

# PHOTOLYSIS

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# Atmospheric Oxygen Species

## Thermodynamic vs. Actual

Normal O<sub>2</sub> molecules

$$\Delta H_f \text{ kcal mol}^{-1}$$

0

34.1

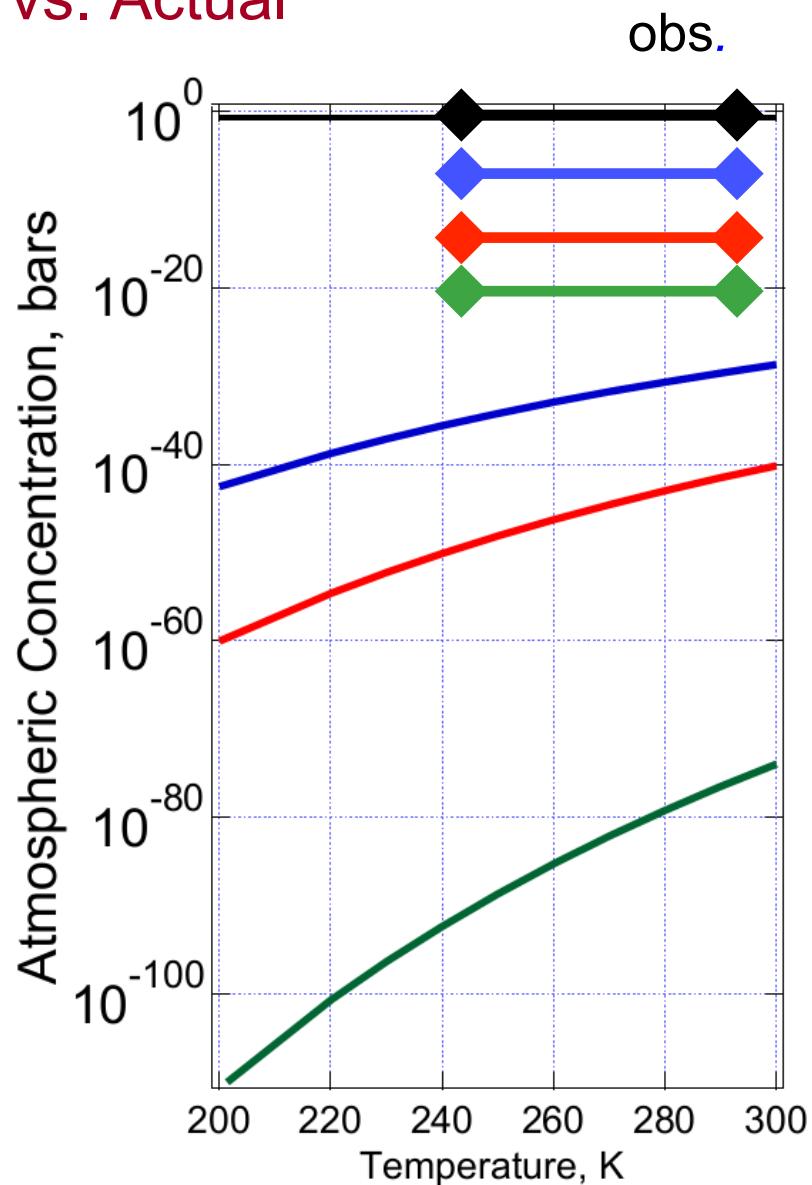
Ozone, O<sub>3</sub>

59.6

Ground state atoms, O

104.9

Excited atoms, O\*



# Photochemistry

Energy input from sunlight, e.g.



## Some Important Photolysis Reactions

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$O_2 + h\nu (\lambda < 240 \text{ nm}) \rightarrow O + O$	source of $O_3$ in stratosphere
$O_3 + h\nu (\lambda < 340 \text{ nm}) \rightarrow O_2 + O(^1D)$	source of OH in troposphere
$NO_2 + h\nu (\lambda < 420 \text{ nm}) \rightarrow NO + O(^3P)$	source of $O_3$ in troposphere
$CH_2O + h\nu (\lambda < 330 \text{ nm}) \rightarrow H + HCO$	source of HOx, everywhere
$H_2O_2 + h\nu (\lambda < 360 \text{ nm}) \rightarrow OH + OH$	source of OH in remote atm.
$HONO + h\nu (\lambda < 400 \text{ nm}) \rightarrow OH + NO$	source of radicals in urban atm.

# Quantifying Photolysis Processes

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Photolysis reaction:



Photolysis rates:

$$\frac{d[AB]}{dt} \Big|_{h\nu} = -J[AB]$$

$$\frac{d[A]}{dt} \Big|_{h\nu} = \frac{d[B]}{dt} \Big|_{h\nu} = +J[AB]$$

Photolysis frequency ( $s^{-1}$ )     $J = \int_{\lambda} F(\lambda) \sigma(\lambda) \phi(\lambda) d\lambda$

(other names: photo-dissociation rate coefficient, J-value)

# CALCULATION OF PHOTOLYSIS COEFFICIENTS

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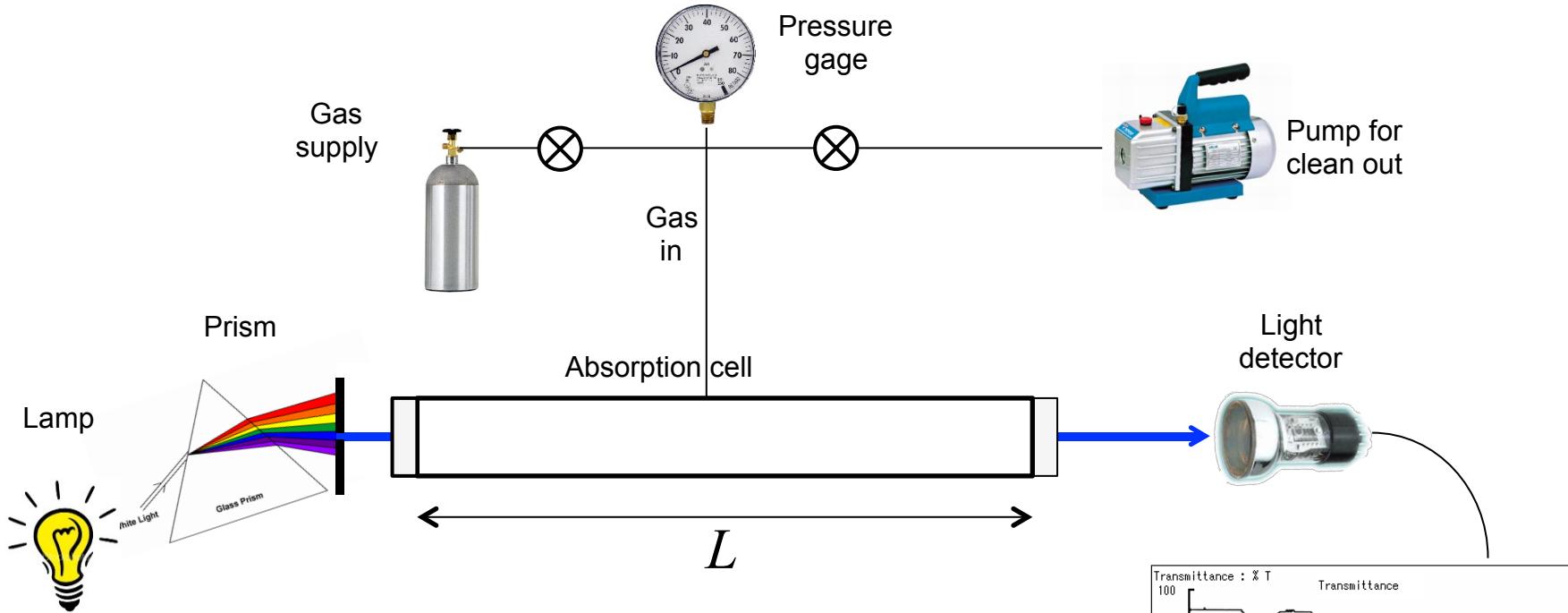
$$J \text{ (s}^{-1}\text{)} = \int_{\lambda} F(\lambda) \sigma(\lambda) \phi(\lambda) d\lambda$$

$F(\lambda)$  = spectral actinic flux, quanta  $\text{cm}^{-2} \text{s}^{-1} \text{nm}^{-1}$   
 $\propto$  probability of photon near molecule.

$\sigma(\lambda)$  = absorption cross section,  $\text{cm}^2 \text{ molec}^{-1}$   
 $\propto$  probability that photon is absorbed.

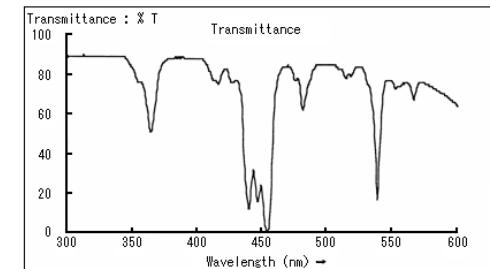
$\phi(\lambda)$  = photodissociation quantum yield,  $\text{molec quanta}^{-1}$   
 $\propto$  probability that absorbed photon causes dissociation.

# Measurement of Absorption Cross Section $\sigma(\lambda)$



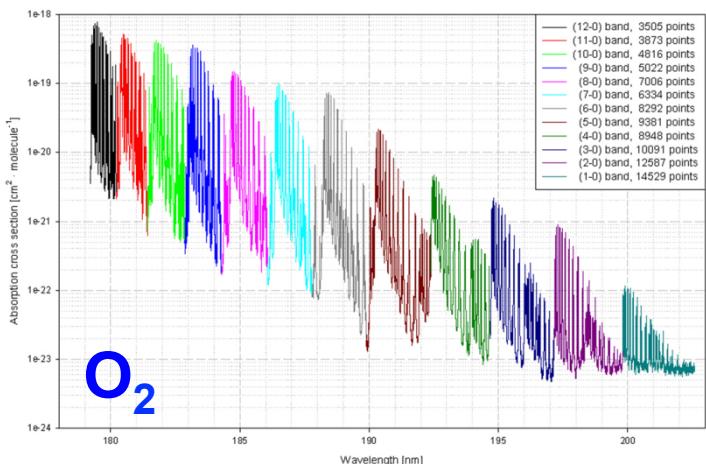
$$\text{Transmittance} = I / I_0 = \exp(-\sigma n L)$$

$$\sigma = -1/(nL) \ln(I/I_0)$$

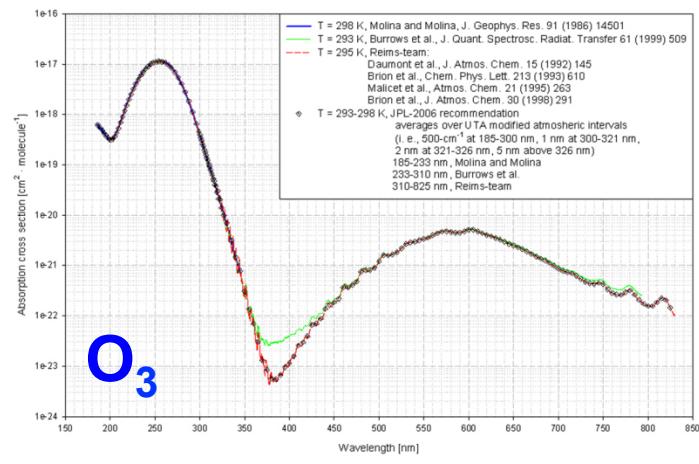


Easy: measure pressure ( $n = P/RT$ ), and relative change in light:  $I / I_0$

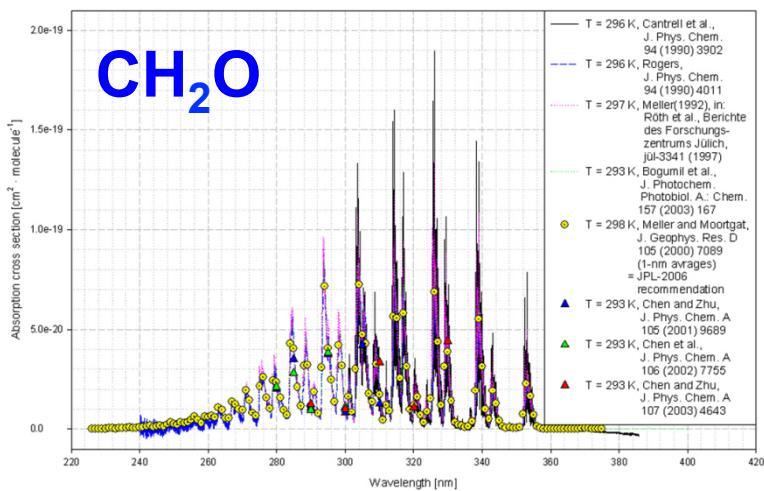
# Absorption cross sections $\sigma(\lambda, T)$



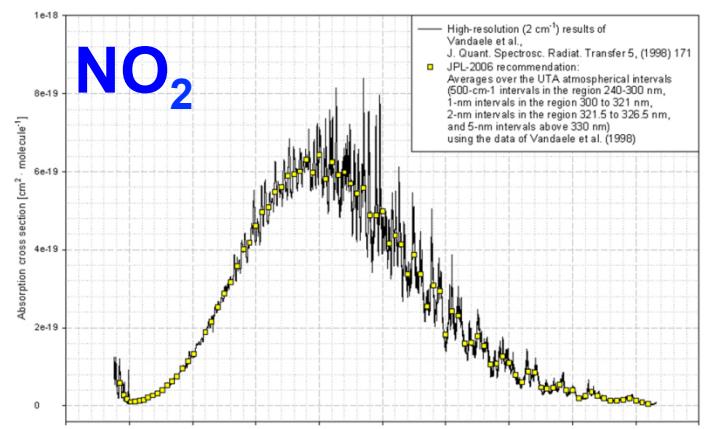
Absorption cross sections in the Schumann-Runge region of oxygen O<sub>2</sub> at 300 K,  
Yoshino et al., Planet. Space Sci. 40 (1992) 185



Absorption cross sections of ozone O<sub>3</sub> at room temperature  
Evaluation for JPL-2006 recommendation

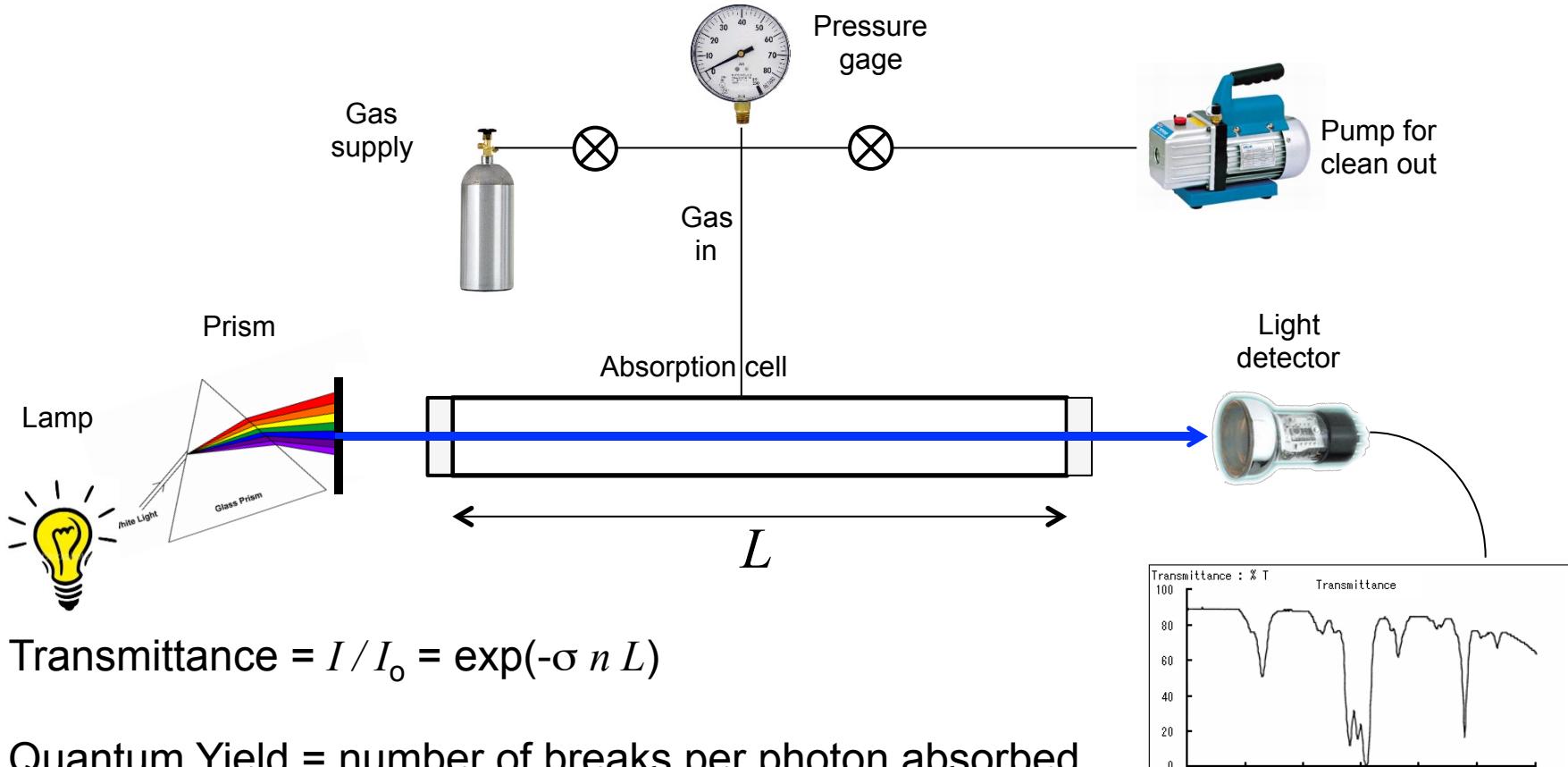


Absorption cross sections of formaldehyde CH<sub>2</sub>O at room temperature (results 1990-2003)



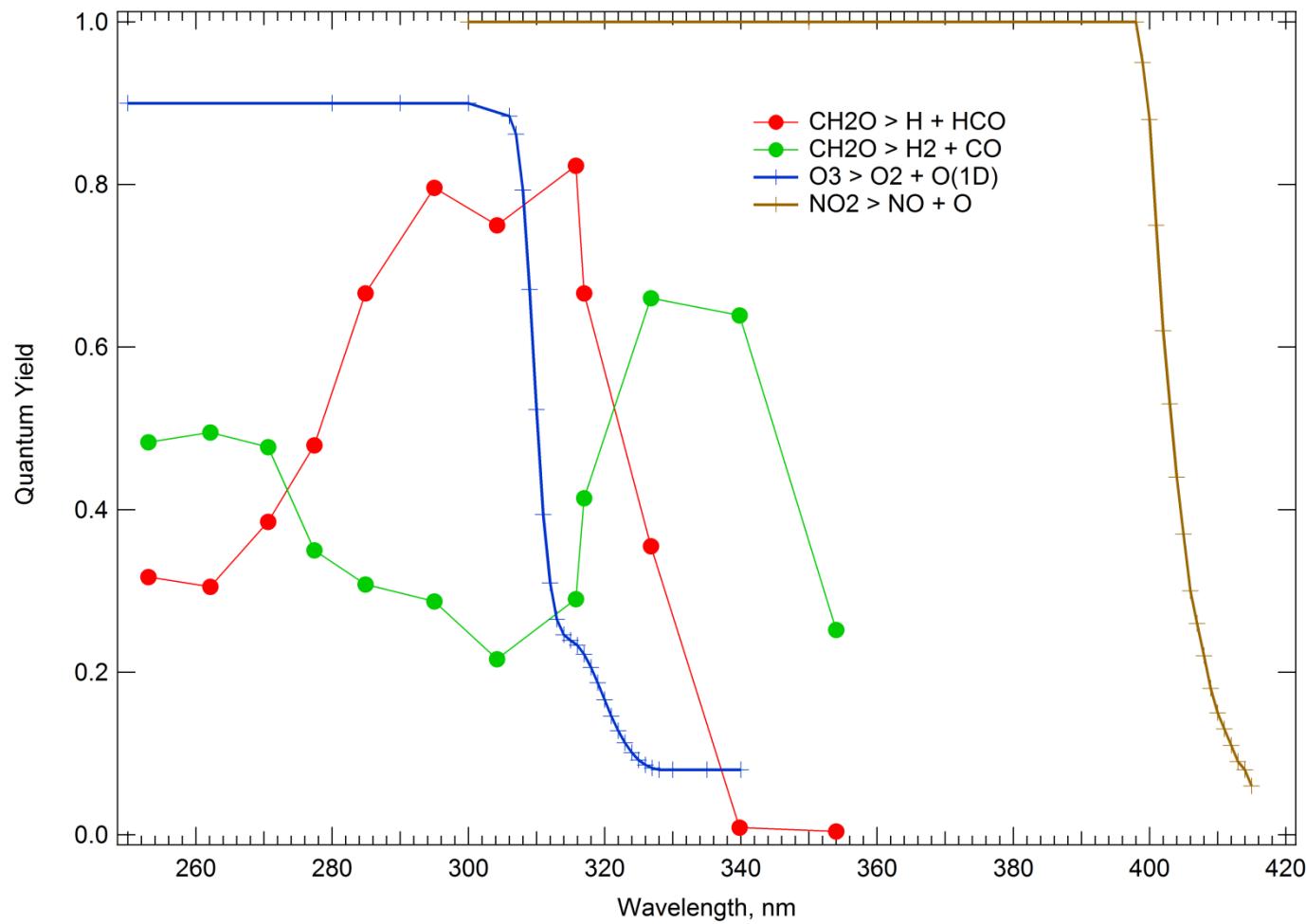
Absorption cross sections of nitrogen dioxide NO<sub>2</sub> at 294 K  
Results from the year 1998 and JPL-2006 recommendation

# Measurement of Quantum Yields $\phi(\lambda)$



Difficult: must measure absolute change in  $n$  (products) and  $I$  (photons absorbed)

# Photo-dissociation Quantum Yields $\phi(\lambda, T, P)$



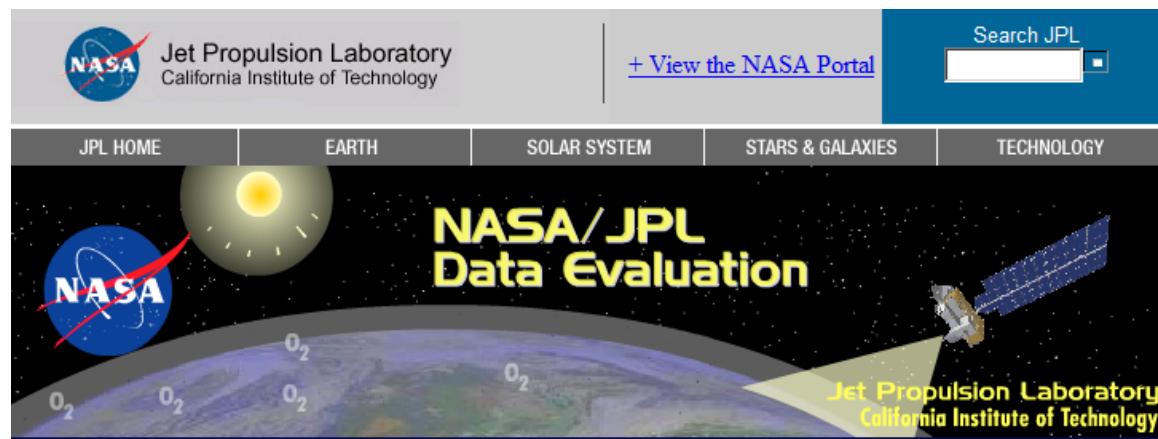
# Compilations of Cross Sections & Quantum Yields

<http://www.atmosphere.mpg.de/enid/2295>



**MPI-Mainz-UV-VIS Spectral Atlas of Gaseous Molecules**  
A Database of Atmospherically Relevant Species, Including Numerical Data and Graphical Representations  
Hannelore Keller-Rudek, Geert K. Moortgat  
Max-Planck-Institut für Chemie, Atmospheric Chemistry Division, Mainz, Germany

<http://jpldataeval.jpl.nasa.gov/>



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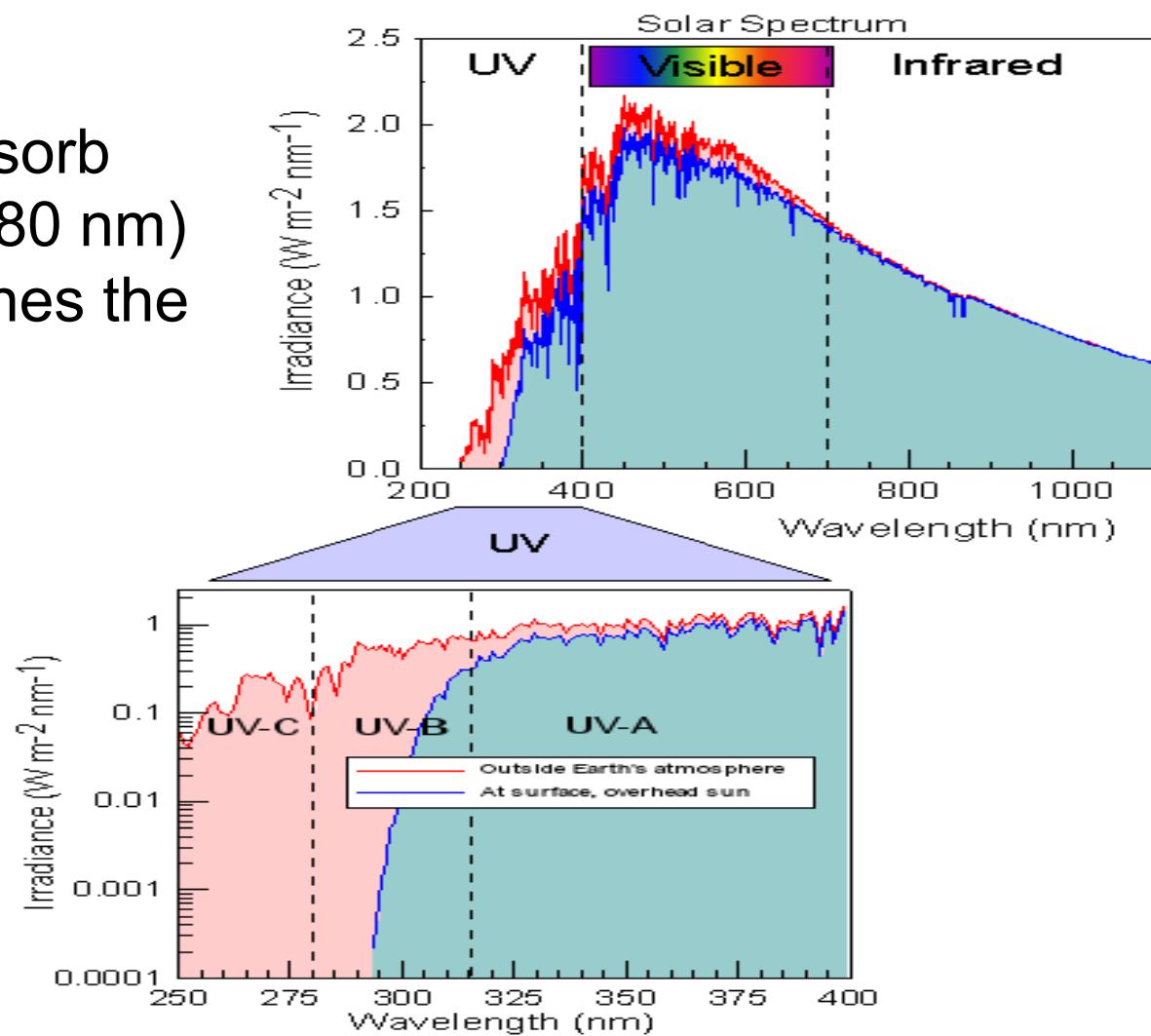
**NASA/JPL Data Evaluation**

Jet Propulsion Laboratory California Institute of Technology

# RADIATIVE TRANSFER CONCEPTS

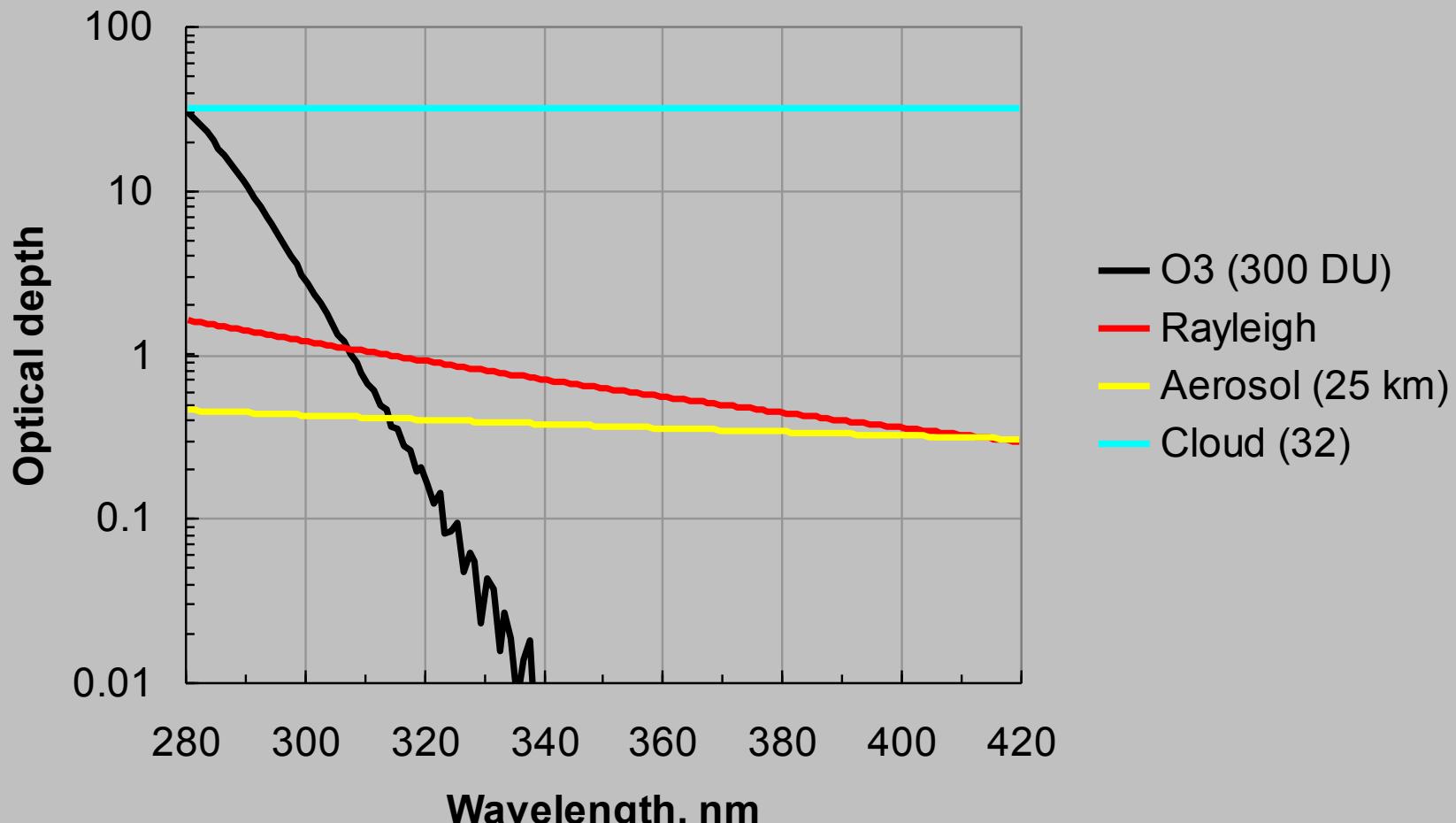
# Solar Spectrum

$O_2$  and  $O_3$  absorb all UV-C ( $\lambda < 280$  nm) before it reaches the troposphere



# Atmospheric Optical Depths, $\tau$

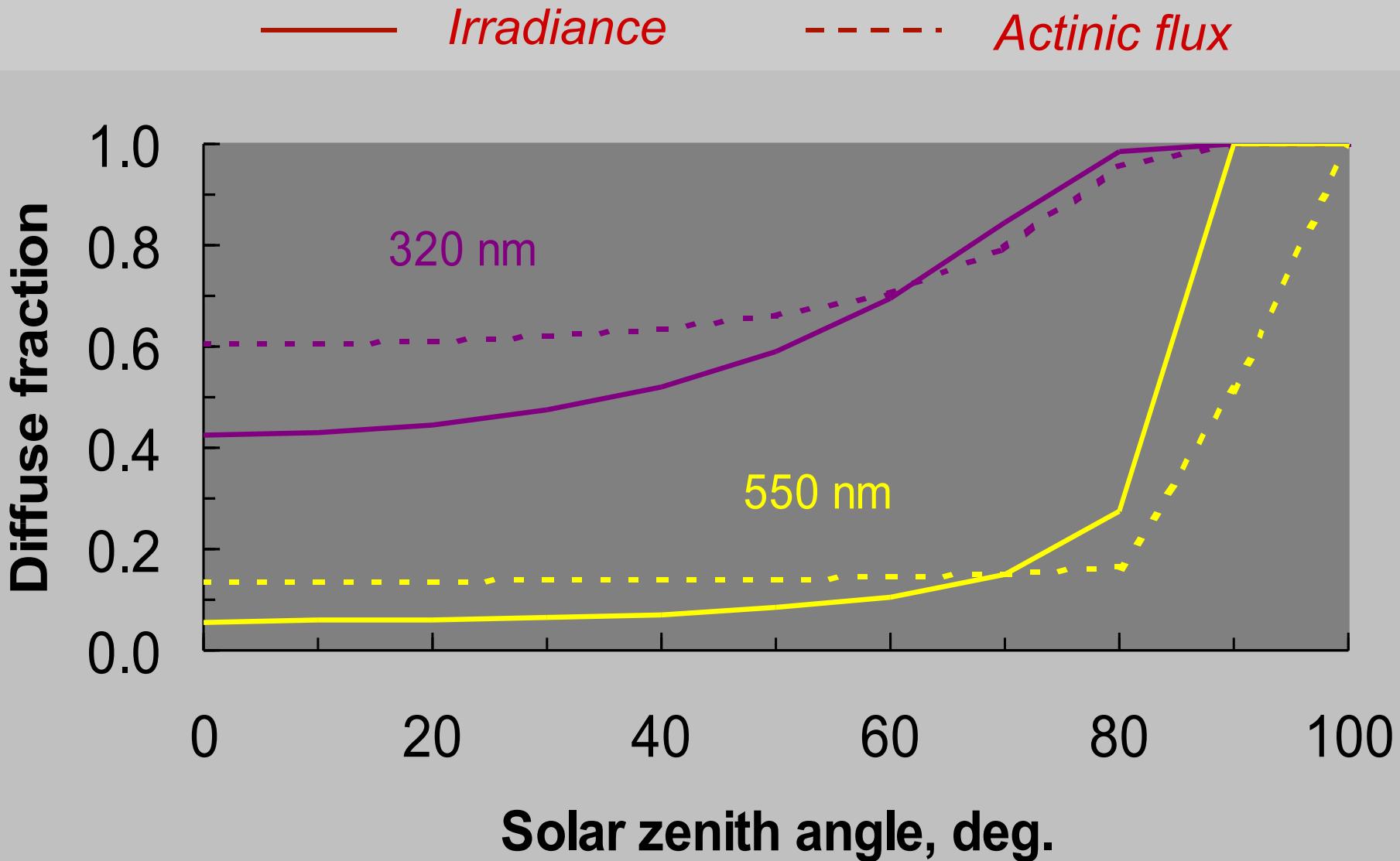
defined by Transmission of a vertical beam =  $\exp(-\tau)$



Diffuse transmission can be much larger

# UV: Diffuse Radiation $\geq$ Direct Solar Beam

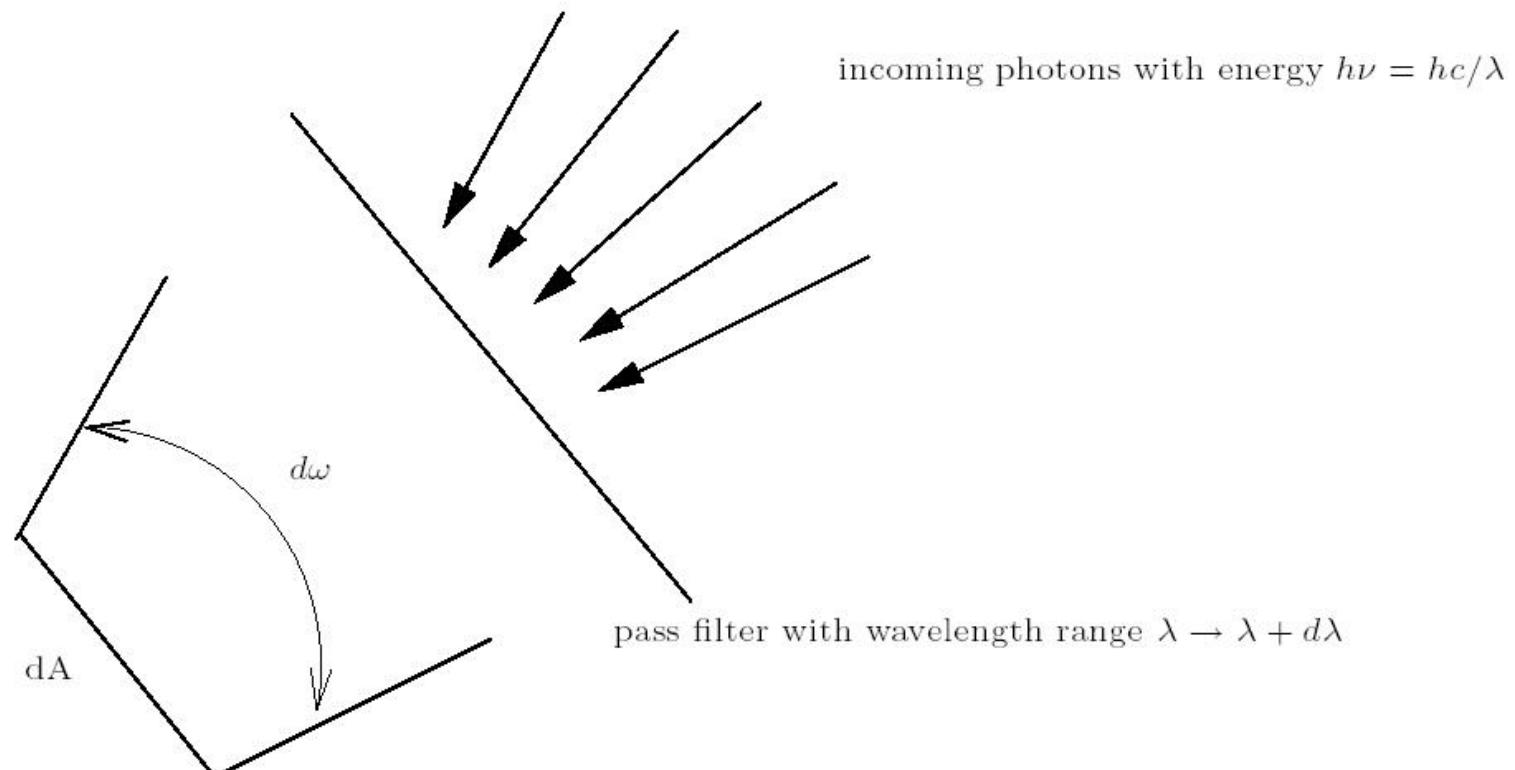
clean skies, sea level



# Spectral Radiance, $I$

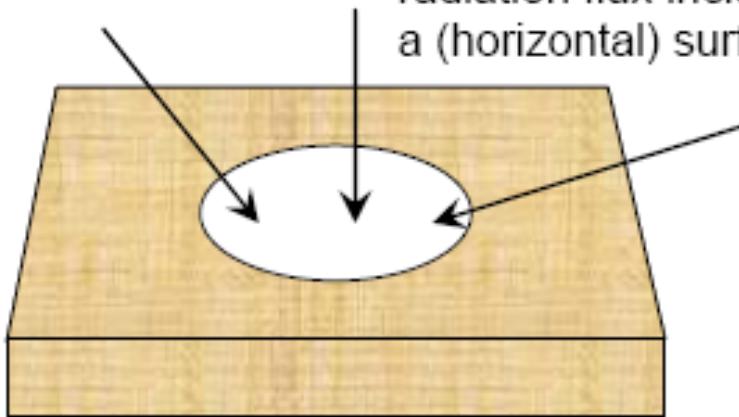
$$I(\lambda, \theta, \phi) = N(hc/\lambda) / (dt dA d\omega d\lambda)$$

units:  $J s^{-1} m^{-2} sr^{-1} nm^{-1}$

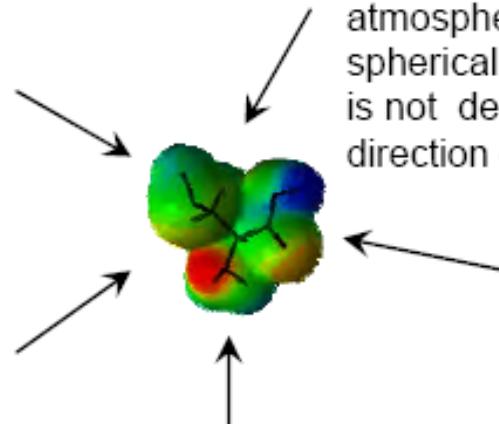


(old name = Specific Intensity)

# INTEGRALS OVER ANGULAR INCIDENCE



**Irradiance:** The radiation flux incident on a (horizontal) surface.



**Actinic flux:** The photochemically active radiation flux in the earth's atmosphere. This flux is spherically integrated and is not dependent the direction of the radiation.

$$E = \iint_0^{\frac{\pi}{2}} I(\theta, \varphi) \cos \theta \sin \theta d\theta d\varphi$$

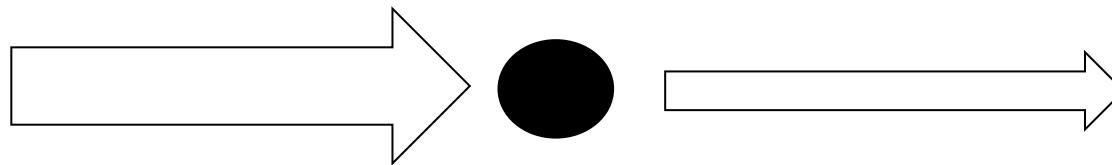
Watts m<sup>-2</sup>

$$F = \iint_0^{2\pi} I(\theta, \varphi) \sin \theta d\varphi d\theta$$

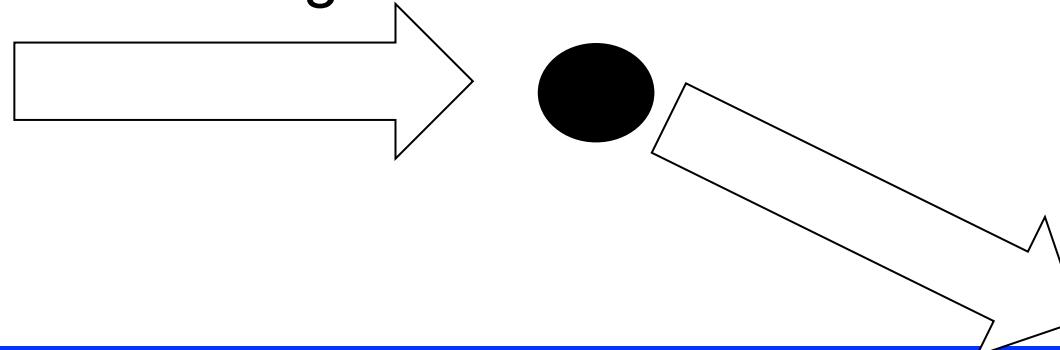
Watts m<sup>-2</sup> or quanta s<sup>-1</sup> cm<sup>-2</sup>

# Absorption and Scattering

- **Absorption** – inelastic, loss of radiant energy:



- **Scattering** – elastic, radiant energy is conserved, direction changes:

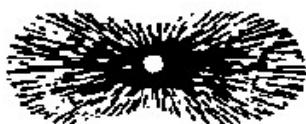


# SCATTERING PHASE FUNCTIONS

$$P(\theta, \phi; \theta', \phi')$$

Small Particles (a)

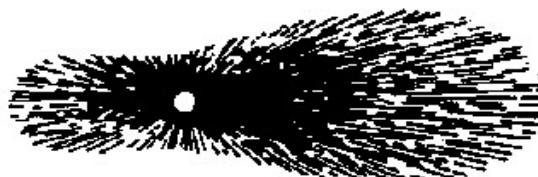
→  
Incident  
beam



Size: smaller than one-tenth the wavelength of light  
Description: symmetric

Large Particles (b)

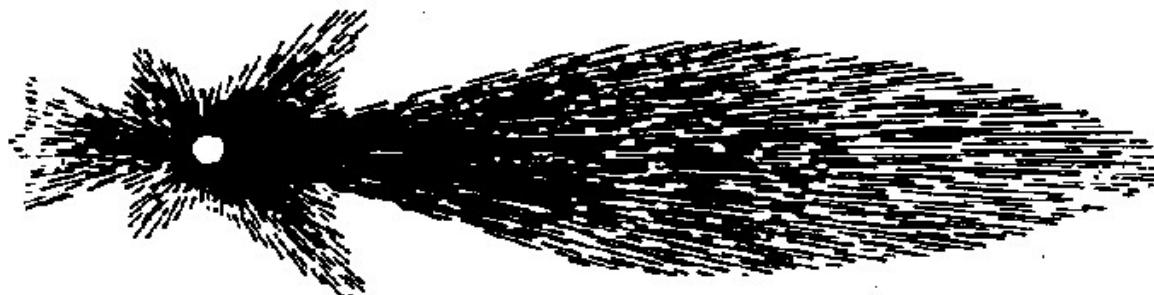
→  
Incident  
beam



Size: approximately one-fourth the wavelength of light  
Description: scattering concentrated in forward direction

Larger Particles (c)

→  
Incident  
beam



Size: larger than the wavelength of light  
Description: extreme concentration of scattering in forward direction;  
development of maxima and minima of scattering at  
wider angles

# The Radiative Transfer Equation

*Propagation derivative*

*Beer-Lambert  
attenuation*

*Scattering from  
direct solar beam*

$$\cos \theta \frac{dI(\tau, \theta, \phi)}{d\tau}$$

$$- I(\tau, \theta, \phi)$$

$$+ \frac{\omega_o}{4\pi} F_\infty e^{-\tau/\cos \theta_o} P(\theta, \phi; \theta_o, \phi_o) +$$

$$+ \frac{\omega_o}{4\pi} \int_0^{2\pi} \int_{-1}^{+1} I(\tau, \theta', \phi') P(\theta, \phi; \theta', \phi') d\cos \theta' d\phi'$$

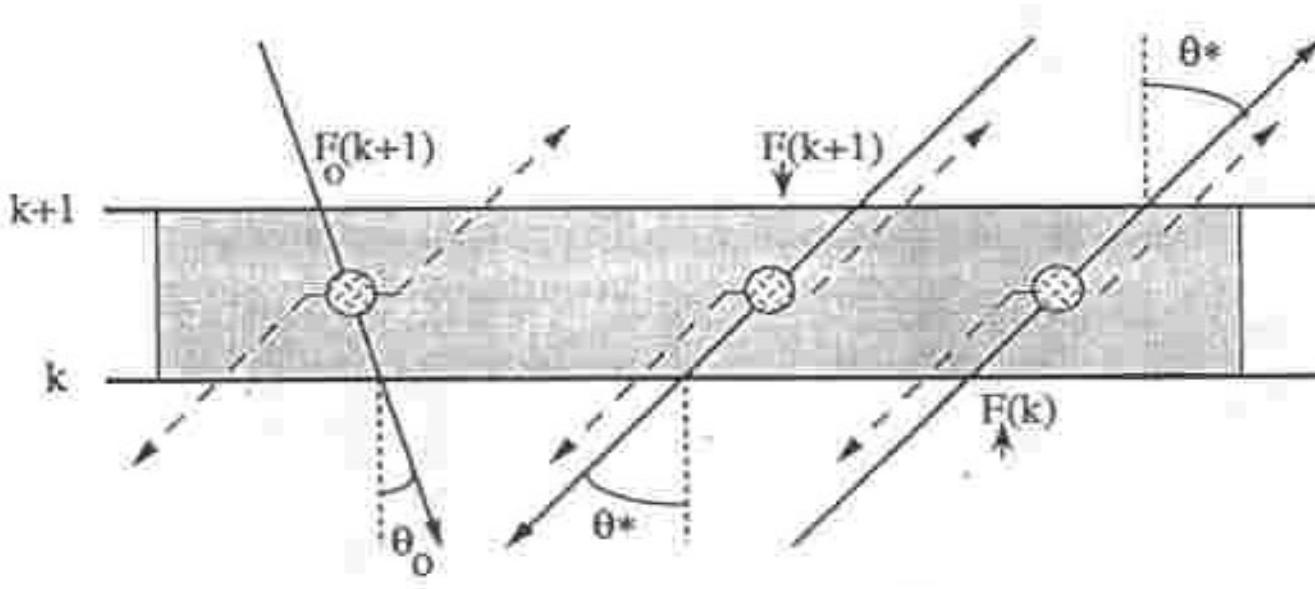
*Scattering from diffuse light  
(multiple scattering)*

# NUMERICAL SOLUTIONS TO RADIATIVE TRANSFER EQUATION

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- Discrete ordinates
  - n-streams ( $n = \text{even}$ ), angular distribution exact as  $n \rightarrow \infty$  but speed  $\propto 1/n^2$
- Two-stream family
  - delta-Eddington, many others
  - very fast but not exact
- Monte Carlo
  - slow, but ideal for 3D problems
- Others
  - matrix operator, Feautrier, adding-doubling, successive orders, etc.

# Multiple Atmospheric Layers Each Assumed to be Homogeneous



Must specify three optical properties:

Optical depth,  $\Delta\tau$

Single scattering albedo,  $\omega_o = \text{scatt.}/(\text{scatt.}+\text{abs.})$

Asymmetry factor,  $g$ : forward fraction  $\sim (1+g)/2$

## For each layer, must specify $\Delta\tau$ , $\omega_o$ , $g$ :

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1. Vertical optical depth,  $\Delta\tau(\lambda, z) = \sigma(\lambda, z) n(z) \Delta z$

for molecules:  $\Delta\tau(\lambda, z) \sim 0 - 30$

Rayleigh scatt.  $\sim 0.1 - 1.0 \sim \lambda^{-4}$   
 $O_3$  absorption  $\sim 0 - 30$

for aerosols:  $0.01 - 5.0$       Mie scatt.       $\Delta\tau(\lambda, z) \sim \lambda^{-\alpha}$   
 $(\alpha = \text{Angstrom exponent})$

for clouds:  $1-1000$

$\alpha \sim 0$   
cirrus  $\sim 1-5$   
cumulonimbus  $\sim > 100$

## For each layer, must specify $\Delta\tau$ , $\omega_o$ , $g$ :

---

2. Single scattering albedo,  $\omega_o(\lambda, z) = \text{scatt.}/(\text{scatt.+abs.})$

range 0 - 1

limits: pure scattering = 1.0  
pure absorption = 0.0

for molecules, strongly  $\lambda$ -dependent, depending on absorber amount, esp. O<sub>3</sub>

for aerosols:

sulfate ~ 0.99  
soot, organics ~ 0.8 or less,  
not well known but probably higher  
at shorter  $\lambda$ , esp. in UV

for clouds: typically 0.9999 or larger (vis and UV)

## For each layer, must specify $\Delta\tau$ , $\omega_o$ , $g$ :

### 3. Asymmetry factor, $g(\lambda, z)$ = first moment of phase function

range -1 to + 1

pure back-scattering = -1

isotropic or Rayleigh = 0

pure forward scattering = +1

$$g = \frac{1}{2} \int_{-1}^{+1} P(\Theta) \cos \Theta d(\cos \Theta)$$

strongly dependent on particle size

for aerosols:, typically 0.5-0.7

for clouds, typically 0.7-0.9

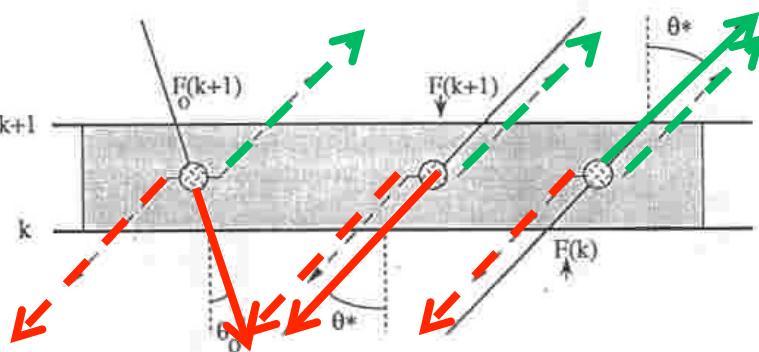
*Mie theory for spherical particles: can compute  $\Delta\tau$ ,  $\omega_o$ ,  $g$  from knowledge of  $\lambda$ , particle radius and complex index of refraction*

# SIMPLE 2-STREAM METHOD: 3 Equations for each layer

$$F_o(k) = F_o(k+1)e^{-\Delta\tau / \cos \theta_o}$$

$$F_{\downarrow}(k) = F_{\downarrow}(k+1)e^{-\Delta\tau / \cos \theta^*} + f\omega_o F_o(k+1)(1 - e^{-\Delta\tau / \cos \theta_o}) + f\omega_o F_{\downarrow}(k+1)(1 - e^{-\Delta\tau / \cos \theta^*}) + (1-f)\omega_o F_{\uparrow}(k)(1 - e^{-\Delta\tau / \cos \theta^*})$$

$$F_{\uparrow}(k+1) = F_{\uparrow}(k)e^{-\Delta\tau / \cos \theta^*} + (1-f)\omega_o F_o(k+1)(1 - e^{-\Delta\tau / \cos \theta_o}) + (1-f)\omega_o F_{\uparrow}(k)(1 - e^{-\Delta\tau / \cos \theta^*}) + f\omega_o F_{\downarrow}(k)(1 - e^{-\Delta\tau / \cos \theta^*})$$



subject to the boundary conditions

at top ( $k = N$ ):  $F_o(N) = F_{\infty} \cos \theta_o$  and  $F_{\downarrow}(N) = 0$

at bottom ( $k = 1$ ):  $F_{\uparrow}(1) = A[F_o(1) + F_{\downarrow}(1)]$

# AEROSOLS

# Many different types of aerosols

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- Size distributions
- Composition (size-dependent)

Need to determine aerosol optical properties:

$\tau(\lambda)$  = optical depth

$\omega_o$  = single scattering albedo

$P(\Theta)$  = phase function or  $g$  = asymmetry factor

# Mie Scattering Theory

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For spherical particles, given:

Complex index of refraction:  $n = m + ik$

Size parameter:  $\alpha = 2\pi r / \lambda$

Can compute:

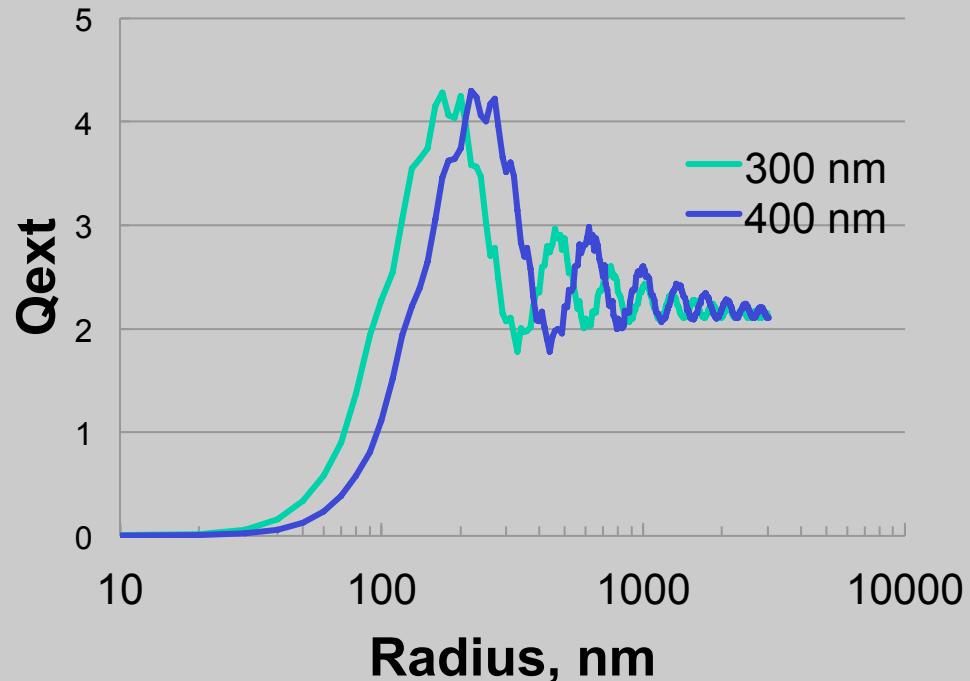
Extinction efficiency  $Q_e(\alpha, n) \propto \pi r^2$

Scattering efficiency  $Q_s(\alpha, n) \propto \pi r^2$

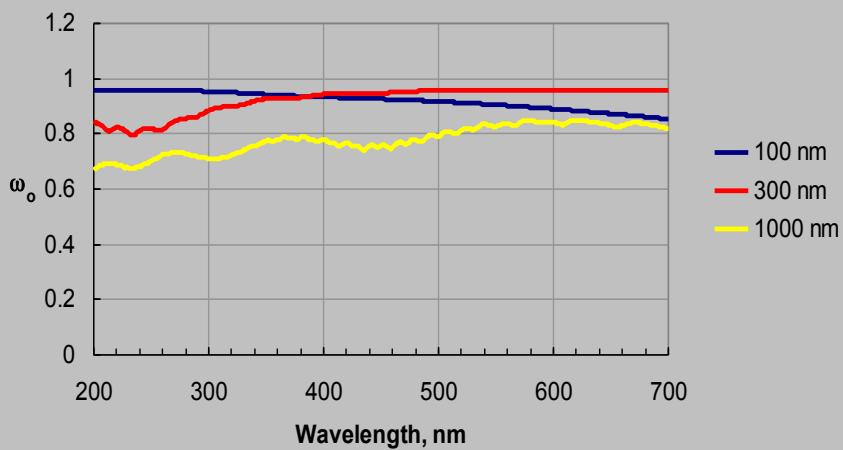
Phase function  
or asymmetry factor  $P(\Theta, \alpha, n)$   
 $g(\alpha, n)$

# Mie Theory Typical Results

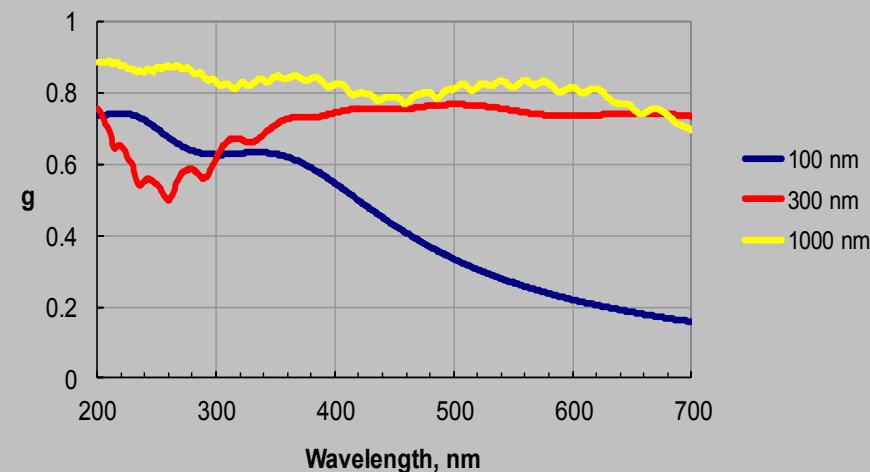
$$\alpha = 2\pi r / \lambda$$



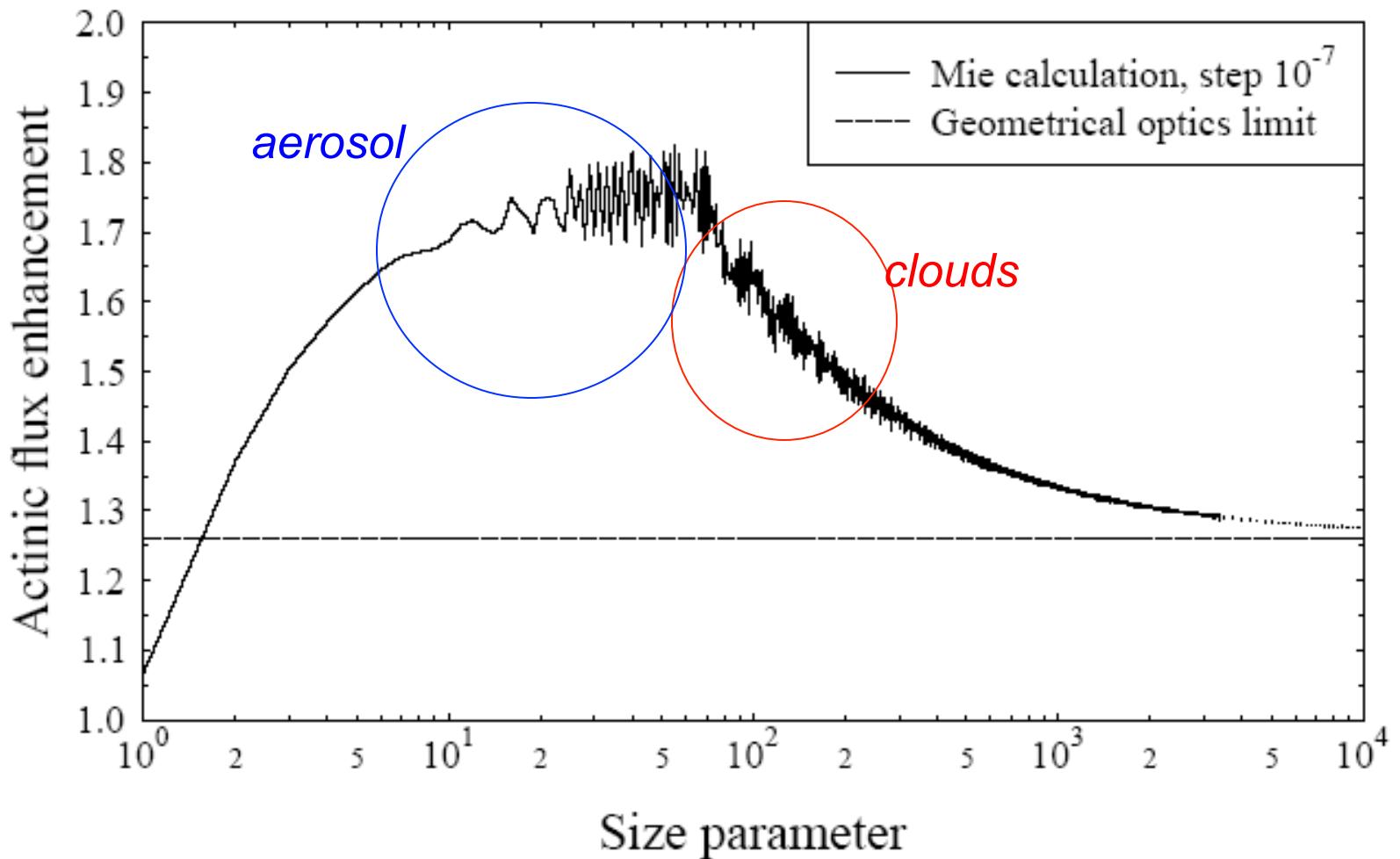
Single Scattering Albedo,  $\omega_0$   
 $n = 1.5 + 0.01 i$



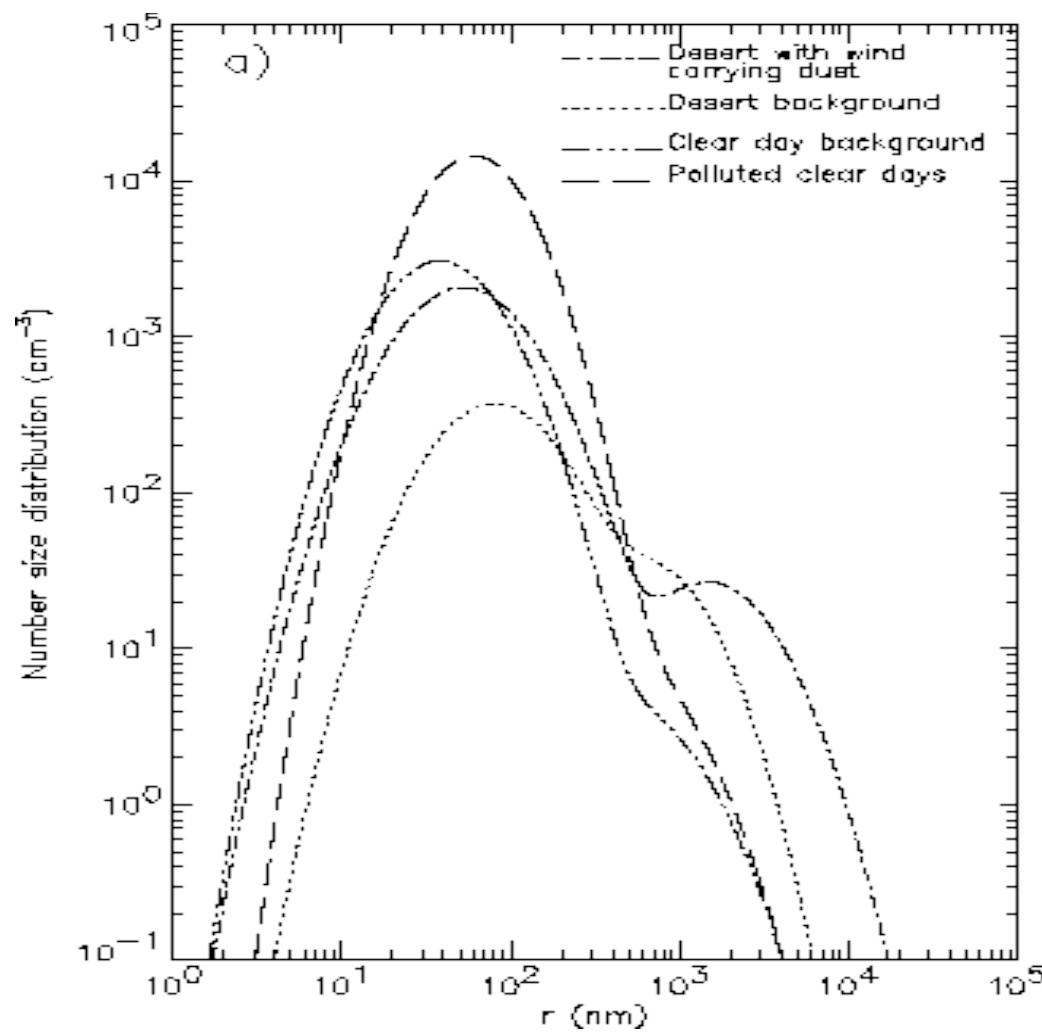
Asymmetry factor, g  
 $n = 1.5 + 0.01 i$



# Radiation Inside Liquid Spheres



# Aerosol size distributions



# Optical properties of aerosol ensembles

Total extinction coefficient = 
$$K_e(\lambda) = \int_0^{\infty} \pi r^2 Q_e(r, \lambda) n(r) dr$$

Total scattering coefficient = 
$$K_s(\lambda) = \int_0^{\infty} \pi r^2 Q_s(r, \lambda) n(r) dr$$

Average single scattering albedo = 
$$\varpi_o(\lambda) = K_s(\lambda) / K_e(\lambda)$$

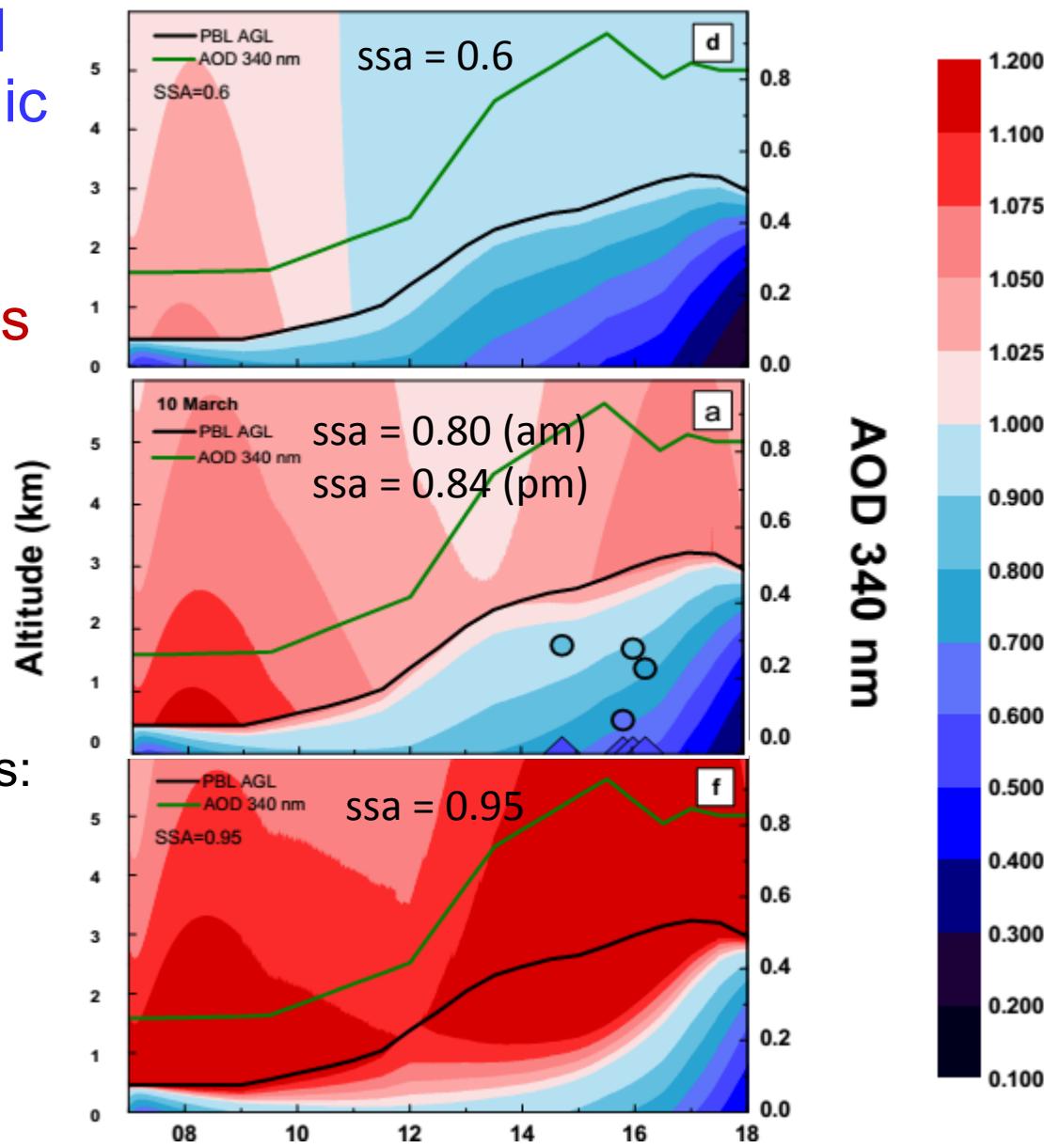
Average asymmetry factor = 
$$\bar{g}(\lambda) = \frac{\int_0^{\infty} g(r, \lambda) \pi r^2 Q_s(r, \lambda) n(r) dr}{\int_0^{\infty} \pi r^2 Q_s(r, \lambda) n(r) dr}$$

# Enhancements and Reductions of Actinic Flux by Aerosols

Mexico City suburbs  
(T1) March 2006

Central panel:  
Model with observed  
ssa, and obs.

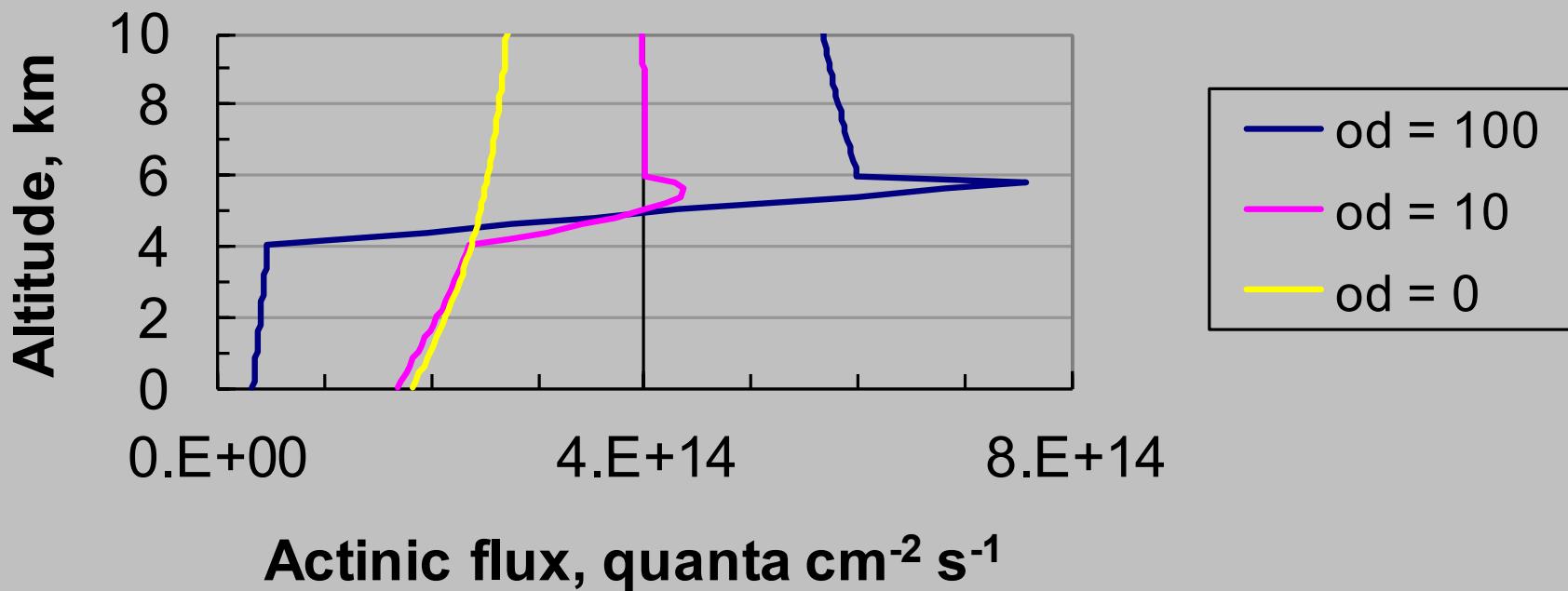
Upper and lower panels:  
Sensitivity to ssa



# CLOUDS

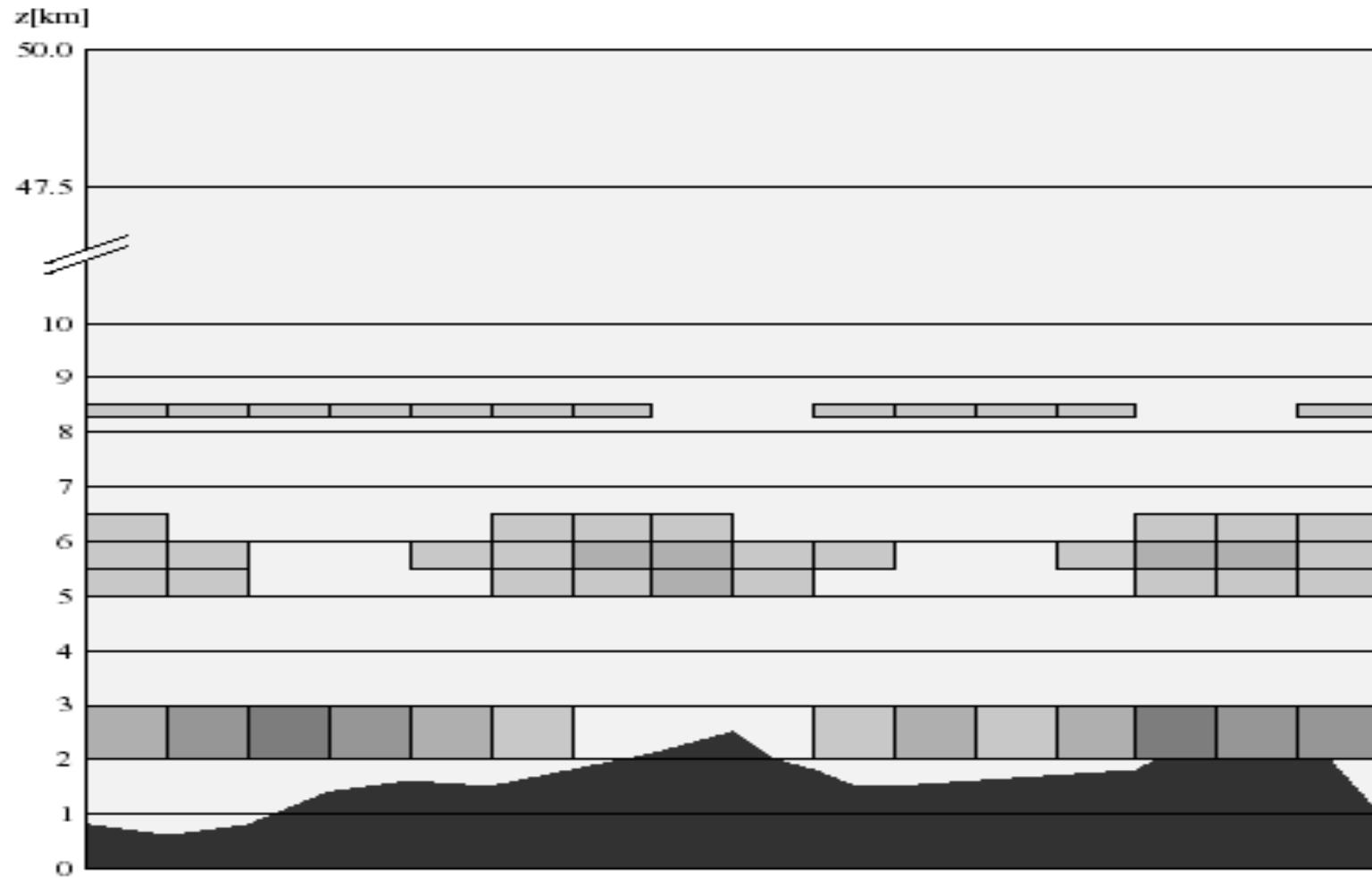
# EFFECT OF UNIFORM CLOUDS ON ACTINIC FLUX

340 nm, sza = 0 deg.,  
cloud between 4 and 6 km



*In liquid spheres, multiply by  $\sim 1.6$*

# Broken Clouds



# Photolysis in WRF-Chem

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- Several radiative transfer options:
  - TUV (delta-Eddington, 140 λ's)
  - Fast-J (8-str Feautrier, 17 λ's)
  - Fast-TUV (delta-Eddington, 17 λ's, correction table)
  - Other? – faster, more accurate
- Sub-grid cloud overlap schemes
  - Max overlap if vertically contiguous, random otherwise
  - Effects of overlap schemes on vertical distribution of actinic flux
  - Need evaluation of WRF-Chem in the presence of clouds
- Aerosols:
  - mixing rules for index of refraction
  - Mie scattering integrated over size distributions,
  - Different core-shell options



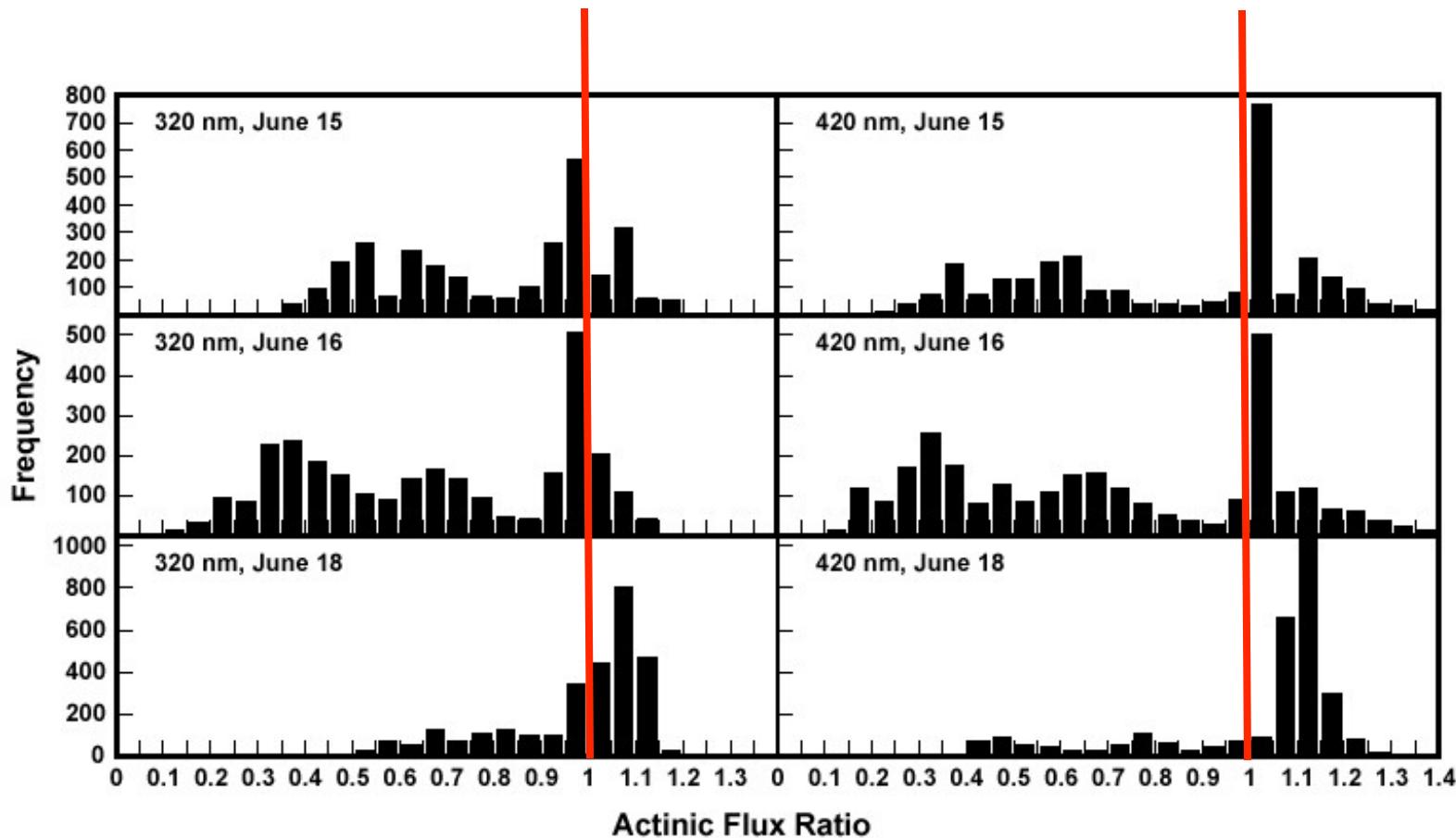
# Independent Pixel Approximation

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- Cloud free:
  - $S_o$  = direct sun
  - $D_o$  = diffuse light from sky
  - $G_o$  = total =  $S_o + D_o$
- Completely covered by clouds:
  - $S_1$  = direct sun (probably very small)
  - $D_1$  = diffuse light from base of cloud
  - $G_1$  = total =  $S_1 + D_1$
- Mix: Clouds cover a fraction  $c$  of the sky
  - If sun is not blocked:       $G_{NB} = S_o + cD_1 + (1-c)D_o$
  - If sun is blocked:             $G_B = S_1 + cD_1 + (1-c)D_o$

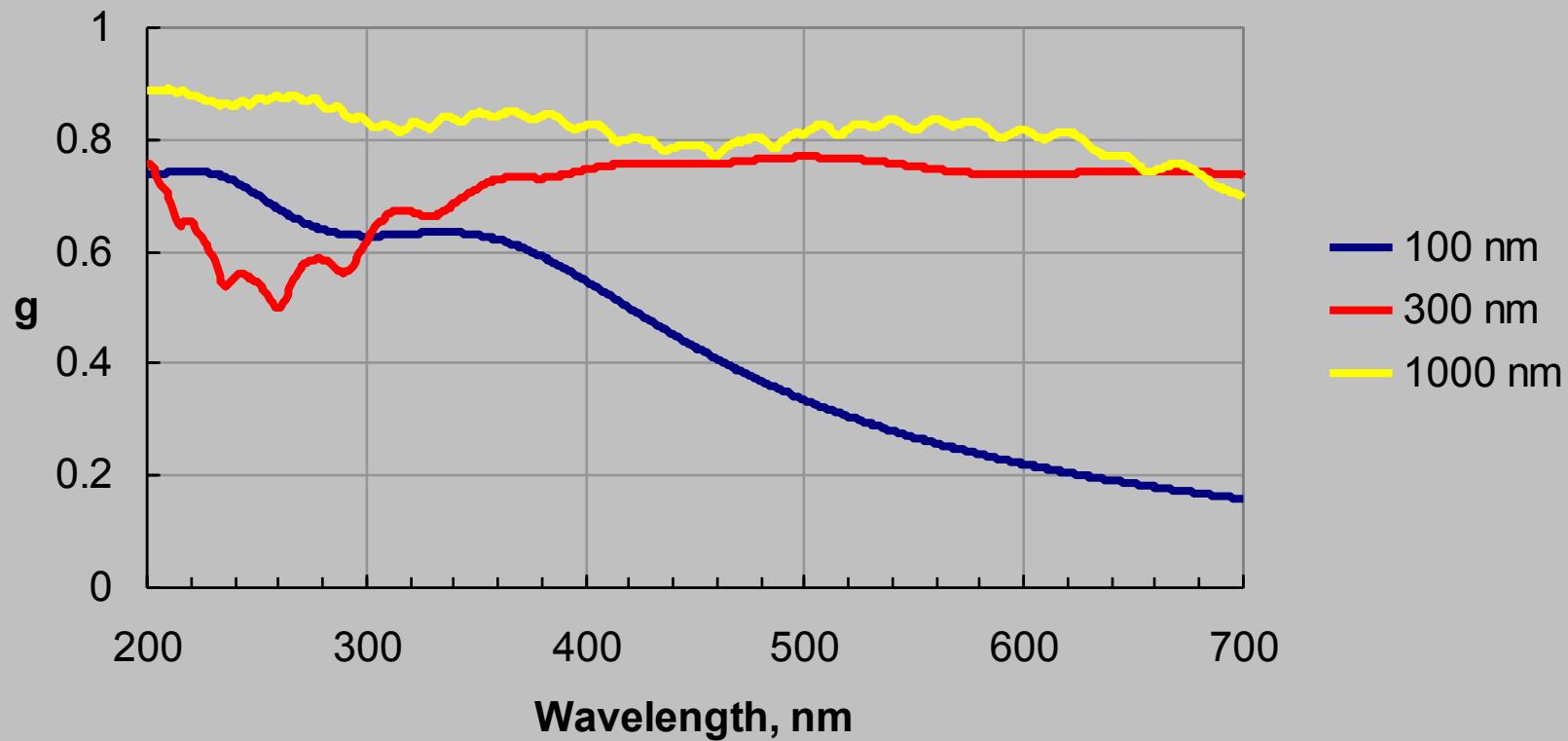
# PARTIAL CLOUD COVER

## Bimodal distributions



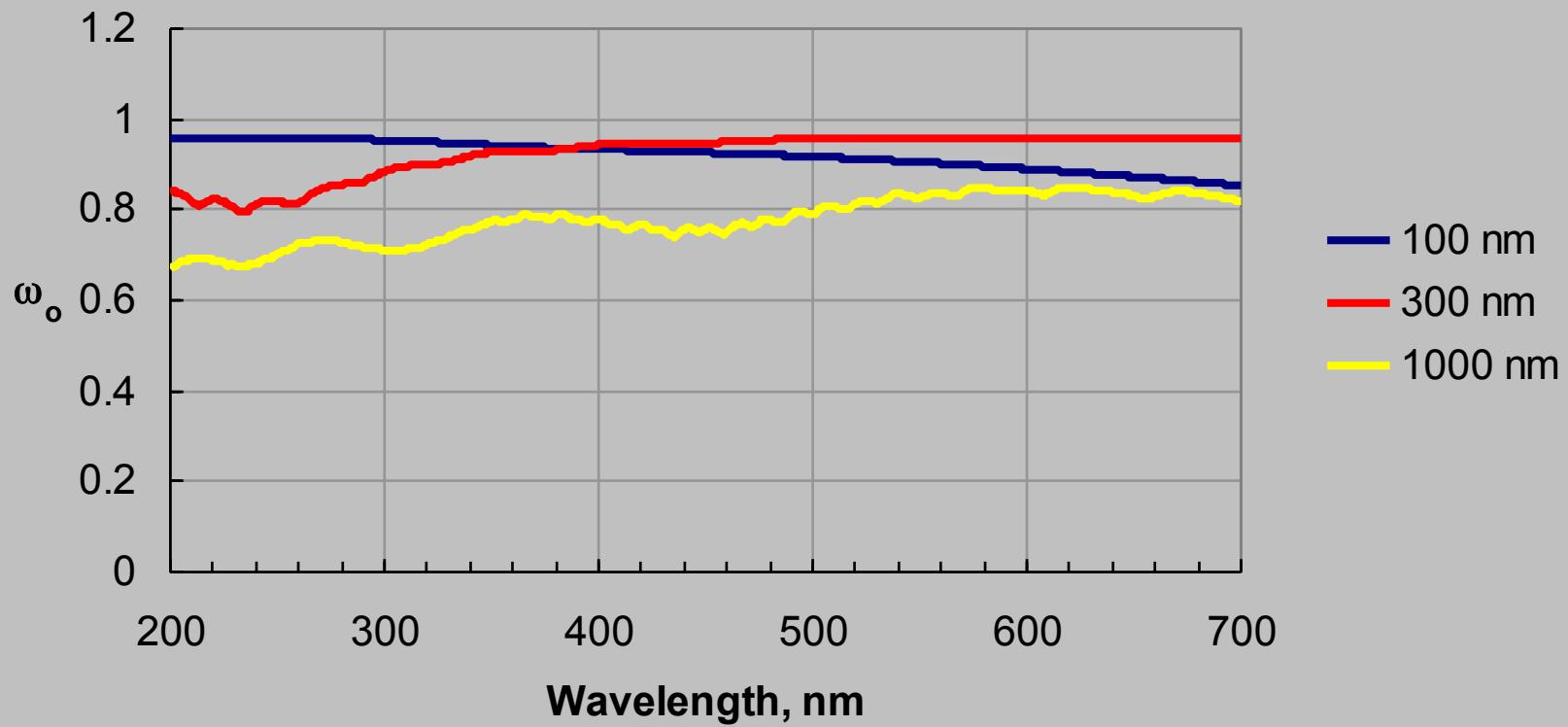
# Phase function or Asymmetry factor, g

Asymmetry factor, g  
 $n = 1.5 + 0.01 i$

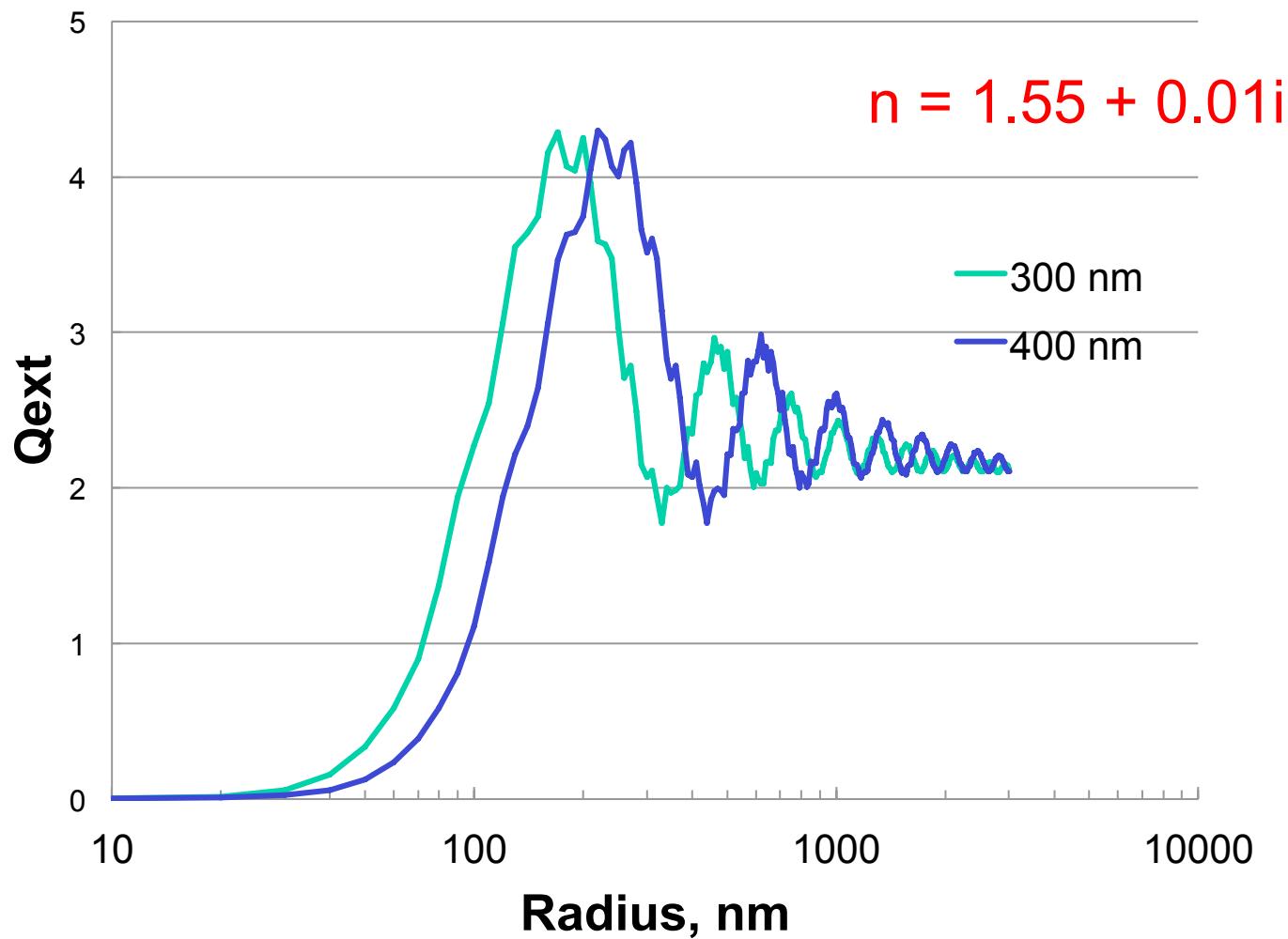


$$\text{Single Scattering Albedo} = Q_{\text{scatt}}/Q_{\text{ext}}$$

**Single Scattering Albedo,  $\omega_o$**   
 $n = 1.5 + 0.01 i$

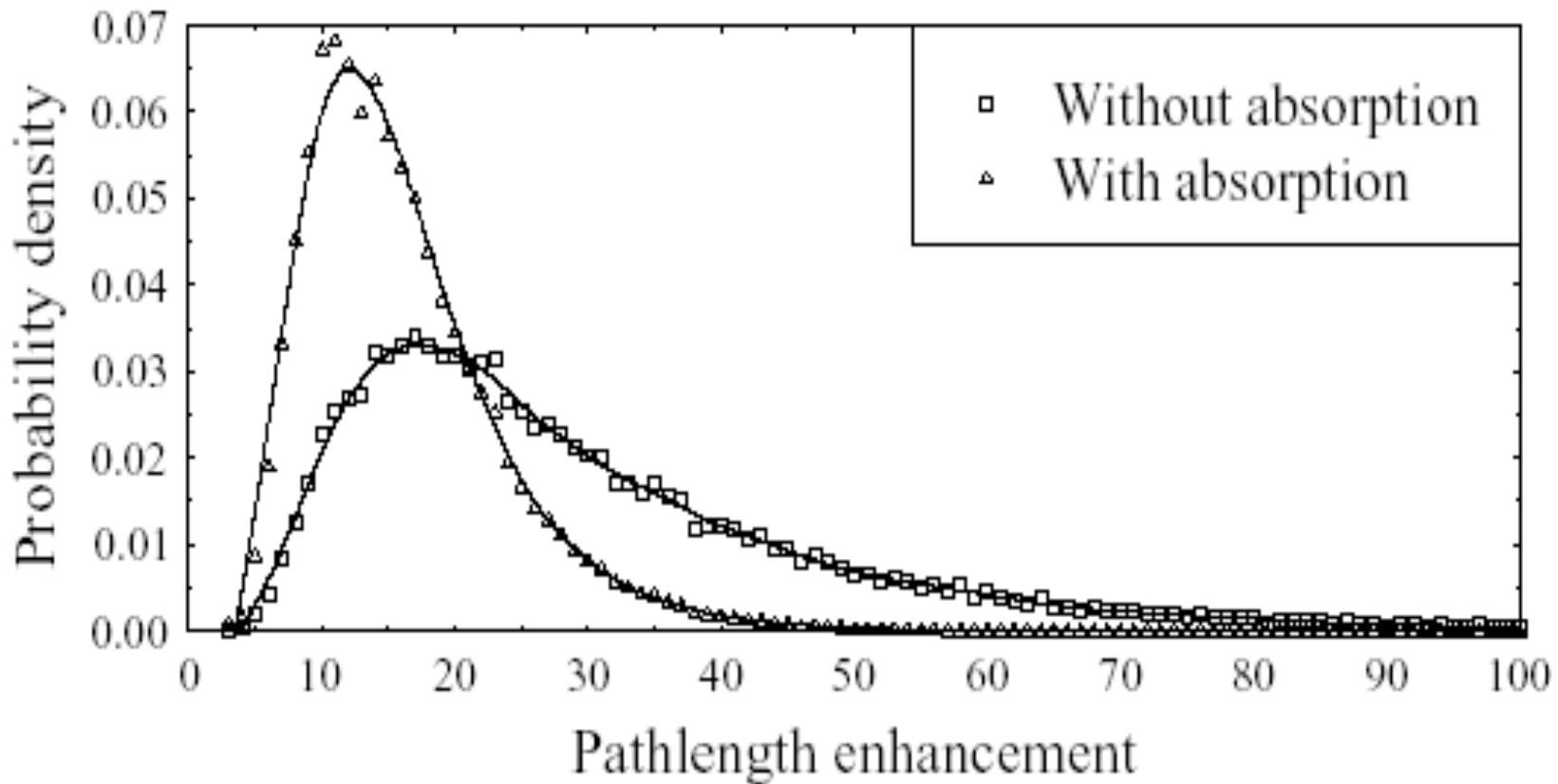


# Extinction Efficiency, $Q_{ext}$



# INSIDE CLOUDS: Photon Path Enhancements

*Cumulonimbus, od=400*

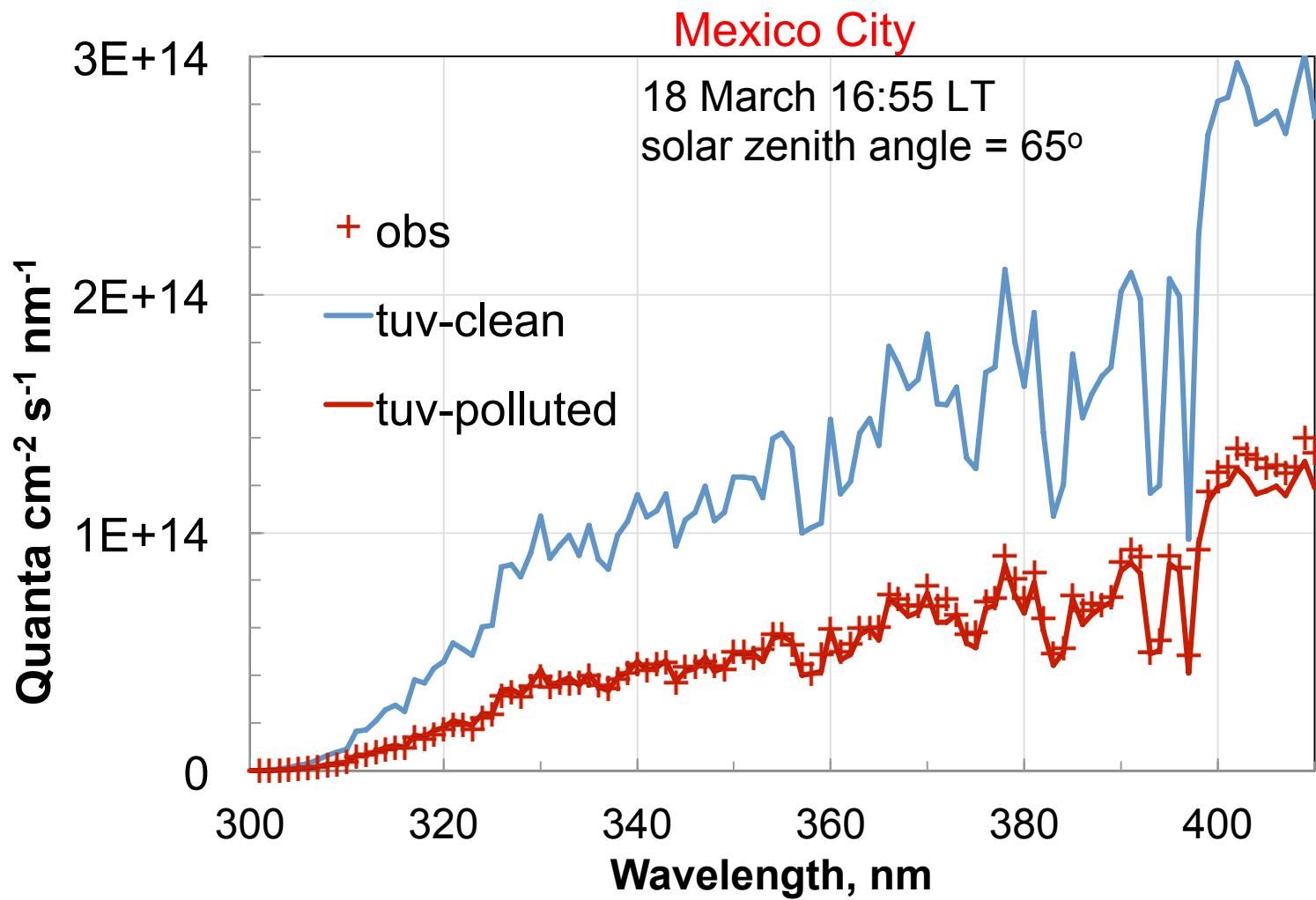


## UNIFORM CLOUD LAYER

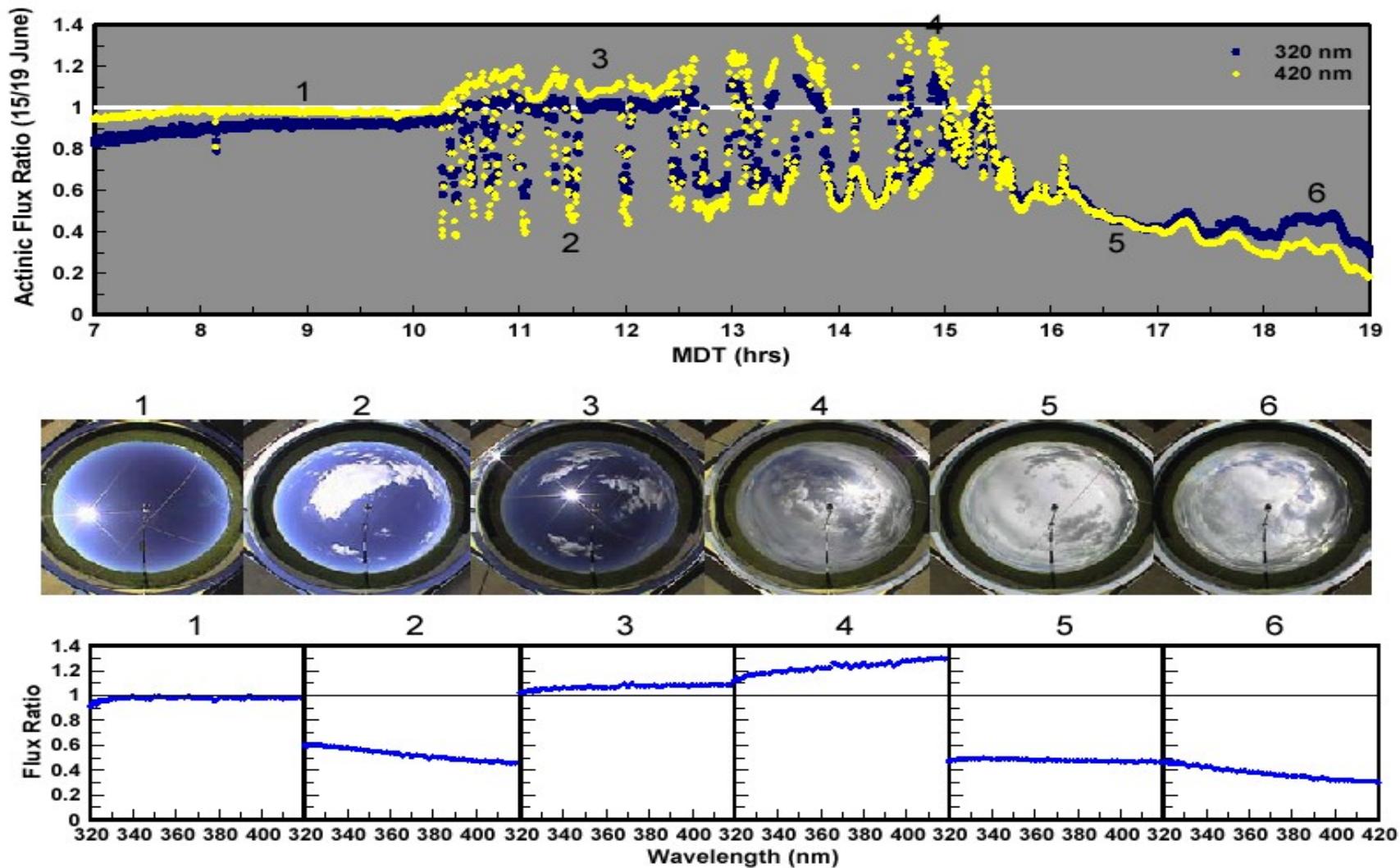
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- **Above cloud:** - high radiation because of reflection
- **Below cloud:** - lower radiation because of attenuation by cloud
- **Inside cloud:** - complicated behavior
  - Top half: very high values (for high sun)
  - Bottom half: lower values

# UV Actinic Flux Reduction → Slower Photochemistry



# SPECTRAL EFFECTS OF PARTIAL CLOUD COVER



# Spectral Region For Tropospheric Photochemistry

