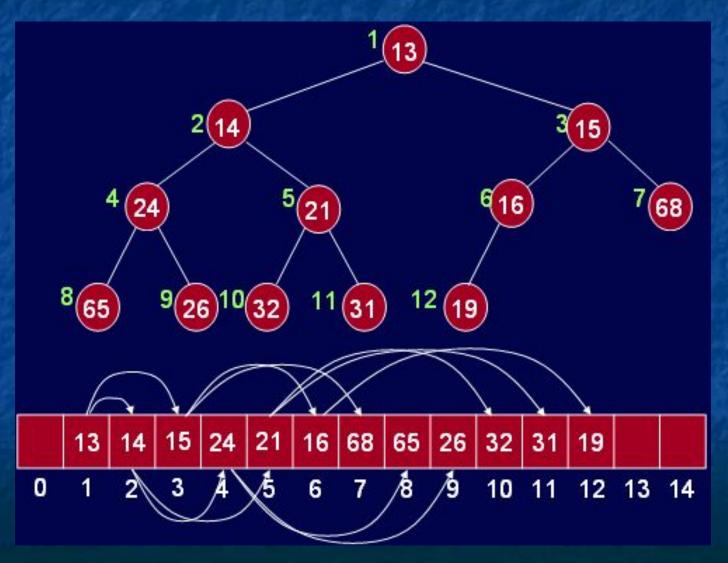


insert(15) with exchange



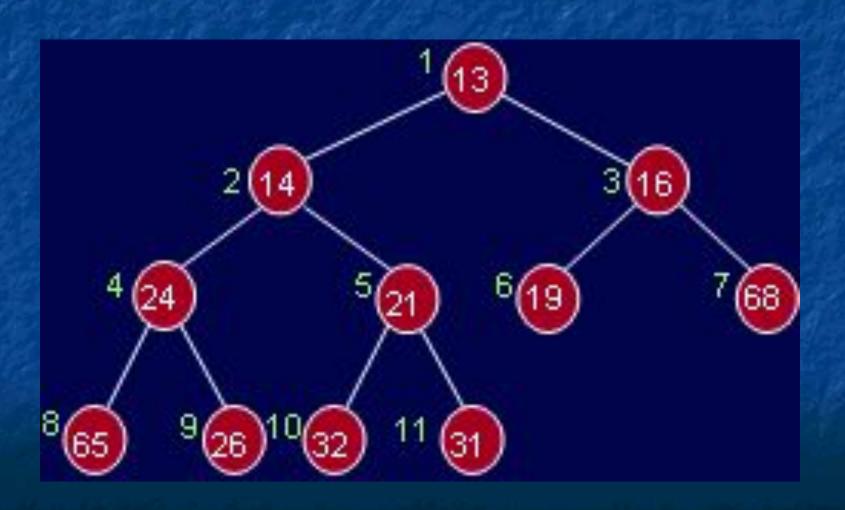


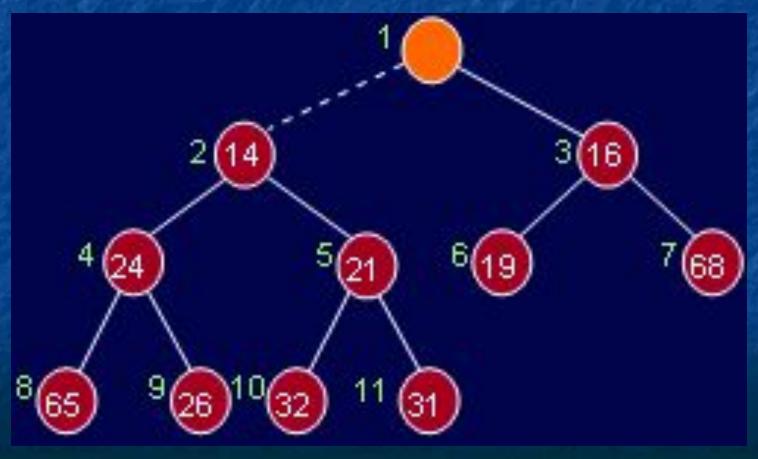


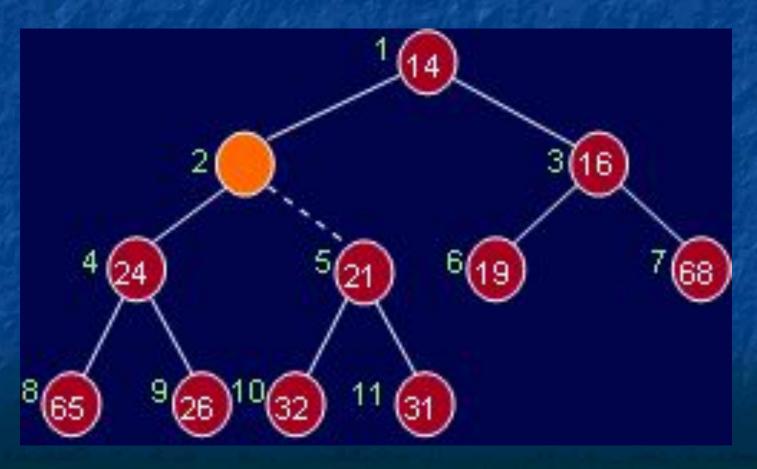


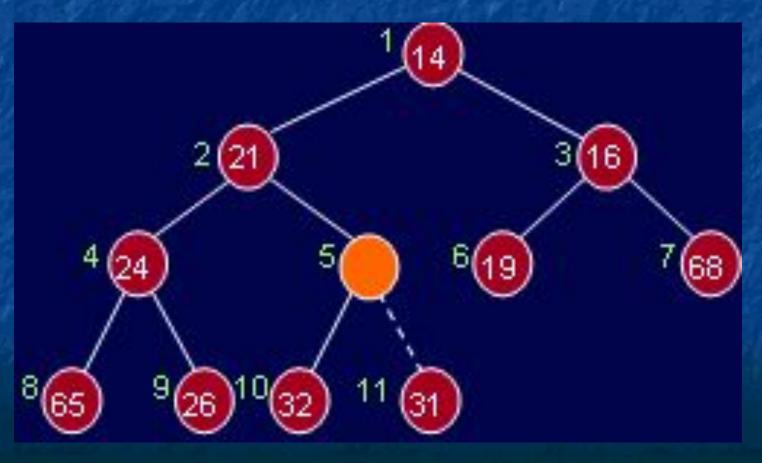
Finding the minimum is easy; it is at the top of the heap.

Deleting it (or removing it) causes a hole which needs to be filled.











deleteMin(): heap size is reduced by 1.

