

HOW TO COMBINE TWO RELATIVE RANKINGS OF CREDIT RISK INTO ONE RANKING?

BY INTERNAL RATINGS MANAGEMENT, GLOBAL RISK MANAGEMENT,
SCOTIABANK

Neal Madras, Alessandro Selvitella, Hatef Dastour,
Tuan Tran, Negin P. Roozbahani, Qiwei Feng,
Caio Hornhardt, Weifei Ouyang and Helen Samara Dos
Santos

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Motivation

- There are two groups of Borrowers: Group 1 (Financial firms) and Group 2 (Oil and Gas); each group has a large number of firms (around 2000 and 9000).
- Each borrower is ranked based on expert opinions. A rank is a number between 1 and 16 (default banks have rank 17). The bank has monthly data on ranks over a period of 10 years for each borrower.
- If two borrowers belong to the same group, it is straightforward to compare the riskiness of these (by comparing the average scores for instance).

- Problem: If there are two borrowers coming from different groups, how can the bank know which borrower is riskier?
- We then need to find a global ranking scale to compare the riskiness amongst borrowers from either groups.
- Data: Group A_i has N_i firms, $i = 1, 2$. The ranks of borrower a at time t is $R_t^a, t = 0, \dots, T, R_t^a \in \{1, \dots, 17\}$.

First Approach

- For borrower $a \in A_1$, we define a local rank \overline{R}_t^a by

$$\overline{R}_t^a = \sum_{i=1}^T w_i R_t^a.$$

- Suppose that $(\overline{R}_t^a)_{a \in A_1}$ are realizations of the same random variable R^1 whose distribution function is F_1 .
- When a varies in A_1 , we can plot a histogram for F_1 .

- We then approximate the discrete empirical distribution F_1 by a smooth well-known distribution function \hat{F}_1 depending on the data.
- We define the conditional probability of default

$$PD^1(x) := PD(R^1 = D | R^1 = x) = \frac{1 - \hat{F}_1(D)}{1 - \hat{F}_1(x)}.$$

- For two arbitrary borrowers a, b : we compare $PD^1(\overline{R}_t^a)$ and $PD^2(\overline{R}_t^b)$.

Second Approach

- In each group, we suppose that borrowers are realizations of the same markov process (R^1 for group 1 and R^2 for group 2).
- From the data, we get estimates for the transition matrices A_1 and A_2 .
- Suppose that a borrower $a \in A_1$ has current rank $R_t^a = x$, we can calculate the probability of default in a time horizon τ by

$$PD^1(x) := PD(R_s^1 = D, s = t, \dots, t + \tau | R_t = x).$$

- Given two borrowers $a \in A_1, b \in A_2$ with current ranks x, y . We compare $PD^1(x)$ and $PD^2(y)$.