

**Question 1****a.**

<b>A</b>	<b>B</b>	<b>Cin</b>	<b>S</b>	<b>Cout</b>
<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>
<b>0</b>	<b>0</b>	<b>1</b>	<b>1</b>	<b>0</b>
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>
<b>0</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>1</b>
<b>1</b>	<b>0</b>	<b>0</b>	<b>1</b>	<b>0</b>
<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>
<b>1</b>	<b>1</b>	<b>0</b>	<b>0</b>	<b>1</b>
<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>

**b.**

$$S = (X \oplus Y) \oplus \text{Cin}$$

$$\text{Cout} = (X.Y) + (X.\text{Cin}) + (Y.\text{Cin})$$

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>W</b>	<b>X</b>	<b>Y</b>	<b>Z</b>
0	0	0	0	0	0	0	0
0	0	0	1	1	1	1	1
0	0	1	0	1	1	1	0
0	0	1	1	1	1	0	1
0	1	0	0	1	1	0	0
0	1	0	1	1	0	1	1
0	1	1	0	1	0	1	0
0	1	1	1	1	0	0	1
1	0	0	0	1	0	0	0
1	0	0	1	0	1	1	1
1	0	1	0	0	1	1	0
1	0	1	1	0	1	0	1
1	1	0	0	0	1	0	0
1	1	0	1	0	0	1	1
1	1	1	0	0	0	1	0
1	1	1	1	0	0	0	1

**b.**

$$W = (B.C.D) \oplus A$$

$$X = (C.D) \oplus B$$

$$Y = C \oplus D$$

$$Z = D$$

### Question 3

A	B	C	D	W	X	Y	Z
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	0	0	0	1	1
0	0	1	1	0	0	1	0
0	1	0	0	0	1	1	1
0	1	0	1	0	1	1	0
0	1	1	0	0	1	0	0
0	1	1	1	0	1	0	1
1	0	0	0	1	1	1	1
1	0	0	1	1	1	1	0
1	0	1	0	1	1	0	0
1	0	1	1	1	1	0	1
1	1	0	0	1	0	0	0
1	1	0	1	1	0	0	1
1	1	1	0	1	0	1	1
1	1	1	1	1	0	1	0

b.

$$W = A$$

$$X = A \oplus B$$

$$Y = (A \oplus B) \oplus C$$

$$Z = ((A \oplus B) \oplus C) \oplus D$$