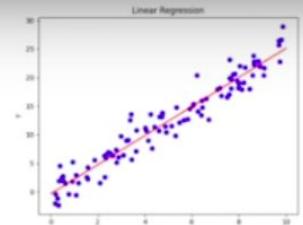


# Regression Metrics

## 1. Mean Absolute Error (MAE)



### Description:

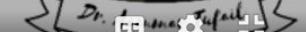
- MAE measures the **average magnitude** of the errors in a set of predictions, without considering their direction.
- It's the average over the test sample of the **absolute differences between prediction and actual observation** where all individual differences have equal weight.

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i|$$

**Interpretation:** Lower values are better. A value of 0 indicates no error.



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# 1. Mean Absolute Error (MAE)

$$MAE = \frac{1}{n} \sum \left| y - \hat{y} \right|$$

Divide by the total number of data points

Predicted output value

Actual output value

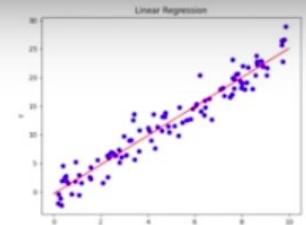
Sum of The absolute value of the residual

The diagram shows a single data point with an actual output value  $y$  (green box) and a predicted output value  $\hat{y}$  (orange box). The difference  $y - \hat{y}$  is taken, and its absolute value is calculated. This process is summed for all  $n$  data points and then divided by  $n$ .



# Regression Metrics

## 2. Mean Squared Error (MSE)



### Description:

- MSE measures the average of the squares of the errors—that is, the **average squared difference between the estimated values and the actual value**.

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

**Interpretation:** Like MAE, lower values are better. MSE is more sensitive to outliers than MAE.



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## 2. Mean Squared Error (MSE)

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

Mean      Error      Squared

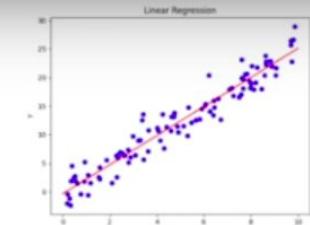


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# Regression Metrics

## 3. Root Mean Squared Error (RMSE)



### Description:

- RMSE is the square root of the **mean of the squared errors**. It's a way to quantify the size of the error made by the model.

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

**Interpretation:** Lower values indicate better fit. RMSE is more sensitive to outliers than MAE and often used when large errors are particularly undesirable.

# Regression Metrics

## 4. R-squared (Coefficient of Determination)

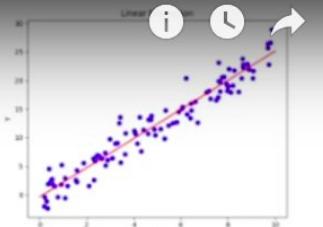
### Description:

- R-squared represents the proportion of the variance for the dependent variable that's explained by the independent variables in a regression model.

$$R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$$

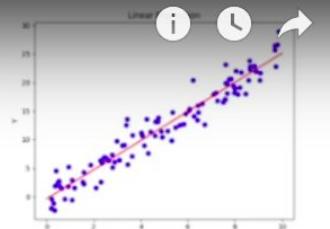
where  $\bar{y}$  is the mean of the observed data.

**Interpretation:** Values range from 0 to 1. A higher R-squared indicates a better fit between the model and the data.



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# Regression Metrics

## 5. Adjusted R-squared

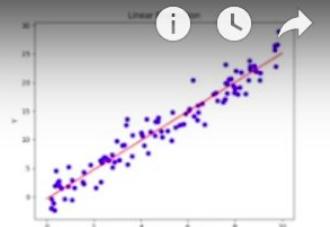
## Description:

- Adjusted R-squared is a modified version of R-squared that has been adjusted for the number of predictors in the model. It accounts for the model complexity.

$$\text{Adjusted } R^2 = 1 - (1 - R^2) \frac{n-1}{n-p-1}$$

where  $n$  is the number of observations and  $p$  is the number of predictors.

**Interpretation:** Compares the explanatory power of regression models that contain different numbers of predictors.



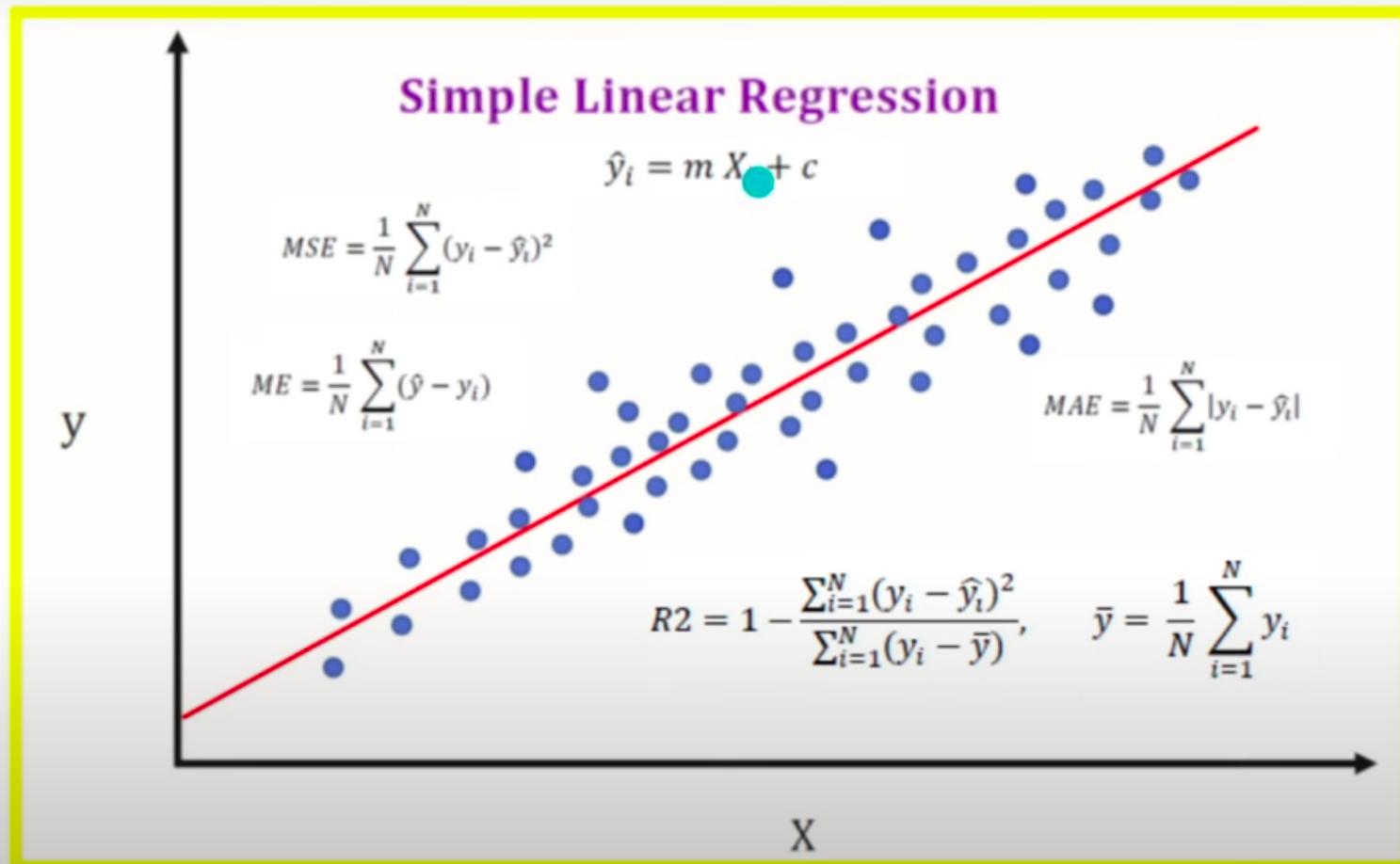
# Regression Metrics

## Choosing the Right Metric:

### Description:

- The choice of metric depends on the specific requirements of your **analysis** and the **nature of the data**.
- For instance, if you are more concerned about outliers, **MSE or RMSE** might be more appropriate.
- R-squared and Adjusted R-squared are useful for understanding the **proportion of variance explained by the model**, but they don't necessarily imply that the model is accurate.





Metric	Pros	Cons	Example
Mean Absolute Error (MAE)	Simple to understand; treats all errors equally	Less sensitive to outliers	For true values [3, -0.5, 2, 7] and predicted [2.5, 0.0, 2, 8], MAE is $(0.5 + 0.5 + 0 + 1)/4 = 0.5$
Mean Squared Error (MSE)	Punishes larger errors more severely	Can be disproportionately influenced by outliers	For the same true and predicted values, MSE is $[(0.5)^2 + (0.5)^2 + 0^2 + 1^2]/4 = 0.375$
Root Mean Squared Error (RMSE)	More interpretable in the original units of the output variable	More sensitive to outliers than MAE	For the same values, RMSE is $\sqrt{0.375} \approx 0.612$
R-squared (Coefficient of Determination)	Measures how well future samples are likely to be predicted	Does not indicate if a regression model is adequate	If the total sum of squares is 10 and the sum of squared errors is 2, $R^2$ is $1 - 2/10 = 0.8$
Adjusted R-squared	Adjusts for the number of predictors in the model	Can be more difficult to interpret	For an $R^2$ of 0.8, 100 observations, and 5 predictors, Adjusted $R^2$ is $1 - (1-0.8) * (100-1)/(100-5-1) = 0.793$
Mean Absolute Percentage Error (MAPE)	Provides error in terms of percentage, making it scale-independent	Can be infinite or undefined for $y_i = 0$	For true values [3, -0.5, 2, 7] and predicted [2.5, 0.0, 2, 8], MAPE is $[(0.5/3) + (0.5/0) + (1/2)] * 25\% \approx 43.57\%$

