

$$\underbrace{(2y \cos 2x - y \sin x) dx}_M + \underbrace{(\sin 2x + \cos x) dy}_N = 0$$

$$M = 2y \cos 2x - y \sin x$$

$$N = \sin 2x + \cos x$$

$$M_y = 2 \cos 2x - \sin x = N_x = 2 \cos 2x - \sin x$$

$$M_y = N_x \rightarrow \text{PD. eksak}$$

$$F_x(x, y) = M$$

$$F(x, y) = \int M dx$$

$$F(x, y) = \int (2y \cos 2x - y \sin x) dx$$

$$F(x, y) = 2y \cdot \frac{1}{2} \sin 2x - y \cdot (-\cos x) + c(y)$$

$$F(x, y) = y \sin 2x + y \cos x + c(y)$$

$$F_y(x, y) = N$$

$$\frac{\partial}{\partial y} (y \sin 2x + y \cos x + c(y)) = \sin 2x + \cos x$$

$$\cancel{\sin 2x} + \cancel{\cos x} + c'(y) = \cancel{\sin 2x} + \cancel{\cos x}$$

$$c'(y) = 0$$

$$c(y) = \int 0 dy$$

$$c(y) = C$$

$$\boxed{F(x, y) = C}$$

$$F(x, y) = y \sin 2x + y \cos x + c(y) = C$$

$$y \sin 2x + y \cos x + C = C$$

$$y \sin 2x + y \cos x = C$$