

Language Technology

<http://cs.lth.se/edan20/>

Chapter 4: Topics in Information Theory and Machine Learning

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Why Machine Learning: Early Artificial Intelligence

Early artificial intelligence techniques used introspection to codify knowledge, often in the form of rules.

Expert systems, one of the most notable applications of traditional AI, were entirely based on the competence of experts.

This has two major drawbacks:

- Need of an expertise to understand and explain the rules
- Bias introduced by the expert



Why Machine Learning: What has Changed

Now terabytes of data available.

Makes it impossible to understand such volumes of data, organize them using manually-crafted rules.

Triggered a major move to empirical and statistical techniques.

In fact, most machine-learning techniques come from traditional statistics.

Applications in natural language processing, medicine, banking, online shopping, image recognition, etc.

The success of companies like Google, Facebook, Amazon, and Netflix, not to mention Wall Street firms and industries from manufacturing and retail to healthcare, is increasingly driven by better tools for extracting meaning from very large quantities of data. 'Data Scientist' is now the hottest job title in Silicon Valley

– Tim O'Reilly



Some Definitions

- 1 Machine learning always starts with **data sets**: a collection of objects or observations.
- 2 Machine-learning algorithms can be classified along two main lines: **supervised** and **unsupervised** classification.
- 3 Supervised algorithms need a **training set**, where the objects are described in terms of attributes and belong to a known class or have a known output.
- 4 The performance of the resulting classifier is measured against a **test set**.
- 5 We can also use N -fold cross validation, where the test set is selected randomly from the training set N times, usually 10.
- 6 Unsupervised algorithms consider objects, where no class is provided.
- 7 Unsupervised algorithms learn regularities in data sets.

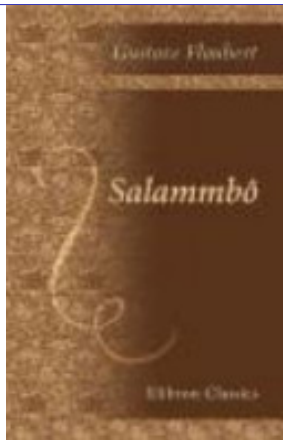
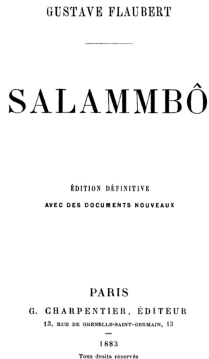


A Dataset: *Salammbô*

A corpus is a collection – a body – of texts.

French original

English translation



Supervised Learning

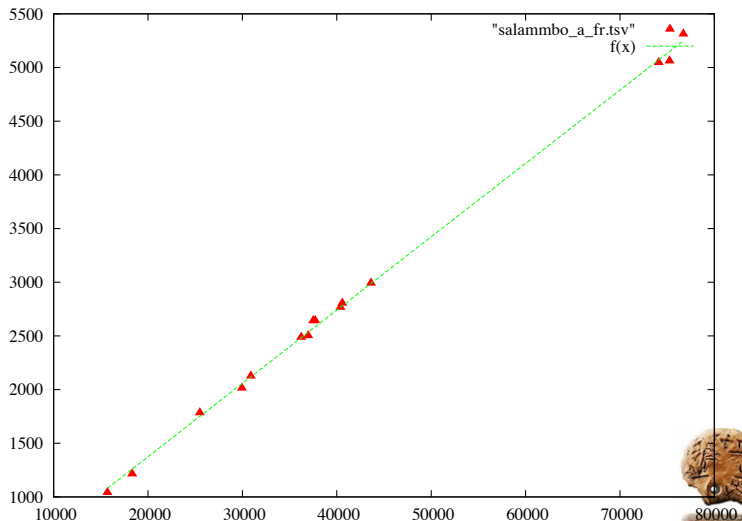
Letter counts from *Salammbo*

Chapter	French		English	
	# characters	# A	# characters	# A
Chapter 1	36,961	2,503	35,680	2,217
Chapter 2	43,621	2,992	42,514	2,761
Chapter 3	15,694	1,042	15,162	990
Chapter 4	36,231	2,487	35,298	2,274
Chapter 5	29,945	2,014	29,800	1,865
Chapter 6	40,588	2,805	40,255	2,606
Chapter 7	75,255	5,062	74,532	4,805
Chapter 8	37,709	2,643	37,464	2,396
Chapter 9	30,899	2,126	31,030	1,993
Chapter 10	25,486	1,784	24,843	1,627
Chapter 11	37,497	2,641	36,172	2,375
Chapter 12	40,398	2,766	39,552	2,560
Chapter 13	74,105	5,047	72,545	4,597
Chapter 14	76,725	5,312	75,352	4,871
Chapter 15	18,317	1,215	18,031	1,119



Supervised Learning: Regression

Letter count from *Salammbô* in French



Models

We will assume that data sets are governed by functions or models.
For instance given the set:

$$\{(\mathbf{x}_i, y_i) | 0 < i \leq N\},$$

there exists a function such that:

$$f(\mathbf{x}_i) = y_i.$$

Supervised machine learning algorithms will produce hypothesized functions or models fitting the data.



Notations

We will follow these notations:

- \mathbf{x} , the vector representing an observation (or sample, or example, or input);
in *Salammô*, an observation is the number of letters in a chapter. We have 15 observations;
- y , the observed response (or target, or output); in programs, the variable names are `y` or `y_true`;
in *Salammô*, the number of As in a chapter. We have 15 responses;
- \hat{y} , the value predicted by the model; in programs, the variable names are `y_pred` or `y_hat`;
- \mathbf{w} , the weights or parameters of the model, so that $\mathbf{w} \cdot \mathbf{x} = \hat{y}$;
another possible notation for \mathbf{w} is β
- X , the matrix of all the observations
- \mathbf{y} , the vector of all the responses and $\hat{\mathbf{y}}$, for all the predictions



Selecting a Model

Often, multiple models can fit a data set:

Three polynomials of degree: 1, a straight line, 8, and 9 to fit the *Salammbo* dataset.



A general rule in machine learning is to prefer the simplest hypotheses, here the lower polynomial degrees. Otherwise, the model can **overfit** the data.

In our case, the optimal model \mathbf{w} has two parameters: (w_0, w_1) .



Loss or Objective Function

What are the optimal values of \mathbf{w} ?

The model should minimize the difference between:

- the predicted values $\hat{\mathbf{y}}$ and
- the observed values \mathbf{y} .

This is called the **loss**

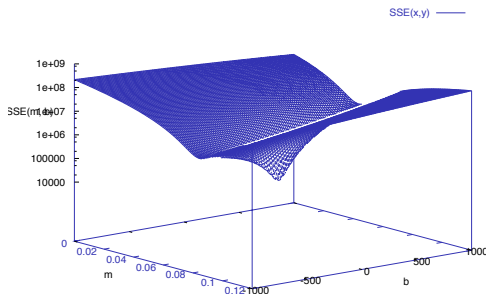
For *Salambô*, the loss is the *mean of the squared errors* (MSE):

$$\frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2$$



Visualizing the Loss

$$\hat{y} = mx + b$$



We will use the notation

$$\hat{y} = w_1 x + w_0$$

to generalize to any dimension



The Matrices

$$X = \begin{bmatrix} 1 & 36961 \\ 1 & 43621 \\ 1 & 15694 \\ 1 & 36231 \\ 1 & 29945 \\ 1 & 40588 \\ 1 & 75255 \\ 1 & 37709 \\ 1 & 30899 \\ 1 & 25486 \\ 1 & 37497 \\ 1 & 40398 \\ 1 & 74105 \\ 1 & 76725 \\ 1 & 18317 \end{bmatrix} ; \mathbf{w} = \begin{bmatrix} 8.7253 \\ 0.0683 \end{bmatrix} ; \mathbf{y} = \begin{bmatrix} 2533.22 \\ 2988.11 \\ 1080.65 \\ 2483.36 \\ 2054.02 \\ 2780.95 \\ 5148.76 \\ 2584.31 \\ 2119.18 \\ 1749.46 \\ 2569.83 \\ 2767.97 \\ 5070.21 \\ 5249.16 \\ 1259.81 \end{bmatrix} ; \mathbf{y} = \begin{bmatrix} 2503 \\ 2992 \\ 1042 \\ 2487 \\ 2014 \\ 2805 \\ 5062 \\ 2643 \\ 2126 \\ 1784 \\ 2641 \\ 2766 \\ 5047 \\ 5312 \\ 1215 \end{bmatrix} ; \mathbf{se} = \begin{bmatrix} 913.26 \\ 15.14 \\ 1493.86 \\ 13.25 \\ 1601.31 \\ 578.40 \\ 7527.51 \\ 3444.53 \\ 46.57 \\ 1193.04 \\ 5065.18 \\ 38920 \\ 538.909 \\ 3948.29 \\ 2603.53 \end{bmatrix} .$$



Minimizing the Loss

The loss function is convex and has a unique minimum.

The loss reaches a minimum when the partial derivatives are zero:

$$\begin{aligned}\frac{\partial \text{Loss}}{\partial m} &= \sum_{i=1}^q \frac{\partial}{\partial m} (y_i - (mx_i + b))^2 = -2 \sum_{i=1}^q x_i (y_i - (mx_i + b)) = 0 \\ \frac{\partial \text{Loss}}{\partial b} &= \sum_{i=1}^q \frac{\partial}{\partial b} (y_i - (mx_i + b))^2 = -2 \sum_{i=1}^q (y_i - (mx_i + b)) = 0\end{aligned}$$



The Gradient Descent

The gradient descent is a numerical method to find the minimum of $f(w_0, w_1, w_2, \dots, w_n) = y$, when there is no analytical solution.

Let us denote $\mathbf{w} = (w_0, w_1, w_2, \dots, w_n)$

We derive successive approximations to find the minimum of f :

$$f(\mathbf{w}_1) > f(\mathbf{w}_2) > \dots > f(\mathbf{w}_k) > f(\mathbf{w}_{k+1}) > \dots > \min$$

Points in the neighborhood of \mathbf{w} are defined by $\mathbf{w} + \mathbf{v}$ with $\|\mathbf{v}\|$ small

Given \mathbf{w} , find \mathbf{v} subject to $f(\mathbf{w}) > f(\mathbf{w} + \mathbf{v})$



The Gradient Descent (Cauchy, 1847)

Using a Taylor expansion: $f(\mathbf{w} + \mathbf{v}) = f(\mathbf{w}) + \mathbf{v} \cdot \nabla f(\mathbf{w}) + \dots$

The gradient is a direction vector corresponding to the steepest slope:

$$\nabla f(w_0, w_1, w_2, \dots, w_n) = \left(\frac{\partial f}{\partial w_0}, \frac{\partial f}{\partial w_1}, \frac{\partial f}{\partial w_2}, \dots, \frac{\partial f}{\partial w_n} \right).$$

$f(\mathbf{w} + \mathbf{v})$ reaches a minimum or a maximum when \mathbf{v} and $\nabla f(\mathbf{w})$ are colinear:

- Steepest ascent: $\mathbf{v} = \alpha \nabla f(\mathbf{w})$,
- Steepest descent: $\mathbf{v} = -\alpha \nabla f(\mathbf{w})$,

where $\alpha > 0$.

We have then: $f(\mathbf{w} - \alpha \nabla f(\mathbf{w})) \approx f(\mathbf{w}) - \alpha \|\nabla f(\mathbf{w})\|^2$.

The inequality:

$$f(\mathbf{w}) > f(\mathbf{w} - \alpha \nabla f(\mathbf{w}))$$

enables us to move one step down to the minimum.

We then use the iteration:

$$\mathbf{w}_{k+1} = \mathbf{w}_k - \alpha_k \nabla f(\mathbf{w}_k).$$



Classification Dataset

A binary classification.

	# char.	# A	class (y)	# char.	# A	class (y)
Chapter 1	36,961	2,503	1	35,680	2,217	0
Chapter 2	43,621	2,992	1	42,514	2,761	0
Chapter 3	15,694	1,042	1	15,162	990	0
Chapter 4	36,231	2,487	1	35,298	2,274	0
Chapter 5	29,945	2,014	1	29,800	1,865	0
Chapter 6	40,588	2,805	1	40,255	2,606	0
Chapter 7	75,255	5,062	1	74,532	4,805	0
Chapter 8	37,709	2,643	1	37,464	2,396	0
Chapter 9	30,899	2,126	1	31,030	1,993	0
Chapter 10	25,486	1,784	1	24,843	1,627	0
Chapter 11	37,497	2,641	1	36,172	2,375	0
Chapter 12	40,398	2,766	1	39,552	2,560	0
Chapter 13	74,105	5,047	1	72,545	4,597	0
Chapter 14	76,725	5,312	1	75,352	4,871	0
Chapter 15	18,317	1,215	1	18,031	1,119	0



Separating Classes



Given the data set, $\{(\mathbf{x}_i, y_i) | 0 < i \leq N\}$ and a model f :

- Classification: $f(\mathbf{x}) = y$ is discrete,
- Regression: $f(\mathbf{x}) = y$ is continuous.



Supervised Machine-Learning Algorithms

Linear classifiers:

- 1 Perceptron
- 2 Logistic regression
- 3 Neural networks (with many flavors)



Classification

We represent classification using a threshold function (a variant of the signum function):

$$H(\mathbf{w} \cdot \mathbf{x}) = \begin{cases} 1 & \text{if } \mathbf{w} \cdot \mathbf{x} \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

The classification function associates P with 1 and N with 0.
We want to find the separating hyperplane:

$$\begin{aligned} \hat{y}(\mathbf{x}) &= H(\mathbf{w} \cdot \mathbf{x}) \\ &= H(w_0 + w_1x_1 + w_2x_2 + \dots + w_nx_n), \end{aligned}$$

given a data set of q examples: $DS = \{(1, x_1^j, x_2^j, \dots, x_n^j, y^j) | j : 1..q\}$.

We use $x_0 = 1$ to simplify the equations.

For a binary classifier, y has then two possible values $\{0, 1\}$ corresponding in our example to $\{\text{French, English}\}$.



Berkson's Data Set (1944)

Drug concentration	Number exposed	Survive Class 0	Die Class 1	Mortality rate	Expected mortality
40	462	352	110	.2359	.2206
60	500	301	199	.3980	.4339
80	467	169	298	.6380	.6085
100	515	145	370	.7184	.7291
120	561	102	459	.8182	.8081
140	469	69	400	.8529	.8601
160	550	55	495	.9000	.8952
180	542	43	499	.9207	.9195
200	479	29	450	.9395	.9366
250	497	21	476	.9577	.9624
300	453	11	442	.9757	.9756

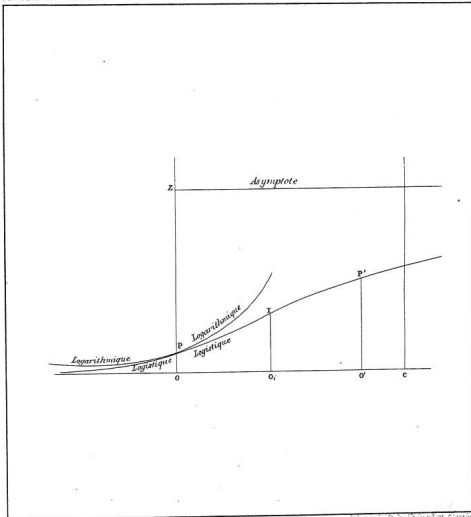
Table: A data set. Adapted and simplified from the original article that described how to apply logistic regression to classification by Joseph Berkson, Application of the Logistic Function to Bio-Assay. *Journal of the American Statistical Association* (1944).



Another Model, the Logistic Curve (Verhulst)

Mémoires de l'Académie.

Tome XVIII.



Mémoire sur la population par M. P. Verhulst.

$$\text{Logistic}(x) = \frac{1}{1 + e^{-x}}$$

$$\begin{aligned} \hat{y}(\mathbf{x}) &= \text{Logistic}(\mathbf{w} \cdot \mathbf{x}) \\ &= \frac{1}{1 + e^{-\mathbf{w} \cdot \mathbf{x}}} \end{aligned}$$



Loss: Binary Cross Entropy

In practice, we use the mean and the natural logarithm:

$$H(P, M) = -\frac{1}{|X|} \sum_{x \in X} P(x) \log M(x),$$

where P is the truth, and M is the prediction of the model, a probability in the case of logistic regression.

In binary classification:

- $P(x) = 1$
- $M(x)$ is the predicted probability of being class 1.
- If the observation belongs to class 0, its predicted probability is $1 - M(x)$.



Example of Cross Entropy

Computing the cross-entropy of six observations:

Observations	1	2	3	4	5	6
Dose	140	300	140	160	140	250
Observed class (Truth)	0	1	1	1	1	1
Model prediction of being class 1	0.3487	0.9964	0.8557	0.9056	0.8557	0.9882
Model prediction of being class 0	0.6513					
$-P(x)\log M(x)$:	0.4287	0.0036	0.1559	0.0992	0.1559	0.0119

Mean = 0.14252826



Code Example: Logistic Regression with sklearn

Experiment: Jupyter Notebook: `ch07_salammbo_dataset.ipynb`



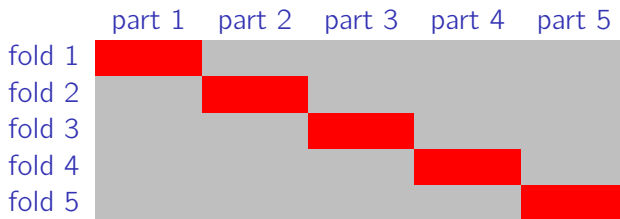
Evaluation

- The standard evaluation procedure is to train the classifier on a training set and evaluate the performance on a test set.
- When we have only one set, we divide it in two subsets: the training set and the test set (or holdout data).
- The split can be 90–10 or 80–20
- This often optimizes the classifier for a specific test set and creates an overfit



Cross Validation

- A N -fold cross validation mitigates the overfit
- The set is partitioned into N subsets, $N = 5$ for example, one of them being the test set (red) and the rest the training set (gray).
- The process is repeated N times with a different test set: N folds



At the extreme, leave-one-out cross-validation

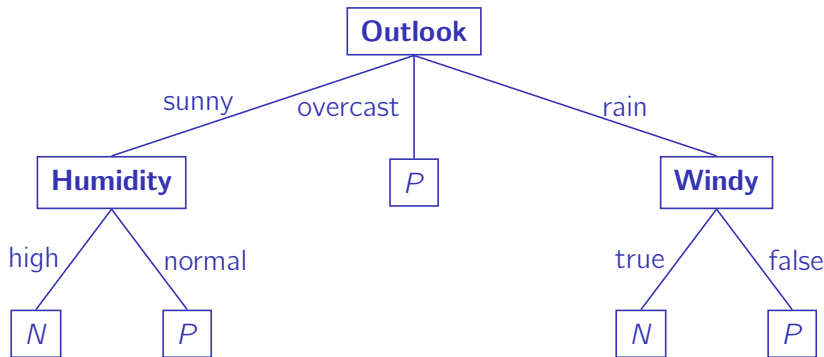


Objects, Attributes, and Classes. After Quinlan (1986)

Object	Attributes				Class
	Outlook	Temperature	Humidity	Windy	
1	Sunny	Hot	High	False	N
2	Sunny	Hot	High	True	N
3	Overcast	Hot	High	False	P
4	Rain	Mild	High	False	P
5	Rain	Cool	Normal	False	P
6	Rain	Cool	Normal	True	N
7	Overcast	Cool	Normal	True	P
8	Sunny	Mild	High	False	N
9	Sunny	Cool	Normal	False	P
10	Rain	Mild	Normal	False	P
11	Sunny	Mild	Normal	True	P
12	Overcast	Mild	High	True	P
13	Overcast	Hot	Normal	False	P
14	Rain	Mild	High	True	N



Classifying Objects with Decision Trees. After Quinlan (1986)



Matrix Notation

- A feature vector (predictors): \mathbf{x} , and feature matrix: X ;
- The class: y and the class vector: \mathbf{y} ;
- The predicted class (response): \hat{y} , and predicted class vector: $\hat{\mathbf{y}}$

$$X = \begin{bmatrix} \text{Sunny} & \text{Hot} & \text{High} & \text{False} \\ \text{Sunny} & \text{Hot} & \text{High} & \text{True} \\ \text{Overcast} & \text{Hot} & \text{High} & \text{False} \\ \text{Rain} & \text{Mild} & \text{High} & \text{False} \\ \text{Rain} & \text{Cool} & \text{Normal} & \text{False} \\ \text{Rain} & \text{Cool} & \text{Normal} & \text{True} \\ \text{Overcast} & \text{Cool} & \text{Normal} & \text{True} \\ \text{Sunny} & \text{Mild} & \text{High} & \text{False} \\ \text{Sunny} & \text{Cool} & \text{Normal} & \text{False} \\ \text{Rain} & \text{Mild} & \text{Normal} & \text{False} \\ \text{Sunny} & \text{Mild} & \text{Normal} & \text{True} \\ \text{Overcast} & \text{Mild} & \text{High} & \text{True} \\ \text{Overcast} & \text{Hot} & \text{Normal} & \text{False} \\ \text{Rain} & \text{Mild} & \text{High} & \text{True} \end{bmatrix}; \mathbf{y} = \begin{bmatrix} \text{N} \\ \text{N} \\ \text{P} \\ \text{P} \\ \text{P} \\ \text{N} \\ \text{P} \\ \text{N} \\ \text{P} \\ \text{P} \\ \text{P} \\ \text{P} \\ \text{P} \\ \text{N} \end{bmatrix}$$



Converting Symbolic Attributes into Numerical Vectors

Linear classifiers are numerical systems.

Symbolic – nominal – attributes are mapped onto vectors of binary values.

A conversion of the weather data set.

Object	Attributes										Class
	Outlook			Temperature			Humidity		Windy		
	Sunny	Overcast	Rain	Hot	Mild	Cool	High	Normal	True	False	
1	1	0	0	1	0	0	1	0	0	1	N
2	1	0	0	1	0	0	1	0	1	0	N
3	0	1	0	1	0	0	1	0	0	1	P
4	0	0	1	0	1	0	1	0	0	1	P
5	0	0	1	0	0	1	0	1	0	1	P
6	0	0	1	0	0	1	0	1	1	0	N
7	0	1	0	0	0	1	0	1	1	0	P
8	1	0	0	0	1	0	1	0	0	1	N
9	1	0	0	0	0	1	0	1	0	1	P
10	0	0	1	0	1	0	0	1	0	1	P
11	1	0	0	0	1	0	0	1	1	0	P
12	0	1	0	0	1	0	1	0	1	0	P
13	0	1	0	1	0	0	0	1	0	1	P
14	0	0	1	0	1	0	1	0	1	0	N



Code Example: Categorical Data with sklearn

Experiment: Jupyter Notebook: `ch07_quinlan_dataset.ipynb`



More than two Classes: Types of Iris



Iris virginica



Iris setosa



Iris versicolor

Courtesy Wikipedia



Supervised Learning: Fisher's Iris data set (1936)

180 MULTIPLE MEASUREMENTS IN TAXONOMIC PROBLEMS

Table I

<i>Iris setosa</i>				<i>Iris versicolor</i>				<i>Iris virginica</i>			
Sepal length	Sepal width	Petal length	Petal width	Sepal length	Sepal width	Petal length	Petal width	Sepal length	Sepal width	Petal length	Petal width
5.1	3.5	1.4	0.2	7.0	3.2	4.7	1.4	6.3	3.3	6.0	2.5
4.9	3.0	1.4	0.2	6.4	3.2	4.5	1.5	5.8	2.7	5.1	1.9
4.7	3.2	1.3	0.2	6.9	3.1	4.9	1.5	7.1	3.0	5.9	2.1
4.6	3.1	1.5	0.2	5.5	2.3	4.0	1.3	6.3	2.9	5.6	1.8
5.0	3.6	1.4	0.2	6.5	2.8	4.6	1.5	6.5	3.0	5.8	2.2
5.4	3.9	1.7	0.4	5.7	2.8	4.5	1.3	7.6	3.0	6.6	2.1
4.6	3.4	1.4	0.3	6.3	3.3	4.7	1.6	4.9	2.5	4.5	1.7
5.0	3.4	1.5	0.2	4.9	2.4	3.3	1.0	7.3	2.9	6.3	1.8
4.4	2.9	1.4	0.2	6.6	2.9	4.6	1.3	6.7	2.5	5.8	1.8
4.9	3.1	1.5	0.1	5.2	2.7	3.9	1.4	7.2	3.6	6.1	2.5
5.4	3.7	1.5	0.2	5.0	2.0	3.5	1.0	6.5	3.2	5.1	2.0
4.8	3.4	1.6	0.2	5.9	3.0	4.2	1.5	6.4	2.7	5.3	1.9
4.8	3.0	1.4	0.1	6.0	2.2	4.0	1.0	6.8	3.0	5.5	2.1
4.3	3.0	1.1	0.1	6.1	2.9	4.7	1.4	5.7	2.5	5.0	2.0
5.8	4.0	1.2	0.2	5.6	2.9	3.6	1.3	5.8	2.8	5.1	2.4
5.7	4.4	1.5	0.4	6.7	3.1	4.4	1.4	6.4	3.2	5.3	2.3
5.4	3.9	1.3	0.4	5.6	3.0	4.5	1.5	6.5	3.0	5.5	1.8
5.1	3.5	1.4	0.3	5.8	2.7	4.1	1.0	7.7	3.8	6.7	2.2
5.7	3.8	1.7	0.3	6.2	2.2	4.5	1.5	7.7	2.6	6.9	2.3
5.1	3.8	1.5	0.3	5.6	2.5	3.9	1.1	6.0	2.2	5.0	1.5
5.4	3.4	1.7	0.2	5.9	3.2	4.8	1.8	6.9	3.2	5.7	2.3
5.1	3.7	1.5	0.4	6.1	2.8	4.0	1.3	5.6	2.8	4.9	2.0

Multiple Categories

We can generalize logistic regression to multiple categories.
We use then the *softmax* function:

$$P(y = i|\mathbf{x}) = \frac{e^{\mathbf{w}_i \cdot \mathbf{x}}}{\sum_{j=1}^C e^{\mathbf{w}_j \cdot \mathbf{x}}},$$

that defines the probability of an observation represented by \mathbf{x} to belong to class i .

Again, we use stochastic gradient descent to compute the weights: \mathbf{w} .

Note: In physics, *softmax* is defined as:

$$P(y = i|\mathbf{x}) = \frac{e^{-\mathbf{w}_i \cdot \mathbf{x}}}{\sum_{j=1}^C e^{-\mathbf{w}_j \cdot \mathbf{x}}},$$

See the Boltzmann distribution

https://en.wikipedia.org/wiki/Boltzmann_distribution



Representing y

In Keras, the default representation of y and \hat{y} are vectors (as opposed to sklearn)

y is an indicator vector (one-hot) and \hat{y} , a probability distribution

```
y[:5]
```

```
> array([2, 1, 0, 2, 0])
```

```
from tensorflow.keras.utils import to_categorical
```

```
Y_cat = to_categorical(y)
```

```
Y_cat[:5]
```

```
> array([[0., 0., 1.],  
        [0., 1., 0.],  
        [1., 0., 0.],  
        [0., 0., 1.],  
        [1., 0., 0.]], dtype=float32)
```



A complete example

The original categories:

```
y[121:126]
[2 0 0 2 0]
```

The encoded categories:

```
Y_cat[121:126]
[[0. 0. 1.]
 [1. 0. 0.]
 [1. 0. 0.]
 [0. 0. 1.]
 [1. 0. 0.]]
```

The predicted probabilities:

```
model.predict(X[121:126])
[[9.4238410e-12 2.8314255e-03 9.9716860e-01]
 [9.9939132e-01 6.0863607e-04 2.5036247e-11]
 [9.9859804e-01 1.4019267e-03 3.5701425e-10]
 [1.2004078e-09 2.8088816e-02 9.7191113e-01]
 [9.9938595e-01 6.1400887e-04 2.7445022e-11]]
```

The predicted classes:

```
list(map(np.argmax, model.predict(X[121:126])))
[2, 0, 0, 2, 0]
```

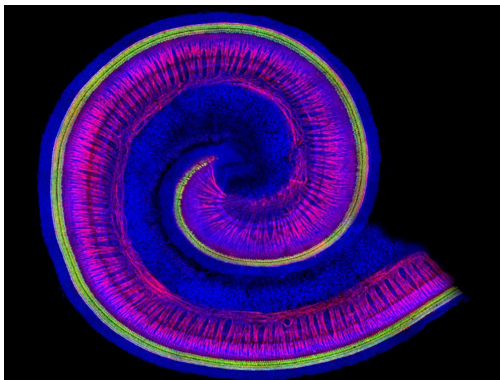
The loss, probability of the truth.

$$-\frac{1}{N}(\log(9.9716860 \cdot 10^{-1}) + \log(9.9939132 \cdot 10^{-1}) + \log(9.9859804 \cdot 10^{-1}) + \dots)$$

In the example, the prediction is also the truth. This is not always the case.



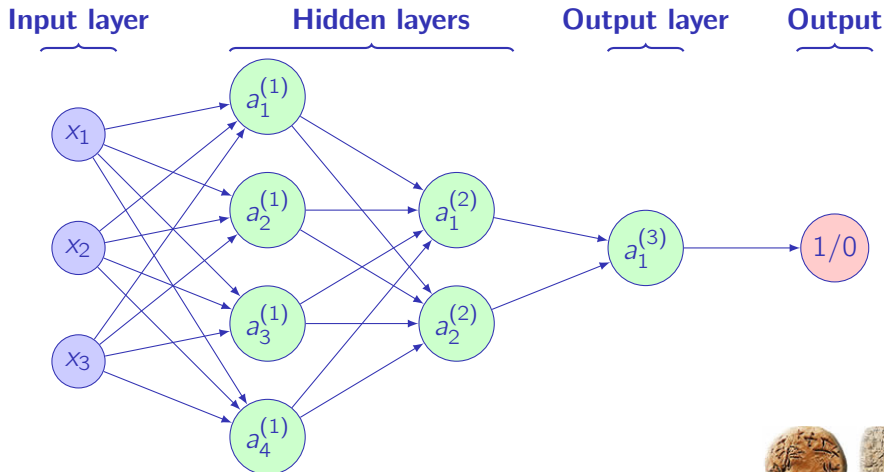
Neural Networks



A photomicrograph showing the classic view of the snail-shaped cochlea with hair cells stained green and neurons showing reddish-purple. [Decibel Therapeutics (<https://www.decibeltx.com>)]. Source: <https://www.genengnews.com/insights/targeting-the-inner-ear/>

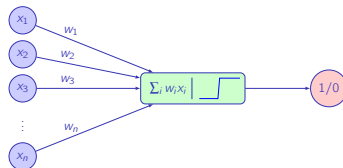


Neural Networks: Computer Model

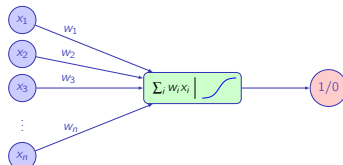


Activation Functions

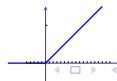
Heaviside (perceptron)



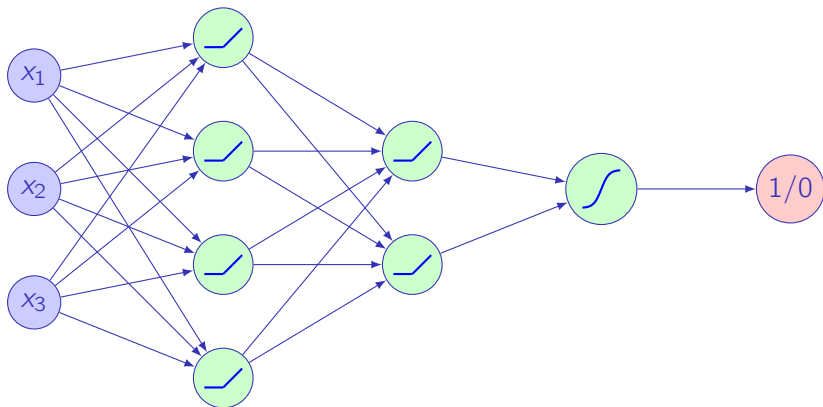
Logistic function (logistic regression)



Rectified linear unit (ReLU) (hidden layers)



Neural Networks with Hidden Layers



Code Example: Binary Classification with Keras and PyTorch

For binary classification, we use binary cross entropy

Experiment 1, Keras: Jupyter Notebook:

https://github.com/pnugues/ilppp/blob/master/programs/ch04/keras/Salamambo_keras.ipynb

Experiment 1, PyTorch: Jupyter Notebook:

[ch07_Salamambo_torch.ipynb](#)



Code Example: Multinomial Classification with Keras and PyTorch

For multinomial (multiclass) classification, we use (categorical) cross entropy

Experiment 2, Keras: Jupyter Notebook:

https://github.com/pnugues/ilppp/blob/master/programs/ch04/keras/Salamambo_multi_keras.ipynb

Experiment 2, PyTorch: Jupyter Notebook:

[ch07_Salamambo_multi_torch.ipynb](https://github.com/pnugues/ilppp/blob/master/programs/ch07/Salamambo_multi_torch.ipynb)



Last Activation Layer in PyTorch

There is a discrepancy in the activation of the last layer in PyTorch between binary and multiclass output

See the reasons here:

- 1 <https://pytorch.org/docs/stable/generated/torch.nn.BCELoss.html>
- 2 <https://pytorch.org/docs/stable/generated/torch.nn.CrossEntropyLoss.html>
- 3 <https://pytorch.org/docs/stable/generated/torch.nn.BCEWithLogitsLoss.html>
- 4 <https://blog.feedly.com/tricks-of-the-trade-logsumexp/>



Model Selection

- Validation can apply to one classification method
- We can use it to select a classification method and its parametrization.
- Needs three sets: training set, development set, and test set.



Evaluation

There are different kinds of measures to evaluate the performance of machine learning techniques, for instance:

- Precision and recall in information retrieval and natural language processing;
- The *receiver operating characteristic* (ROC) in medicine.

	Positive examples: P	Negative examples: N
Classified as P	True positives: A	False positives: B
Classified as N	False negatives: C	True negatives: D

More on the receiver operating characteristic here: http://en.wikipedia.org/wiki/Receiver_operating_characteristic



Recall, Precision, and the F-Measure

The **accuracy** is $\frac{|AUD|}{|PUN|}$.

Recall measures how much relevant examples the system has classified correctly, for P :

$$\text{Recall} = \frac{|A|}{|A \cup C|}.$$

Precision is the accuracy of what has been returned, for P :

$$\text{Precision} = \frac{|A|}{|A \cup B|}.$$

Recall and precision are combined into the **F-measure**, which is defined as the harmonic mean of both numbers:

$$F = \frac{2 \cdot \text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}.$$



Measuring Quality: The Confusion Matrix

A task in natural language processing: Identify the parts of speech (POS) of words.

Example: *The can rusted*

- The human: *The*/art (DT) *can*/noun (NN) *rusted*/verb (VBD)
- The POS tagger: *The*/art (DT) *can*/modal (MD) *rusted*/verb (VBD)

↓Correct	Tagger →									
	DT	IN	JJ	NN	RB	RP	VB	VBD	VBG	VCN
DT	99.4	0.3	–	–	0.3	–	–	–	–	–
IN	0.4	97.5	–	–	1.5	0.5	–	–	–	–
JJ	–	0.1	93.9	1.8	0.9	–	0.1	0.1	0.4	1.5
NN	–	–	2.2	95.5	–	–	0.2	–	0.4	–
RB	0.2	2.4	2.2	0.6	93.2	1.2	–	–	–	–
RP	–	24.7	–	1.1	12.6	61.5	–	–	–	–
VB	–	–	0.3	1.4	–	–	96.0	–	–	0.2
VBD	–	–	0.3	–	–	–	–	94.6	–	4.8
VBG	–	–	2.5	4.4	–	–	–	–	93.0	–
VCN	–	–	4.6	–	–	–	–	4.3	–	90.6

After Franz (1996, p. 124)