

8-puzzle game

Overview:

An instance of the 8-puzzle game consists of a board holding 8 distinct movable tiles, plus an empty space. For any such board, the empty space may be legally swapped with any tile horizontally or vertically adjacent to it. In this assignment, the blank space is going to be represented with the number 0.

Objective:

Given an initial state of the board, the search problem is to find a sequence of moves that transitions this state to the goal state by applying three algorithms : BFS , DFS and A*;

The search space is the set of all possible states reachable from the initial state. The blank space may be swapped with a component in one of the four directions 'Up', 'Down', 'Left', 'Right', one move at a time. The cost of moving from one configuration of the board to another is the same and equal to one. Thus, the total cost of path is equal to the number of moves made from the initial state to the goal state.

Algorithms:

BFS search

```
function BREADTH-FIRST-SEARCH(initialState, goalTest)
    returns SUCCESS or FAILURE :

    frontier = Queue.new(initialState)
    explored = Set.new()

    while not frontier.isEmpty():
        state = frontier.dequeue()
        explored.add(state)

        if goalTest(state):
            return SUCCESS(state)

        for neighbor in state.neighbors():
            if neighbor not in frontier ∪ explored:
                frontier.enqueue(neighbor)

    return FAILURE
```

DFS search

```
function DEPTH-FIRST-SEARCH(initialState, goalTest)
    returns SUCCESS or FAILURE :

    frontier = Stack.new(initialState)
    explored = Set.new()

    while not frontier.isEmpty():
        state = frontier.pop()
        explored.add(state)

        if goalTest(state):
            return SUCCESS(state)

        for neighbor in state.neighbors():
            if neighbor not in frontier  $\cup$  explored:
                frontier.push(neighbor)

    return FAILURE
```

Taken from the edX course ColumbiaX: CSMM101x Artificial Intelligence (AI)

A* search

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```
function A-STAR-SEARCH(initialState, goalTest)
    returns SUCCESS or FAILURE : /* Cost  $f(n) = g(n) + h(n)$  */

    frontier = Heap.new(initialState)
    explored = Set.new()

    while not frontier.isEmpty():
        state = frontier.deleteMin()
        explored.add(state)

        if goalTest(state):
            return SUCCESS(state)

        for neighbor in state.neighbors():
            if neighbor not in frontier  $\cup$  explored:
                frontier.insert(neighbor)
            else if neighbor in frontier:
                frontier.decreaseKey(neighbor)

    return FAILURE
```

Data Structures Used:

Queue

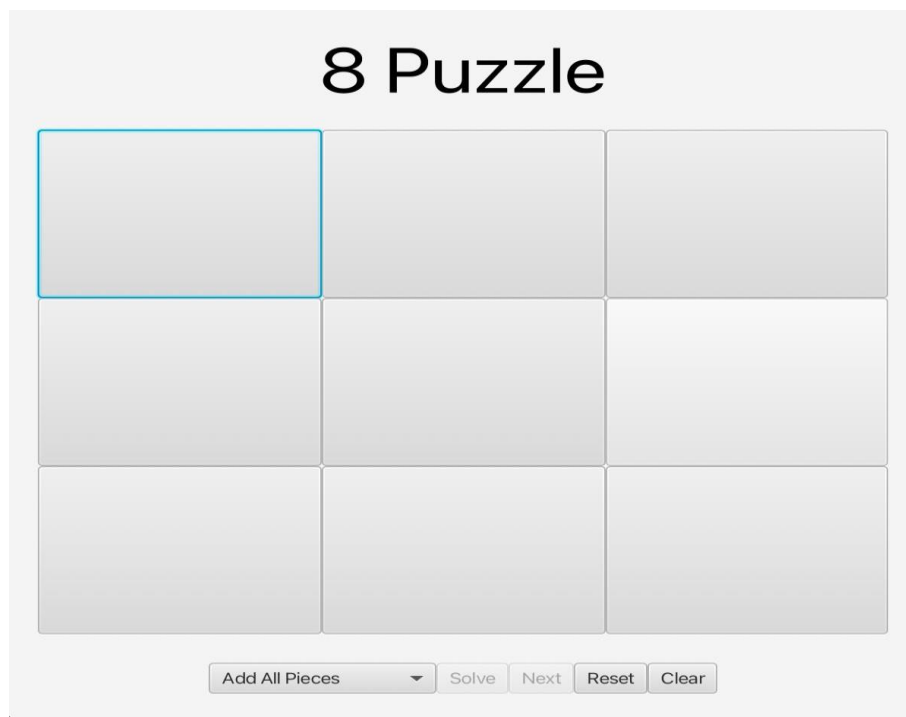
Priority queue

Hash map

Stack

ArrayList

Test Cases:



8 Puzzle

1	2	5
3	4	
6	7	8

Select an algorithm ▼ Solve Next Reset Clear

8 Puzzle

1		2
3	4	5
6	7	8

BFS ▼ Solve Next Reset Clear

8 Puzzle

1		2
3	4	5
6	7	8

BFS ▼ Solve Next Reset Clear

8 Puzzle

	1	2
3	4	5
6	7	8

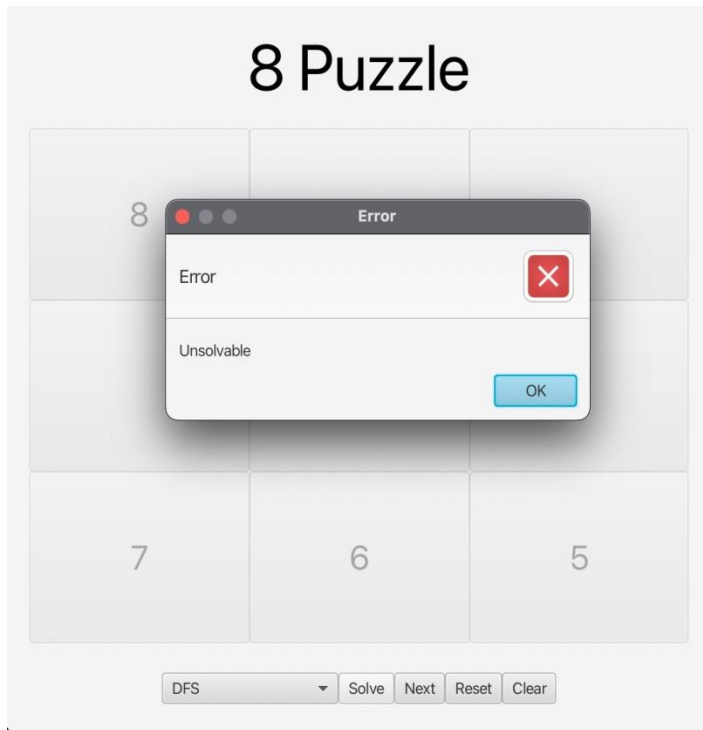
BFS

Test case unsolvable:

8 Puzzle

8	1	2
	4	3
7	6	5

DFS



Test Case:

```
1,2,5,3,4,0,6,7,8
A* search(Manh):
Success
Path
125340678|
120345678
102345678
012345678

Cost
3

Expanded
120345678, 102345678, 125340678, 012345678,
Max depth
3
Execution time: 79 milliseconds
```

```
A* search(Eucli)
Success
Path
125340678
120345678
102345678
012345678

Cost
3

Expanded
125340678, 102345678, 012345678, 120345678,
Max depth
3
Execution time: 0 milliseconds
```

```
*****
BFS search
Success
Path
125340678
120345678
102345678
012345678

Cost
3

Expanded
125348607, 125304678, 012345678, 125374608, 125348670, 125034678, 125340678, 102345678, 120345678, 105324678,
Max depth
3
Execution time: 0 milliseconds
```

```

DFS search
Success
Path
125340678
125348670
125348607
125348067
125048367
125408367
125480367
125487360
125487306
125487036
125087436
125807436
125870436
125876430
125876403
125876043
125076843
125706843
125760843
125763840
125763804
125763804

Cost
157
Expanded
312087546, 125634078, 312764085, 125630784, 125870436, 543218067, 254761803, 543087126, 431076825, 312764805, 125
Max depth
157
Execution time: 16 milliseconds
*****
```

Test Case:

0, 1, 3, 4, 2, 5, 7, 8, 6

A* search(Manh):

Success

Path

013425786

413025786

413725086

413725806

413725860

413720865

413702865

413762805

413762085

413062785

413602785

403612785

430612785

432610785

432615780

432615708

432615078

432015678

032415678

302415678

312405678

312045678

012345678

Cost

22

Expanded

213540786, 241536708, 410532786, 413268075, 412536708, 345082176, 123705846, 415802376, 412056738, 162438750, 413875026, 243185076, 512304786, 302415786,

Max depth

22

Execution time: 184 milliseconds

```

A* search(EucLi)
Success
Path
013425786
413025786
413725086
413725806
413725860
413720865
413702865
413762805
413762085
413062785
413602785
403612785
430612785
432610785
432615780
432615708
432615078
432015678
032415678
302415678
312405678
312045678
012345678

```

```

Cost
22
Expanded
241503786, 345160728, 715032846, 412783605, 013462785, 120463758, 123856407, 243716058, 412530678, 182403765, 432815670, 102
Max depth
22
Execution time: 285 milliseconds
*****

```

Test Cases:

1,2,0,3,4,5,6,7,8

A* search(Manh):

Success

Path

120345678

102345678

012345678

Cost

2

Expanded

102345678, 012345678, 120345678,

Max depth

2

Execution time: 64 milliseconds

A* search(Eucli)

Success

Path

120345678

102345678

012345678

Cost

2

Expanded

102345678, 120345678, 012345678,

Max depth

2

Execution time: 0 milliseconds

```
*****
      BFS search
      Success
      Path
120345678
102345678
012345678

      Cost
2

      Expanded
102345678, 120345678, 012345678, 125340678,
      Max depth
2
Execution time: 8 milliseconds
*****
```

```
DFS search
Success
Path
```

```
120345678
125340678
125348670
125348607
125348067
125048367
125408367
125480367
125487360
125487306
125487036
125087436
125807436
125870436
125876430
125876403
125876043
125076843
125706843
125760843
125763840
125763804
125763084
125063784
125603784
```

```
Cost
158
Expanded
312706854, 254138607, 312045678, 250134678, 125763840, 543087126, 254613078, 543706812, 431605782, 312645078, 1
Max depth
158
Execution time: 16 milliseconds
*****
Process finished with exit code 0
```