



CS-2001

Data Structures

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Introduction to Queue ADT

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Queues

- Queue is **First-In-First-Out (FIFO)** data structure
 - **First element added** to the queue will be **first one to be removed**
- Queue implements a special kind of list
 - Items are **inserted** at one end (the **rear**)
 - Items are **deleted** at the other end (the **front**)

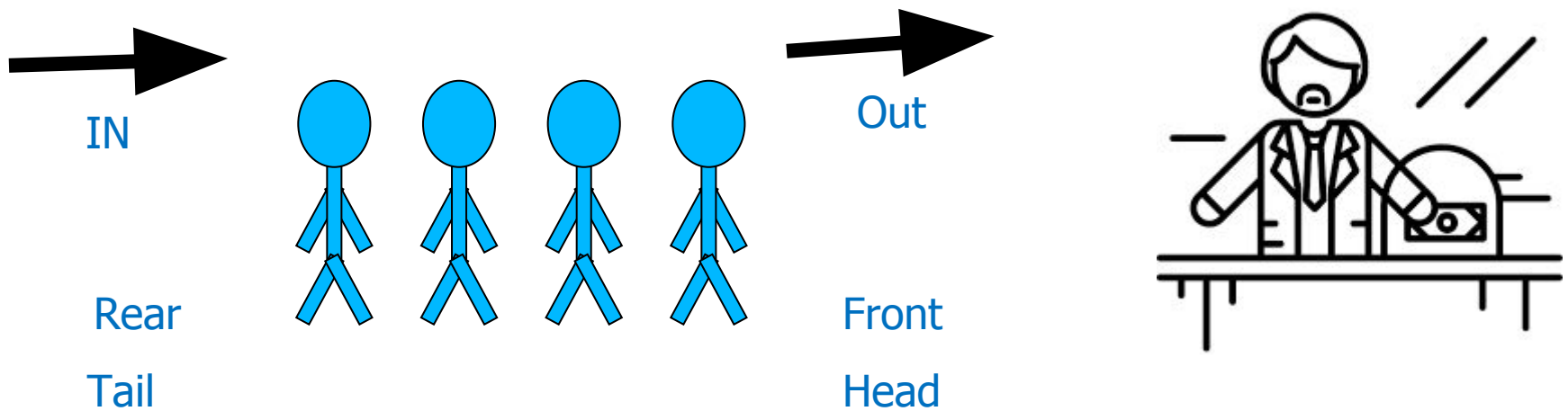
Queues Vs Stack

- Stack is Last-In-First-Out (**LIFO**) data structure
- Queue is First-In-First-Out (**FIFO**) data structure



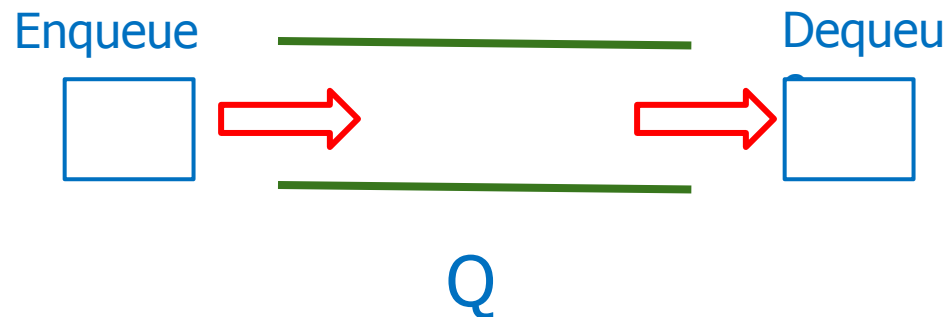
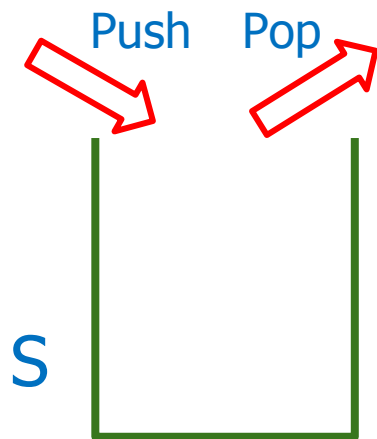
Queue – Analogy (1)

- A queue is like a line of people waiting for a bank teller
- The queue has a **front** and a **rear**



Queue – ADT

- A list or collection with the restriction that
 - insertion can be performed at one end (**Rear**)
 - deletion can be performed at another end (**Front**)
- Operations
 - Enqueue(x)
 - Dequeue(x)
 - Front()
 - IsEmpty()
 - IsFull()



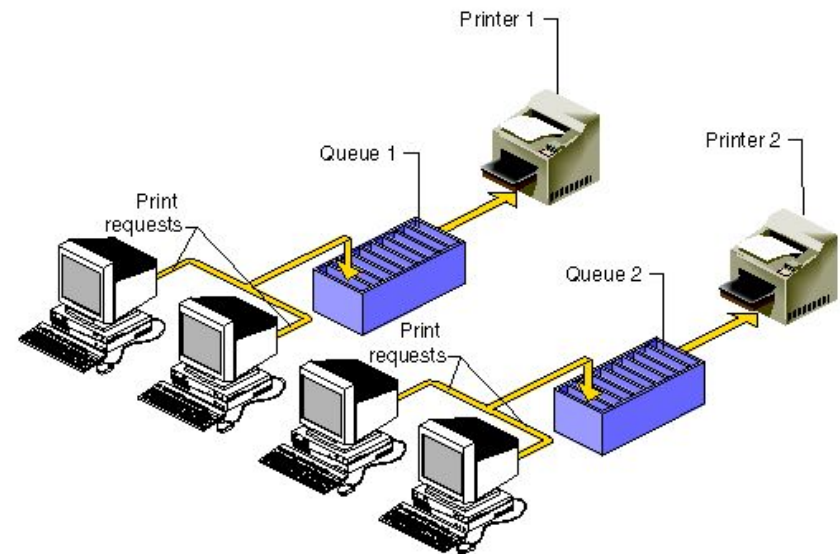
Queue - Library Implementation

```
// CPP code to illustrate Queue in Standard Template Library (STL)
#include <iostream>
#include <queue>
using namespace std;
// Driver Code
int main()
{
    queue<int> gquiz;
    gquiz.push(10);
    gquiz.push(20);
    gquiz.push(30);

    cout << "\ngquiz.size() : " << gquiz.size();
    cout << "\ngquiz.front() : " << gquiz.front();
    cout << "\ngquiz.back() : " << gquiz.back();
    gquiz.pop();
    while (!g.empty()) {
        cout << '\t' << g.front();
        g.pop();
    }
    return 0;
}
```

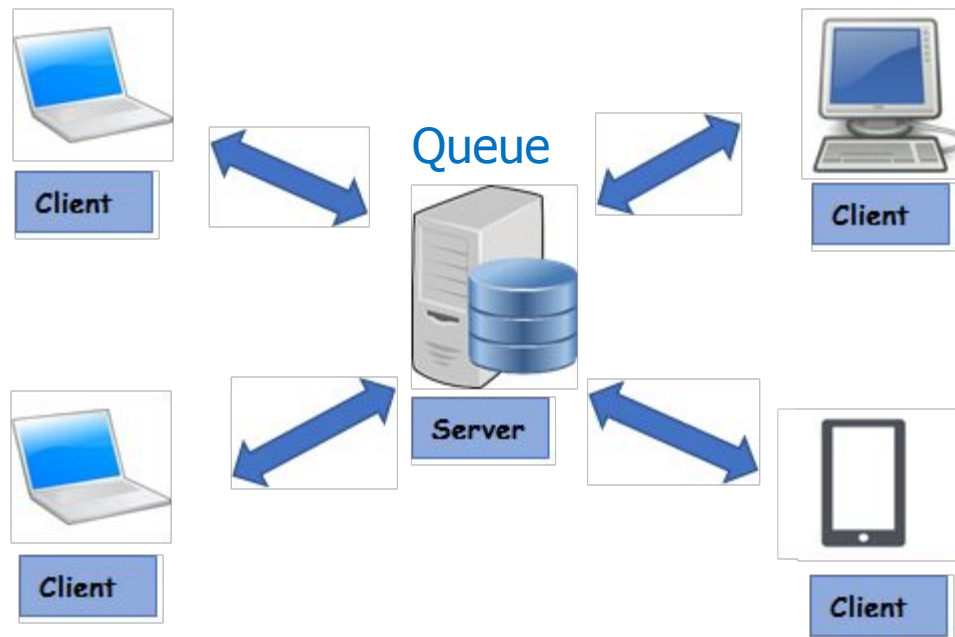
Queues – Examples

- Billing counter
 - Booking movie tickets
 - Queue for paying bills
- Vehicles on toll-tax bridge
- Luggage checking machine
- A printer queue of computers
- Processes scheduling queue in OS
- And others?



Queues – Applications

- Operating systems
 - Process scheduling in multiprogramming environment
 - Controlling provisioning of resources to multiple users (or processes)
- Middleware/Communication software
 - The most common application is in client-server models
 - Multiple clients may be requesting services from one or more servers

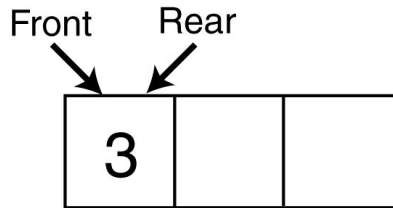


Basic Operations (Queue ADT)

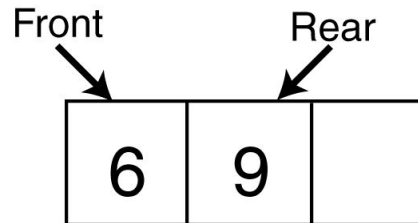
- **MAKENULL(Q)**
 - Makes Queue Q be an empty list
- **FRONT(Q)**
 - Returns the first element on Queue Q
- **ENQUEUE(x,Q)**
 - Inserts element x at the end of Queue Q
- **DEQUEUE(Q)**
 - Deletes the first element of Q
- **EMPTY(Q)**
 - Returns true if and only if Q is an empty queue

Enqueue And Dequeue Operations

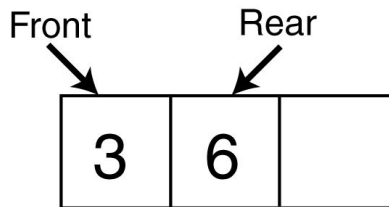
Enqueue(3);



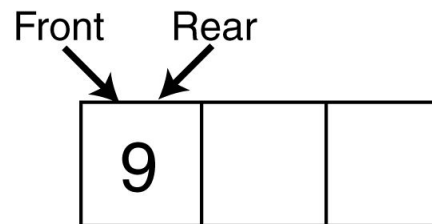
Dequeue();



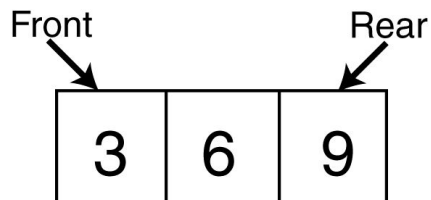
Enqueue(6);



Dequeue();

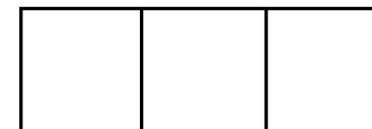


Enqueue(9);



Dequeue();

Front = -1 Rear = -1

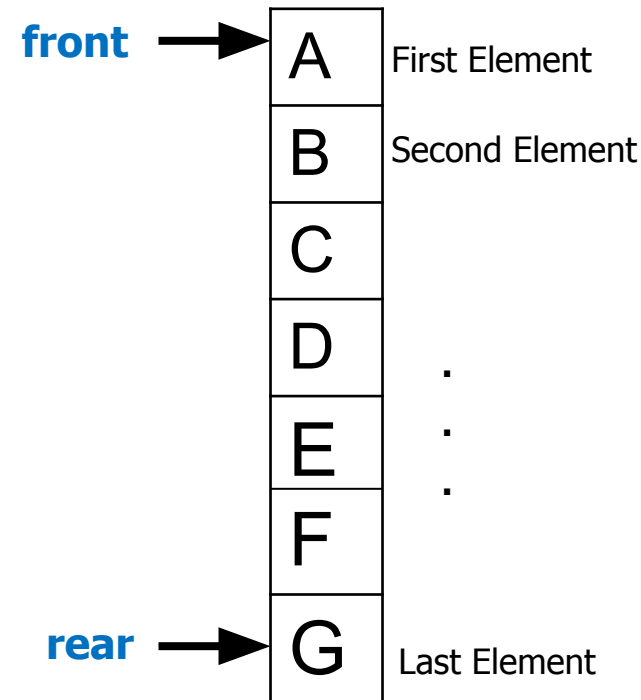


Implementation

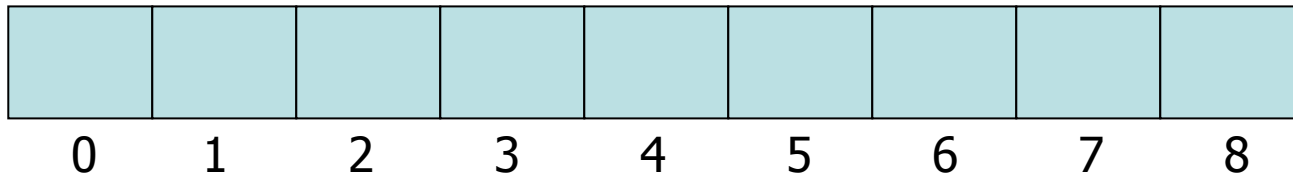
- Static
 - Queue is implemented by an array
 - Size of queue remains fix
- Dynamic
 - A queue can be implemented as a linked list
 - Expand or shrink with each enqueue or dequeue operation

Array Implementation

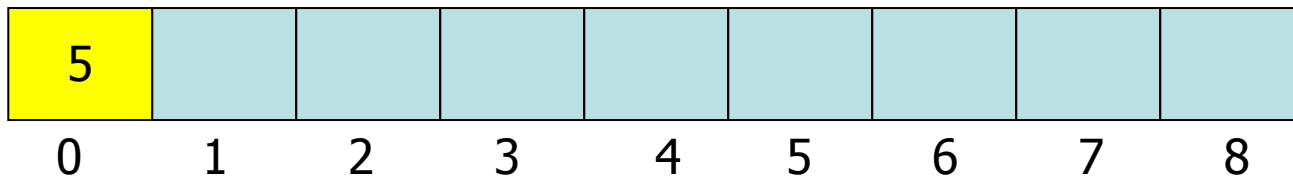
- Use **two counters** that signify **rear** and **front**
- When queue is **empty**
 - Both **front** and **rear** are set to **-1**
- When there is **only one value** in the Queue,
 - Both **rear** and **front** have **same** index
- While **enqueueing** increment **rear** by 1
- While **dequeueing**, increment **front** by 1



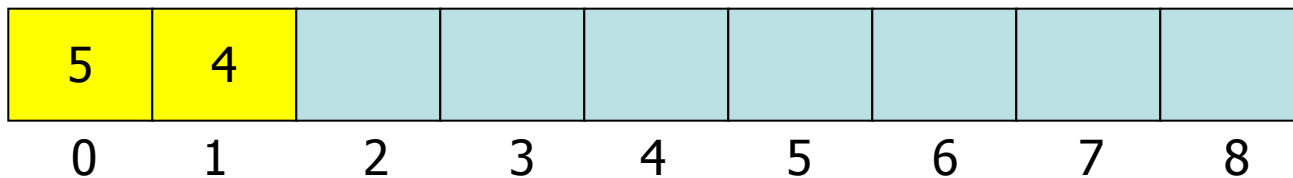
Array Implementation Example (1)



front = -1
rear = -1

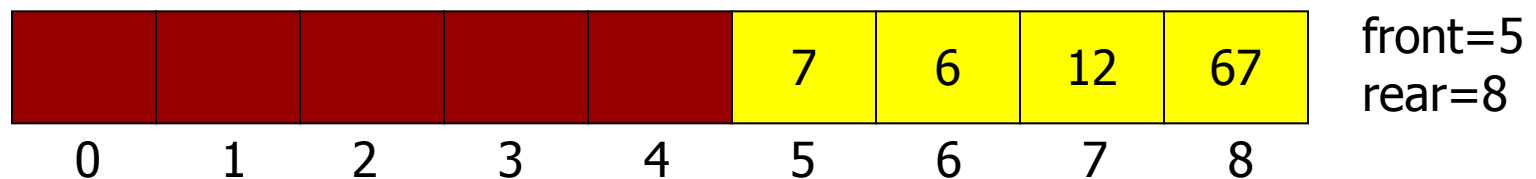
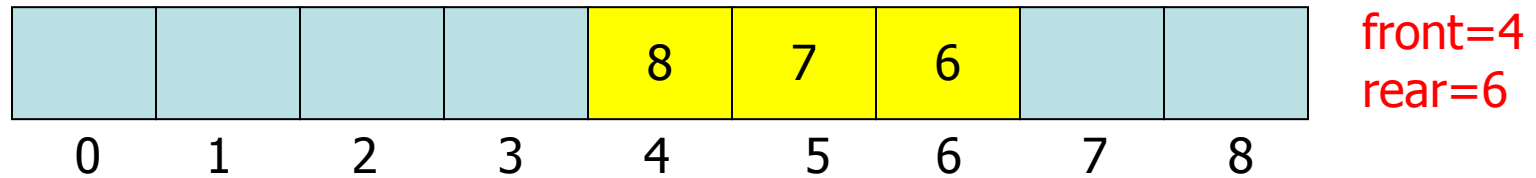
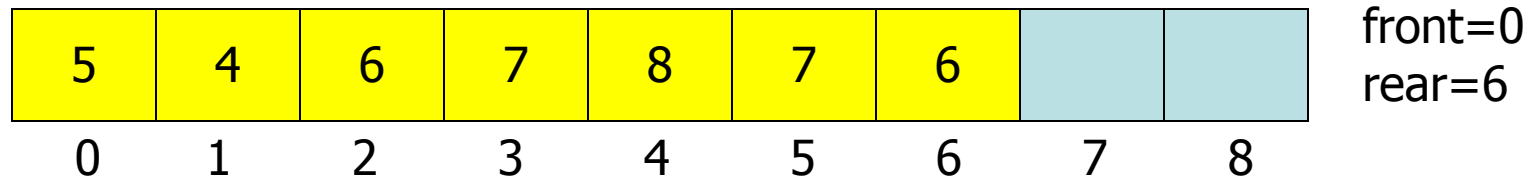


front = 0
rear = 0



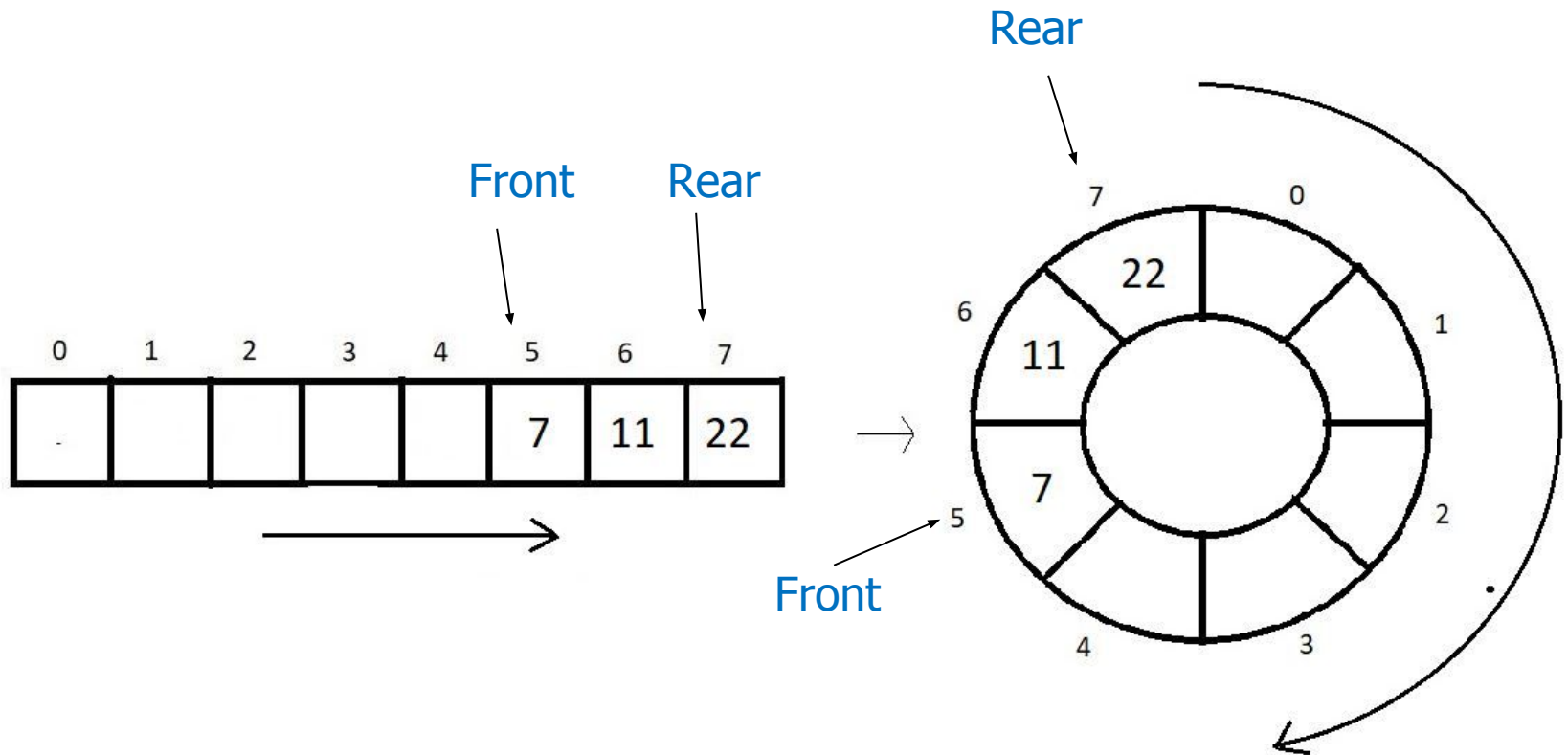
front = 0
rear = 1

Array Implementation Example (2)



Problem: How can we insert more elements?
Rear index can not move beyond the last element....

Array Implementation Example (2)



current position = i
next position = $i + 1 \% N$
previous position ???

Logical Representation

Using Circular Queue

- Allow **rear** to wrap around the array

```
if(rear == queueSize-1)
    rear = 0;
else
    rear++;
```

- Alternatively, use modular arithmetic

```
rear = (rear + 1) % queueSize;
```


Example

					7	6	12	67
0	1	2	3	4	5	6	7	8

front=5
rear=8

Enqueue 39

- $\text{Rear} = (\text{Rear} + 1) \bmod \text{queueSize} = (8 + 1) \bmod 9 = 0$

39					7	6	12	67
0	1	2	3	4	5	6	7	8

front=5
rear=0

Problem: How to avoid overwriting an existing element?

How to Determine Empty and Full Queues?

- A counter indicating number of values/items in the queue
 - Covered in first array-based implementation
- Without using an additional counter (only relying on front and rear)
 - Covered in alternative array-based implementation

Array-based Implementation

Implementation – Code (1)

```
class CQueue
{
    Private:
        int *queueArray; // Pointer to array implemented as Queue
        int queueSize;   // Total size of the Queue
        int front;
        int rear;
    public:
        CQueue(int size);
        ~CQueue();
        bool isFull();
        bool isEmpty();
        bool enqueue(int num);
        bool dequeue(int& num);
        void makeNull();
};
```

Implementation – Code (2)

```
CQueue::CQueue(int size)
{
    front=rear=-1;
    queueArray =new int[size];
    queueSize = size;
}

CQueue::~~CQueue() //destructor
{
    delete [] queueArray;
}

void IntQueue::makeNull()
{
    front = - 1;
    rear = - 1;
}
```

Implementation – Code (3)

- `isEmpty()` returns true if the queue is empty and false otherwise

```
bool CQueue::isEmpty()
{
    if (front==-1)
        return true; // we can check "rear" too
    else
        return false;
}
```

- `isFull()` returns true if the queue is full and false otherwise

```
bool CQueue::isFull()
{
    if ( ( (rear+1)%queueSize ) == front )
        return true;
    else
        return false;
}
```

Implementation – Code (4)

- Function `enqueue` inserts the value in `num` at the end of the Queue

```
bool CQueue ::enqueue(int num);
{
    if ( isFull() ) {
        cout<<"Overflow";
        return false;
    }
    if (isEmpty())
        rear = front = 0;
    else
        rear=(rear+1) % queueSize;

    queueArray[rear] = num;
    return true;
}
```

Comparison: enqueue Operation

```
bool CQueue ::enqueue(int num);
{
    if ( isFull() ) {
        cout<<"Overflow";
        return false;
    }
    if (isEmpty())
        rear = front = 0;
    else
        rear=(rear+1) % queueSize;

    queueArray[rear] = num;
    return true;
}
```

```
bool IntQueue::enqueue(int num)
{
    if (isFull())
    {
        cout << "Overflow.\n";
        return false;
    }

    // Calculate the new rear position
    rear = (rear + 1) % queueSize;
    // Insert new item
    queueArray[rear] = num;
    // Update item count
    numItems++;
    return true;
}
```


Implementation – Code (5)

- Function `dequeue` removes and returns the value at the front of the Queue

```
bool CQueue ::dequeue(int &num)
{
    if ( isEmpty() ) {
        cout<<"Underflow";
        return false;
    }
    num = queueArray[front];

    if ( front == rear ) //only one element in the queue
                        //skipping this step will effect
        front = rear = -1; //the isEmpty() function
    else
        front = (front+1) % queueSize;

    return true;
}
```

Alternative Array-based Implementation

Array Implementation – Code (1)

```
class IntQueue
{
    private:
        int *queueArray; // Pointer to array implemented as Queue
        int queueSize;   // Total size of the Queue
        int front;
        int rear;
        int numItems;    // Number of items currently in the Queue
    public:
        IntQueue(int);
        ~IntQueue();
        bool isEmpty();
        bool isFull();
        bool enqueue(int);
        int dequeue();
        void makeNull();
};
```

Array Implementation – Code (2)

```
class IntQueue
{
    private:
        int *queueArray; // Pointer to array implemented as Queue
        int queueSize;    // Total size of the Queue
        int front;
        int rear;
        int numItems;     // Number of items currently in the Queue
    public:
        IntQueue(int);
        ~IntQueue();
        bool isEmpty();
        bool isFull();
        bool enqueue(int);
        int dequeue();
        void makeNull();
};
```

Clears the queue by resetting the `front` and `rear` indices, and setting the `numItems` to 0.

Array Implementation – Code (3)

- **Constructor**

```
IntQueue::IntQueue(int s) //constructor
{
    queueArray = new int[s];
    queueSize = s;
    front = -1;
    rear = -1;
    numItems = 0;
}
```

- **Destructor**

```
IntQueue::~~IntQueue() //destructor
{
    delete [] queueArray;
}
```

Array Implementation – Code (4)

```
//*****  
// Function isEmpty returns true if the queue *  
// is empty, and false otherwise.           *  
//*****
```

```
bool IntQueue::isEmpty()  
{  
    if (numItems == 0)  
        return true;  
    else  
        return false;  
}
```

Array Implementation – Code (5)

```
/** *****  
// Function isFull returns true if the queue *  
// is full, and false otherwise.           *  
/** *****
```

```
bool IntQueue::isFull()  
{  
    if (numItems == queueSize)  
        return true;  
    else  
        return false;  
}
```

Array Implementation – Code (6)

```
//*****
// Function enqueue inserts the value in num *
// at the rear of the queue.                  *
//*****

bool IntQueue::enqueue(int num)
{
    if (isFull())
    {
        cout << "Overflow.\n";
        return false;
    }
    // Calculate the new rear position
    rear = (rear + 1) % queueSize;
    //front is only updated in de-queuing an item
    // Insert new item
    queueArray[rear] = num;
    // Update item count
    numItems++;
    return true;
}
```


Array Implementation – Code (7)

```
//*****  
// Function dequeue removes the value at the *  
// front of the queue, and copies it into num.*  
//*****  
  
bool IntQueue::dequeue(int &num)  
{  
    if (isEmpty())  
    {  
        cout << "The queue is empty.\n";  
        return false;  
    }  
  
    // Move front  
    front = (front + 1) % queueSize;  
    // Retrieve the front item  
    num = queueArray[front];  
    // Update item count  
    numItems--;  
    return true;  
}
```

Array Implementation – Code (8)

```
//*****  
// Function clear resets the front and rear *  
// indices, and sets numItems to 0.          *  
//*****
```

```
void IntQueue::makeNull()  
{  
    front = - 1;  
    rear = - 1;  
    numItems = 0;  
}
```

Using Queues

```
int main()
{
    IntQueue iQueue(5);
    cout << "Enqueueing 5 items...\n";
    // Enqueue 5 items.
    for (int x = 0; x < 5; x++)
        iQueue.enqueue(x);
    // Attempt to enqueue a 6th item.
    cout << "Now attempting to enqueue again...\n";
    iQueue.enqueue(5);
    // Dequeue and retrieve all items in the queue
    cout << "The values in the queue were:\n";
    while (!iQueue.isEmpty()){
        int value;
        iQueue.dequeue(value);
        cout << value << endl;
    }
}
```

Output:

Enqueueing 5 items...
Now attempting to enqueue again...
Overflow.

The values in the queue were:

0
1
2
3
4

Any Question So Far?

