

1.

A	B	C	F_1	F_2
0	0	0	1	1
0	0	1	1	0
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	1
1	1	0	1	0
1	1	1	0	0

a. $F_1 = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}BC + A\bar{B}C + ABC$
 $= \bar{A}\bar{B}\bar{C} + \bar{A}C(\bar{B} + B) + AC(\bar{B} + B)$
 $= \bar{A}\bar{B}\bar{C} + \bar{A}C + AC$
 $= \bar{A}\bar{B}\bar{C} + C(\bar{A} + A)$
 $= \bar{A}\bar{B}\bar{C} + C$
 $= \bar{A}\bar{B} + C$

b. $F_2 = (\bar{A} + \bar{B} + \bar{C})(\bar{A} + B + \bar{C})(A + \bar{B} + \bar{C})(A + \bar{B} + C)$
 $= (\bar{A}\bar{A} + \bar{A}B + \bar{A}\bar{C} + \bar{B}\bar{A} + \bar{B}B + \bar{B}\bar{C} + \bar{C}\bar{A} + \bar{C}B + \bar{C}\bar{C})(A\bar{A} + A\bar{B} + AC + \bar{B}A + \bar{B}\bar{B} + \bar{B}C + \bar{C}A + \bar{C}\bar{B} + \bar{C}C)$
 $= (\bar{A} + \bar{A}C + \bar{C})(A + A\bar{B} + \bar{B})$
 $= (\bar{A} + \bar{C})(A + \bar{B})$
 $= \bar{A}A + A\bar{B} + A\bar{C} + \bar{B}\bar{C}$
 $= A(\bar{B} + \bar{C}) + \bar{B}\bar{C}$

$$2. F(x_1, x_2, x_3) = \sum m(0, 1, 4, 5, 7)$$

x_1	x_2	x_3	F
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

$$\begin{aligned}
 F &= \bar{x}_1 \bar{x}_2 \bar{x}_3 + \bar{x}_1 \bar{x}_2 x_3 + x_1 \bar{x}_2 \bar{x}_3 + x_1 \bar{x}_2 x_3 + x_1 x_2 x_3 \\
 &= \bar{x}_1 \bar{x}_2 (\bar{x}_3 + x_3) + x_1 \bar{x}_2 (\bar{x}_3 + x_3) + x_1 x_2 x_3 \\
 &= \bar{x}_1 \bar{x}_2 + x_1 \bar{x}_2 + x_1 x_2 x_3 \\
 &= (\bar{x}_1 + x_1) \bar{x}_2 + x_1 x_2 x_3 \\
 &= \bar{x}_2 + x_1 x_2 x_3 \\
 &= \bar{x}_2 + x_1 x_3
 \end{aligned}$$

$$3. a. T = A\bar{C} + A\bar{B}C$$

$$= A(\bar{C} + \bar{B}C)$$

$$= A(\bar{B} + \bar{C})$$

$$b. F = \bar{A} + A B \bar{C} + \overline{\bar{A} + C}$$

$$= \bar{A} + B \bar{C} + \bar{A} \cdot \bar{C}$$

$$= \bar{A} + B \bar{C} + A \bar{C}$$

$$= \bar{A} + B \bar{C} + \bar{C}$$

$$= \bar{A} + B + \bar{C}$$