

Qr. Describe 5 hashing strategies/functions, what are different types of hash resolution techniques.
Answer

Introduction to Hashing

Hashing is a fundamental technique in Computer Science that transforms data into fixed-size hash values, enabling efficient data retrieval & storage. It is widely used in applications such as data indexing, Password Storage, & ensuring data integrity. Hashing functions assign unique identifiers to data, facilitating quick access & retrieval in various algorithms & data structures.

Hashing strategies/functions :

1 Division Hashing

This simple hashing strategy involves dividing the key by a Prime number & using the remainder as hash value.

Example If key is 54 & divisor is 11, hash value would be 10.

2 Multiplicative Hashing

Multiply key by constant A in range $(0, 1)$ & extract the fractional part of the product. Then, multiply this fraction part by the size of hash table to get hash value.

Example With key 27, Constant $A = 0.618$, & hash table size 100, hash value is $\text{floor}(\frac{27 \times 0.618}{1 \times 100}) = 1$

3 Universal Hashing

Use family of hash functions, randomly selecting one at runtime. This reduces the likelihood of collisions, improves overall performance.

Example If we have a family of hash function $H = \{h_1, h_2, h_3, \dots, h_n\}$, we randomly choose one function from family to hash the key.

4 SHA-256 (Secure Hash Algo 256-bit)

Part of SHA-256 family, this cryptographic hash function transforms input data into a fixed-size (256-bit) hash value, ensuring a secure & irreversible process.

Example For input "hello", SHA-256 generates the hash value
2424d6a5f60a30e26e8362ac569e29e
1b161e5c1fa7425e73c4336293e698247

5 Hash/City Hash

Developed by Google, Cityhash is designed for fast hashing of Short Character Strings.

It operates in multiple rounds with a variety of shifts & bitwise operations.

Given the input "example-string", City Hash produces the hash value "102067849232353369₆₄".

Hash Collision Resolution Techniques:

1 Chaining

In Chaining, each slot in the hash table maintains a linkedlist of elements that hash to same location. Collision are resolved by appending elements of list.

Example If two keys hash to same location, they are simply added to linkedlist at that position.

2 Open Addressing - Linear Probing

In linear Probing, if a collision occurs, the algorithm searches for next available slot linearly until an empty slot found.

Example If the initial hash index is occupied,

The algorithm checks next index & continues until an empty slot is found.

3 Double Hashing

Double Hashing involves using a secondary hash function to determine the interval between probe attempts, providing a more varied exploration of hash table.

Example If collision occurs at index H , double hashing might attempt to insert the key at indices $H+f(k)$, $H+2 \times f(k)$, $H+3 \times f(k)$ & so on.

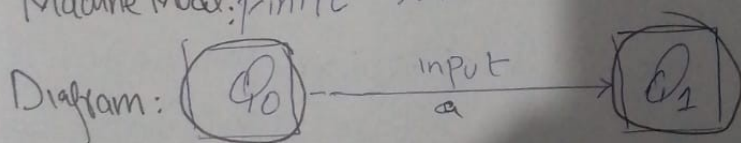
These hash collision resolution techniques show the diverse approaches employed in Computer Science to efficiently manage & ~~store~~ retrieval of data. Each method has its strengths & weaknesses, making it suitable for specific use cases & applications.

Q2 Write note of Chomsky hierarchy & mention what kind of machine will be used (make diagram of Turing machine used with each type of grammar in Chomsky hierarchy).

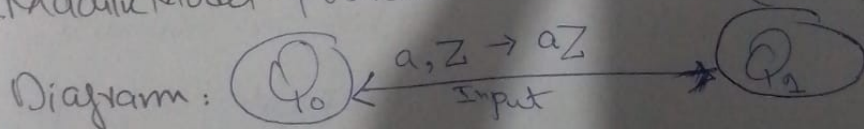
Answer

The Chomsky Hierarchy, Proposed by linguist & cognitive scientist Noam Chomsky, classifies formal grammar into four types based on their generative power. Each type corresponds to a different class of language, & various machine models, includes Turing machines, are associated with these grammatical types.

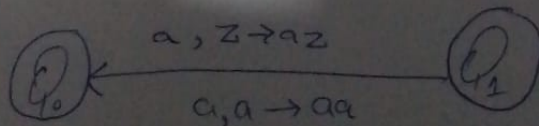
1 Type-3 - Regular Grammar (Regular language)
Machine Model: Finite State Machine (FSM)



2 Type 2 - Context-Free Grammar (Context-Free language)
Machine Model: Pushdown Automaton (PDA)

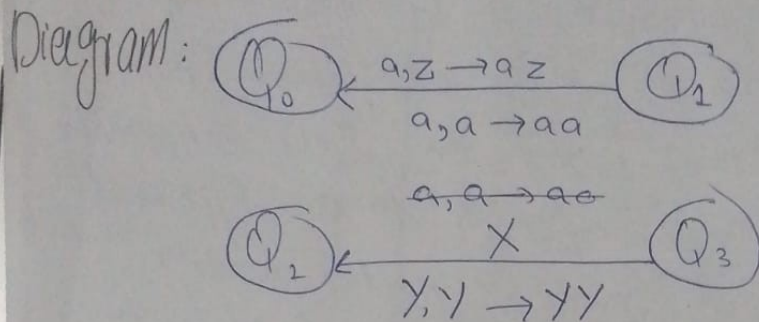


3 Type-1 Context Sensitive Grammar
Machine Model: Linear Bounded Automaton (LBA)



4 Type-0 Unrestricted Grammar (Recursively Enumerable languages)

Machine Model: Turing Machine (TM)



In Chomsky as we progress from Type-3 to type-0, the generative power of the grammar increases, & the associated machine models become more complex. Regular languages are recognized by finite state machines, Context free languages by Pushdown automata, Context Sensitive Languages by linear-bounded automata; & recursively enumerable languages by Turing machines.

These models represent the theoretical foundation for understanding the computational capacity of different types of formal languages.
