

Problem 7:

We will use Transformation matrix that we change a Current (x, y) Position into the next (x_t, y_t)

$$\text{begin} = \text{Vec}([x, y, 1])$$

$$\text{matrix} = \text{Matrix}(\dots)$$

$$\text{next} = \text{start} * \text{matrix} / \text{multiplication of matrices}$$

Now go backwards to figure out the matrix if your next is expected to look like $\text{Vec}([a*x+x', b*y+y', 1])$.

Examine only the x component at first. We'll take the dot Product of our start vector and the topmost row of our matrix, resulting in $a*x+x'$

we can do the same thing for the other two rows of the matrix to get the following:

Matrix

$$\begin{bmatrix} [a, 0, x'] \\ [0, b, y'] \\ [1, 0, 0] \end{bmatrix}$$

If we take our start vector and multiply it with this matrix, we'll get the translated vector. ~~next~~

~~as Vec~~

The actual beauty of this is that the matrix doesn't care what our inputs are at all it's fully ~~self-contained~~ Self-Contained.

Fortunately, we have an efficient method for computing a matrix to a power it's called **exponentiation by squaring**.

In a nutshell, rather than multiplying the number or matrix n times we square it and multiply intermediate value by original number / matrix at the appropriate intervals. quickly In **$\log(n)$** Time