

3. Filter A : $f \leq 8 \text{ Hz}$

Filter B : $4 \text{ Hz} < f \leq 12,5 \text{ Hz}$

$F_s = 25 \text{ Hz}$

a. $\omega_{cA} = \frac{8}{25} \pi = 0,32 \pi$

$$H_A(e^{j\omega}) = \begin{cases} e^{-j\omega}, & 0 \leq \omega \leq 0,32 \pi \\ 0, & 0,32 \pi < \omega \leq \pi \end{cases}$$

$\omega_{cB1} = \frac{4}{25} \pi = 0,16 \pi$

$\omega_{cB2} = \frac{12,5}{25} \pi = 0,5 \pi$

$$H_B(e^{j\omega}) = \begin{cases} 0, & 0 \leq \omega \leq 0,16 \pi \\ e^{-j\omega}, & 0,16 \pi < \omega \leq 0,5 \pi \\ 0, & 0,5 \pi < \omega \leq \pi \end{cases}$$

$\Delta \omega = \frac{6,2 \pi}{M+1}$

$0,5 \cdot 2 \pi = \frac{6,2 \pi}{M+1}$

$M = \frac{6,2 \pi}{0,5 \cdot 2 \pi} - 1 = \lfloor 5,2 \rfloor = 5$

$M = 2 \alpha + 1$

$5 = 2 \alpha + 1$

$\alpha = 2$

$$H_A(e^{j\omega}) = \begin{cases} e^{-j2\omega}, & 0 \leq \omega \leq 0,32\pi \\ 0, & 0,32\pi < \omega \leq \pi \end{cases}$$

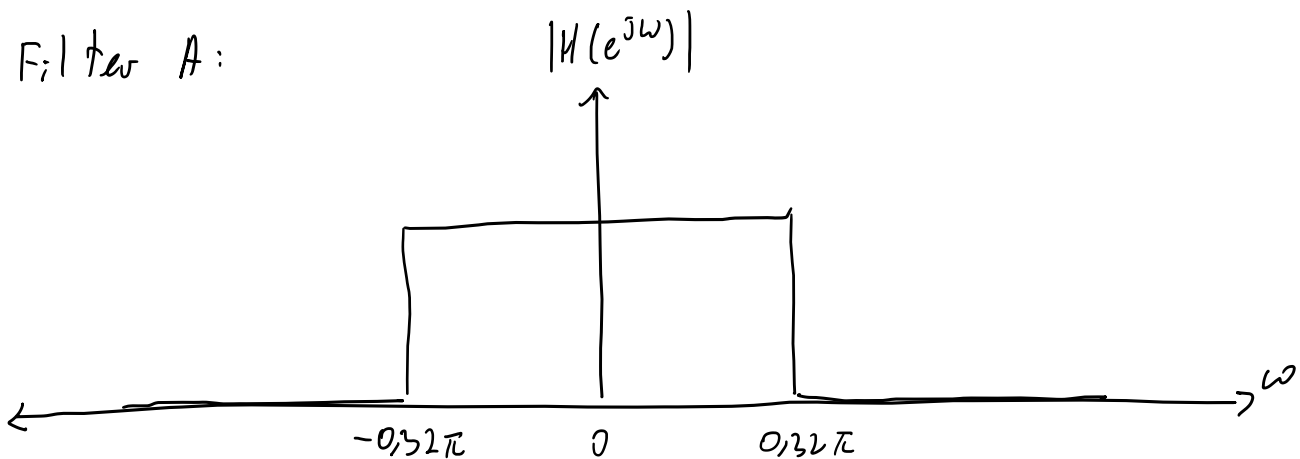
$$H_B(e^{j\omega}) = \begin{cases} 0, & 0 \leq \omega \leq 0,16\pi \\ e^{-j2\omega}, & 0,16\pi < \omega \leq 0,5\pi \\ 0, & 0,5\pi < \omega \leq \pi \end{cases}$$

$$b. \quad h_A[n] = \frac{\sin[\omega_c(n-2)]}{\pi(n-2)} = \frac{\sin[0,32\pi(n-2)]}{\pi(n-2)}$$

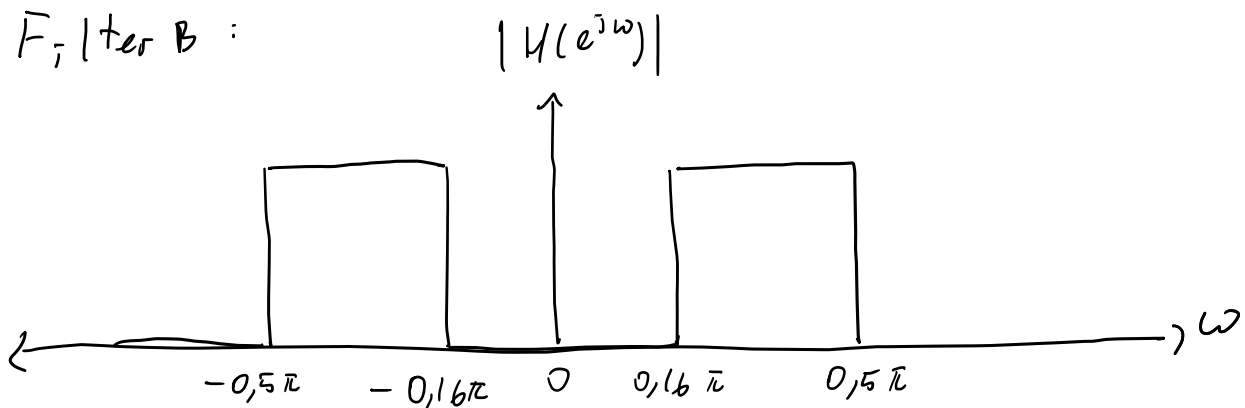
$$h_B[n] = \frac{\sin[\omega_{c2}(n-2)] - \sin[\omega_{c1}(n-2)]}{\pi(n-2)}$$

$$= \frac{\sin[0,5\pi(n-2)] - \sin[0,16\pi(n-2)]}{\pi(n-2)}$$

c. Filter A:



Filter B:



d. Window Planning

e. $M = 5$