

# Photolysis

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# Atmospheric Oxygen Species

## Thermodynamic vs. Actual

Normal O<sub>2</sub> molecules

$$\Delta H_f \text{ kcal mol}^{-1}$$

0

34.1

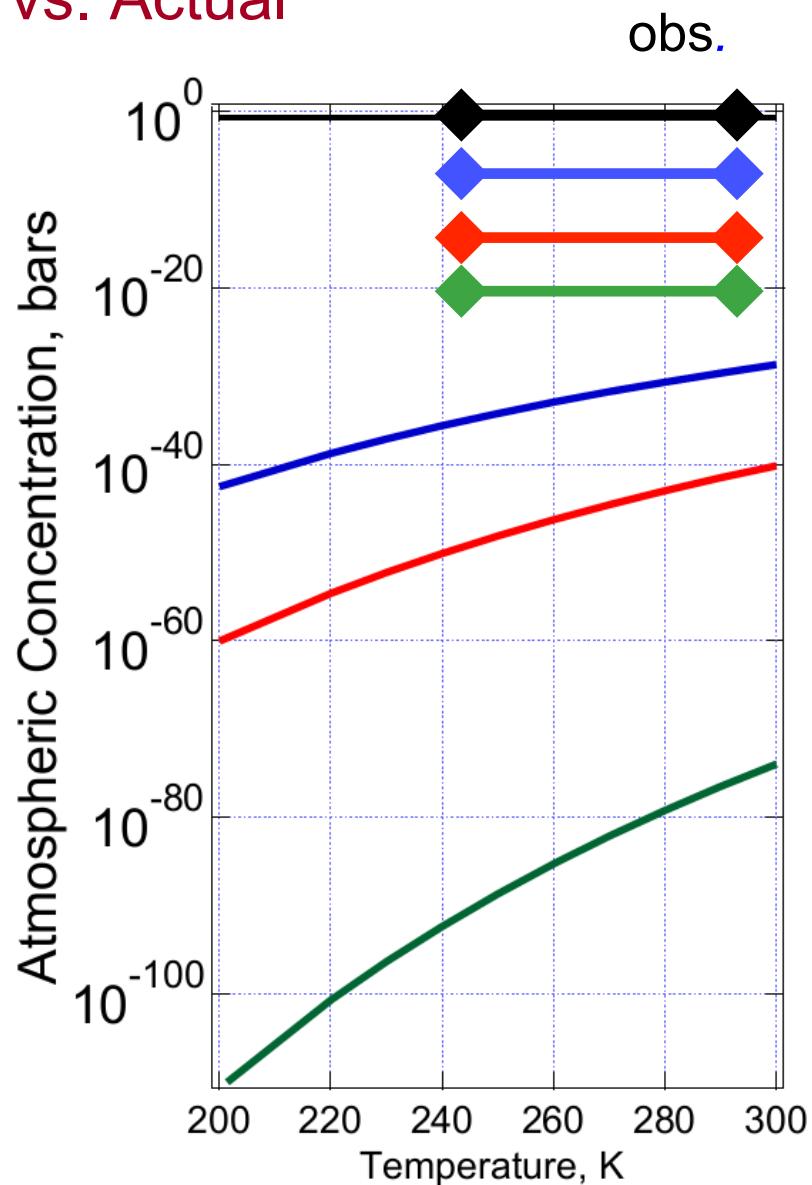
Ozone, O<sub>3</sub>

59.6

Ground state atoms, O

104.9

Excited atoms, O\*



# Photochemistry

Energy input from sunlight, e.g.



## Some Important Photolysis Reactions

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$O_2 + h\nu (\lambda < 240 \text{ nm}) \rightarrow O + O$	source of $O_3$ in stratosphere
$O_3 + h\nu (\lambda < 340 \text{ nm}) \rightarrow O_2 + O(^1D)$	source of OH in troposphere
$NO_2 + h\nu (\lambda < 420 \text{ nm}) \rightarrow NO + O(^3P)$	source of $O_3$ in troposphere
$CH_2O + h\nu (\lambda < 330 \text{ nm}) \rightarrow H + HCO$	source of HOx, everywhere
$H_2O_2 + h\nu (\lambda < 360 \text{ nm}) \rightarrow OH + OH$	source of OH in remote atm.
$HONO + h\nu (\lambda < 400 \text{ nm}) \rightarrow OH + NO$	source of radicals in urban atm.

# Quantifying Photolysis Processes

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Photolysis reaction:



Photolysis rates:

$$\frac{d[AB]}{dt} \Big|_{h\nu} = -J[AB]$$

$$\frac{d[A]}{dt} \Big|_{h\nu} = \frac{d[B]}{dt} \Big|_{h\nu} = +J[AB]$$

Photolysis frequency ( $s^{-1}$ )     $J = \int_{\lambda} F(\lambda) \sigma(\lambda) \phi(\lambda) d\lambda$

(other names: photo-dissociation rate coefficient, J-value)

# CALCULATION OF PHOTOLYSIS COEFFICIENTS

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$$J \text{ (s}^{-1}\text{)} = \int_{\lambda} F(\lambda) \sigma(\lambda) \phi(\lambda) d\lambda$$

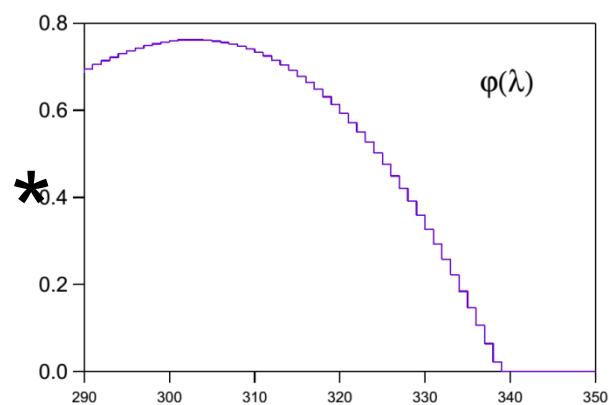
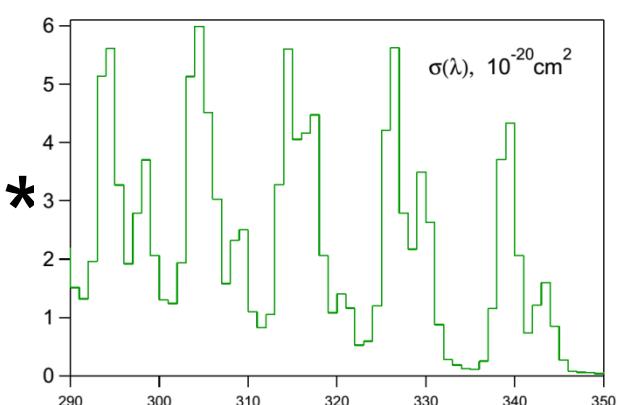
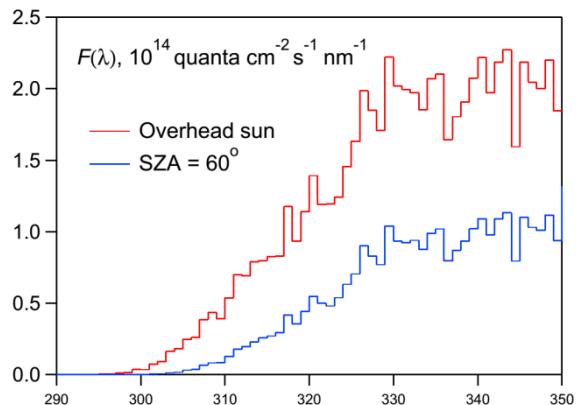
$F(\lambda)$  = spectral actinic flux, quanta  $\text{cm}^{-2} \text{s}^{-1} \text{nm}^{-1}$   
 $\propto$  probability of photon near molecule.

$\sigma(\lambda)$  = absorption cross section,  $\text{cm}^2 \text{ molec}^{-1}$   
 $\propto$  probability that photon is absorbed.

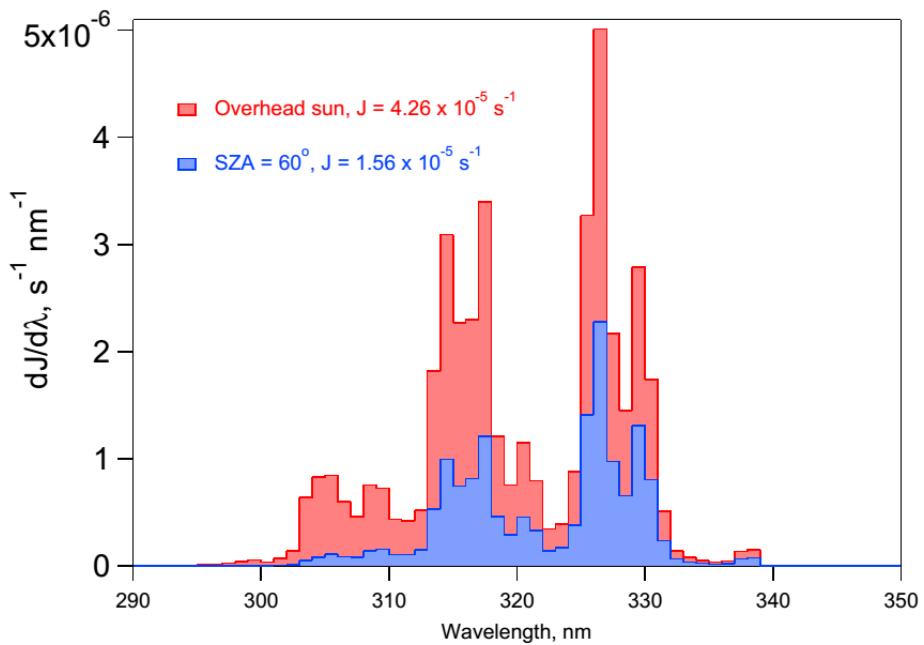
$\phi(\lambda)$  = photodissociation quantum yield,  $\text{molec quanta}^{-1}$   
 $\propto$  probability that absorbed photon causes dissociation.

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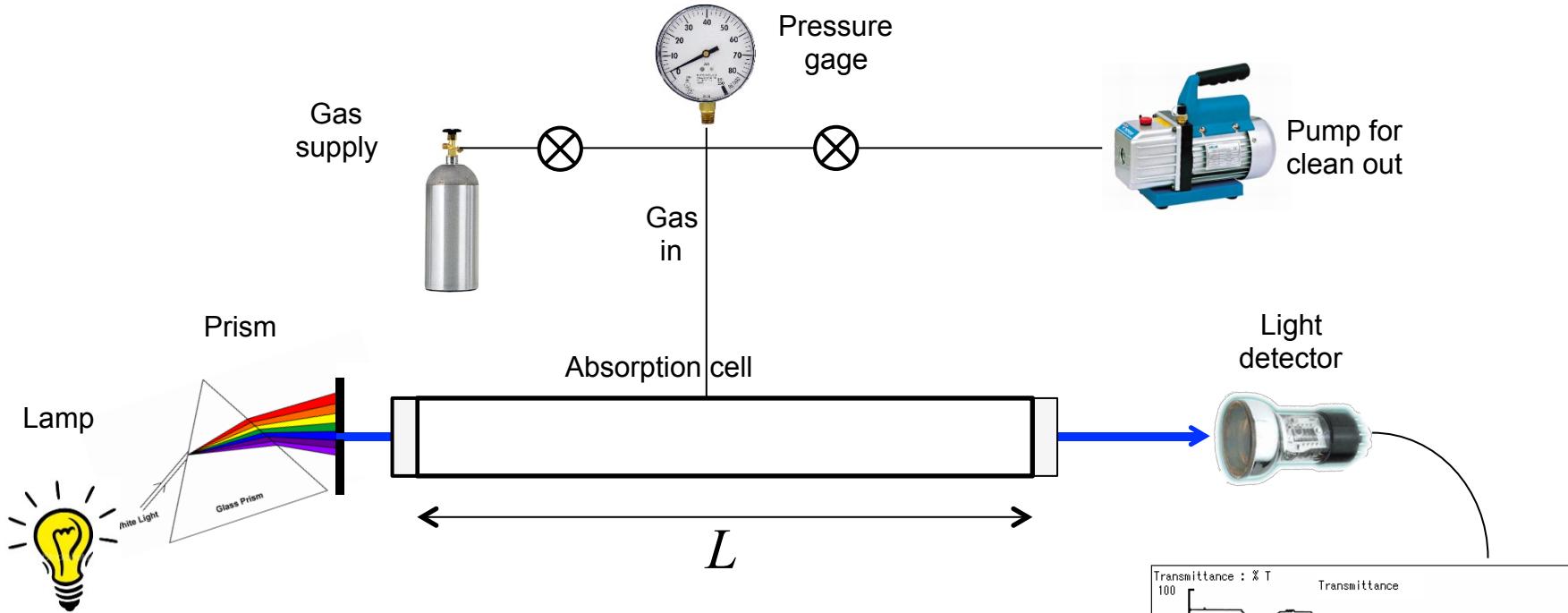
# Calculation of $J$ for $\text{CH}_2\text{O} + \text{h}\nu \rightarrow \text{CHO} + \text{H}$



||

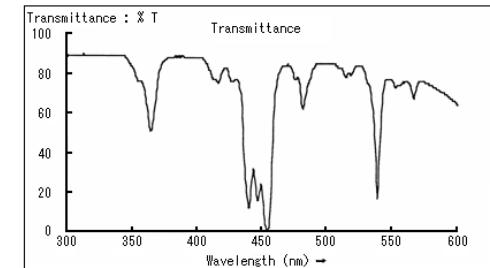


# Measurement of Absorption Cross Section $\sigma(\lambda)$



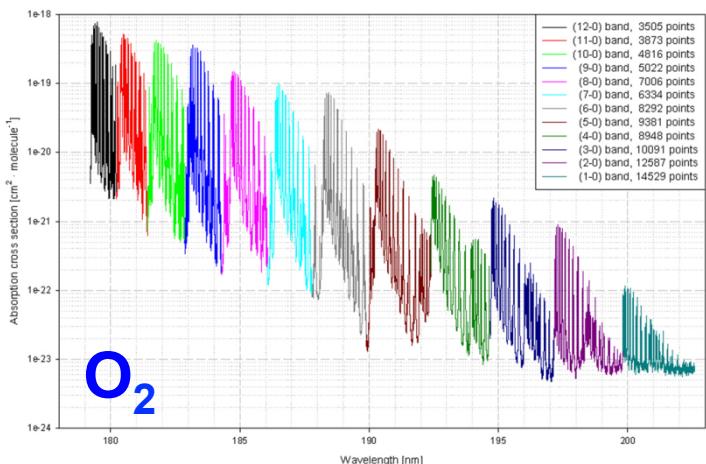
$$\text{Transmittance} = I / I_0 = \exp(-\sigma n L)$$

$$\sigma = -1/(nL) \ln(I/I_0)$$

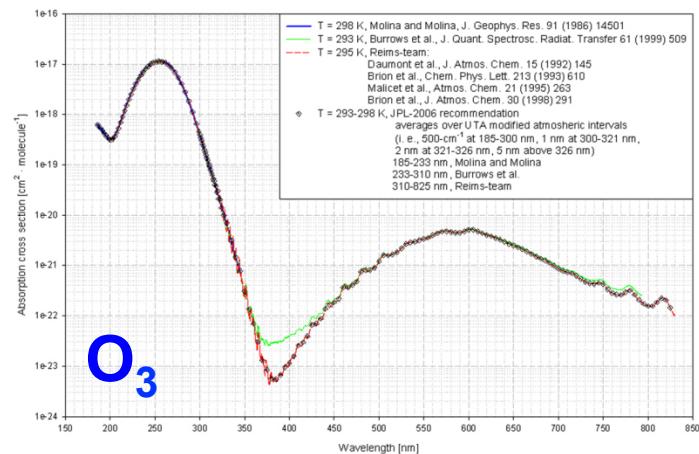


Easy: measure pressure ( $n = P/RT$ ), and relative change in light:  $I / I_0$

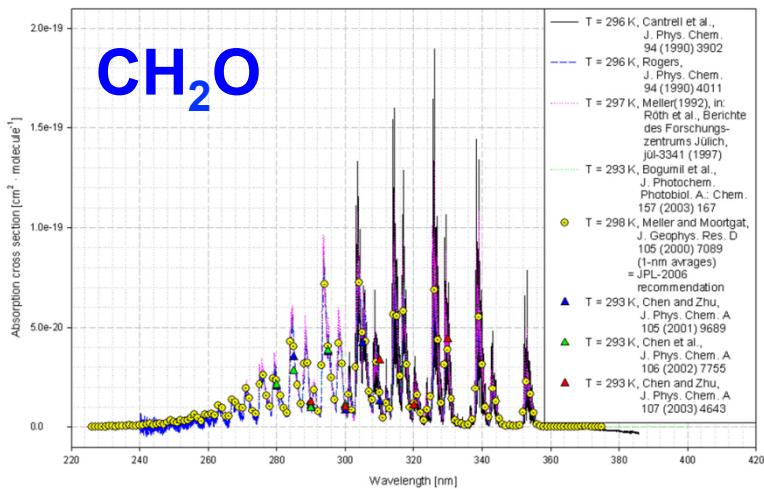
# Absorption cross sections $\sigma(\lambda, T)$



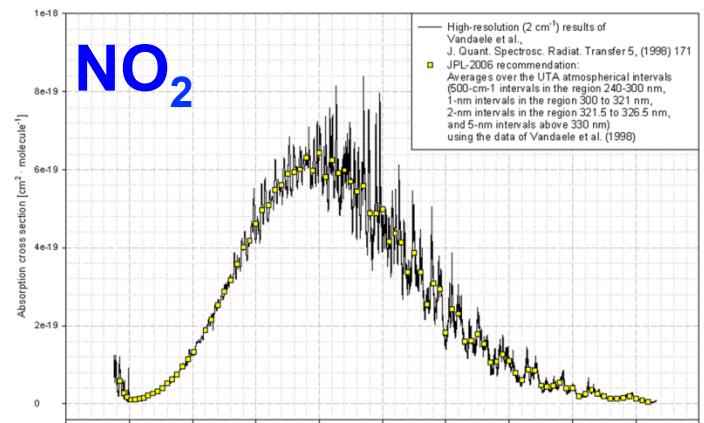
Absorption cross sections in the Schumann-Runge region of oxygen  $\text{O}_2$  at 300 K,  
Yoshino et al., Planet. Space Sci. 40 (1992) 185



Absorption cross sections of ozone  $\text{O}_3$  at room temperature  
Evaluation for JPL-2006 recommendation

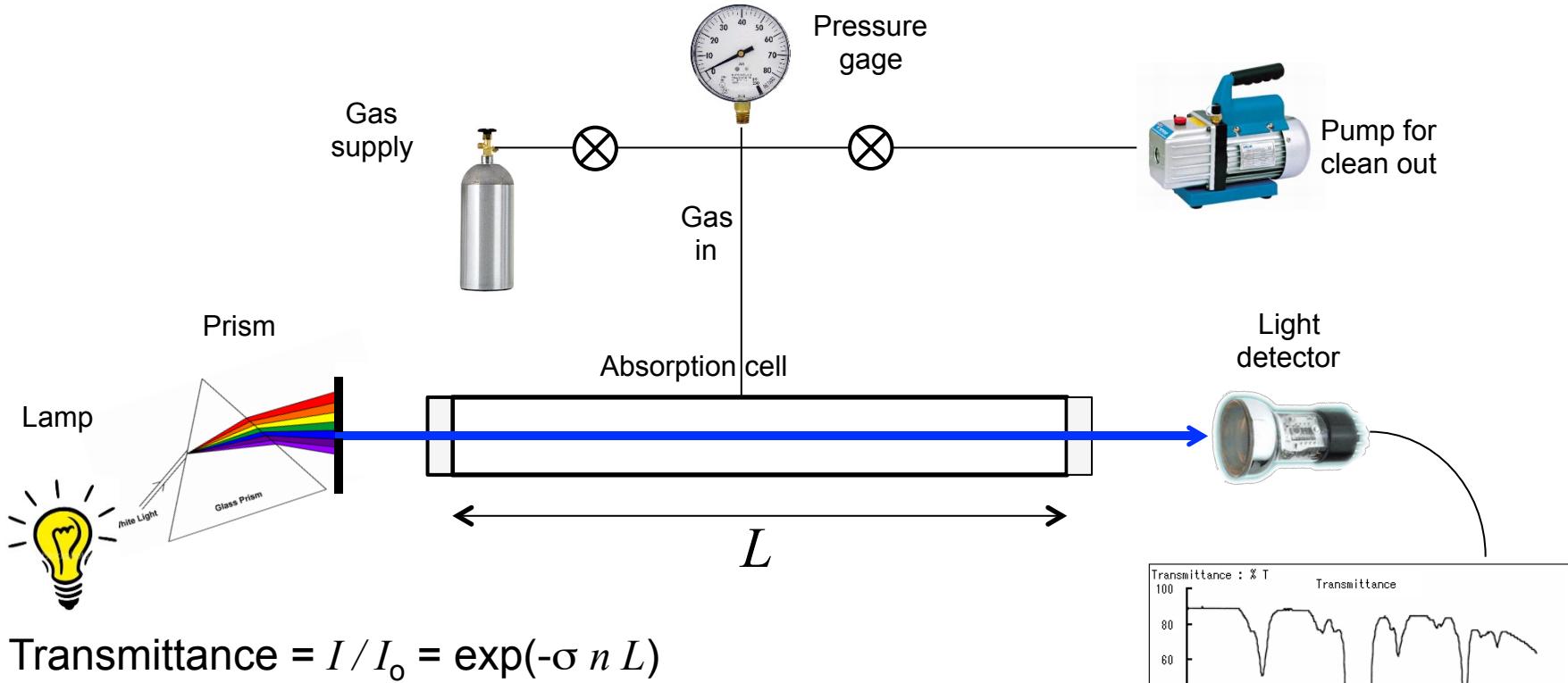


Absorption cross sections of formaldehyde  $\text{CH}_2\text{O}$  at room temperature (results 1990-2003)



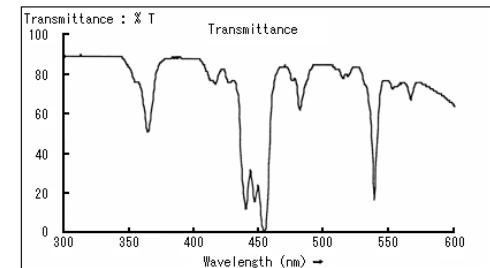
Absorption cross sections of nitrogen dioxide  $\text{NO}_2$  at 294 K  
Results from the year 1998 and JPL-2006 recommendation

# Measurement of Quantum Yields $\phi(\lambda)$

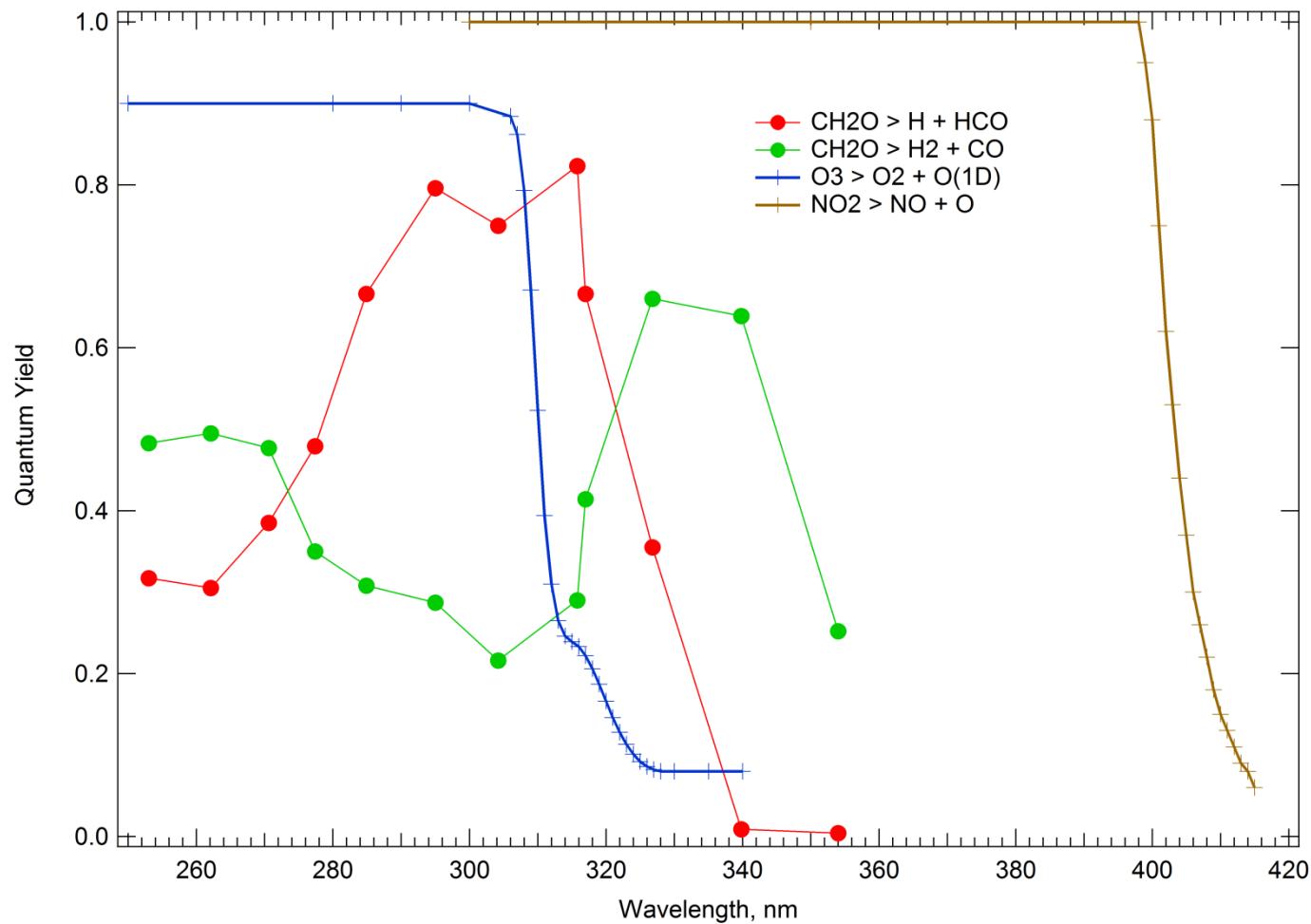


Quantum Yield = number of breaks per photon absorbed  
 $\phi = \Delta n / \Delta I$

Difficult: must measure absolute change in  $n$  (products) and  $I$  (photons absorbed)



# Photo-dissociation Quantum Yields $\phi(\lambda, T, P)$



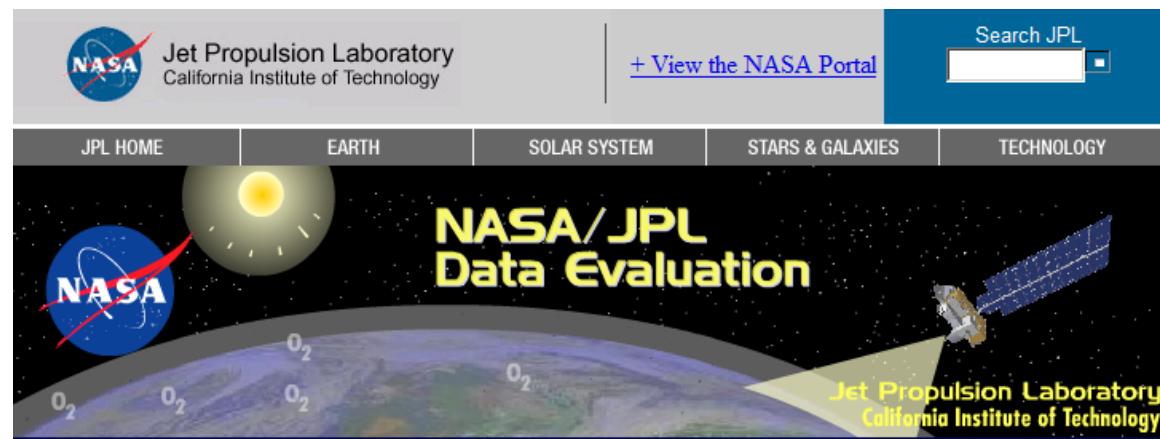
# Compilations of Cross Sections & Quantum Yields

<http://www.atmosphere.mpg.de/enid/2295>



**MPI-Mainz-UV-VIS Spectral Atlas of Gaseous Molecules**  
A Database of Atmospherically Relevant Species, Including Numerical Data and Graphical Representations  
Hannelore Keller-Rudek, Geert K. Moortgat  
Max-Planck-Institut für Chemie, Atmospheric Chemistry Division, Mainz, Germany

<http://jpldataeval.jpl.nasa.gov/>



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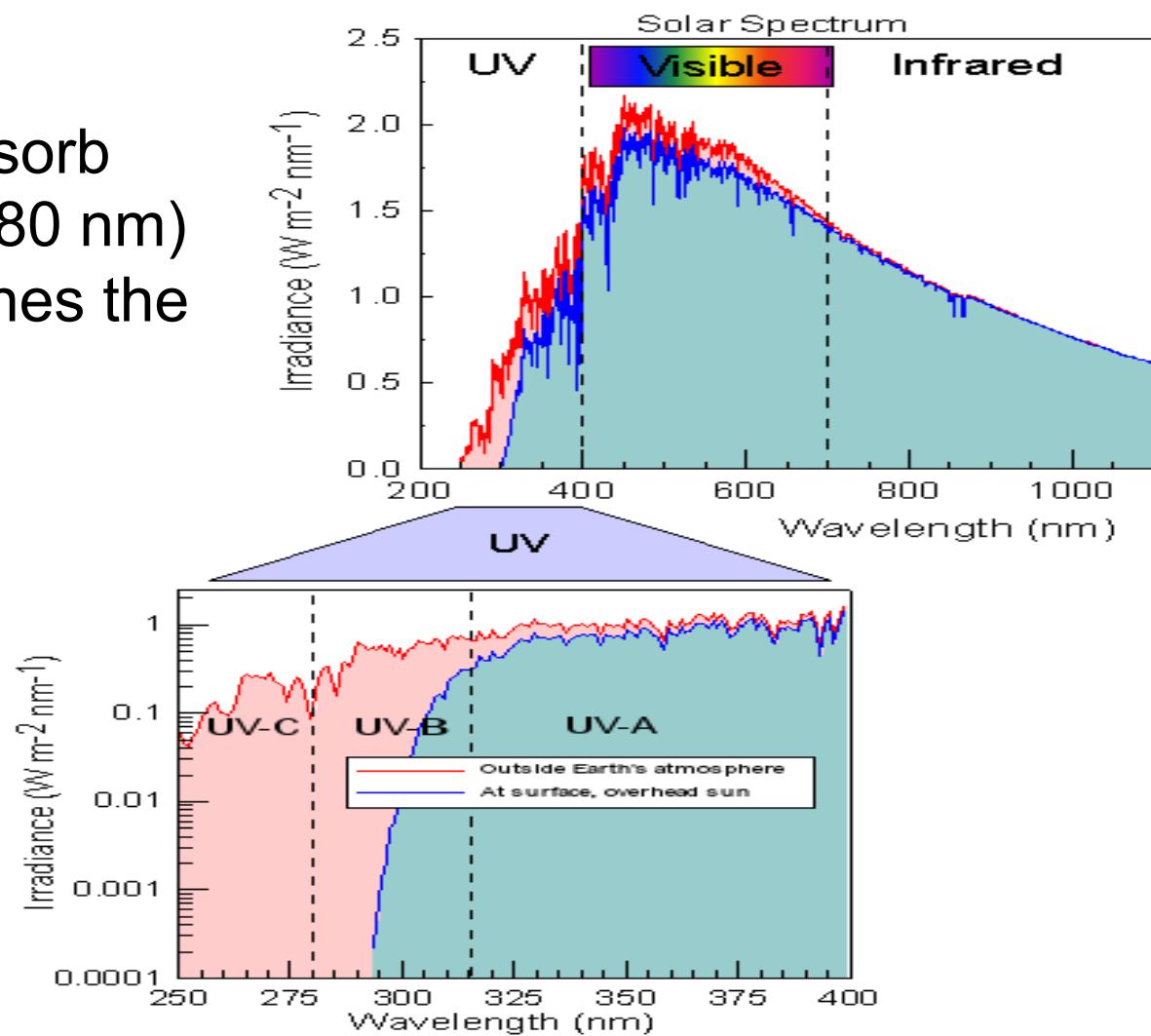
JPL HOME EARTH SOLAR SYSTEM STARS & GALAXIES TECHNOLOGY

**NASA/JPL Data Evaluation**

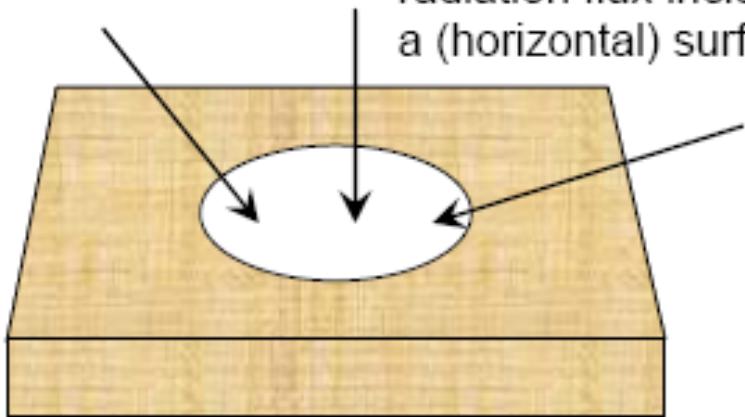
Jet Propulsion Laboratory California Institute of Technology

# Solar Spectrum

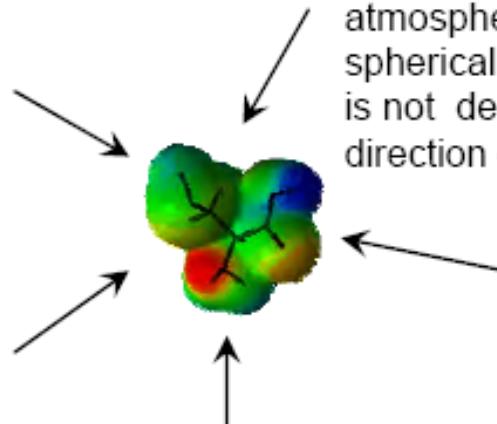
$O_2$  and  $O_3$  absorb all UV-C ( $\lambda < 280$  nm) before it reaches the troposphere



# INTEGRALS OVER INCIDENT DIRECTIONS



**Irradiance:** The radiation flux incident on a (horizontal) surface.



**Actinic flux:** The photochemically active radiation flux in the earth's atmosphere. This flux is spherically integrated and is not dependent the direction of the radiation.

$$E = \iint_0^{\frac{\pi}{2}} I(\theta, \varphi) \cos \theta \sin \theta d\theta d\varphi$$

Watts m<sup>-2</sup>

$$F = \iint_0^{2\pi} I(\theta, \varphi) \sin \theta d\varphi d\theta$$

Watts m<sup>-2</sup> or quanta s<sup>-1</sup> cm<sup>-2</sup>

# Optical Depth

$n$  = particles per unit volume

$\sigma$  = cross sectional area of each particle

*Beer-Lambert law*

*differential form*

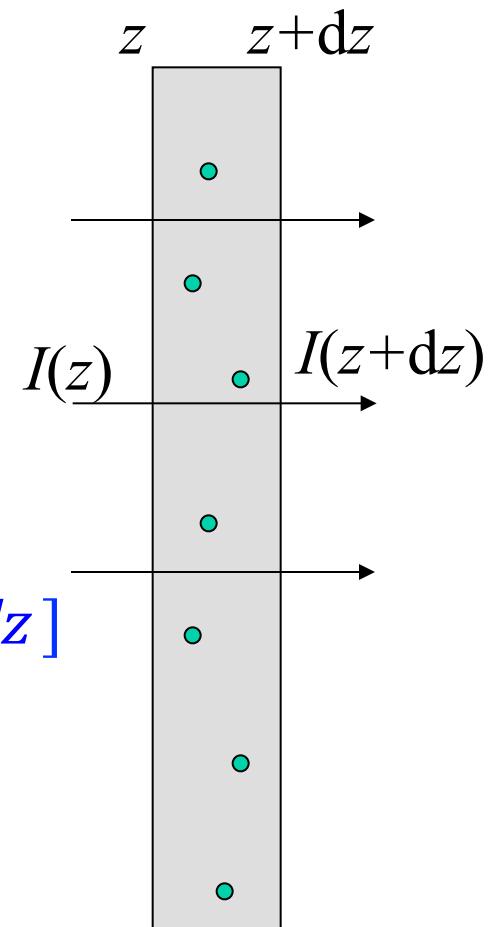
$$dI/I = -\sigma n dz$$

*integral form*

$$I(z_2) = I(z_1) \exp [-\int_{z_1}^{z_2} \sigma n dz]$$

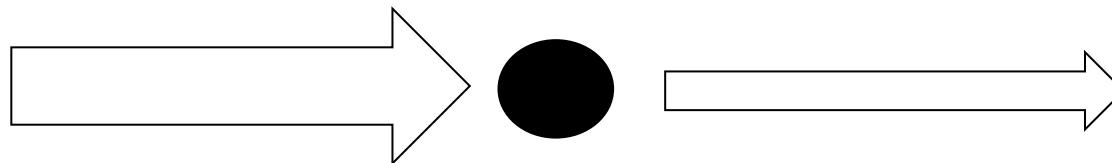
*Optical Depth:*

$$\tau = \int_{z_1}^{z_2} \sigma(z) n(z) dz$$

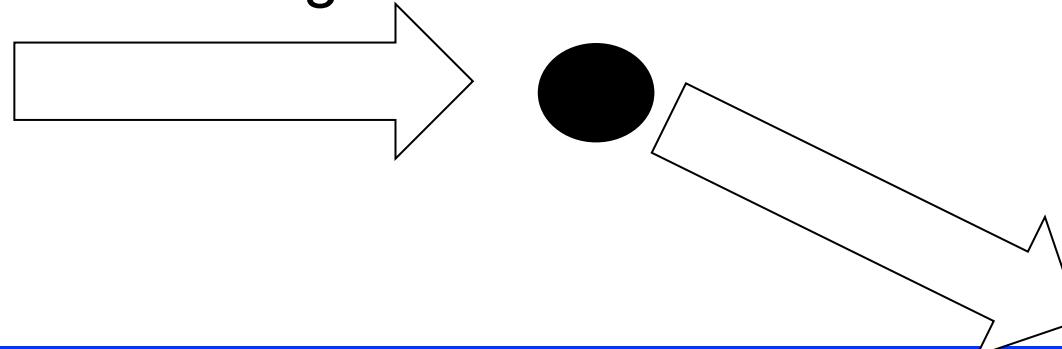


# Absorption and Scattering

- **Absorption** – inelastic, loss of radiant energy:



- **Scattering** – elastic, radiant energy is conserved, direction changes:

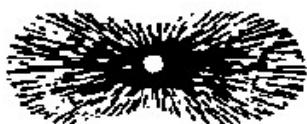


# SCATTERING PHASE FUNCTIONS

$$P(\theta, \phi; \theta', \phi')$$

Small Particles (a)

→  
Incident  
beam



Size: smaller than one-tenth the wavelength of light  
Description: symmetric

Large Particles (b)

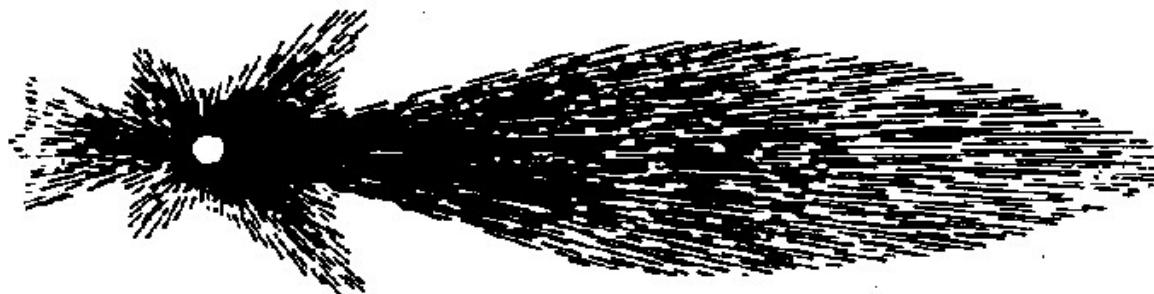
→  
Incident  
beam



Size: approximately one-fourth the wavelength of light  
Description: scattering concentrated in forward direction

Larger Particles (c)

→  
Incident  
beam



Size: larger than the wavelength of light  
Description: extreme concentration of scattering in forward direction;  
development of maxima and minima of scattering at  
wider angles

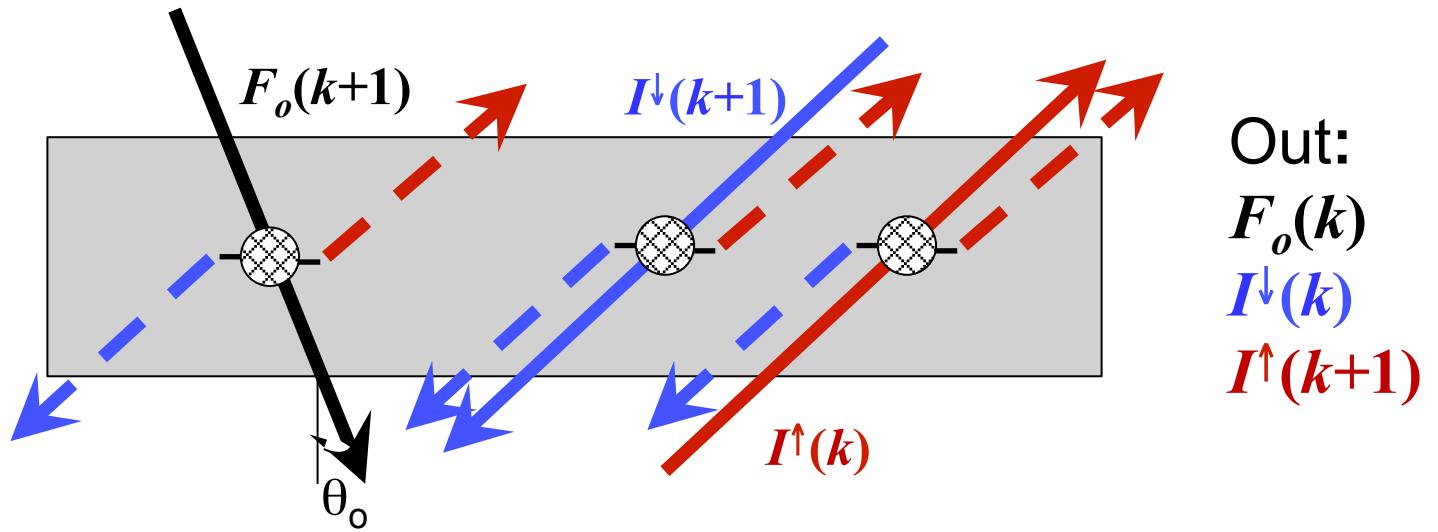
# Multiple Atmospheric Layers Each Assumed to be Homogeneous

In:

$$F_o(k+1)$$

$$I^{\downarrow}(k+1)$$

$$I^{\uparrow}(k)$$



Out:

$$F_o(k)$$

$$I^{\downarrow}(k)$$

$$I^{\uparrow}(k+1)$$

Each layer described by 3 parameters:

Optical depth,  $\Delta\tau$

Single scattering albedo,  $\omega_o$  = scatt./(scatt.+abs.)

Asymmetry factor,  $g$ : forward fraction  $\sim (1+g)/2$

# Typical Values

	Optical Depth	Single Scattering Albedo	Asymmetry Factor
Molecular scattering (Rayleigh)	0.5 – 2.0 $\lambda^{-4}$	1	0
Molecular absorption O <sub>2</sub> , O <sub>3</sub> , NO <sub>2</sub> , SO <sub>2</sub> ,	0 – 30 spectra	0	na
Aerosols	0.01 – 5 $\lambda^{-\alpha}$ , $\alpha = 0.5 – 2.0$ (Angstrom exponent)	0.99 sulfate 0.6 soot	0.6 – 0.8
Clouds	1 – 1000 white, $\alpha = 0$	0.9999	0.7 – 0.9

# Radiative Transfer Equation

*Propagation derivative*

$$\cos \theta \frac{dI(\tau, \theta, \phi)}{d\tau}$$

*Beer-Lambert  
attenuation*

$$- I(\tau, \theta, \phi)$$

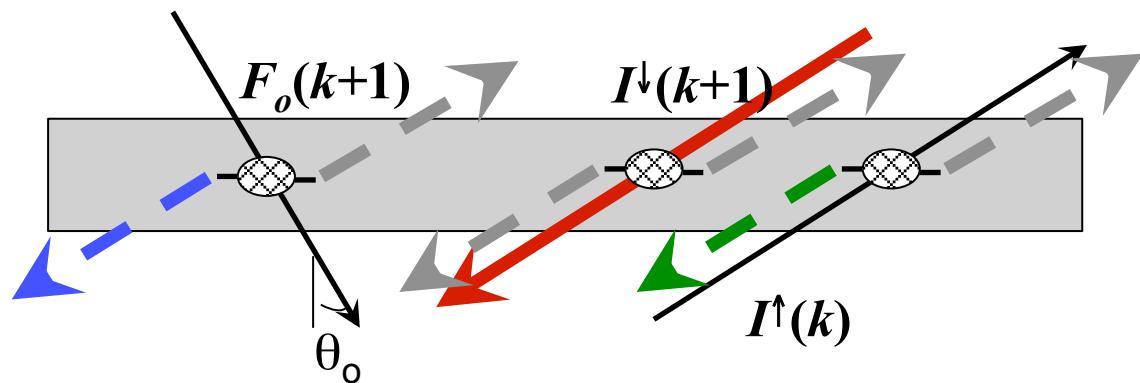
*Scattering from  
direct solar beam*

$$+ \frac{\omega_o}{4\pi} F_\infty e^{-\tau/\cos \theta_o} P(\theta, \phi; \theta_o, \phi_o) +$$

$$+ \frac{\omega_o}{4\pi} \int_0^{2\pi} \int_{-1}^{+1} I(\tau, \theta', \phi') P(\theta, \phi; \theta', \phi') d\cos \theta' d\phi'$$

*Equivalent coordinates:  
optical or geometric  
 $d\tau = \sigma n dz$*

*Scattering from diffuse light  
(multiple scattering)*



# NUMERICAL SOLUTIONS TO RADIATIVE TRANSFER EQUATION

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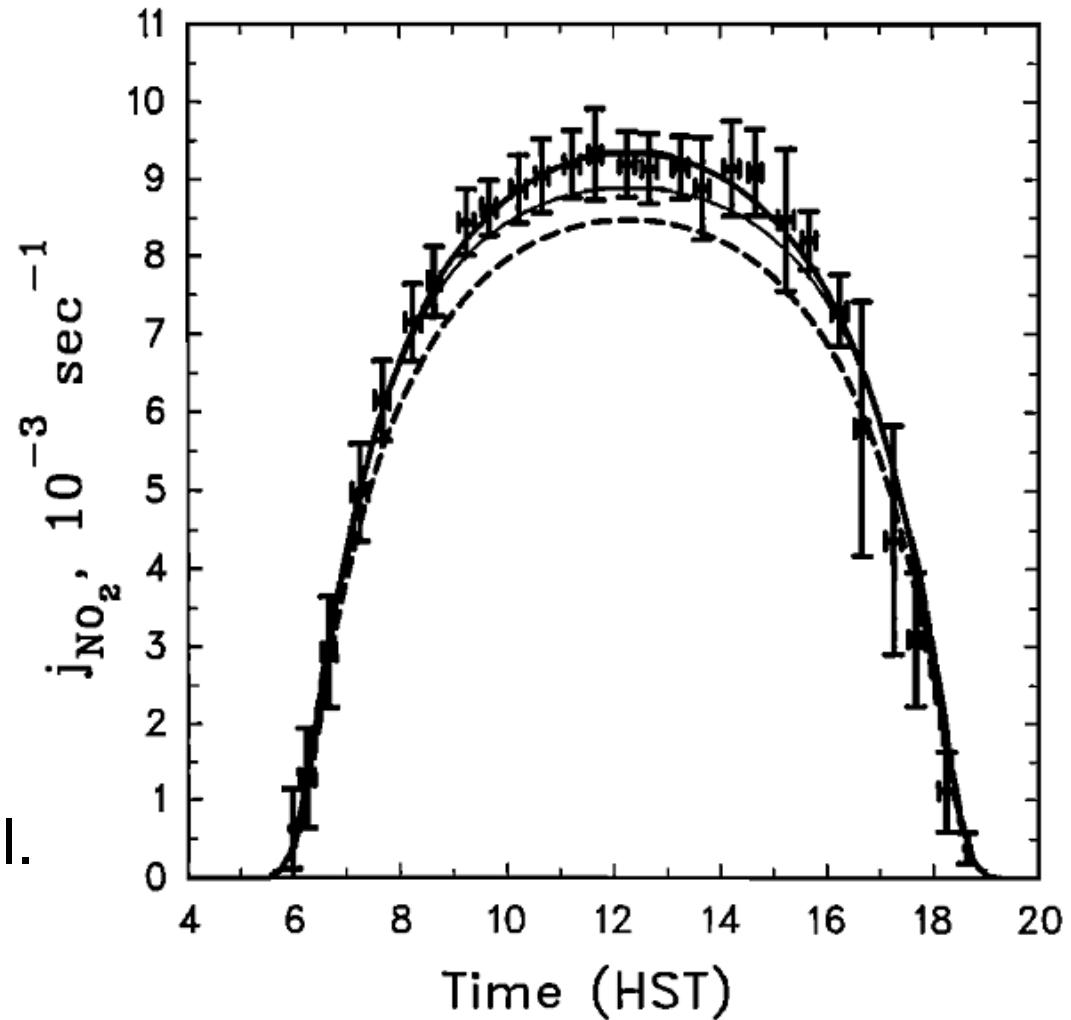
- Discrete ordinates
  - n-streams ( $n = \text{even}$ ), angular distribution exact as  $n \rightarrow \infty$  but speed  $\propto 1/n^2$
- Two-stream family
  - delta-Eddington, many others
  - very fast but not exact
- Monte Carlo
  - slow, but ideal for 3D problems
- Others
  - matrix operator, Feautrier, adding-doubling, successive orders, etc.

## $J$ for $\text{NO}_2 \rightarrow \text{NO} + \text{O}$

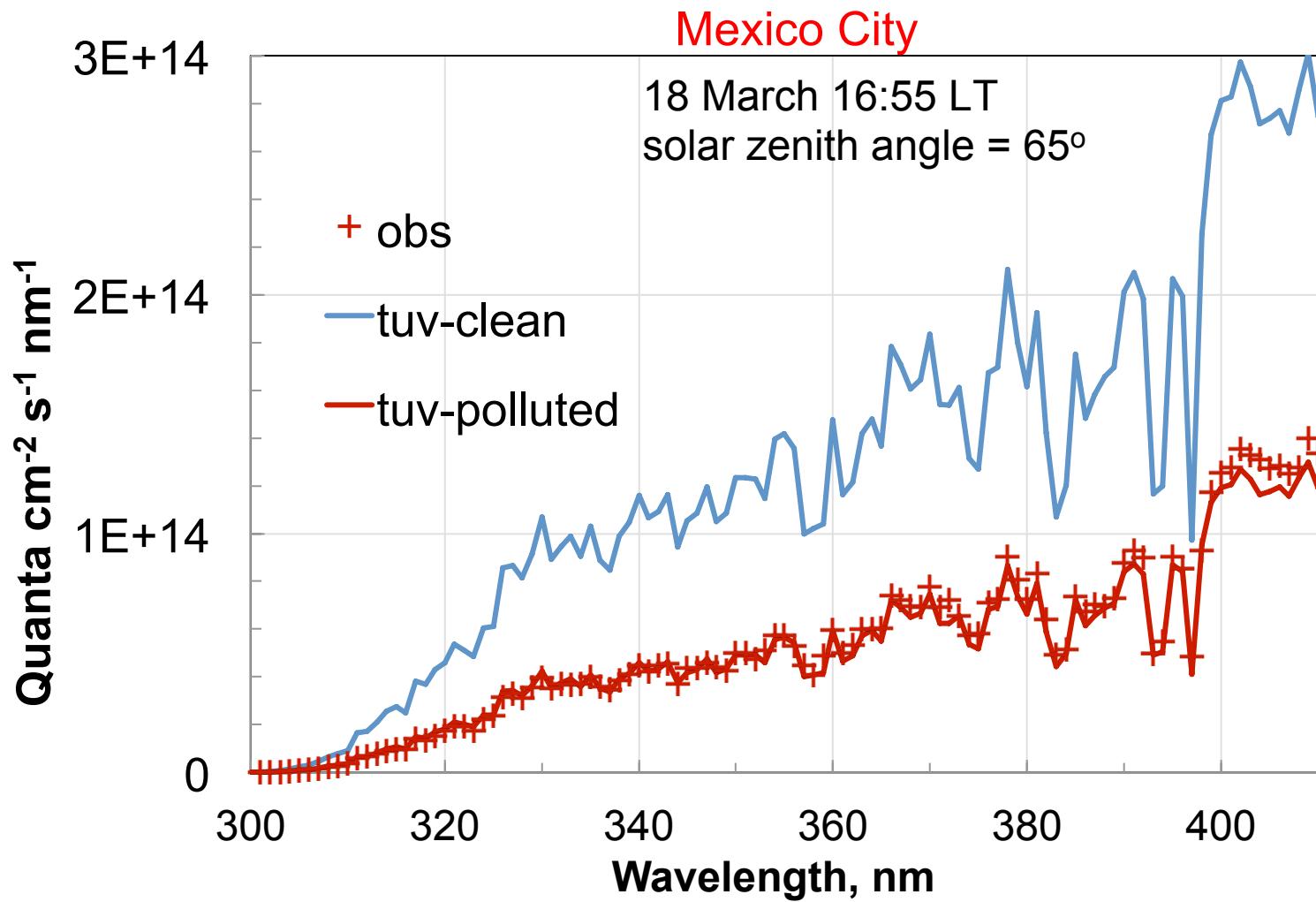
Direct measurement  
with chemical  
actinometers

Good agreement  
with model for  
pristine conditions

e.g.,  
Mauna Loa, Hawaii  
3.4 km elevation a.s.l.



# Aerosols Can Attenuate Urban Actinic Flux → Slower Photochemistry

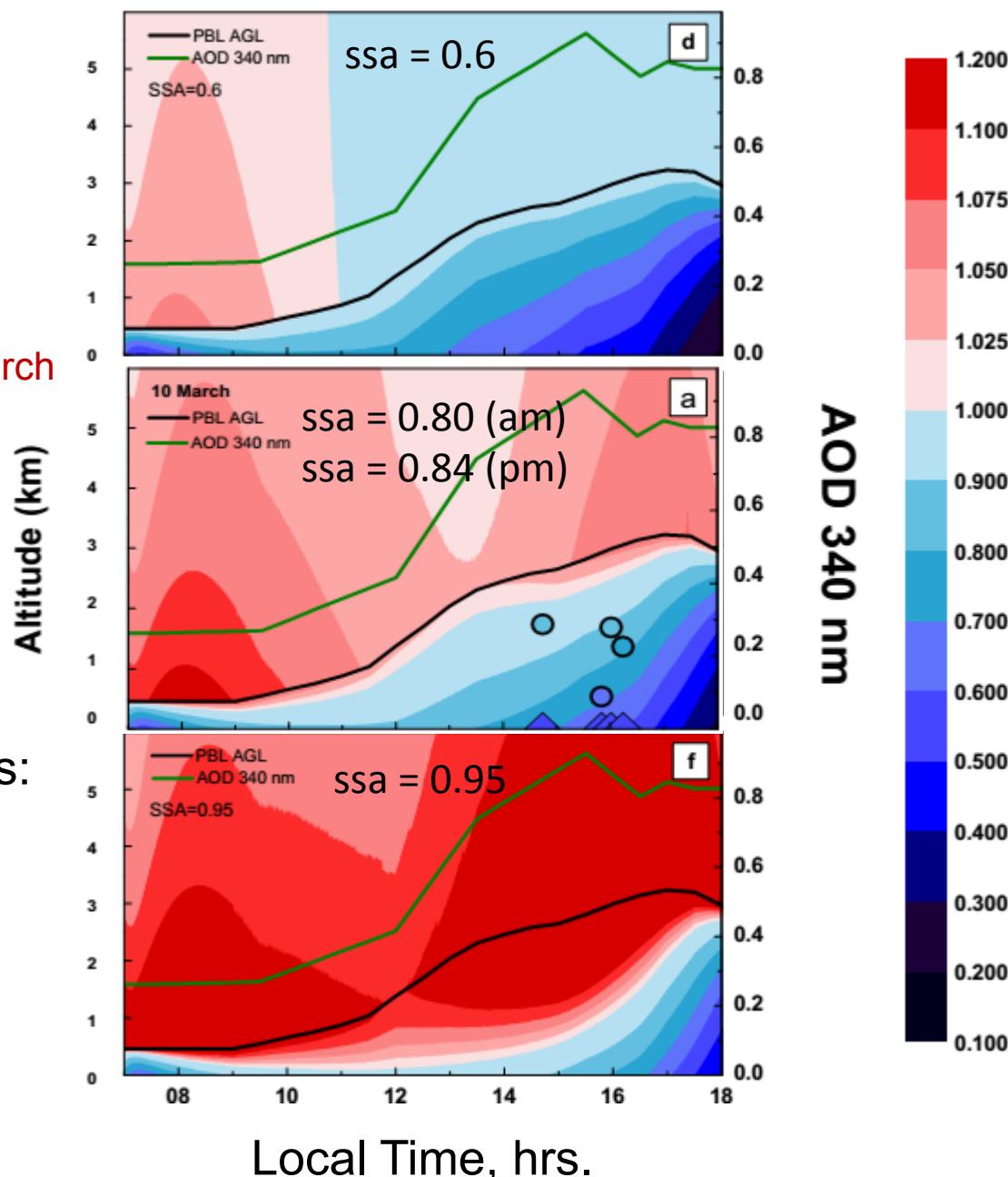


# Vertical Profile Is Sensitive to Single Scattering Albedo

Mexico City suburbs (T1) March 2006

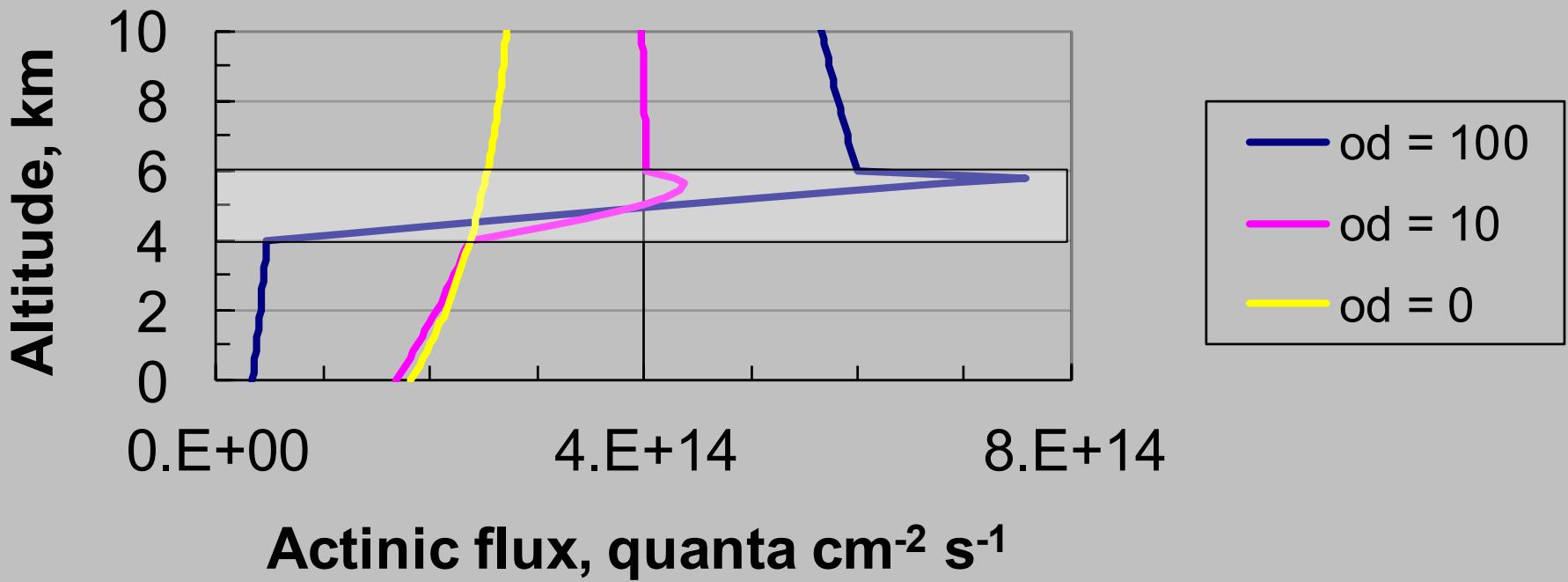
Central panel:  
Model with observed  
ssa, and obs.

Upper and lower panels:  
Sensitivity to ssa

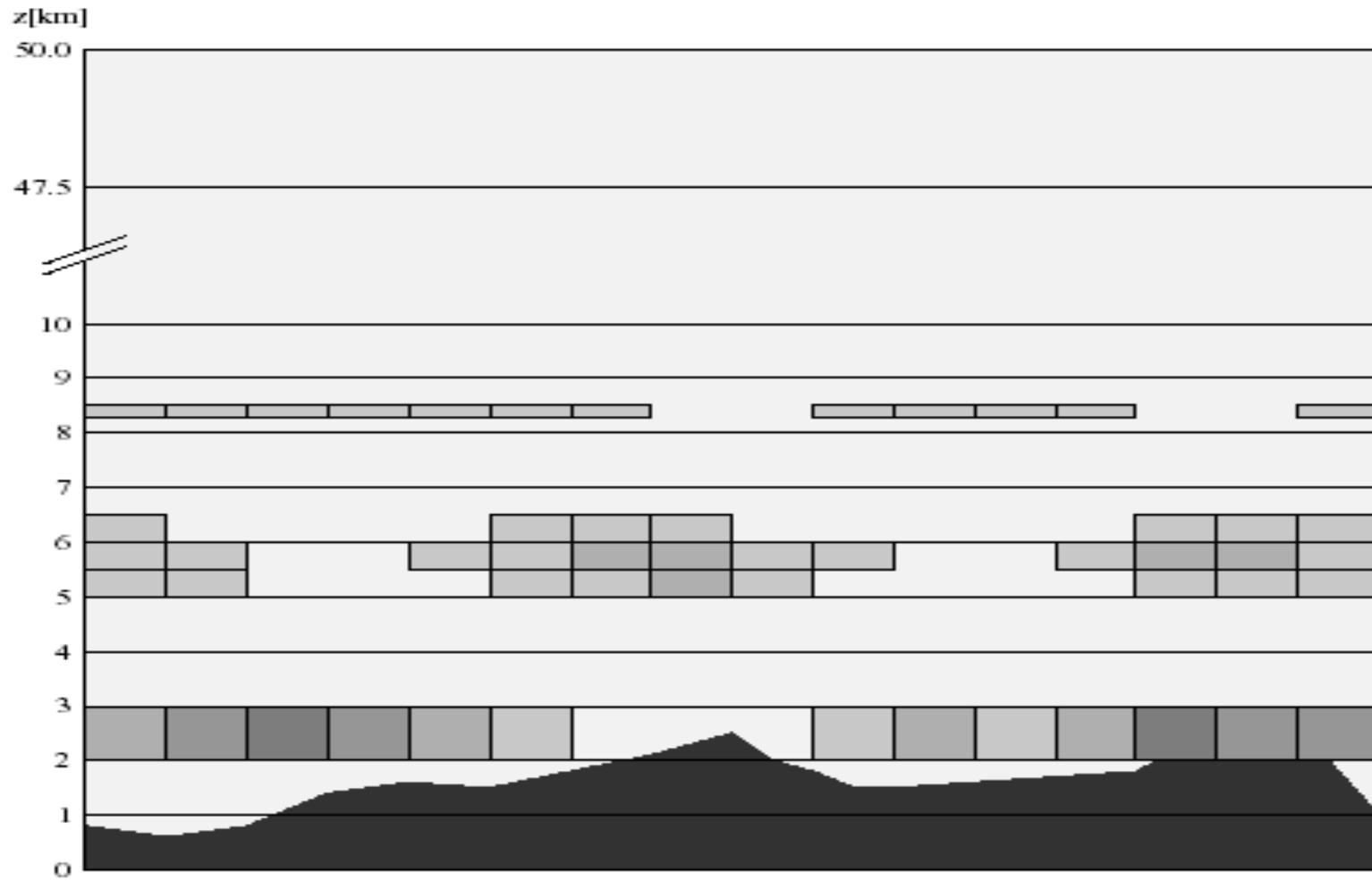


# EFFECT OF UNIFORM CLOUDS ON ACTINIC FLUX

340 nm, sza = 0 deg.,  
cloud between 4 and 6 km

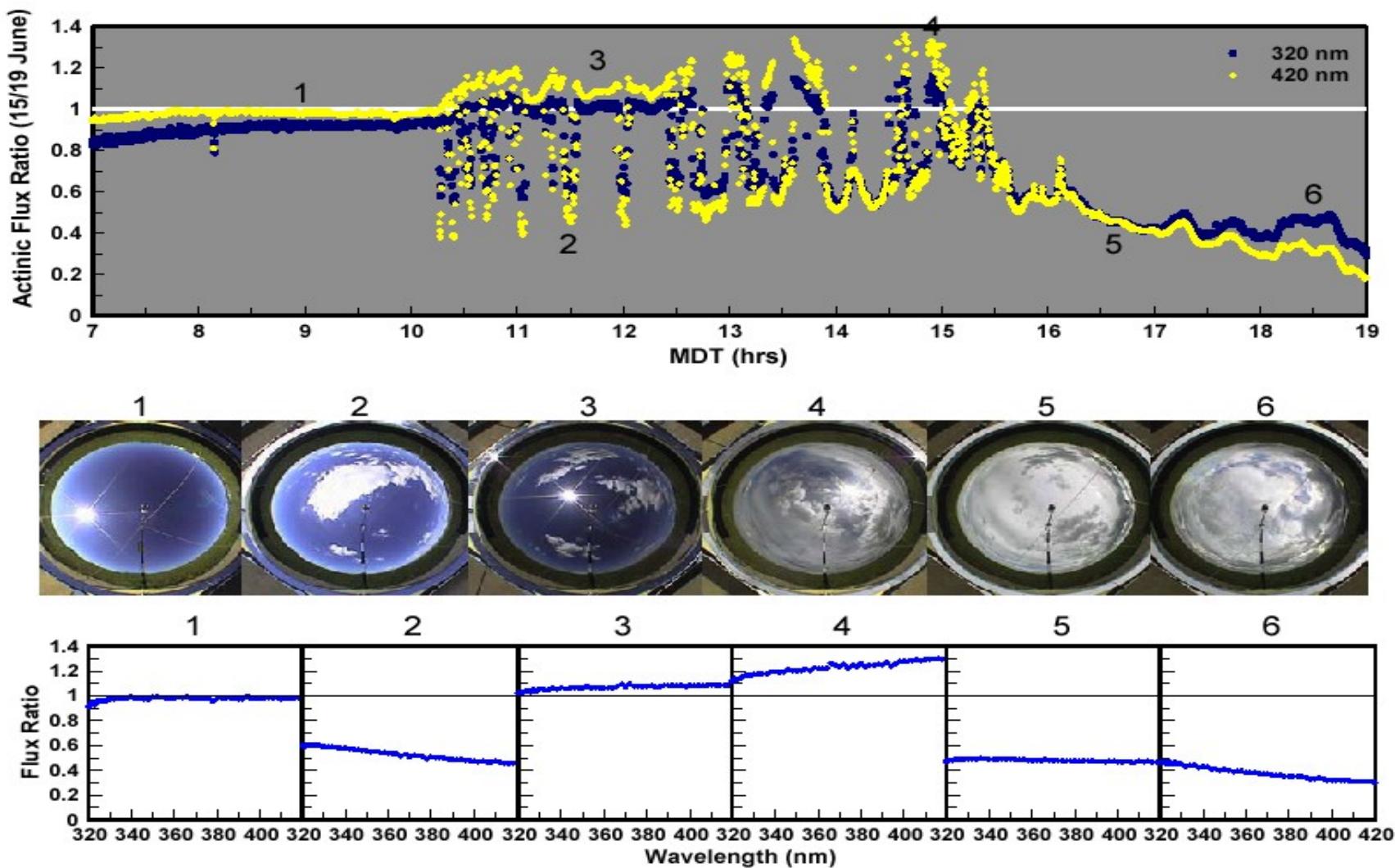


# Broken Clouds

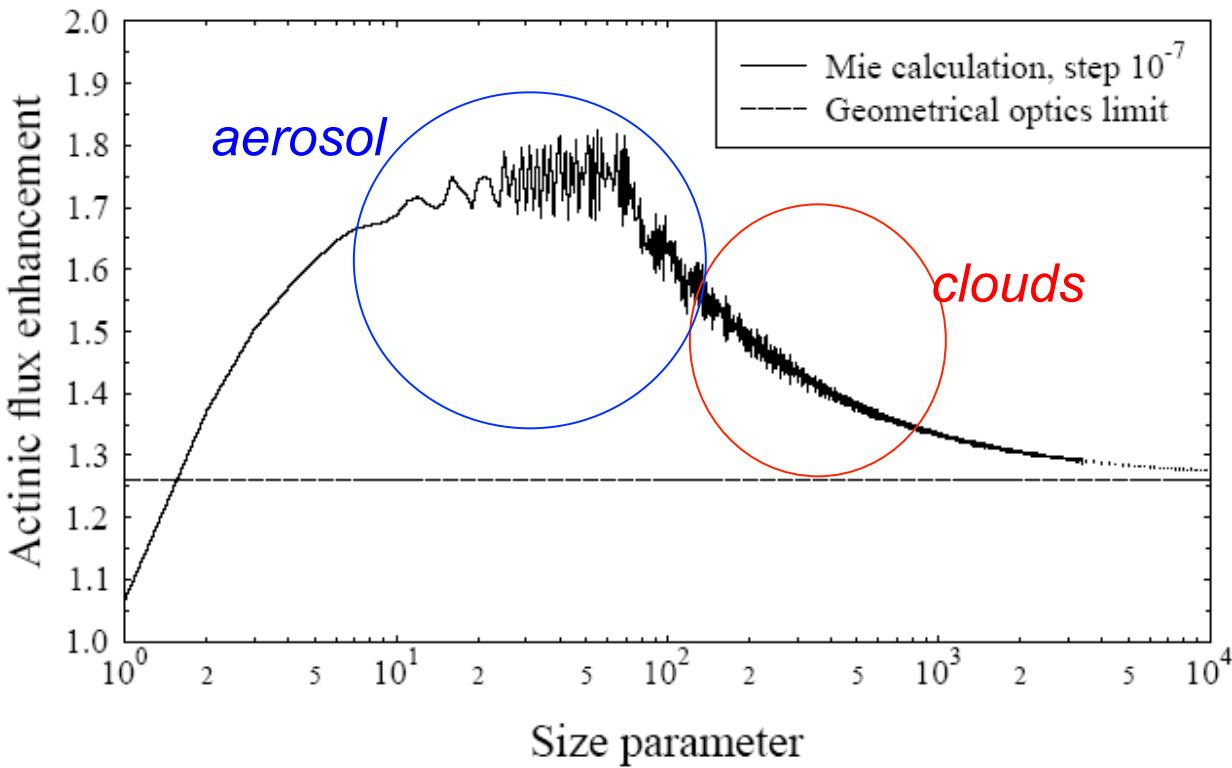


# PARTIAL CLOUD COVER

## enhancements and reductions

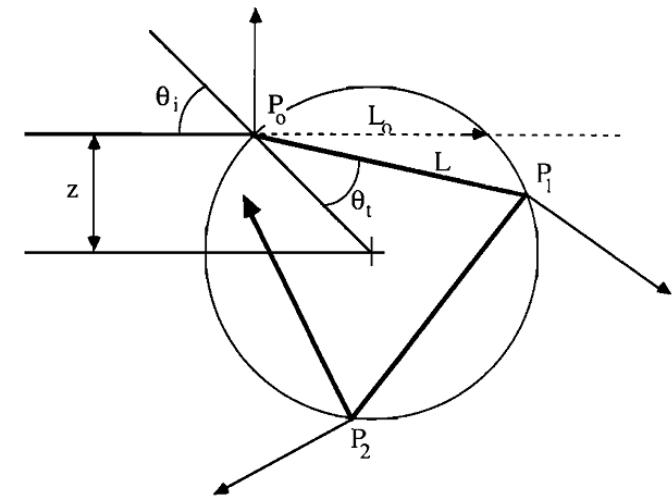


# Photochemistry Inside Liquid Particles



Actinic flux enhancements due to  
refraction/diffraction

Mayer and Madronich, 2004



# Photolysis in WRF-Chem

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- Several radiative transfer options:
  - TUV (delta-Eddington, 140 λ's) – major update soon
  - Fast-J (8-str Feautrier, 17 λ's)
  - Fast-TUV (delta-Eddington, 17 λ's, correction table)
  - Other? – faster, more accurate
- Sub-grid cloud overlap schemes
  - Max overlap if vertically contiguous, random otherwise
  - Effects of overlap schemes on vertical distribution of actinic flux
  - Need evaluation of WRF-Chem in the presence of clouds
- Aerosols:
  - Mixing rules for index of refraction
  - Mie scattering integrated over size distributions
  - Different core-shell options

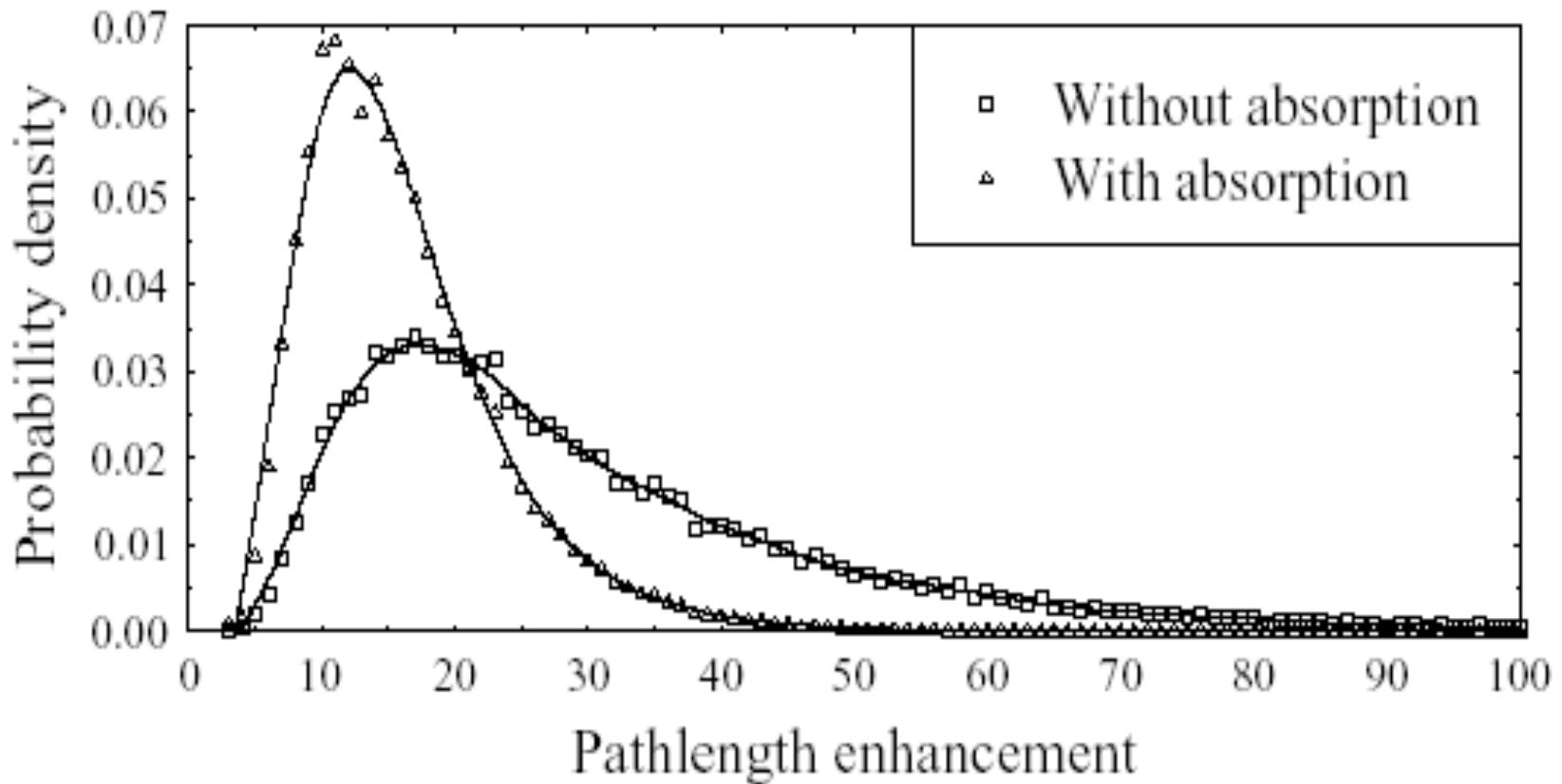
# OUTLINE

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- role of photolysis
- j vals
- xsects & qys
- radiation
- aerosols
- clouds
- wrf-chem

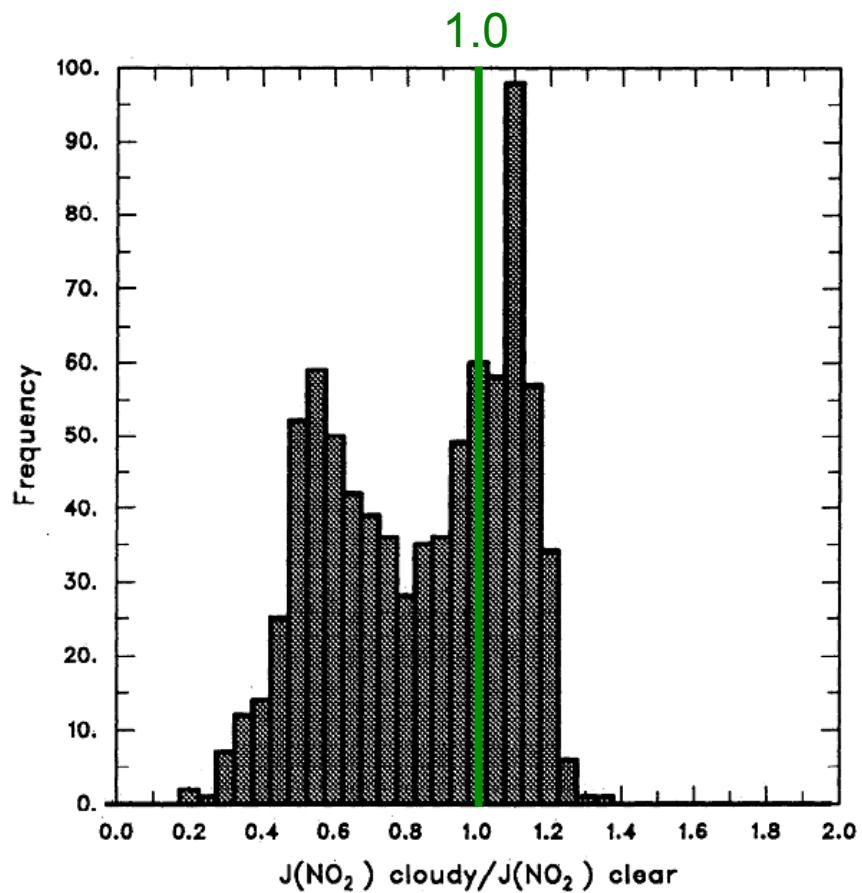
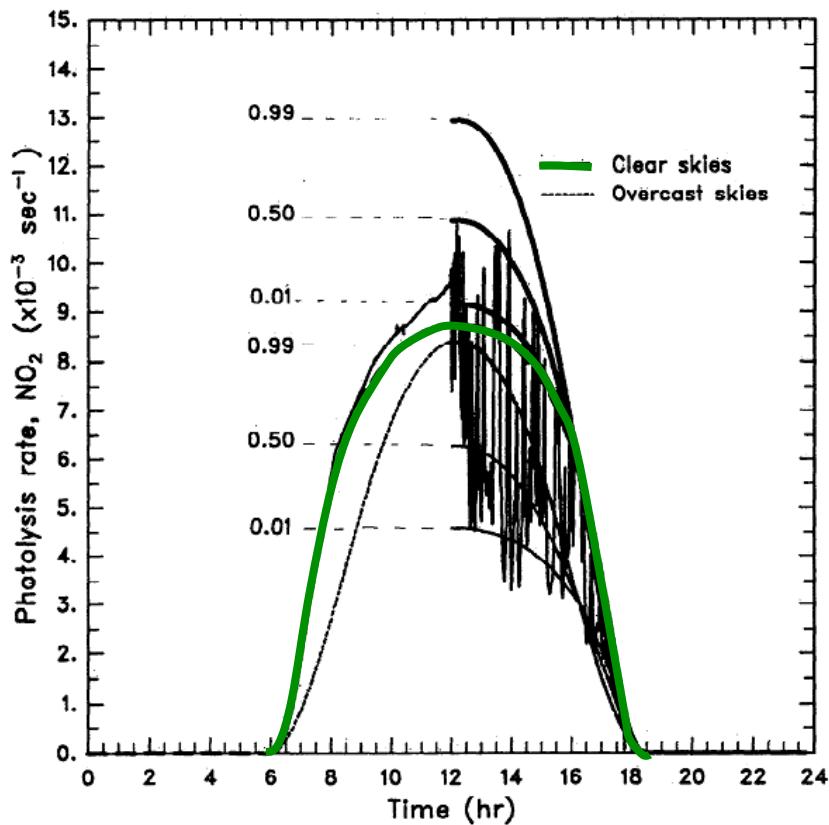
# INSIDE CLOUDS: Photon Path Enhancements

*Cumulonimbus, od=400*



# Enhancements Possible with Broken Clouds

## bimodal distribution



# SPECTRALLY INTEGRATED RADIATION

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- Radiometry

$$\text{Signal (W m}^{-2}\text{)} = \int_{\lambda} E(\lambda) R(\lambda) d\lambda$$

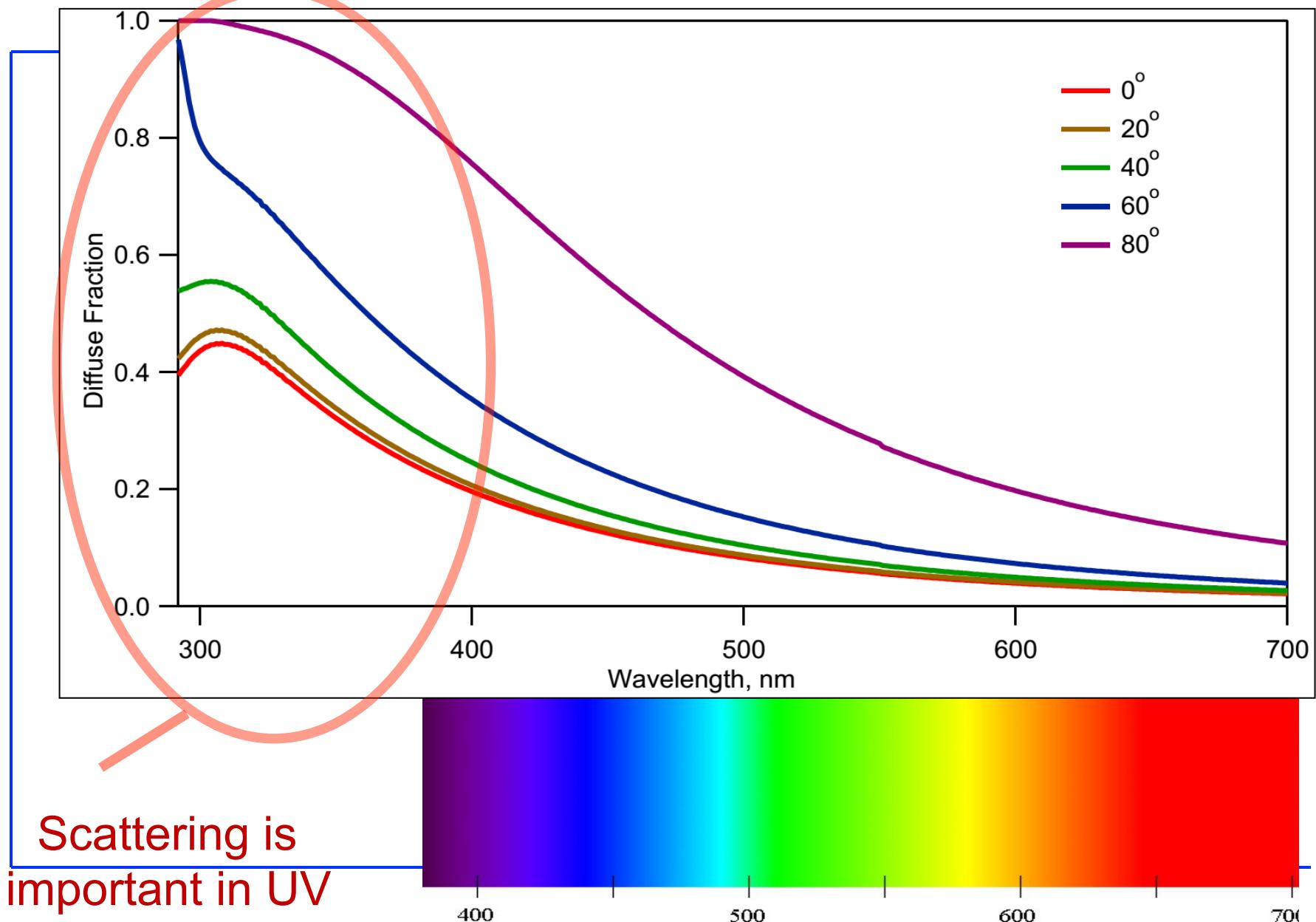
- Biological effects

$$\text{Dose rate (W m}^{-2}\text{)} = \int_{\lambda} E(\lambda) B(\lambda) d\lambda$$

- Photo-dissociation of atmospheric chemicals

$$\text{Photolysis frequency (s}^{-1}\text{)} = \int_{\lambda} F(\lambda) \sigma(\lambda) \phi(\lambda) d\lambda$$

# Diffuse Skylight vs. Direct Solar Beam (at sea level)



# Solid Angle

(units = steradians, sr)

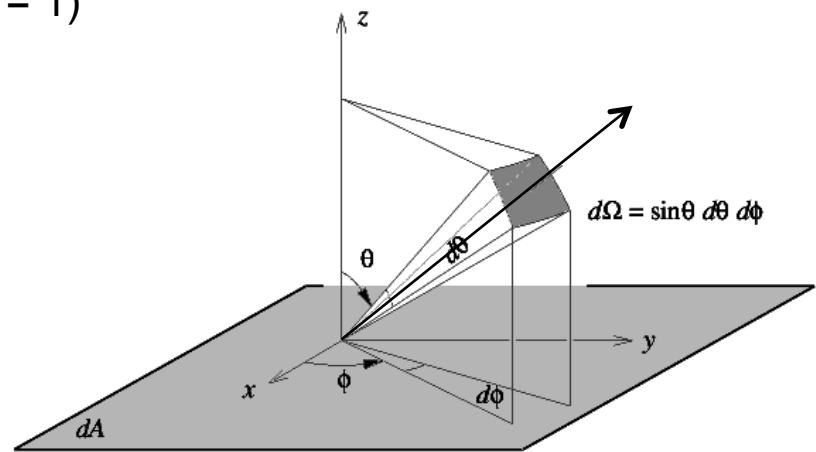
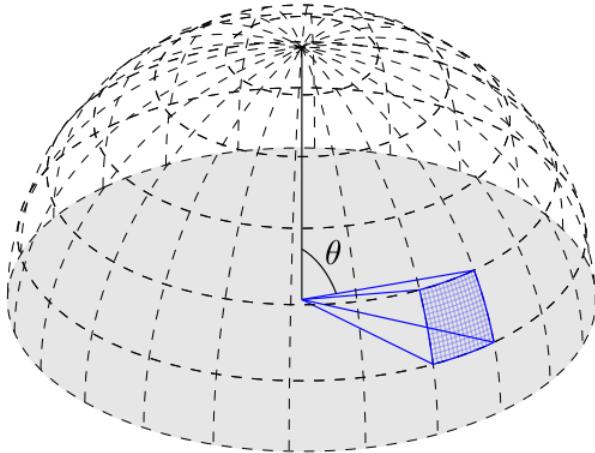
Solid Angle = area of patch on unit sphere ( $R = 1$ )

e.g.:

hemisphere =  $2\pi$  sr

full sphere =  $4\pi$  sr

Sun (seen from Earth)  $\approx 7 \times 10^{-5}$  sr



Spherical coordinates:

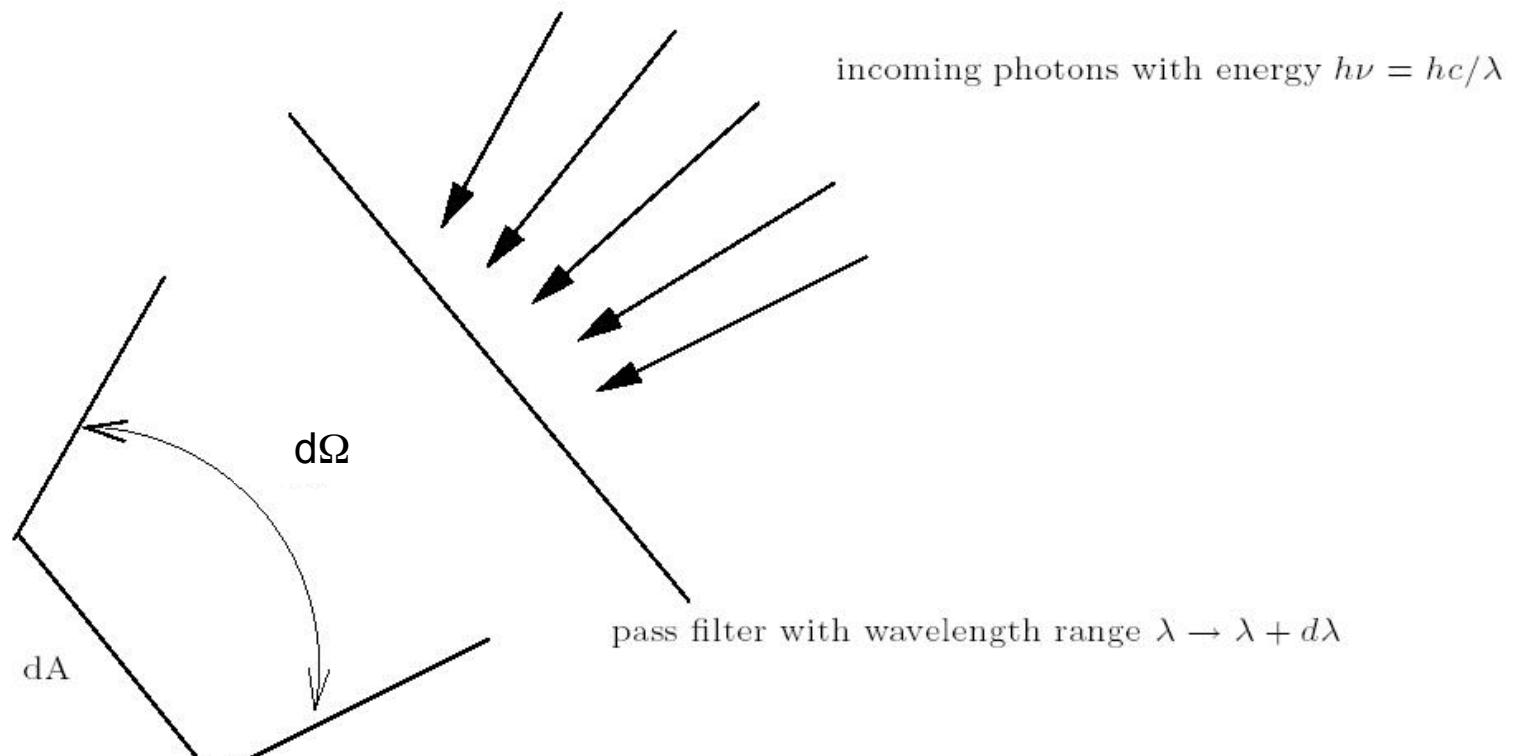
$\theta$  = zenith angle = Angle from vertical axis

$\phi$  = azimuth angle = angle in horizontal plane,  
from a reference direction, usually North

# Spectral Radiance, $I$

$$I(\lambda, \theta, \phi) = N(hc/\lambda) / (dt dA d\Omega d\lambda)$$

units:  $J s^{-1} m^{-2} sr^{-1} nm^{-1}$



(old name = Specific Intensity)

# Definition of Optical Depth

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$$\frac{dI}{dz} = -\sigma n I$$

(integral form)

$$I(z_2) = I(z_1) \exp [-\sigma n (z_2 - z_1)]$$

*Beer-Lambert Law:*  $I(z_2) = I(z_1) \exp [-\sigma n (z_2 - z_1)]$

*If  $\sigma$  and/or  $n$  depend on  $z$ , then*

$$\tau = \int_{z1}^{z2} \sigma(z) n(z) dz$$

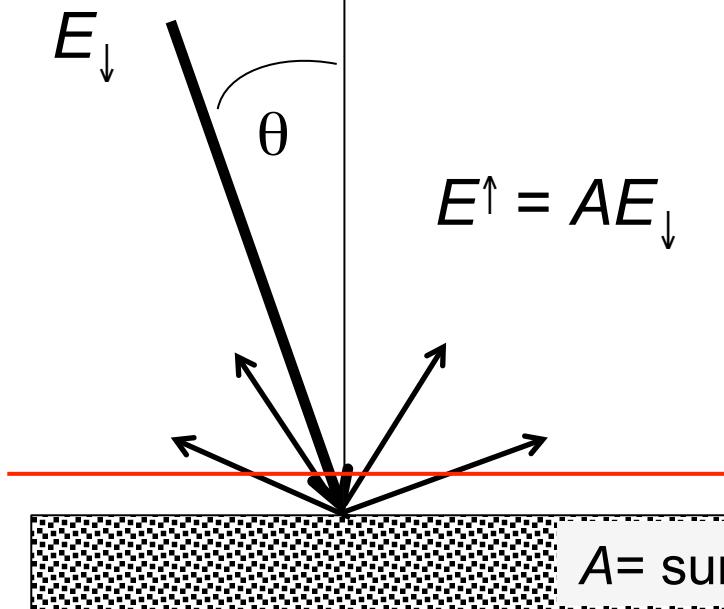
*Optical depth:*  $\tau = \sigma n (z_2 - z_1)$

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# Lambertian (isotropic) Reflection

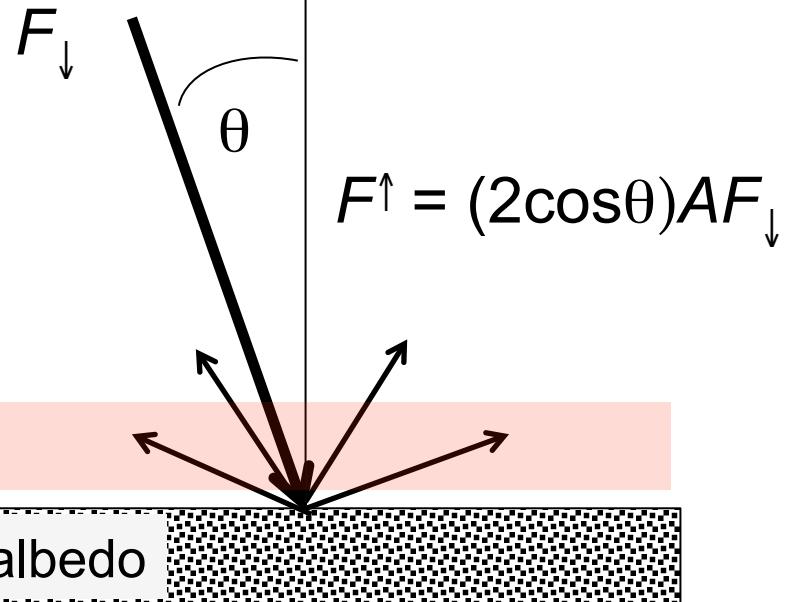
(e.g. approximately true for snow)

Irradiance:



$$E^{\uparrow} = AE_{\downarrow}$$

Actinic Flux:



$$F^{\uparrow} = (2\cos\theta)AF_{\downarrow}$$

$A$  = surface albedo

Limit for overhead sun,  $A = 1$ ,  $\theta = 0^{\circ}$ :

$E^{\uparrow} = E_{\downarrow}$  (conservation of energy), but  $F^{\uparrow} = 2F_{\downarrow}$  (not conserved)

# Mie Scattering Theory

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For spherical particles, given:

Complex index of refraction:  $n = m + ik$

Size parameter:  $\alpha = 2\pi r / \lambda$

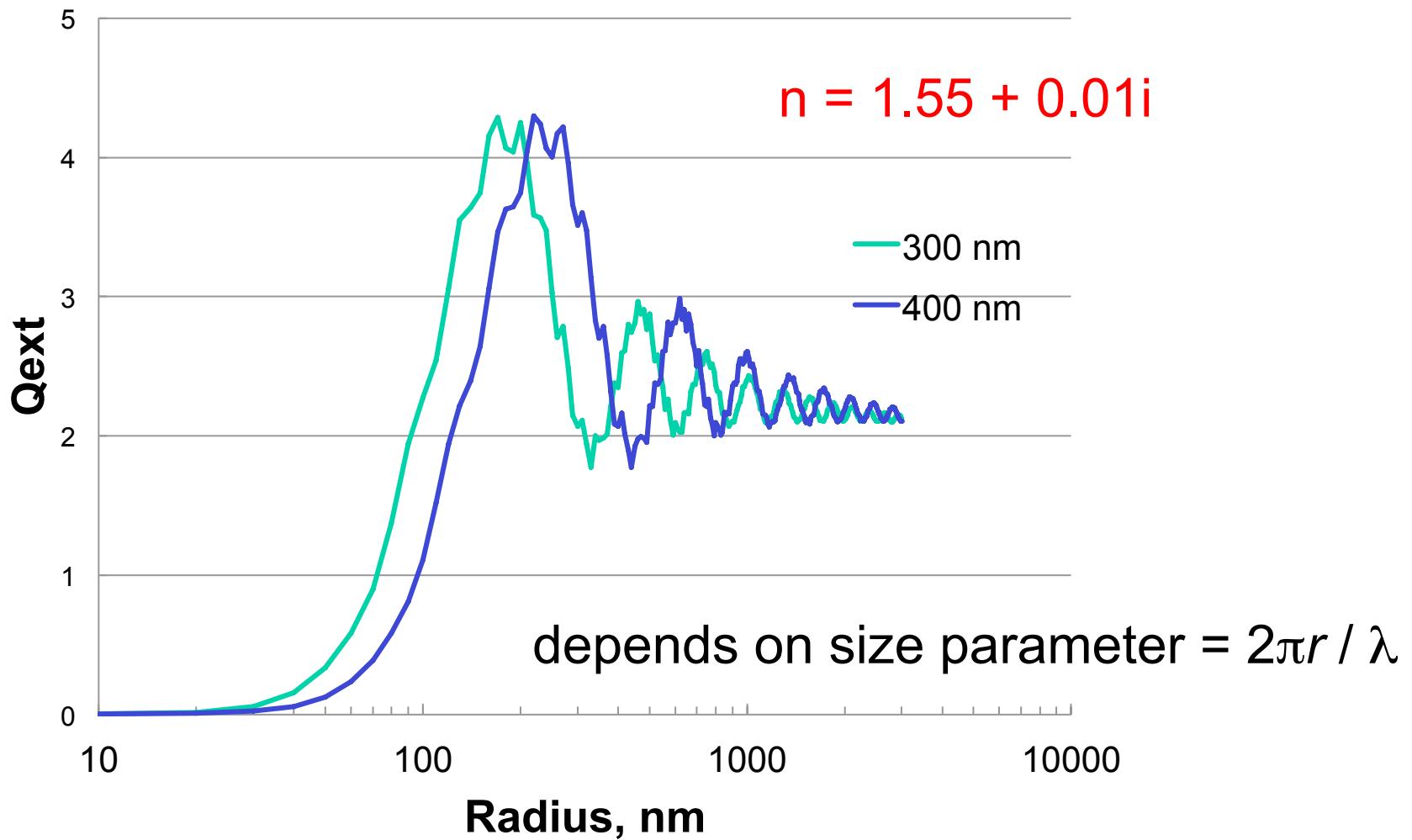
Can compute:

Extinction efficiency  $Q_e(\alpha, n) \propto \pi r^2$

Scattering efficiency  $Q_s(\alpha, n) \propto \pi r^2$

Phase function  
or asymmetry factor  $P(\Theta, \alpha, n)$   
 $g(\alpha, n)$

# Extinction Efficiency, $Q_{\text{ext}}$



## EFFECT OF CLOUDS (UNIFORM LAYER)

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- **Above cloud**: - high radiation because of reflection
- **Below cloud**: - lower radiation because of attenuation by cloud
- **Inside cloud**: - complicated behavior
  - Top half: very high values (for high sun)
  - Bottom half: lower values

## SIMPLE

### 2-STREAM

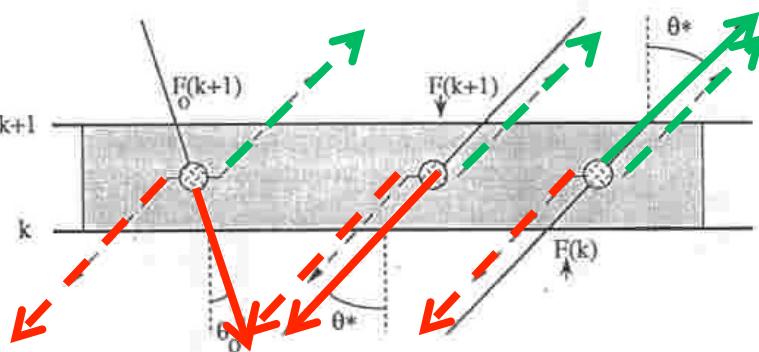
### METHOD:

3 Equations  
for each layer

$$F_o(k) = F_o(k+1)e^{-\Delta\tau / \cos \theta_o}$$

$$F_{\downarrow}(k) = F_{\downarrow}(k+1)e^{-\Delta\tau / \cos \theta^*} + f\omega_o F_o(k+1)(1 - e^{-\Delta\tau / \cos \theta_o}) + f\omega_o F_{\downarrow}(k+1)(1 - e^{-\Delta\tau / \cos \theta^*}) + (1-f)\omega_o F_{\uparrow}(k)(1 - e^{-\Delta\tau / \cos \theta^*})$$

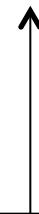
$$F_{\uparrow}(k+1) = F_{\uparrow}(k)e^{-\Delta\tau / \cos \theta^*} + (1-f)\omega_o F_o(k+1)(1 - e^{-\Delta\tau / \cos \theta_o}) + (1-f)\omega_o F_{\uparrow}(k)(1 - e^{-\Delta\tau / \cos \theta^*}) + f\omega_o F_{\downarrow}(k)(1 - e^{-\Delta\tau / \cos \theta^*})$$



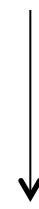
subject to the boundary conditions

at top ( $k = N$ ):  $F_o(N) = F_{\infty} \cos \theta_o$  and  $F_{\downarrow}(N) = 0$

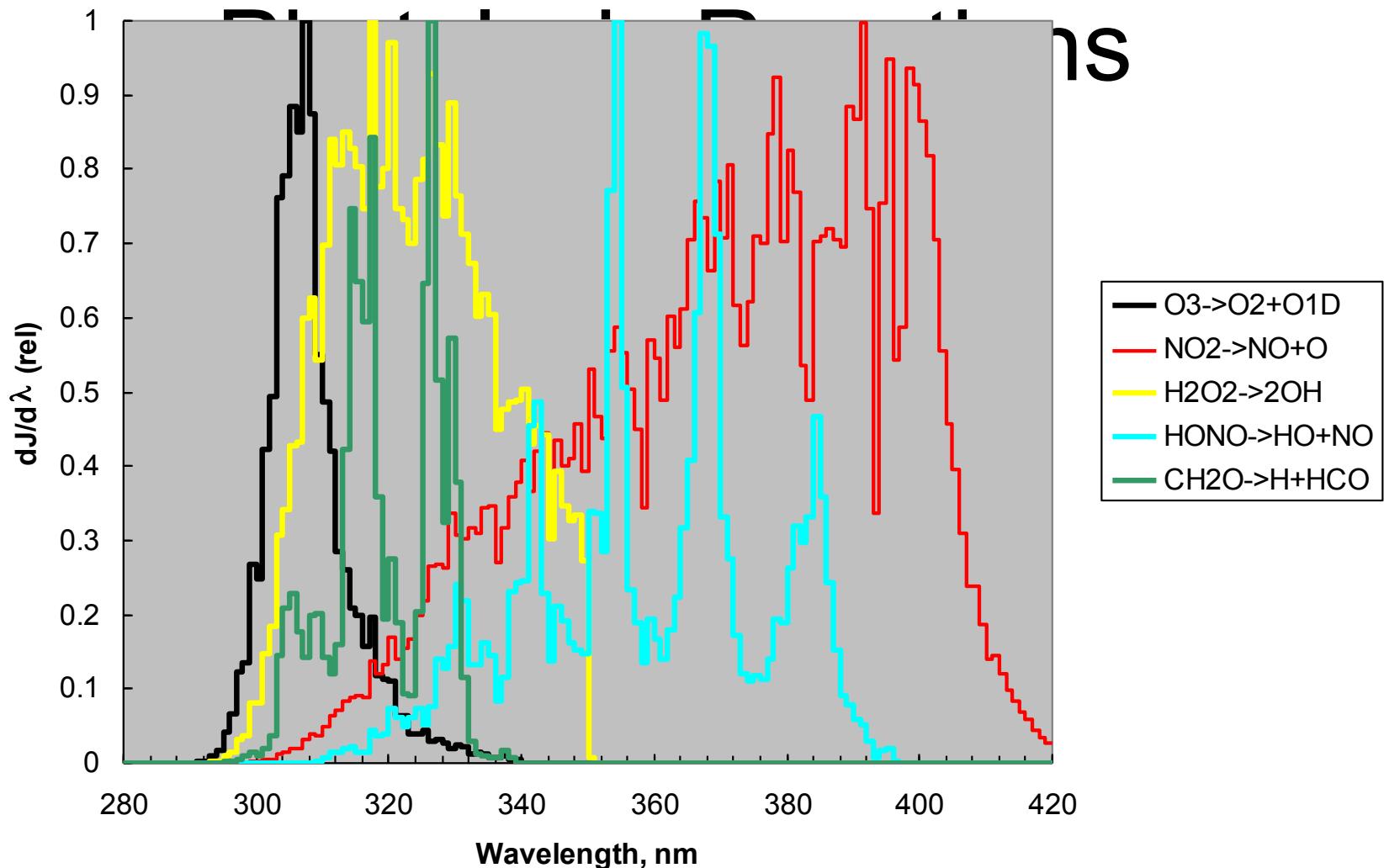
at bottom ( $k = 1$ ):  $F_{\uparrow}(1) = A[F_o(1) + F_{\downarrow}(1)]$



solve rt eq in each layer, get boundary values:



# Wavelengths for Different



*surface, overhead sun*

