Operations on word vectors

Welcome to your first assignment of this week!

Because word embeddings are very computionally expensive to train, most ML practitioners will load a pretrained set of embeddings.

After this assignment you will be able to:

- Load pre-trained word vectors, and measure similarity using cosine similarity
- Use word embeddings to solve word analogy problems such as Man is to Woman as King is to ___.
- Modify word embeddings to reduce their gender bias

Let's get started! Run the following cell to load the packages you will need.

```
In [36]:
```

import numpy as np

```
from w2v_utils import *
print("end...")

end...

In [37]:

import numpy as np
x=np.zeros((2,2))
print(x)

[[ 0.  0.]
```

Next, lets load the word vectors. For this assignment, we will use 50-dimensional GloVe vectors to represent words. Run the following cell to load the word_to_vec_map.

```
In [ ]:
```

.0

0.]]

```
words, word_to_vec_map = read_glove_vecs('data/glove.6B.50d.txt')
#print(words) #400k
#print(word_to_vec_map)
print("end...")
```

You've loaded:

- words: set of words in the vocabulary.
- word to vec map: dictionary mapping words to their GloVe vector representation.

You've seen that one-hot vectors do not do a good job cpaturing what words are similar. GloVe vectors provide much more useful information about the meaning of individual words. Lets now see how you can use GloVe vectors to decide how similar two words are.

1 - Cosine similarity

To measure how similar two words are, we need a way to measure the degree of similarity between two embedding vectors for the two words. Given two vectors u and v, cosine similarity is defined as follows:

CosineSimilarity(u, v) =
$$\frac{u \cdot v}{\|u\|_2 \|v\|_2} = \cos(\theta)$$
 (1)

where u. v is the dot product (or inner product) of two vectors, $||u||_2$ is the norm (or length) of the vector u, and θ is the angle between u and v. This similarity depends on the angle between u and v. If u and v are very similar, their cosine similarity will be close to 1; if they are dissimilar, the cosine similarity will take a smaller value.

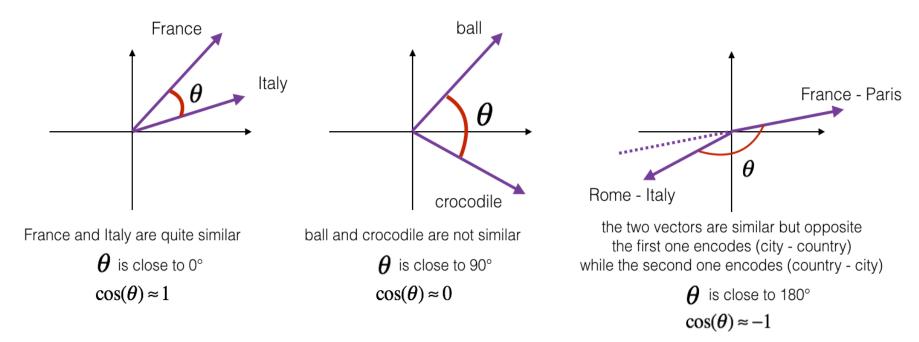


Figure 1: The cosine of the angle between two vectors is a measure of how similar they are

Exercise: Implement the function cosine similarity() to evaluate similarity between word vectors.

Reminder: The norm of u is defined as $||u||_2 = \sqrt{\sum_{i=1}^n u_i^2}$

```
In [38]:
# GRADED FUNCTION: cosine_similarity
def cosine similarity(u, v):
    Cosine similarity reflects the degree of similariy between u and v
    Arguments:
        u -- a word vector of shape (n,)
        v -- a word vector of shape (n,)
    Returns:
        cosine similarity -- the cosine similarity between u and v defined by the
    distance = 0.0
    ### START CODE HERE ###
    # Compute the dot product between u and v (≈1 line)
    dot = np.dot(u,v)
    # Compute the L2 norm of u (≈1 line)
    norm u = np.sqrt(np.sum(u**2))
    # Compute the L2 norm of v (≈1 line)
    norm v = np.sqrt(np.sum(v**2))
    # Compute the cosine similarity defined by formula (1) (≈1 line)
    cosine similarity = dot/(norm u*norm v)
    ### END CODE HERE ###
    return cosine similarity
In [40]:
father = word to vec map["father"]
#print("father",father)
mother = word_to_vec_map["mother"]
#print("mother", mother)
ball = word to vec map["ball"]
crocodile = word to vec map["crocodile"]
france = word to vec map["france"]
italy = word_to_vec_map["italy"]
paris = word_to_vec_map["paris"]
rome = word to vec map["rome"]
print("cosine_similarity(father, mother) = ", cosine_similarity(father, mother))
print("cosine_similarity(ball, crocodile) = ",cosine_similarity(ball, crocodile))
print("cosine_similarity(france - paris, rome - italy) = ",cosine_similarity(fran
cosine similarity(father, mother) = 0.890903844289
cosine similarity(ball, crocodile) = 0.274392462614
```

cosine similarity(france - paris, rome - italy) = -0.675147930817

```
In [41]:
```

```
print("cosine_similarity(france, italy) = ", cosine_similarity(france, italy))
print("cosine_similarity(paris, rome) = ", cosine_similarity(paris, rome))

queen=word_to_vec_map["queen"]
king=word_to_vec_map["king"]
man=word_to_vec_map["man"]
woman=word_to_vec_map["woman"]
result=cosine_similarity(queen, king-man+woman)
print("similarity of queen with (king-queen+woman):",result)

nurse=word_to_vec_map["nurse"]
doctor=word_to_vec_map["doctor"]
result2=cosine_similarity(nurse, mother-(father-doctor))
print("similarity of nurse with (mother-(father-doctor)):",result2)

cosine_similarity(france, italy) = 0.778863739208
cosine_similarity(paris, rome) = 0.709941134171
```

Expected Output:

```
cosine_similarity(father, mother) = 0.890903844289

cosine_similarity(ball, crocodile) = 0.274392462614

cosine_similarity(france - paris, rome - italy) = -0.675147930817
```

After you get the correct expected output, please feel free to modify the inputs and measure the cosine similarity between other pairs of words! Playing around the cosine similarity of other inputs will give you a better sense of how word vectors behave.

2 - Word analogy task

In the word analogy task, we complete the sentence "a is to b as c is to __". An example is 'man is to woman as king is to queen'. In detail, we are trying to find a word d, such that the associated word vectors e_a, e_b, e_c, e_d are related in the following manner: $e_b - e_a \approx e_d - e_c$. We will measure the similarity between $e_b - e_a$ and $e_d - e_c$ using cosine similarity.

Exercise: Complete the code below to be able to perform word analogies!

similarity of queen with (king-queen+woman): 0.860958125858

similarity of nurse with (mother-(father-doctor)): 0.846305950147

```
In [42]:
# GRADED FUNCTION: complete_analogy
def complete_analogy(word_a, word_b, word_c, word_to_vec_map):
    Performs the word analogy task as explained above: a is to b as c is to
    Arguments:
    word a -- a word, string
    word b -- a word, string
    word c -- a word, string
    word_to_vec_map -- dictionary that maps words to their corresponding vectors.
    Returns:
    best word -- the word such that v b - v a is close to v best word - v c, as
    # convert words to lower case
    word a, word b, word c = word a.lower(), word b.lower(), word c.lower()
    ### START CODE HERE ###
    # Get the word embeddings v a, v b and v c (≈1-3 lines)
    e a, e b, e_c = word_to_vec_map[word_a], word_to_vec_map[word_b], word_to_vec_m
    ### END CODE HERE ###
    words = word_to_vec_map.keys()
    \max \text{ cosine sim} = -100
                                       # Initialize max cosine sim to a large neg
    best word = None
                                       # Initialize best word with None, it will
    # loop over the whole word vector set
    for w in words:
        # to avoid best word being one of the input words, pass on them.
        if w in [word a, word b, word c] :
            continue
        ### START CODE HERE ###
        # Compute cosine similarity between the vector (e b - e a) and the vector
        cosine sim = cosine similarity(e b-e a, word to vec map[w]-e c)
        # If the cosine sim is more than the max cosine sim seen so far,
            # then: set the new max cosine sim to the current cosine sim and the
        if cosine sim > max cosine sim:
            max cosine sim = cosine sim
            best word = w
        ### END CODE HERE ###
```

Run the cell below to test your code, this may take 1-2 minutes.

return best word

```
In [43]:
triads_to_try = [('italy', 'italian', 'spain'), ('india', 'delhi', 'japan'), ('ma
                 ('small', 'smaller', 'large')]
for triad in triads_to_try:
    print ('{} -> {} :: {} -> {}'.format( *triad, complete_analogy(*triad,word_to
italy -> italian :: spain -> spanish
india -> delhi :: japan -> tokyo
man -> woman :: boy -> girl
small -> smaller :: large -> larger
In [31]:
triads_to_try = [('read', 'book', 'write'),('small', 'smaller', 'big'), ('car', '
for triad in triads_to_try:
    print ('{} -> {} :: {} -> {}'.format( *triad, complete_analogy(*triad,word to
read -> book :: write -> novel
small -> smaller :: big -> competitors
car -> foot :: computer -> 1.2-meter
```

Expected Output:

italy -> italian :: spain -> spanish
india -> delhi :: japan -> tokyo
man -> woman :: boy -> girl
small -> smaller :: large -> larger

Once you get the correct expected output, please feel free to modify the input cells above to test your own analogies. Try to find some other analogy pairs that do work, but also find some where the algorithm doesn't give the right answer: For example, you can try small->smaller as big->?.

Congratulations!

You've come to the end of this assignment. Here are the main points you should remember:

- Cosine similarity a good way to compare similarity between pairs of word vectors. (Though L2 distance works too.)
- For NLP applications, using a pre-trained set of word vectors from the internet is often a good way to get started.

Even though you have finished the graded portions, we recommend you take a look too at the rest of this notebook.

Congratulations on finishing the graded portions of this notebook!

3 - Debiasing word vectors (OPTIONAL/UNGRADED)

In the following exercise, you will examine gender biases that can be reflected in a word embedding, and explore algorithms for reducing the bias. In addition to learning about the topic of debiasing, this exercise will also help hone your intuition about what word vectors are doing. This section involves a bit of linear algebra, though you can probably complete it even without being expert in linear algebra, and we encourage you to give it a shot. This portion of the notebook is optional and is not graded.

Lets first see how the GloVe word embeddings relate to gender. You will first compute a vector $g=e_{woman}-e_{man}$, where e_{woman} represents the word vector corresponding to the word woman, and e_{man} corresponds to the word vector corresponding to the word woman. The resulting vector woman roughly encodes the concept of "gender". (You might get a more accurate representation if you compute $woman}=e_{mother}-e_{father}$, $woman}=e_{mother}-e_{boy}$, etc. and average over them. But just using $woman}-e_{man}$ will give good enough results for now.)

In [45]:

g = word_to print(g)	_vec_map['wc	man'] - word	d_to_vec_map['	man']		
[-0.087144 5	0.2182	-0.40986	-0.03922	-0.1032	0.9416	
-0.06042 4	0.32988	0.46144	-0.35962	0.31102	-0.8682	
0.96006	0.01073	0.24337	0.08193	-1.02722	-0.2112	
0.695044	-0.00222	0.29106	0.5053	-0.099454	0.4044	
0.30181 5	0.1355	-0.0606	-0.07131	-0.19245	-0.0611	
-0.3204 57	0.07165	-0.13337	-0.25068714	-0.14293	-0.2249	
-0.149	0.048882	0.12191	-0.27362	-0.165476	-0.2042	
0.54376	-0.271425	-0.10245	-0.32108	0.2516	-0.3345	
_	0.01258]				

Now, you will consider the cosine similarity of different words with g. Consider what a positive value of similarity means vs a negative cosine similarity.

```
In [46]:
print ('List of names and their similarities with constructed vector:')
# girls and boys name
name_list = ['john', 'marie', 'sophie', 'ronaldo', 'priya', 'rahul', 'danielle',
for w in name list:
    print (w, cosine similarity(word to vec map[w], g))
List of names and their similarities with constructed vector:
john -0.23163356146
marie 0.315597935396
sophie 0.318687898594
ronaldo -0.312447968503
priya 0.17632041839
rahul -0.169154710392
danielle 0.243932992163
reza -0.079304296722
katy 0.283106865957
yasmin 0.233138577679
As you can see, female first names tend to have a positive cosine similarity with our constructed vector g,
while male first names tend to have a negative cosine similarity. This is not suprising, and the result seems
acceptable.
But let's try with some other words.
In [47]:
print('Other words and their similarities:')
word_list = ['lipstick', 'guns', 'science', 'arts', 'literature', 'warrior','doct
              'technology', 'fashion', 'teacher', 'engineer', 'pilot', 'computer'
for w in word list:
    print (w, cosine_similarity(word_to_vec_map[w], g))
Other words and their similarities:
lipstick 0.276919162564
guns -0.18884855679
science -0.0608290654093
arts 0.00818931238588
literature 0.0647250443346
warrior -0.209201646411
doctor 0.118952894109
tree -0.0708939917548
receptionist 0.330779417506
technology -0.131937324476
fashion 0.0356389462577
teacher 0.179209234318
engineer -0.0803928049452
pilot 0.00107644989919
computer -0.103303588739
```

singer 0.185005181365

Do you notice anything surprising? It is astonishing how these results reflect certain unhealthy gender stereotypes. For example, "computer" is closer to "man" while "literature" is closer to "woman". Ouch!

We'll see below how to reduce the bias of these vectors, using an algorithm due to Boliukbasi et al., 2016 (https://arxiv.org/abs/1607.06520). Note that some word pairs such as "actor"/"actress" or "grandmother"/"grandfather" should remain gender specific, while other words such as "receptionist" or "technology" should be neutralized, i.e. not be gender-related. You will have to treat these two type of words differently when debiasing.

3.1 - Neutralize bias for non-gender specific words

The figure below should help you visualize what neutralizing does. If you're using a 50-dimensional word embedding, the 50 dimensional space can be split into two parts: The bias-direction g, and the remaining 49 dimensions, which we'll call g_{\perp} . In linear algebra, we say that the 49 dimensional g_{\perp} is perpendicular (or "othogonal") to g, meaning it is at 90 degrees to g. The neutralization step takes a vector such as $e_{receptionist}$ and zeros out the component in the direction of g, giving us $e_{receptionist}^{debiased}$

Even though g_{\perp} is 49 dimensional, given the limitations of what we can draw on a screen, we illustrate it using a 1 dimensional axis below.

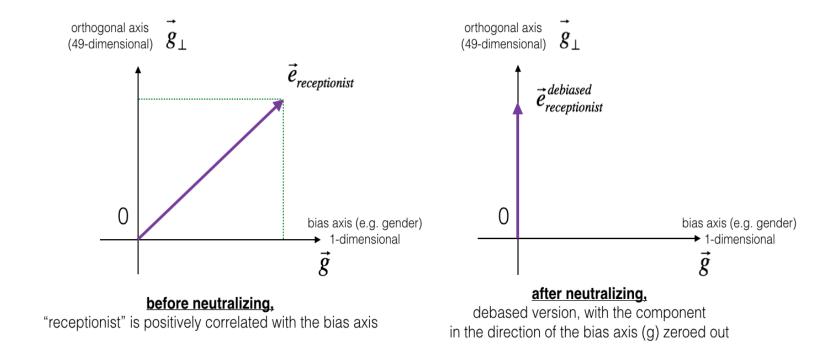


Figure 2: The word vector for "receptionist" represented before and after applying the neutralize operation.

Exercise: Implement neutralize() to remove the bias of words such as "receptionist" or "scientist". Given an input embedding e, you can use the following formulas to compute $e^{de biased}$:

$$e^{bias_component} = \frac{e \cdot g}{\|g\|_2^2} * g$$

$$e^{debiased} = e - e^{bias_component}$$
(2)

$$e^{debiased} = e - e^{bias_component} \tag{3}$$

If you are an expert in linear algebra, you may recognize $e^{bias_component}$ as the projection of e onto the direction g. If you're not an expert in linear algebra, don't worry about this.

```
In [49]:
def neutralize(word, g, word_to_vec_map):
   Removes the bias of "word" by projecting it on the space orthogonal to the bi
    This function ensures that gender neutral words are zero in the gender subspa
   Arguments:
        word -- string indicating the word to debias
        g -- numpy-array of shape (50,), corresponding to the bias axis (such as
        word to vec map -- dictionary mapping words to their corresponding vector
   Returns:
        e debiased -- neutralized word vector representation of the input "word"
    ### START CODE HERE ###
    # Select word vector representation of "word". Use word_to_vec_map. (≈ 1 line
    e = word to vec map[word]
    # Compute e biascomponent using the formula give above. (≈ 1 line)
    e biascomponent = (np.dot(e,g)/(np.sum(g**2)))*g
    # Neutralize e by substracting e biascomponent from it
    # e debiased should be equal to its orthogonal projection. (≈ 1 line)
    e debiased = e - e biascomponent
    ### END CODE HERE ###
    return e debiased
```

```
In [51]:
```

```
cosine similarity between receptionist and g, before neutralizing: 0.330779417506 cosine similarity between receptionist and g, after neutralizing: - 5.60374039375e-17
```

Expected Output: The second result is essentially 0, up to numerical roundof (on the order of 10^{-17}).

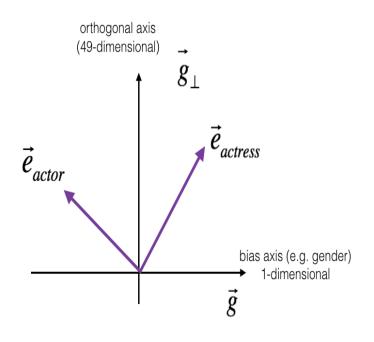
cosine similarity between receptionist and g, before neutralizing: 0.330779417506

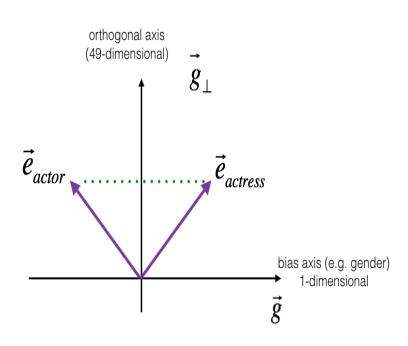
cosine similarity between receptionist and g, after neutralizing: -3.26732746085e-17

3.2 - Equalization algorithm for gender-specific words

Next, lets see how debiasing can also be applied to word pairs such as "actress" and "actor." Equalization is applied to pairs of words that you might want to have differ only through the gender property. As a concrete example, suppose that "actress" is closer to "babysit" than "actor." By applying neutralizing to "babysit" we can reduce the gender-stereotype associated with babysitting. But this still does not guarantee that "actor" and "actress" are equidistant from "babysit." The equalization algorithm takes care of this.

The key idea behind equalization is to make sure that a particular pair of words are equi-distant from the 49-dimensional g_{\perp} . The equalization step also ensures that the two equalized steps are now the same distance from $e_{receptionist}^{debiased}$, or from any other work that has been neutralized. In pictures, this is how equalization works:





before equalizing, "actress" and "actor" differ in many ways beyond the direction of \vec{g}

after equalizing,

"actress" and "actor" differ only in the direction of \vec{g} , and further are equal in distance from \vec{g}_{\perp}

The derivation of the linear algebra to do this is a bit more complex. (See Bolukbasi et al., 2016 for details.) But the key equations are:

$$\mu = \frac{e_{w1} + e_{w2}}{2} \tag{4}$$

$$\mu_B = \frac{\mu \cdot \text{bias_axis}}{\|\text{bias_axis}\|_2^2} * \text{bias_axis}$$
 (5)

$$\mu_{\perp} = \mu - \mu_B \tag{6}$$

$$e_{w1B} = \frac{e_{w1} \cdot \text{bias_axis}}{\|\text{bias_axis}\|_2^2} * \text{bias_axis}$$
(7)

$$e_{w1B} = \frac{e_{w1} \cdot \text{bias_axis}}{\|\text{bias_axis}\|_{2}^{2}} * \text{bias_axis}$$

$$e_{w2B} = \frac{e_{w2} \cdot \text{bias_axis}}{\|\text{bias_axis}\|_{2}^{2}} * \text{bias_axis}$$

$$(8)$$

$$e_{w1B}^{corrected} = \sqrt{|1 - ||\mu_{\perp}||_{2}^{2}|} * \frac{e_{w1B} - \mu_{B}}{|(e_{w1} - \mu_{\perp}) - \mu_{B})|}$$
(9)

$$e_{w2B}^{corrected} = \sqrt{|1 - ||\mu_{\perp}||_{2}^{2}|} * \frac{e_{w2B} - \mu_{B}}{|(e_{w2} - \mu_{\perp}) - \mu_{B})|}$$
(10)

$$e_1 = e_{w1R}^{corrected} + \mu_{\perp} \tag{11}$$

$$e_1 = e_{w1B}^{corrected} + \mu_{\perp}$$

$$e_2 = e_{w2B}^{corrected} + \mu_{\perp}$$
(11)

Exercise: Implement the function below. Use the equations above to get the final equalized version of the pair of words. Good luck!

```
In [ ]:
def equalize(pair, bias axis, word to vec map):
   Debias gender specific words by following the equalize method described in th
   Arguments:
   pair -- pair of strings of gender specific words to debias, e.g. ("actress",
   bias axis -- numpy-array of shape (50,), vector corresponding to the bias axi
   word to vec map -- dictionary mapping words to their corresponding vectors
   Returns
    e 1 -- word vector corresponding to the first word
    e 2 -- word vector corresponding to the second word
    ### START CODE HERE ###
    # Step 1: Select word vector representation of "word". Use word to vec map. (
   w1, w2 = None
    e w1, e w2 = None
    # Step 2: Compute the mean of e w1 and e w2 (≈ 1 line)
   mu = None
    # Step 3: Compute the projections of mu over the bias axis and the orthogonal
   mu B = None
   mu orth = None
    # Step 4: Use equations (7) and (8) to compute e w1B and e w2B (≈2 lines)
    e w1B = None
    e w2B = None
    # Step 5: Adjust the Bias part of e w1B and e w2B using the formulas (9) and
    corrected e w1B = None
    corrected_e_w2B = None
    # Step 6: Debias by equalizing el and e2 to the sum of their corrected project
    e1 = None
    e2 = None
```

return e1, e2

END CODE HERE

```
In []:

print("cosine similarities before equalizing:")
print("cosine_similarity(word_to_vec_map[\"man\"], gender) = ", cosine_similarity
print("cosine_similarity(word_to_vec_map[\"woman\"], gender) = ", cosine_similari
print()
e1, e2 = equalize(("man", "woman"), g, word_to_vec_map)
print("cosine similarities after equalizing:")
print("cosine_similarity(e1, gender) = ", cosine_similarity(e1, g))
```

print("cosine_similarity(e2, gender) = ", cosine_similarity(e2, g))

Expected Output:

cosine similarities before equalizing:

```
cosine_similarity(word_to_vec_map["man"], gender) = -0.117110957653
cosine_similarity(word_to_vec_map["woman"], gender) = 0.356666188463
```

cosine similarities after equalizing:

```
cosine_similarity(u1, gender) = -0.700436428931
cosine_similarity(u2, gender) = 0.700436428931
```

Please feel free to play with the input words in the cell above, to apply equalization to other pairs of words.

These debiasing algorithms are very helpful for reducing bias, but are not perfect and do not eliminate all traces of bias. For example, one weakness of this implementation was that the bias direction g was defined using only the pair of words woman and man. As discussed earlier, if g were defined by computing $g_1 = e_{woman} - e_{man}$; $g_2 = e_{mother} - e_{father}$; $g_3 = e_{girl} - e_{boy}$; and so on and averaging over them, you would obtain a better estimate of the "gender" dimension in the 50 dimensional word embedding space. Feel free to play with such variants as well.

Congratulations

You have come to the end of this notebook, and have seen a lot of the ways that word vectors can be used as well as modified.

Congratulations on finishing this notebook!

References:

- The debiasing algorithm is from Bolukbasi et al., 2016, <u>Man is to Computer Programmer as Woman is to Homemaker? Debiasing Word Embeddings (https://papers.nips.cc/paper/6228-man-is-to-computer-programmer-as-woman-is-to-homemaker-debiasing-word-embeddings.pdf)</u>
- The GloVe word embeddings were due to Jeffrey Pennington, Richard Socher, and Christopher D.
 Manning. (https://nlp.stanford.edu/projects/glove/)

Operations on word vectors

Welcome to your first assignment of this week!

Because word embeddings are very computionally expensive to train, most ML practitioners will load a pretrained set of embeddings.

After this assignment you will be able to:

- Load pre-trained word vectors, and measure similarity using cosine similarity
- Use word embeddings to solve word analogy problems such as Man is to Woman as King is to ___.
- Modify word embeddings to reduce their gender bias

Let's get started! Run the following cell to load the packages you will need.

```
In [36]:
end...
In [37]:

[[ 0.  0.]
[ 0.  0.]]
```

Next, lets load the word vectors. For this assignment, we will use 50-dimensional GloVe vectors to represent words. Run the following cell to load the word to vec map.

```
In [ ]:
```

You've loaded:

- words: set of words in the vocabulary.
- word to vec map: dictionary mapping words to their GloVe vector representation.

You've seen that one-hot vectors do not do a good job cpaturing what words are similar. GloVe vectors provide much more useful information about the meaning of individual words. Lets now see how you can use GloVe vectors to decide how similar two words are.

1 - Cosine similarity

To measure how similar two words are, we need a way to measure the degree of similarity between two embedding vectors for the two words. Given two vectors \$u\$ and \$v\$, cosine similarity is defined as follows:

 $\star \c \{||u||_2 ||v||_2\} = \cos(\theta) \$

where u.v is the dot product (or inner product) of two vectors, $||u||_2$ is the norm (or length) of the vector u, and t is the angle between u and v. This similarity depends on the angle between u and v. If u and v are very similar, their cosine similarity will be close to 1; if they are dissimilar, the cosine similarity will take a smaller value.

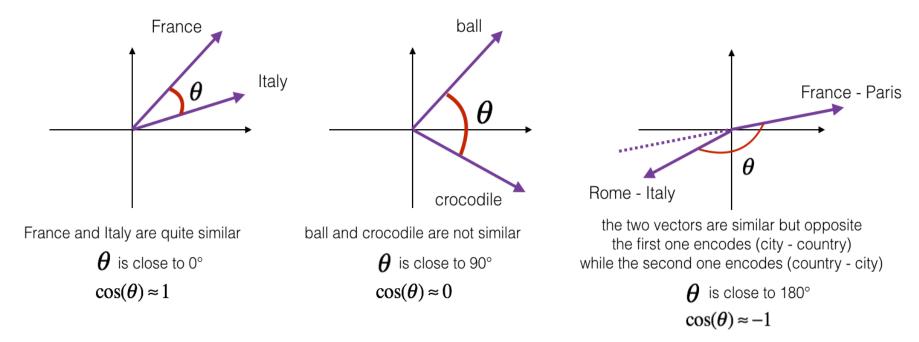


Figure 1: The cosine of the angle between two vectors is a measure of how similar they are

Exercise: Implement the function cosine_similarity() to evaluate similarity between word vectors.

Reminder: The norm of u is defined as $||u||_2 = \sqrt{i=1}^{n} u_i^2$

In [38]:

```
In [40]:
```

```
cosine_similarity(father, mother) = 0.890903844289
cosine_similarity(ball, crocodile) = 0.274392462614
cosine_similarity(france - paris, rome - italy) = -0.675147930817
```

In [41]:

```
cosine_similarity(france, italy) = 0.778863739208
cosine_similarity(paris, rome) = 0.709941134171
similarity of queen with (king-queen+woman): 0.860958125858
similarity of nurse with (mother-(father-doctor)): 0.846305950147
```

Expected Output:

cosine_similarity(father, mother) = 0.890903844289 cosine_similarity(ball, crocodile) = 0.274392462614 cosine_similarity(france - paris, rome - italy) = -0.675147930817 After you get the correct expected output, please feel free to modify the inputs and measure the cosine similarity between other pairs of words! Playing around the cosine similarity of other inputs will give you a better sense of how word vectors behave.

2 - Word analogy task

In the word analogy task, we complete the sentence "a is to b as c is to __". An example is 'man is to woman as king is to queen'. In detail, we are trying to find a word d, such that the associated word vectors e_a , e_b , e_c , e_d are related in the following manner: e_b - e_a \approx e_d - e_c . We will measure the similarity between e_b - e_a and e_d - e_c using cosine similarity.

Exercise: Complete the code below to be able to perform word analogies!

```
In [42]:
```

Run the cell below to test your code, this may take 1-2 minutes.

```
In [43]:
```

```
italy -> italian :: spain -> spanish
india -> delhi :: japan -> tokyo
man -> woman :: boy -> girl
small -> smaller :: large -> larger
```

```
In [31]:
```

```
read -> book :: write -> novel
small -> smaller :: big -> competitors
car -> foot :: computer -> 1.2-meter
```

Expected Output:

italy -> italian :: spain -> spanish

india -> delhi :: japan -> tokyo

man -> woman :: boy -> girl

small -> smaller :: large -> larger

Once you get the correct expected output, please feel free to modify the input cells above to test your own analogies. Try to find some other analogy pairs that do work, but also find some where the algorithm doesn't give the right answer: For example, you can try small->smaller as big->?.

Congratulations!

You've come to the end of this assignment. Here are the main points you should remember:

- Cosine similarity a good way to compare similarity between pairs of word vectors. (Though L2 distance works too.)
- For NLP applications, using a pre-trained set of word vectors from the internet is often a good way to get started.

Even though you have finished the graded portions, we recommend you take a look too at the rest of this notebook.

Congratulations on finishing the graded portions of this notebook!

3 - Debiasing word vectors (OPTIONAL/UNGRADED)

In the following exercise, you will examine gender biases that can be reflected in a word embedding, and explore algorithms for reducing the bias. In addition to learning about the topic of debiasing, this exercise will also help hone your intuition about what word vectors are doing. This section involves a bit of linear algebra, though you can probably complete it even without being expert in linear algebra, and we encourage you to give it a shot. This portion of the notebook is optional and is not graded.

Lets first see how the GloVe word embeddings relate to gender. You will first compute a vector \$g = e_{woman}-e_{man}\$, where \$e_{woman}\$ represents the word vector corresponding to the word *woman*, and \$e_{man}\$ corresponds to the word vector corresponding to the word *man*. The resulting vector \$g\$ roughly encodes the concept of "gender". (You might get a more accurate representation if you compute \$g_1 = e_{mother}-e_{father}\$, \$g_2 = e_{girl}-e_{boy}\$, etc. and average over them. But just using \$e_{woman}-e_{man}\$ will give good enough results for now.)

In [45]:

[-0.087144 5	0.2182	-0.40986	-0.03922	-0.1032	0.9416
-0.06042 4	0.32988	0.46144	-0.35962	0.31102	-0.8682
0.96006	0.01073	0.24337	0.08193	-1.02722	-0.2112
0.695044	-0.00222	0.29106	0.5053	-0.099454	0.4044
0.30181	0.1355	-0.0606	-0.07131	-0.19245	-0.0611
-0.3204 57	0.07165	-0.13337	-0.25068714	-0.14293	-0.2249
-0.149 6	0.048882	0.12191	-0.27362	-0.165476	-0.2042
0.54376	-0.271425	-0.10245	-0.32108	0.2516	-0.3345
-0.04371	0.01258]			

Now, you will consider the cosine similarity of different words with \$g\$. Consider what a positive value of similarity means vs a negative cosine similarity.

```
In [46]:
```

```
List of names and their similarities with constructed vector: john -0.23163356146
marie 0.315597935396
sophie 0.318687898594
ronaldo -0.312447968503
priya 0.17632041839
rahul -0.169154710392
danielle 0.243932992163
reza -0.079304296722
katy 0.283106865957
yasmin 0.233138577679
```

As you can see, female first names tend to have a positive cosine similarity with our constructed vector \$g\$, while male first names tend to have a negative cosine similarity. This is not suprising, and the result seems acceptable.

But let's try with some other words.

In [47]:

```
lipstick 0.276919162564
quns -0.18884855679
science -0.0608290654093
arts 0.00818931238588
literature 0.0647250443346
warrior -0.209201646411
doctor 0.118952894109
tree -0.0708939917548
receptionist 0.330779417506
technology -0.131937324476
fashion 0.0356389462577
teacher 0.179209234318
engineer -0.0803928049452
pilot 0.00107644989919
computer -0.103303588739
singer 0.185005181365
```

Other words and their similarities:

Do you notice anything surprising? It is astonishing how these results reflect certain unhealthy gender stereotypes. For example, "computer" is closer to "man" while "literature" is closer to "woman". Ouch!

We'll see below how to reduce the bias of these vectors, using an algorithm due to <u>Boliukbasi et al., 2016 (https://arxiv.org/abs/1607.06520)</u>. Note that some word pairs such as "actor"/"actress" or "grandmother"/"grandfather" should remain gender specific, while other words such as "receptionist" or "technology" should be neutralized, i.e. not be gender-related. You will have to treat these two type of words differently when debiasing.

3.1 - Neutralize bias for non-gender specific words

The figure below should help you visualize what neutralizing does. If you're using a 50-dimensional word embedding, the 50 dimensional space can be split into two parts: The bias-direction \$g\$, and the remaining 49 dimensions, which we'll call \$g_{\perp}\$. In linear algebra, we say that the 49 dimensional \$g_{\perp}\$ is perpendicular (or "othogonal") to \$g\$, meaning it is at 90 degrees to \$g\$. The neutralization step takes a vector such as \$e_{\text{receptionist}}\$ and zeros out the component in the direction of \$g\$, giving us \$e_{\text{receptionist}}^{\text{debiased}}\$.

Even though \$g_{\perp}\$ is 49 dimensional, given the limitations of what we can draw on a screen, we illustrate it using a 1 dimensional axis below.

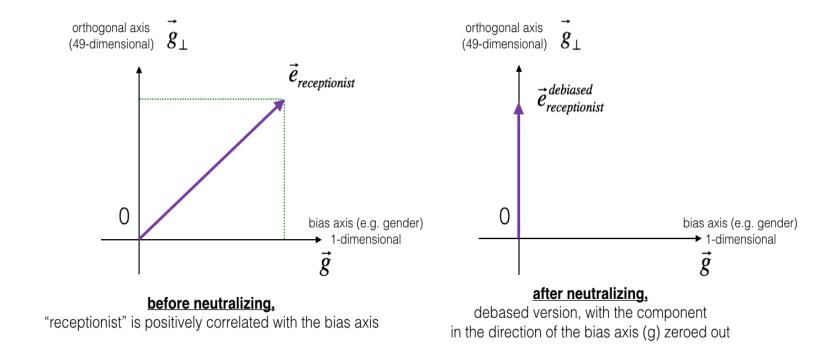


Figure 2: The word vector for "receptionist" represented before and after applying the neutralize operation.

Exercise: Implement neutralize() to remove the bias of words such as "receptionist" or "scientist". Given an input embedding \$e\$, you can use the following formulas to compute \$e^{debiased}:

 $\ensuremath{\$e^{bias_component} = \frac{e \cdot g}{\|g\|_2^2} * g \cdot g} $$

If you are an expert in linear algebra, you may recognize \$e^{bias_component}\$ as the projection of \$e\$ onto the direction \$g\$. If you're not an expert in linear algebra, don't worry about this.

```
In [51]:
```

```
cosine similarity between receptionist and g, before neutralizing: 0.330779417506 cosine similarity between receptionist and g, after neutralizing: 5.60374039375e-17
```

Expected Output: The second result is essentially 0, up to numerical roundof (on the order of \$10^{-17}\$).

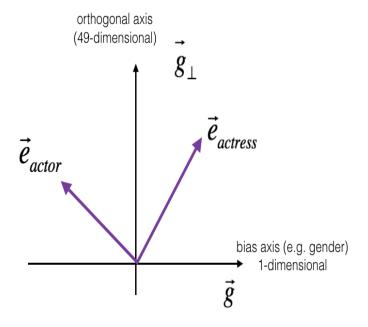
cosine similarity between receptionist and g, before neutralizing: 0.330779417506

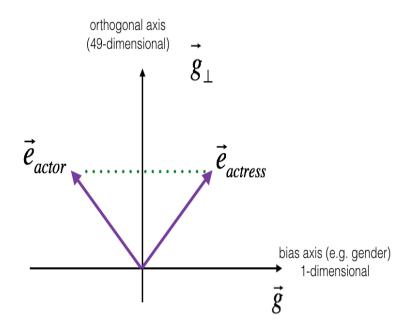
cosine similarity between receptionist and g, after neutralizing: -3.26732746085e-17

3.2 - Equalization algorithm for gender-specific words

Next, lets see how debiasing can also be applied to word pairs such as "actress" and "actor." Equalization is applied to pairs of words that you might want to have differ only through the gender property. As a concrete example, suppose that "actress" is closer to "babysit" than "actor." By applying neutralizing to "babysit" we can reduce the gender-stereotype associated with babysitting. But this still does not guarantee that "actor" and "actress" are equidistant from "babysit." The equalization algorithm takes care of this.

The key idea behind equalization is to make sure that a particular pair of words are equi-distant from the 49-dimensional \$g_\perp\$. The equalization step also ensures that the two equalized steps are now the same distance from \$e_{receptionist}^{debiased}\$, or from any other work that has been neutralized. In pictures, this is how equalization works:





before equalizing,

"actress" and "actor" differ in many ways beyond the direction of \vec{g}

after equalizing,

"actress" and "actor" differ only in the direction of \vec{g} , and further are equal in distance from \vec{g}_1

The derivation of the linear algebra to do this is a bit more complex. (See Bolukbasi et al., 2016 for details.) But the key equations are:

 $\m = \frac{e_{w1} + e_{w2}}{2} \tan{4}$

 $\$ \mu_{B} = \frac {\mu \cdot \text{bias_axis}}{\\\text{bias_axis}_2^2\} *\text{bias_axis} \tag{5}\$\$

\$\$\mu_{\perp} = \mu - \mu_{B} \tag{6}\$\$

 $\ensuremath{\$e_{w1B}^{corrected} = \sqrt{|\{1 - ||\mu_{\varepsilon}\}|^2_2\}|} * \frac{e_{\star w1B}} - \mu_B {|(e_{w1} - \mu_{\varepsilon}) - \mu_B)|} \ensuremath{\$g} - \mu_B {|(e_{w1} - \mu_{\varepsilon}) - \mu_B)|} \ensuremath{\$g} - \mu_B {|(e_{w1} - \mu_B)|} - \mu_B {|(e_{w1} - \mu_B)|$

 $\$ e_{w2B}^{corrected} = $\left\{ |\{1 - \|\mu_{\perp} \|^2_2\} |\} * \frac{e_{\xy2B}} - \mu_B \left\{ |(e_{\xy2B} - \mu_B)| \right\} \right\}$

 $= e_{w1B}^{corrected} + \sum_{1}^{corrected} +$

Exercise: Implement the function below. Use the equations above to get the final equalized version of the pair of words. Good luck!

In []:

In []:

Expected Output:

cosine similarities before equalizing:

```
cosine_similarity(word_to_vec_map["man"], gender) = -0.117110957653
cosine_similarity(word_to_vec_map["woman"], gender) = 0.356666188463
```

cosine similarities after equalizing:

```
cosine_similarity(u1, gender) = -0.700436428931

cosine_similarity(u2, gender) = 0.700436428931
```

Please feel free to play with the input words in the cell above, to apply equalization to other pairs of words.

These debiasing algorithms are very helpful for reducing bias, but are not perfect and do not eliminate all traces of bias. For example, one weakness of this implementation was that the bias direction \$g\$ was defined using only the pair of words *woman* and *man*. As discussed earlier, if \$g\$ were defined by computing \$g_1 = e_{woman} - e_{man}\$; \$g_2 = e_{mother} - e_{father}\$; \$g_3 = e_{girl} - e_{boy}\$; and so on and averaging over them, you would obtain a better estimate of the "gender" dimension in the 50 dimensional word embedding space. Feel free to play with such variants as well.

Congratulations

You have come to the end of this notebook, and have seen a lot of the ways that word vectors can be used as well as modified.

Congratulations on finishing this notebook!

References:

- The debiasing algorithm is from Bolukbasi et al., 2016, <u>Man is to Computer Programmer as Woman is to Homemaker? Debiasing Word Embeddings (https://papers.nips.cc/paper/6228-man-is-to-computer-programmer-as-woman-is-to-homemaker-debiasing-word-embeddings.pdf)</u>
- The GloVe word embeddings were due to Jeffrey Pennington, Richard Socher, and Christopher D.
 Manning. (https://nlp.stanford.edu/projects/glove/))