

Artificial Intelligence and Machine Learning

Neural Networks

Lecture Outline

أكاديمية كاوست KAUST ACADEMY

- Logistic Regression Review
- Neural Networks
 - Forward pass
 - Backward pass

Review: Logistic Regression





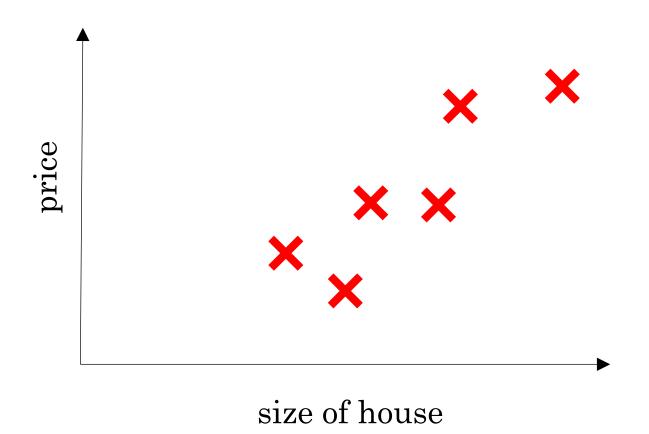


Introduction to Deep Learning

What is a Neural Network?



Housing Price Prediction

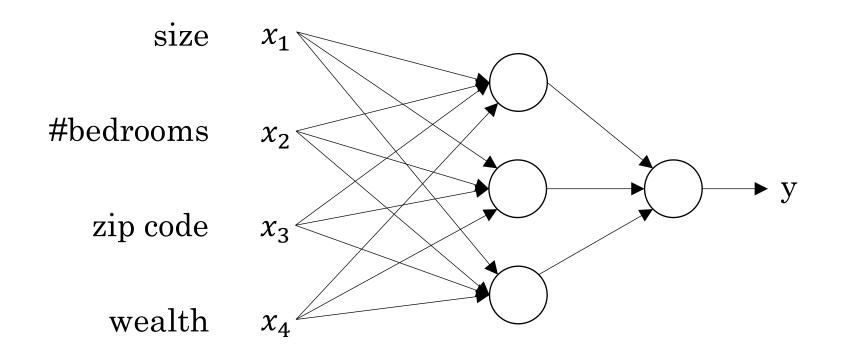








Housing Price Prediction







Introduction to Deep Learning

Supervised Learning with Neural Networks

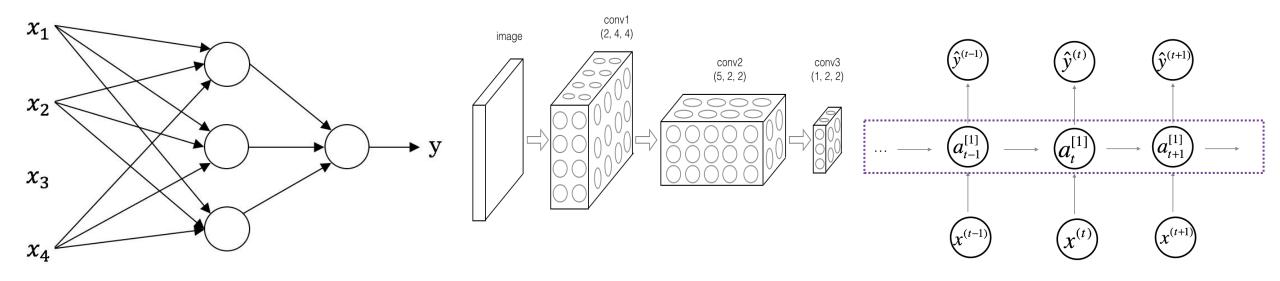




| Input(x) | Output (y) | Application |
|-------------------|------------------------|---------------------|
| Home features | Price | Real Estate |
| Ad, user info | Click on ad? (0/1) | Online Advertising |
| Image | Object (1,,1000) | Photo tagging |
| Audio | Text transcript | Speech recognition |
| English | Chinese | Machine translation |
| Image, Radar info | Position of other cars | Autonomous driving |
| | | |

Neural Network examples





Standard NN

Convolutional NN

Recurrent NN



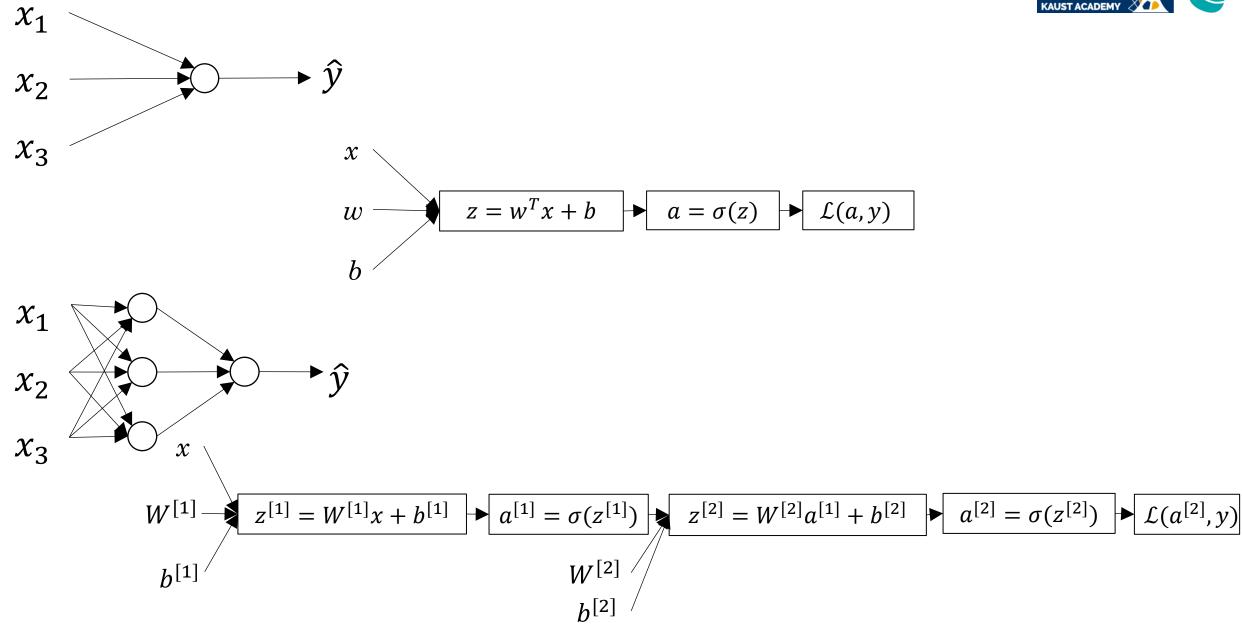


One hidden layer Neural Network

Neural Networks Overview

What is a Neural Network?



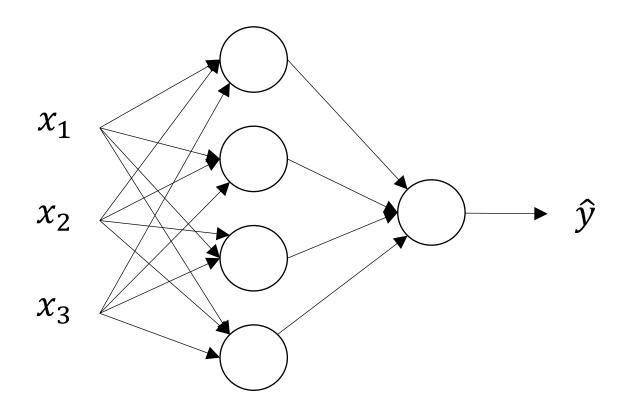






One hidden layer Neural Network





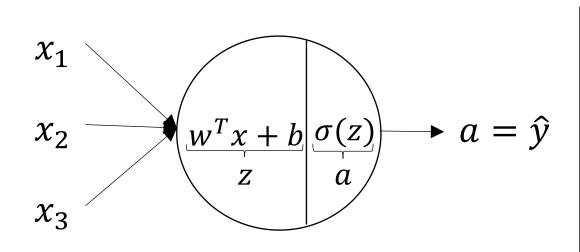


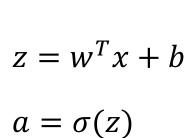


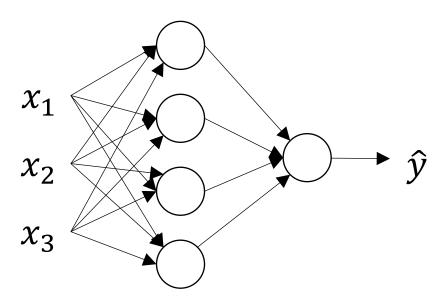
One hidden layer Neural Network

Computing a Neural Network's Output

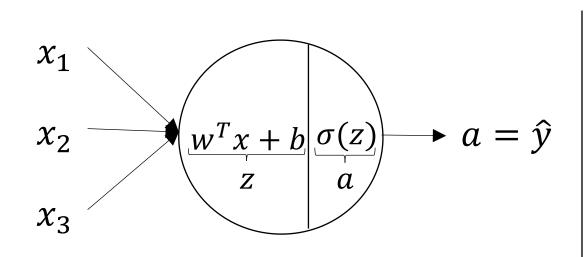




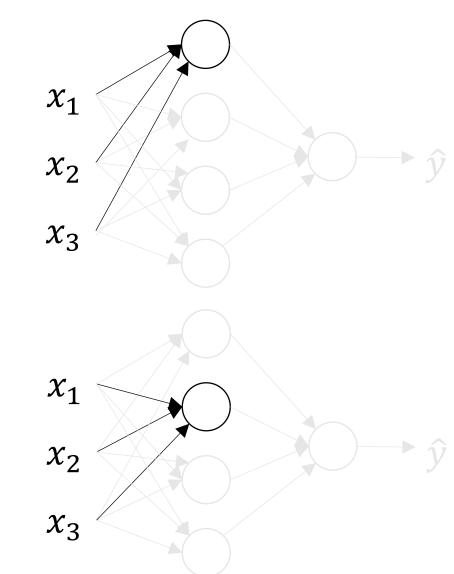




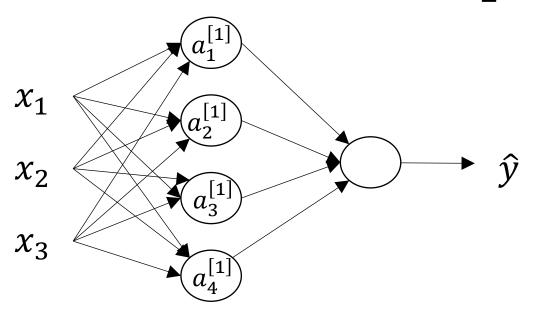




$$z = w^T x + b$$
$$a = \sigma(z)$$







$$z_{1}^{[1]} = w_{1}^{[1]T} x + b_{1}^{[1]}, \ a_{1}^{[1]} = \sigma(z_{1}^{[1]})$$

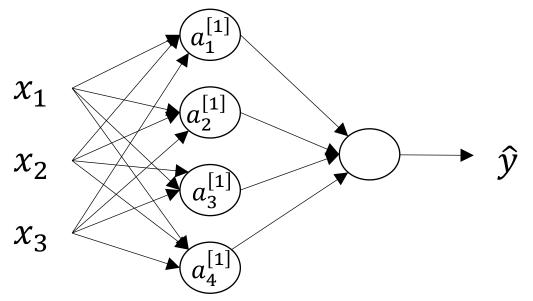
$$z_{2}^{[1]} = w_{2}^{[1]T} x + b_{2}^{[1]}, \ a_{2}^{[1]} = \sigma(z_{2}^{[1]})$$

$$z_{3}^{[1]} = w_{3}^{[1]T} x + b_{3}^{[1]}, \ a_{3}^{[1]} = \sigma(z_{3}^{[1]})$$

$$z_{4}^{[1]} = w_{4}^{[1]T} x + b_{4}^{[1]}, \ a_{4}^{[1]} = \sigma(z_{4}^{[1]})$$

Neural Network Representation learning





Given input x:

$$z^{[1]} = W^{[1]}x + b^{[1]}$$

$$a^{[1]} = \sigma(z^{[1]})$$

$$z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

$$a^{[2]} = \sigma(z^{[2]})$$



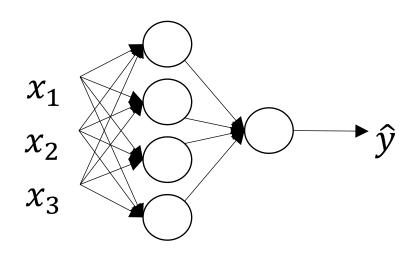


One hidden layer Neural Network

Vectorizing across multiple examples

Vectorizing across multiple examples





$$z^{[1]} = W^{[1]}x + b^{[1]}$$

$$a^{[1]} = \sigma(z^{[1]})$$

$$z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

$$a^{[2]} = \sigma(z^{[2]})$$

Vectorizing across multiple examples



```
for i = 1 to m:

z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}
a^{[1](i)} = \sigma(z^{[1](i)})
z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}
a^{[2](i)} = \sigma(z^{[2](i)})
```





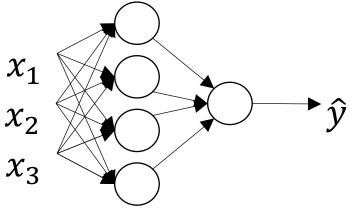
One hidden layer Neural Network

Explanation for vectorized implementation

Justification for vectorized implementation



Recap of vectorizing across multiple example e



$$X = \begin{bmatrix} & & & & & & \\ & & & & & & \\ & \chi^{(1)} & \chi^{(2)} & \dots & \chi^{(m)} \\ & & & & & & \end{bmatrix}$$

for i = 1 to m
$$z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}$$

$$a^{[1](i)} = \sigma(z^{[1](i)})$$

$$z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}$$

$$a^{[2](i)} = \sigma(z^{[2](i)})$$

$$Z^{[1]} = W^{[1]}X + b^{[1]}$$

$$A^{[1]} = \sigma(Z^{[1]})$$

$$Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}$$

$$A^{[2]} = \sigma(Z^{[2]})$$



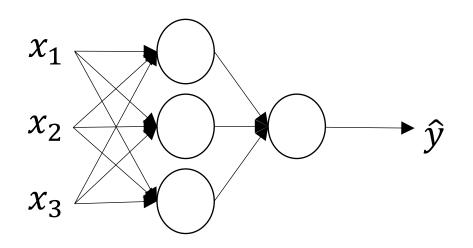


One hidden layer Neural Network

Activation functions

Activation functions





Given x:

$$z^{[1]} = W^{[1]}x + b^{[1]}$$

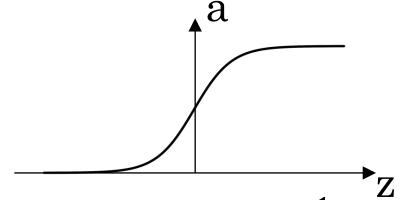
$$a^{[1]} = \sigma(z^{[1]})$$

$$z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

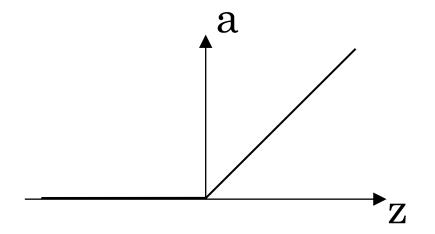
$$a^{[2]} = \sigma(z^{[2]})$$

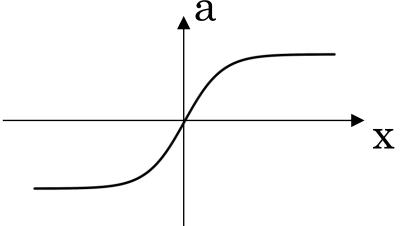
Pros and cons of activation functions

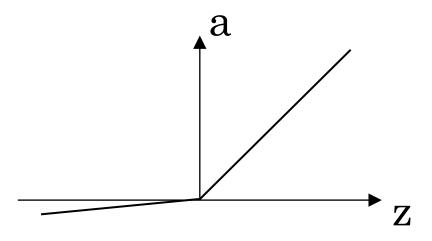




sigmoid:
$$a = \frac{1}{1 + e^{-z}}$$









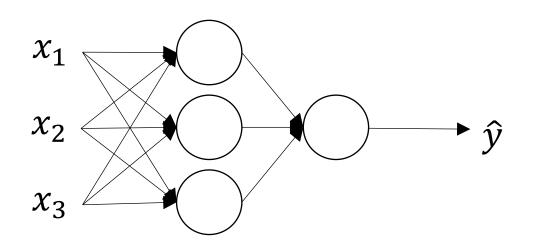


One hidden layer Neural Network

Why do you need non-linear activation functions?

Activation function





Given x:

$$z^{[1]} = W^{[1]}x + b^{[1]}$$

$$a^{[1]} = g^{[1]}(z^{[1]})$$

$$z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

$$a^{[2]} = g^{[2]}(z^{[2]})$$





One hidden layer Neural Network

Gradient descent for neural networks

Gradient descent for neural networks







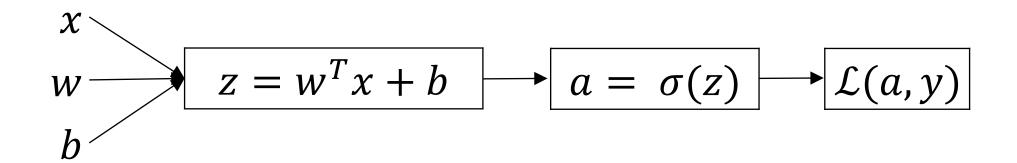
One hidden layer Neural Network

Backpropagation intuition

Computing gradients

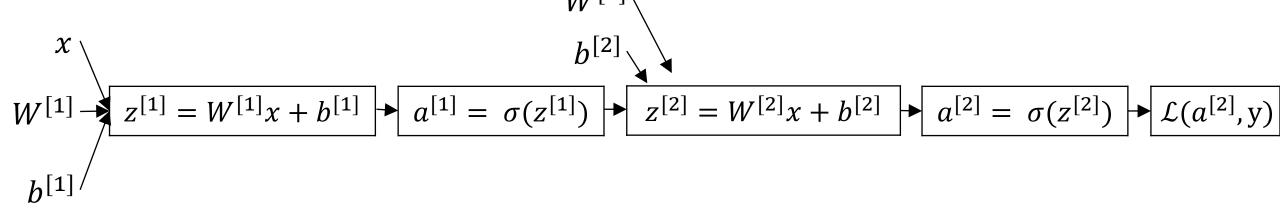


Logistic regression



Neural network gradients $W^{[2]}$





Summary of gradient descent



$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

Summary of gradient descent



$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]}) dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dZ^{[2]} = A^{[2]} - Y$$

$$dW^{[2]} = \frac{1}{m} dZ^{[2]} A^{[1]^T}$$

$$db^{[2]} = \frac{1}{m}np.sum(dZ^{[2]}, axis = 1, keepdims = True)$$

$$dZ^{[1]} = W^{[2]T} dZ^{[2]} * g^{[1]'}(Z^{[1]})$$

$$dW^{[1]} = \frac{1}{m} dZ^{[1]} X^T$$

$$db^{[1]} = \frac{1}{m} np. sum(dZ^{[1]}, axis = 1, keepdims = True)$$



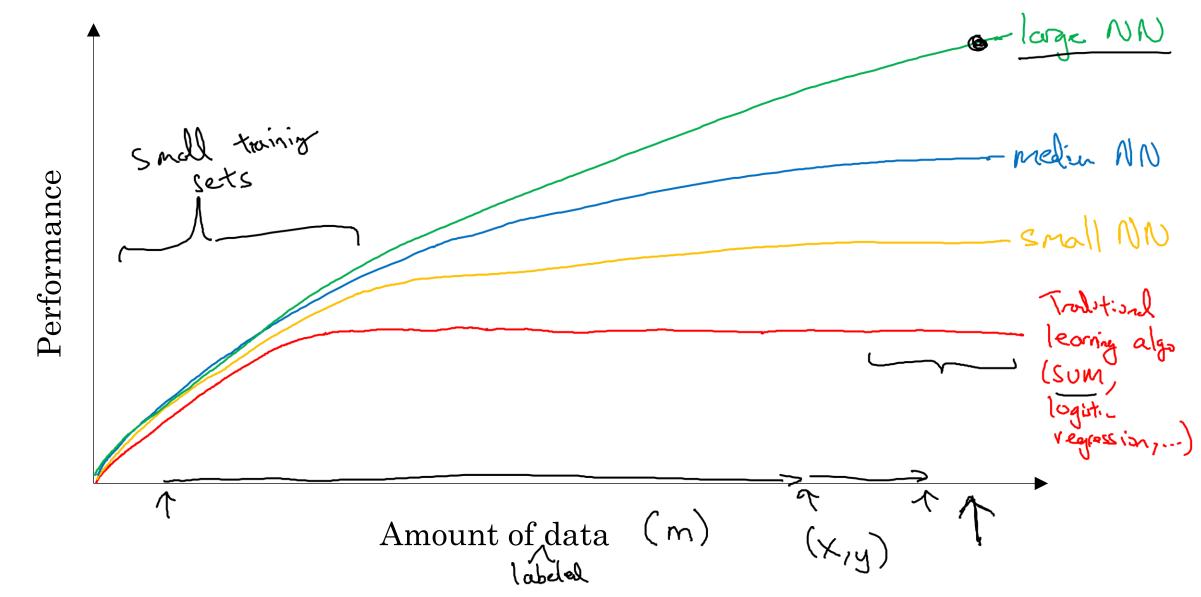


Introduction to Neural Networks

Why is Deep Learning taking off?

Scale drives deep learning progress





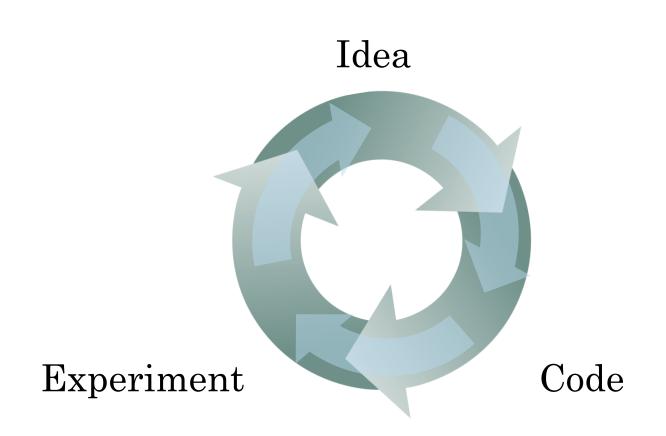
Scale drives deep learning progress



• Data

Computation

• Algorithms



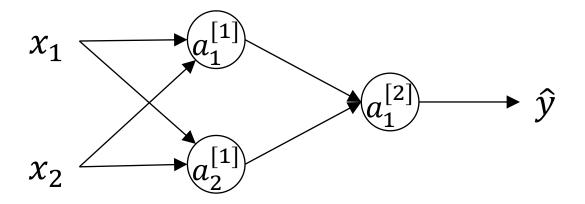




One hidden layer Neural Network

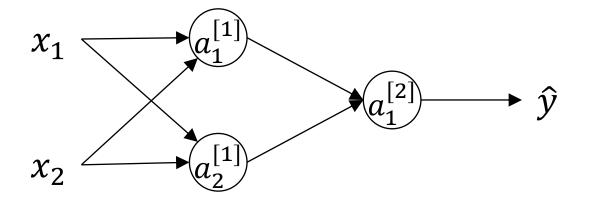
Random Initialization

What happens if you initialize weights to zero?



Random initialization





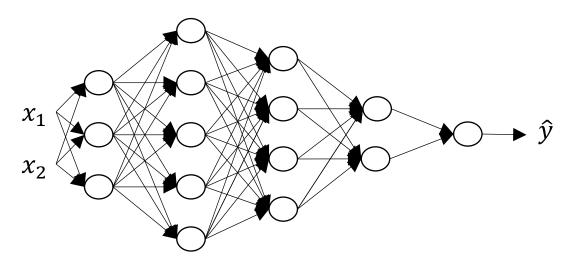




Deep Neural Networks

Getting your matrix dimensions right

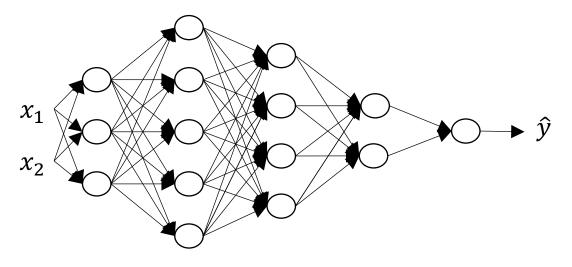
Parameters $W^{[l]}$ and $b^{[l]}$





Vectorized implementation







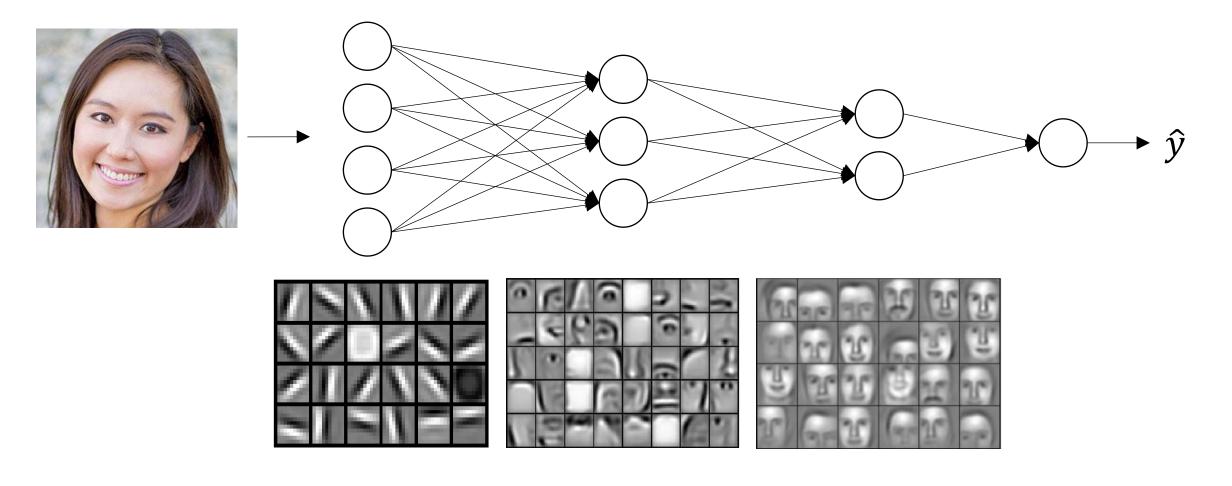


Deep Neural Networks

Why deep representations?



Intuition about deep representation





Circuit theory and deep learning

Informally: There are functions you can compute with a "small" L-layer deep neural network that shallower networks require exponentially more hidden units to compute.



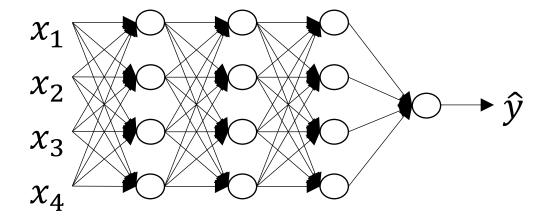


Deep Neural Networks

Building blocks of deep neural networks

Forward and backward functions





Forward and backward functions







Deep Neural Networks

Forward and backward propagation

Forward propagation for layer /



Input $a^{[l-1]}$

Output $a^{[l]}$, cache $(z^{[l]})$

Backward propagation for layer /



Input $da^{[l]}$

Output $da^{[l-1]}$, $dW^{[l]}$, $db^{[l]}$

Summary

