

قوانين التكامل الغير محدد

$$① \int du = u + c$$

$$② \int a du = a \int du = a(u) + c$$

$$③ \int u(x) \mp v(x) dx = \int u(x) dx \mp \int v(x) dx$$

$$④ \int u^a du = \frac{u^{a+1}}{a+1} + c \quad \text{when } \int u^{-1} du = \int \frac{1}{u} du = \ln u + c$$

$$⑤ \int a^u du = \frac{a^u}{\ln a} + c \Rightarrow \int e^u du = e^u + c$$

$$⑥ \int \sin u du = -\cos u + c$$

(sin u dx = -1/2 cos u x)

$$⑦ \int \cos u du = \sin u + c$$

$$⑧ \int \sec^2 u du = \tan u + c$$

$$⑨ \int \csc^2 u du = -\cot u + c$$

$$⑩ \int \csc u \cdot \cot u du = -\csc u + c$$

$$⑪ \int \sec u \cdot \tan u du = \sec u + c$$

$$⑫ \int \tan u du = -\ln |\cos u| + c$$

$$⑬ \int \cot u du = \ln |\sin u| + c$$

$$⑭ \int \sec u du = \ln |\sec u + \tan u| + c$$

$$⑮ \int \csc u du = \ln |\csc u + \cot u| + c$$

السابع

$$⑯ \frac{du}{\sqrt{a^2 - u^2}} = \int \frac{du}{\sqrt{a^2 - u^2}} = \begin{cases} \sin^{-1} \frac{u}{a} + c & -u \\ -\cos^{-1} \frac{u}{a} + c \end{cases}$$

$$⑰ \frac{du}{a^2 + u^2} = \int \frac{du}{a^2 + u^2} = \begin{cases} \frac{1}{a} \tan^{-1} \frac{u}{a} + c \\ -\frac{1}{a} \cot^{-1} \frac{u}{a} + c \end{cases}$$

$$⑱ \frac{du}{|u| \sqrt{u^2 - a^2}} = \int \frac{du}{|u| \sqrt{u^2 - a^2}} = \begin{cases} \frac{1}{a} \sec^{-1} \frac{|u|}{a} + c \\ -\frac{1}{a} \csc^{-1} \frac{|u|}{a} + c \end{cases}$$

$$(19) \int \sinh u \, du = \cosh u + c$$

$$(20) \int \cosh u \, du = \sinh u + c$$

$$(21) \int \operatorname{sech}^2 u \, du = \tanh u + c$$

$$(22) \int \operatorname{csch}^2 u \, du = -\coth u + c$$

$$(23) \int \operatorname{sech} u \cdot \tanh u \, du = -\operatorname{sech} u + c$$

$$(24) \int \coth u \cdot \operatorname{csch} u \, du = -\operatorname{csch} u + c$$

$$(25) \int \tanh u = \ln |\cosh u| + c$$

$$(26) \int \coth u = \ln |\sinh u| + c$$

$$(27) \int \frac{du}{\sqrt{u^2+1}} = \sinh^{-1} u + c \quad \underbrace{(+1) \quad (-1)}$$

$$(28) \int \frac{du}{\sqrt{u^2-1}} = \cosh^{-1} u + c$$

$$(29) \int \frac{du}{u\sqrt{1-u^2}} = -\operatorname{sech}^{-1} u + c \quad \underbrace{(-u) \quad +u}$$

$$(30) \int \frac{du}{u\sqrt{1+u^2}} = -\operatorname{csch}^{-1} u + c$$

$(31) \frac{du}{1-u^2} =$	$\tanh^{-1} u + c$
	$\coth^{-1} u + c$

(Differentiation)

① ملحق L4 و L5
(مشتقات الدوال)

فيما يلي جدول بالمشتقات يوضح كل دالة ومشتقتها

Function $y = f(x)$	Derivative $\bar{y} = \frac{dy}{dx}$
$C = \text{Constant}$ ثابت	0
x	1
Cx	$C \cdot 1 = C$
x^n	$n x^{n-1}$
u^n	$n u^{n-1} \cdot \bar{u}$
$u \cdot v$	$u \cdot \bar{v} + v \cdot \bar{u}$
$\frac{u}{v}$	$\frac{v \cdot \bar{u} - u \cdot \bar{v}}{v^2}$
$\sin x$	$\cos x$
$\sin u$	$\cos u \cdot \bar{u}$
$\cos x$	$-\sin x$
$\cos u$	$-\sin u \cdot \bar{u}$
$\tan x$	$\frac{1}{\cos^2 x} = \sec^2 x$
$\tan u$	$\frac{1}{\cos^2 u} \cdot \bar{u} = \sec^2 u \cdot \bar{u}$
e^x	e^x
e^u	$e^u \cdot \bar{u}$
$\ln x$	$\frac{1}{x}$
$\ln u$	$\frac{1}{u} \cdot \bar{u}$
$\log_a x$	$\frac{1}{x} \cdot \log_a e$
$\log_a u$	$\frac{1}{u} \cdot \log_a e \cdot \bar{u}$
a^x	$a^x \cdot \ln a$
a^u	$a^u \cdot \ln a \cdot \bar{u}$

مشتقات الدوال المثلثية الأخرى

$\sec x$	$\sec x \cdot \tan x$
$\sec u$	$\sec u \cdot \tan u \cdot \bar{u}$
$\csc x$	$-\csc x \cdot \cot x$
$\csc u$	$-\csc u \cdot \cot u \cdot \bar{u}$
$\cot x$	$-\csc^2 x$
$\cot u$	$-\csc^2 u \cdot \bar{u}$

مشتقات الدوال المثلثية العكسية

$\sin^{-1} x$	$\frac{1}{\sqrt{1-x^2}}$	
$\sin^{-1} u$	$\frac{1}{\sqrt{1-u^2}} \cdot \bar{u}$	
$\cos^{-1} x$	$\frac{-1}{\sqrt{1-x^2}}$	
$\cos^{-1} u$	$\frac{-1}{\sqrt{1-u^2}} \cdot \bar{u}$	
$\tan^{-1} x$	$\frac{1}{1+x^2}$	
$\tan^{-1} u$	$\frac{1}{1+u^2} \cdot \bar{u}$	
$\cot^{-1} x$	$\frac{-1}{1+x^2}$	$\frac{1}{2x}$
$\cot^{-1} u$	$\frac{-1}{1+u^2} \cdot \bar{u}$	
$\sec^{-1} x$	$\frac{1}{x\sqrt{x^2-1}}$	
$\sec^{-1} u$	$\frac{1}{u\sqrt{u^2-1}} \cdot \bar{u}$	
$\csc^{-1} x$	$\frac{-1}{x\sqrt{x^2-1}}$	
$\csc^{-1} u$	$\frac{-1}{u\sqrt{u^2-1}} \cdot \bar{u}$	

hyperbolic fun. $\frac{d}{dx}$

$$\sinh x$$

$$\cosh x$$

$$\sinh u$$

$$\cosh u \cdot \bar{u}$$

$$\cosh x$$

$$\sinh x$$

$$\cosh u$$

$$\sinh u \cdot \bar{u}$$

$$\tanh x$$

$$\operatorname{sech}^2 x$$

$$\tanh u$$

$$\operatorname{sech}^2 u \cdot \bar{u}$$

$$\coth x$$

$$-\operatorname{csch}^2 x$$

$$\coth u$$

$$-\operatorname{csch}^2 u \cdot \bar{u}$$

$$\operatorname{sech} x$$

$$-\operatorname{sech} x \cdot \tanh x$$

$$\operatorname{sech} u$$

$$-\operatorname{sech} u \cdot \tanh u \cdot \bar{u}$$

$$\operatorname{csch} x$$

$$-\operatorname{csch} x \cdot \coth x$$

$$\operatorname{csch} u$$

$$-\operatorname{csch} u \cdot \coth u \cdot \bar{u}$$

hyper. fun. $\frac{d}{dx}$ $\frac{d}{du}$ $\frac{d}{d\bar{u}}$

$$\sinh^{-1} x$$

$$\frac{1}{\sqrt{1+x^2}}$$

$$\sinh^{-1} u$$

$$\frac{1}{\sqrt{1+u^2}} \cdot \bar{u}$$

$$\cosh^{-1} x$$

$$\frac{1}{\sqrt{x^2-1}}$$

$$(x > 1)$$

$$\cosh^{-1} u$$

$$\frac{1}{\sqrt{u^2-1}} \cdot \bar{u} \quad (u > 1)$$

$$\tanh^{-1} x$$

$$\frac{1}{1-x^2} \quad (|x| < 1 \text{ units})$$

$$\tanh^{-1} u$$

$$\frac{1}{1-u^2} \cdot \bar{u} \quad (|u| < 1)$$

$$\coth^{-1} x$$

$$\frac{1}{1-x^2} \quad (|x| > 1 \text{ units})$$

$$\coth^{-1} u$$

$$\frac{1}{1-u^2} \cdot \bar{u} \quad (|u| > 1)$$

$$\operatorname{sech}^{-1} x$$

$$\frac{-1}{x\sqrt{1-x^2}}$$

$$\operatorname{sech}^{-1} u$$

$$\frac{-1}{u\sqrt{1-u^2}} \cdot \bar{u}$$

$$\operatorname{csch}^{-1} x$$

$$\frac{-1}{|x|\sqrt{1+x^2}}$$

$$\operatorname{csch}^{-1} u$$

$$\frac{-1}{|u|\sqrt{1+u^2}} \cdot \bar{u}$$