INTEGRATION AND DIFFERENCIATION

HE POWER RULF:

the power rule is used to find the first derivative of any function.

If we have a function $f(x) = \chi^2$

We can apply the power rule as follows:

If $f(x) = x^2$ — D a = 1, so not shown.

 $f'(x) = 2x x^{2-1}$ another way to STEPS: for any function f(x)=ax n if f(x) then f'(x)= f'(x) = anx n-1 $n \times f(x)$ n-1

1) Ist we times the coefficient of x by the power (n)

2) then we minus I from the power

In our example, a=1, so it was not shown.

In short:

one of writing it:

one of $f(x) = \chi^2$ one of $f(x) = \chi^2$

then f'(x) = 2x f'(x)

 $= 2 \times x^{2-1}$

The opposite of deriving is integrating.

So we do the exact opposite in order to get the integral of a function.

If
$$f(x) = 2x$$

STEPS: (1) first add 1 to the exponent 1 (2) then divide f (x) by the a value 2

Sx dx with our example with (espect Megrate

the steps are <u>a/20 161613601</u>

Therefore becomes:

$$\frac{2x^{1+1}}{z}$$

Lour toimula for neverse power rulis:

$$= \int_{n+1}^{\infty} f(x) dx$$

If we take the power rule above, but we have a question with brackets, we can use the chain rule so that we don't have to expand the brackets.

for example if $f(x) = (3z-2)^4$ this would take long to expand

The chain rule states that in this case,

for any f(x), f'(x) is equal to

the 1st derivative of outside the bracket times by the first derivative of the contents inside the bracket, like this:

If g (x) - looks likethis:

Then: $g'(x) = n \times (f(x))^{n-1} \times f'(x)$

So using our example:

If f(0=(3z-2)4

note that the contents of the bracket are left the same here

 $44^{\circ} + (\alpha) = 4 \times (3x - 2) \times 3$

to finish this: 4x3=12

 $12(3x-2)^3$

derivative of the contents of the bracket.

	REVERSING THE CHAIN RULE: (integration) 4
-	Just like the power rule, the chain rule is reversable. This is used to INTEGRATE.
	1/12/12 1/2 1/4/15 1/4/16.
	The reverse chain rule could be shown as follows:
	In order to Stoc) do where we have
	brackets:
	Our integrated function would be found by:
	· · · · · · · · · · · · · · · · · · ·
	f(x) n+1 - pariginal plus 1
	(n+1) × f(x) divide by the f(x) first derivative of f(x) to reverse it again to this is again the integral of the integral of the integral of
bis:	first derivative or to reverse it again
114,	add to reverse it again to reverse it again to the this is again the devivative ral of the integral of the fix
142	to it devisation and
71h	eyst the Mil
(1)	
	using our answeras an example:
	$\int 12(3x-2)^3 dx$
	4
	$= 12(3x-2)^4$
	04 × 3 1
	$= 12(3x-2)^4 = (3x-2)^4$
	12

POWER RULE:

if $f(x)^n$

then $f'(x) = n \times f(x)^{n-1}$

REVERSE POWER RULE:

If $\int f(x) dx$

then f (x) n+1

CHAIN RULE:

If $g(x) = 7 (f(x))^h$ then $g'(x) = n \times (f(x))^{h-1} \times f(x)$

REVERSE CHAIN RULE:

If $\int f(x)^n dx = >$ with brackets

then $(f(x))^{n+1}$ + $C \sim C$ the constant

ferm sturing this started on the property of

When you differenciate f (x) the constant term falls away.

When you integrate, you need to bring that

constant term back.

Eq: 1+ +(x) = x2+1 $f(\alpha) = 2x$

IF Zzdx

WC Att X2

So: We are missing the +1 jurn:

1 + Civ: 1.0 + C Sub point (1,2)

Knopoint given, leave it like this:

from here we would need further information

to solve for c, such as subbing in a

Point on our graph.

This information will be given, or found, on the example, or the function can beleft in this form.