

5.

$$a. F(i\omega) = \frac{1}{i\omega + 3}$$

$$F(i\omega) = \frac{1}{i\omega - (-3)}$$

$$f(t) = e^{-3t} \cdot u(t)$$

$$b. F(i\omega) = -i\pi \delta(\omega - 2\pi) + i\pi \delta(\omega + 2\pi) + 1$$

$$F(i\omega) = i\pi \left[\delta(\omega + 2\pi) - \delta(\omega - 2\pi) \right] + 1$$

$$f(t) = \sin 2\pi t + \delta(t)$$

$$c. F(i\omega) = (2 + e^{3i\omega})\pi \delta(\omega) - \frac{i(1 + e^{3i\omega})}{\omega}$$

$$= 2\pi \delta(\omega) + e^{3i\omega} \pi \delta(\omega) - \frac{1}{\omega} - \frac{i}{\omega} e^{3i\omega}$$

$$= 2\pi \delta(\omega) + e^{3i\omega} \cdot \frac{1}{2} \cdot 2\pi \delta(\omega) - \frac{i^2}{i\omega} - \frac{i^2}{i\omega} e^{3i\omega}$$

$$= 2\pi \delta(\omega) + \frac{1}{2} e^{3i\omega} \cdot 2\pi \delta(\omega) - i^2 \frac{1}{i\omega - 0} - i^2 e^{3i\omega} \cdot \frac{1}{i\omega - 0}$$

$$= 1 + \frac{1}{2} e^{-3t} \cdot 1 - i^2 e^{0t} - i^2 e^{-3t} \cdot e^{0t}$$

$$= 1 + \frac{1}{2} e^{-3t} - (-1) - (-1) e^{-3t}$$

$$= 1 + \frac{1}{2} e^{-3t} + 1 + e^{-3t}$$

$$= 2 + \frac{3}{2} e^{-3t}$$