# COMPUTER Systems & Programming Lecture #04 -Bits and Bit wise Operators KOC UNIVERSITY Applicable Programming Application of the Computer o



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#### Plan For Today

- Casting and Combining Types (cont'd.)
- Bitwise Operators
- Bitmasks
- Bit Shift Operators

Disclaimer: Slides for this lecture were borrowed from

—Nick Troccoli's Stanford CS107 class

# Good news, everyone!

 Labs start this week. Check your section assignment.

 Assg1 will be out on Oct 16 (due Oct 26)

 From nowon, I will be having my office hour every Thursday from 2pm to 3pm.



- Threads
- வ All DMs
- : More
- ▼ Channels
- # general
- # linux
- # macosx
- △ staff
- # windows
- + Add channels
- Direct messages
- ▼ Apps
- + Add apps



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#### https://join

#### Slack Developer Community Code of Conduct

This code of conduct governs Slack Platform's Community events and discussions.

#### Introduction

- Diversity and inclusion make our community strong. We encourage participation from the most varied and diverse backgrounds possible and want to be very clear about where we stand.
- Our goal is to maintain a safe, helpful and friendly community for everyone, regardless of experience, gender identity and expression, sexual orientation, disability, personal appearance, body size, race, ethnicity, age, religion, nationality, or other defining characteristic.
- This code and related procedures apply to unacceptable behavior occurring in all
  community venues, including behavior outside the scope of community activities —
  online and in-person— as well as in all one-on-one communications, and anywhere
  such behavior has the potential to adversely affect the safety and well-being of
  community members.

#### **Expected Behavior**

- Be welcoming.
- · Be kind.
- · Look out for each other.

#### **Unacceptable Behavior**

- Conduct or speech which might be considered sexist, racist, homophobic, transphobic, ableist or otherwise discriminatory or offensive in nature.
  - Do not use unwelcome, suggestive, derogatory or inappropriate nicknames or terms.
  - o Do not show disrespect towards others. (Jokes, innuendo, dismissive attitudes.)
- Intimidation or harassment (online or in-person). Please read the Citizen Code of Conduct for how we interpret harassment.
- · Disrespect towards differences of opinion.
- Inappropriate attention or contact. Be aware of how your actions affect others. If it

20/signup

#### Last Time

- Signed Integers
- Overflow
- Casting and Combining Types

#### Lecture Plan

- Casting and Combining Types (cont'd.)
- Bitwise Operators
- Bitmasks
- Bit Shift Operators

## Expanding Bit Representations

- Sometimes, we want to convert between two integers of different sizes (e.g. **short** to **int**, or **int** to **long**).
- We might not be able to convert from a bigger data type to a smaller data type, but we do want to always be able to convert from a smaller data type to a bigger data type.
- For **unsigned** values, we can add *leading zeros* to the representation ("zero extension")
- For **signed** values, we can *repeat the sign of the value* for new digits ("sign extension")
- Note: when doing <, >, <=, >= comparison between different size types, it will *promote to the larger type*.

## **Expanding Bit Representation**

#### **Expanding Bit Representation**

```
short s = 4;
                                                    s = 0000 \ 0000 \ 0000 \ 0100b
// short is a 16-bit format, so
int i = si
// conversion to 32-bit int, so i = 0000 0000 0000 0000 0000 0000 0100b
— or —
short s = -4;
// short is a 16-bit format, so
                                                        1111 1111 1111 1100b
int i = si
// conversion to 32-bit int, so i = 1111 1111 1111 1111 1111 1111 1100b
```

#### Truncating Bit Representation

If we want to **reduce** the bit size of a number, C *truncates* the representation and discards the *more significant bits*.

```
int x = 53191;
short sx = x;
int y = sx;
```

What happens here? Let's look at the bits in x (a 32-bit int), 53191:

#### 0000 0000 0000 0000 1100 1111 1100 0111

When we cast x to a short, it only has 16-bits, and C truncates the number:

#### 1100 1111 1100 0111

This is -12345! And when we cast sx back an int, we sign-extend the number.

```
1111 1111 1111 1111 1100 1111 1100 0111 // still -12345
```

#### Truncating Bit Representation

If we want to **reduce** the bit size of a number, C *truncates* the representation and discards the *more significant bits*.

```
int x = -3;

short sx = x;

int y = sx;
```

What happens here? Let's look at the bits in x (a 32-bit int), -3:

```
1111 1111 1111 1111 1111 1111 1111 1101
```

When we cast x to a short, it only has 16-bits, and C truncates the number:

```
1111 1111 1111 1101
```

This is -3! If the number does fit, it will convert fine. y looks like this:

#### Truncating Bit Representation

If we want to **reduce** the bit size of a number, C *truncates* the representation and discards the *more significant bits*.

```
unsigned int x = 128000;
unsigned short sx = x;
unsigned int y = sx;
```

What happens here? Let's look at the bits in x (a 32-bit unsigned int), 128000:

#### 0000 0000 0000 0001 1111 0100 0000 0000

When we cast x to a short, it only has 16-bits, and C truncates the number:

#### 1111 0100 0000 0000

This is 62464! **Unsigned numbers can lose info too**. Here is what y looks like:

**0000 0000 0000 1111 0100 0000 0000** // still 62464

#### The size of Operator

```
long sizeof(type);
```

```
// Example
long int_size_bytes = sizeof(int);  // 4
long short_size_bytes = sizeof(short); // 2
long char_size_bytes = sizeof(char); // 1
```

**sizeof** takes a variable type as a parameter and returns the size of that type, in bytes.

#### Bits and Bytes So Far

- all data is ultimately stored in memory in binary
- When we declare an integer variable, under the hood it is stored in binary

```
int x = 5;// really 0b0...0101 in memory!
```

- Until now, we only manipulate our integer variables in base 10 (e.g. increment, decrement, set, etc.)
- Today, we will learn about how to manipulate the underlying binary representation!
- This is useful for: more efficient arithmetic, more efficient storing of data, etc.

#### Aside: ASCII

- ASCII is an encoding from common characters (letters, symbols, etc.) to bit representations (chars).
  - E.g. 'A' is 0x41
- Neat property: all uppercase letters, and all lowercase letters, are sequentially represented!
  - E.g. 'B' is 0x42

#### Lecture Plan

- Casting and Combining Types (cont'd.)
- Bitwise Operators
- Bitmasks
- Bit Shift Operators

# Now that we understand binary representations, how can we manipulate them at the bit level?

#### Bitwise Operators

- You're already familiar with many operators in C:
  - Arithmetic operators: +, -, \*, /, %
  - Comparison operators: ==, !=, <, >, <=, >=
  - Logical Operators: &&, | |, !

- Today, we're introducing a new category of operators: bitwise operators:
  - &, |, ~, ^, <<, >>

# And (&)

AND is a binary operator. The AND of 2 bits is 1 if both bits are 1, and 0 otherwise.

| outpu | it = a | & b;   |
|-------|--------|--------|
| a     | b      | output |
| 0     | 0      | 0      |
| 0     | 1      | 0      |
| 1     | 0      | 0      |
| 1     | 1      | 1      |

& with 1 to let a bit through, & with 0 to zero out a bit

# Or (|)

OR is a binary operator. The OR of 2 bits is 1 if either (or both) bits is 1.

| output | = a | b;     |
|--------|-----|--------|
| a      | b   | output |
| 0      | 0   | 0      |
| 0      | 1   | 1      |
| 1      | 0   | 1      |
| 1      | 1   | 1      |

with 1 to turn on a bit, | with 0 to let a bit go through

## Not (~)

NOT is a unary operator. The NOT of a bit is 1 if the bit is 0, or 1 otherwise.

| output | = ~a;  |
|--------|--------|
| a      | output |
| 0      | 1      |
| 1      | 0      |

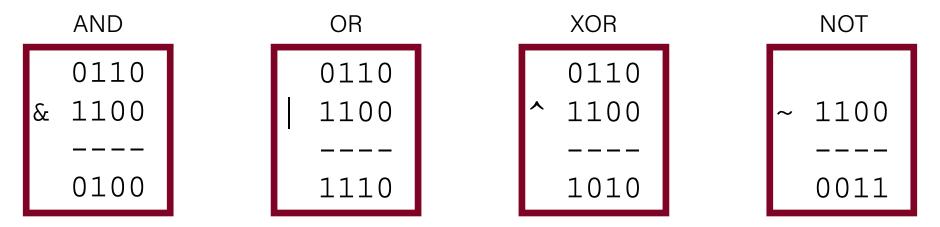
#### Exclusive Or (^)

Exclusive Or (XOR) is a binary operator. The XOR of 2 bits is 1 if *exactly* one of the bits is 1, or 0 otherwise.

| output | = a | ^ b;   |
|--------|-----|--------|
| a      | b   | output |
| 0      | 0   | 0      |
| 0      | 1   | 1      |
| 1      | 0   | 1      |
| 1      | 1   | 0      |

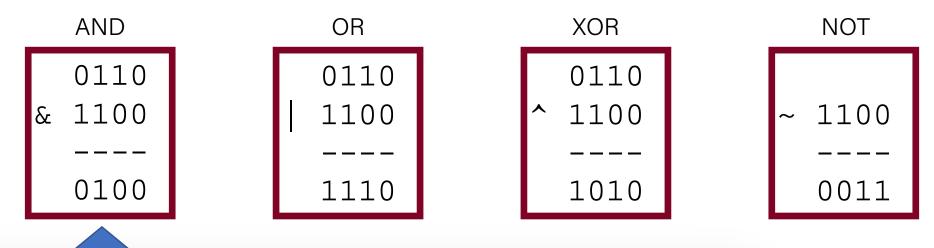
<sup>^</sup> with 1 to flip a bit, ^ with 0 to let a bit go through

 When these operators are applied to numbers (multiple bits), the operator is applied to the corresponding bits in each number. For example:



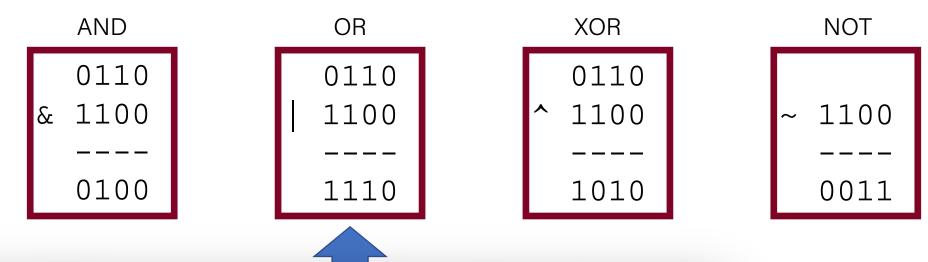
**Note:** these are different from the logical operators AND (&&), OR (||) and NOT (!).

 When these operators are applied to numbers (multiple bits), the operator is applied to the corresponding bits in each number. For example:



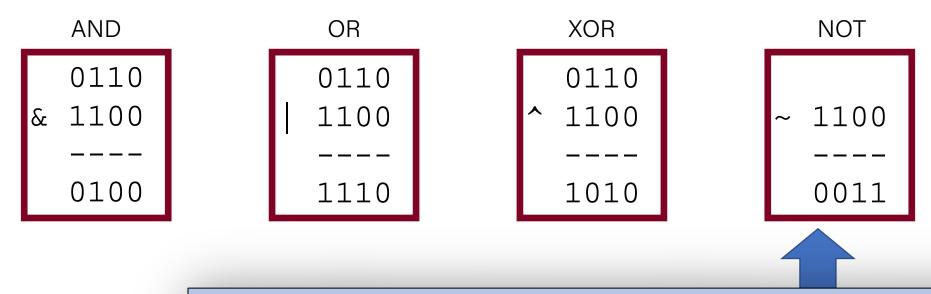
This is different from logical AND (&&). The logical AND returns true if both are nonzero, or false otherwise. With &&, this would be 6 && 12, which would evaluate to **true** (1).

 When these operators are applied to numbers (multiple bits), the operator is applied to the corresponding bits in each number. For example:



This is different from logical OR (||). The logical OR returns true if either are nonzero, or false otherwise. With ||, this would be 6 || 12, which would evaluate to **true** (1).

 When these operators are applied to numbers (multiple bits), the operator is applied to the corresponding bits in each number. For example:



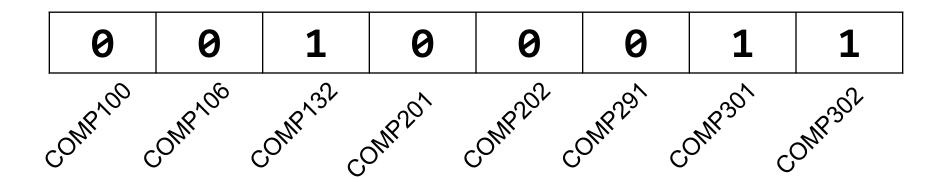
This is different from logical NOT (!). The logical NOT returns true if this is zero, and false otherwise. With !, this would be !12, which would evaluate to **false** (0).

#### Lecture Plan

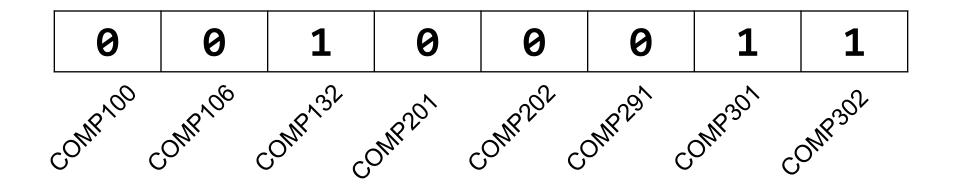
- Casting and Combining Types (cont'd.)
- Bitwise Operators
- Bitmasks
- Bit Shift Operators

#### Bit Vectors and Sets

- We can use bit vectors (ordered collections of bits) to represent finite sets, and perform functions such as union, intersection, and complement.
- Example: we can represent current courses taken using a char.



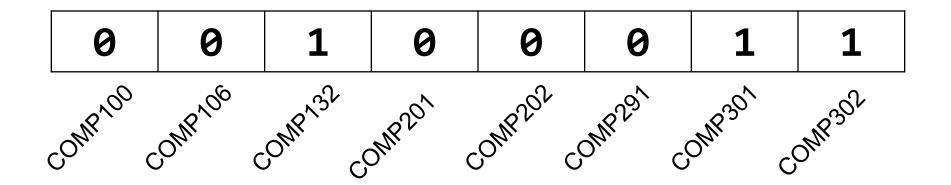
#### Bit Vectors and Sets



How do we find the union of two sets of courses taken? Use OR:

```
00100011
| 01100001
| -----
01100011
```

#### Bit Vectors and Sets

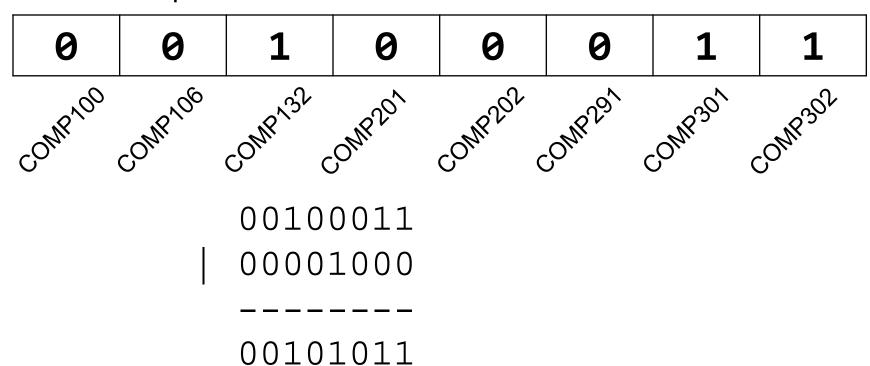


How do we find the intersection of two sets of courses taken? Use AND:

 We will frequently want to manipulate or isolate out specific bits in a larger collection of bits. A **bitmask** is a constructed bit pattern that we can use, along with bit operators, to do this.

• Example: how do we update our bit vector to indicate we've taken

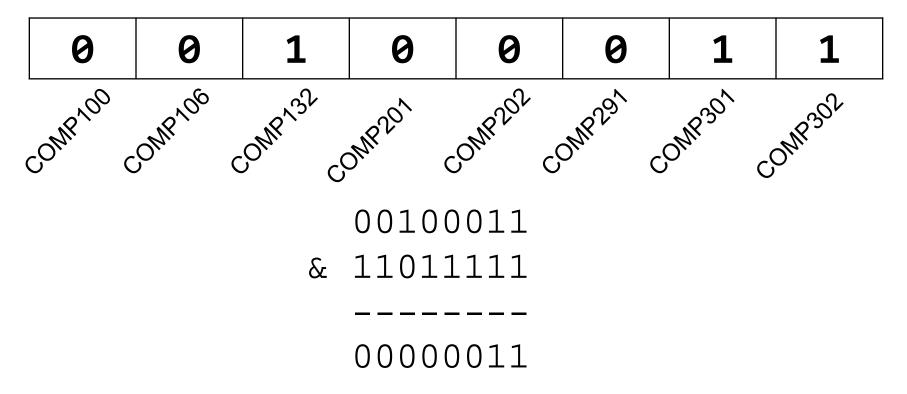
COMP202?



```
#define COMP100 0x1
                   /* 0000 0001 */
                      /* 0000 0010 */
#define COMP106 0x2
                      /* 0000 0100 */
#define COMP132 0x4
#define COMP201
              0x8 /* 0000 1000 */
#define COMP202 0x10 /* 0001 0000 */
#define COMP291 0x20
                    /* 0010 0000 */
#define COMP301 0x40 /* 0100 0000 */
#define COMP302
                0x80
                      /* 1000 0000 */
char myClasses = ...;
myClasses = myClasses | COMP201; // Add COMP201
```

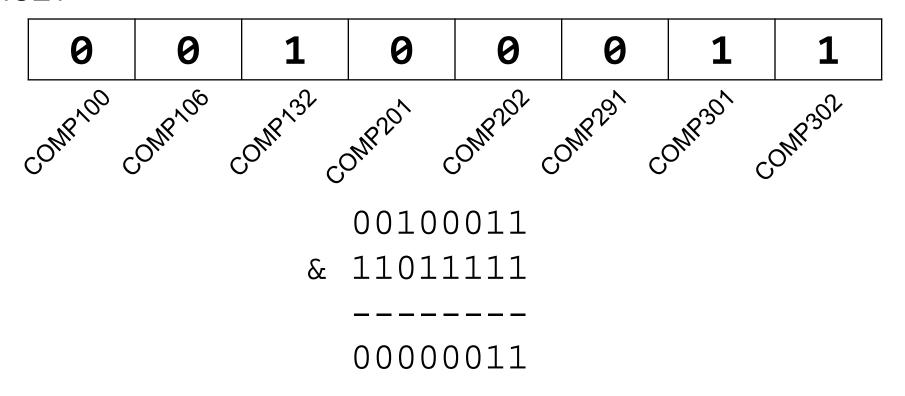
```
#define COMP100 0x1
                       /* 0000 0001 */
                       /* 0000 0010 */
#define COMP106 0x2
                       /* 0000 0100 */
#define COMP132 0x4
#define COMP201
               0x8 /* 0000 1000 */
                       /* 0001 0000 */
#define COMP202
               0x10
#define COMP291 0x20
                       /* 0010 0000 */
#define COMP301 0x40 /* 0100 0000 */
#define COMP302
                0x80
                       /* 1000 0000 */
char myClasses = ...;
myClasses |= COMP201; // Add COMP201
```

• Example: how do we update our bit vector to indicate we've *not* taken COMP132?



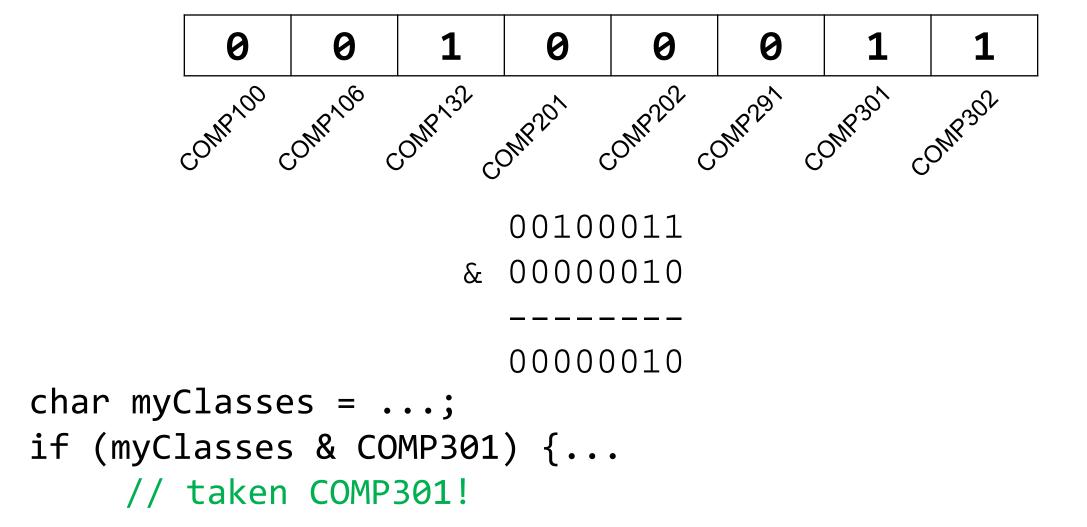
```
char myClasses = ...;
myClasses = myClasses & ~COMP132; // Remove COMP132
```

• Example: how do we update our bit vector to indicate we've *not* taken COMP132?

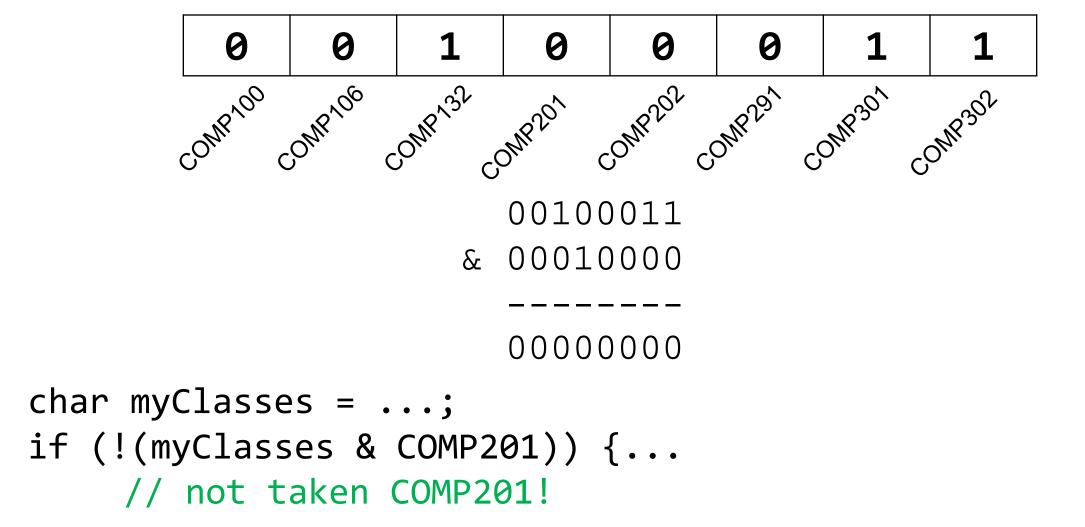


```
char myClasses = ...;
myClasses &= ~COMP132; // Remove COMP132
```

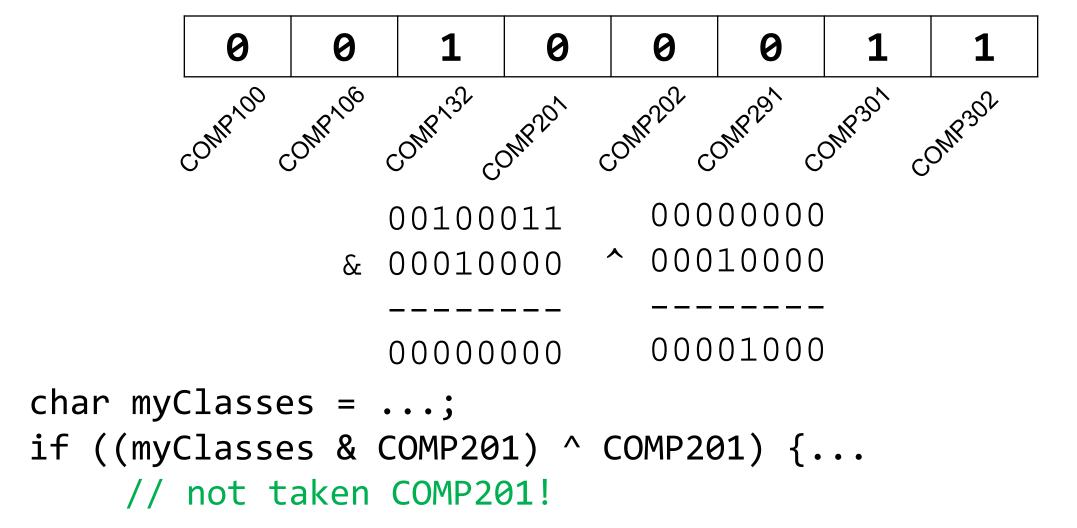
• Example: how do we check if we've taken COMP301?



• Example: how do we check if we've not taken COMP201?



• Example: how do we check if we've not taken COMP201?



### Bitwise Operator Tricks

- | with 1 is useful for turning select bits on
- & with 0 is useful for turning select bits off
- I is useful for taking the union of bits
- & is useful for taking the intersection of bits
- ^ is useful for flipping select bits
- ~ is useful for flipping all bits

• Bit masking is also useful for integer representations as well. For instance, we might want to check the value of the most-significant bit, or just one of the middle bytes.

• **Example**: If I have a 32-bit integer **j**, what operation should I perform if I want to get *just the lowest byte* in **j**?

```
int j = ...;
int k = j & 0xff; // mask to get just lowest byte
```

# Practice: Bit Masking

• **Practice 1**: write an expression that, given a 32-bit integer j, sets its least-significant byte to all 1s, but preserves all other bytes.

• **Practice 2**: write an expression that, given a 32-bit integer j, flips ("complements") all but the least-significant byte, and preserves all other bytes.

### Practice: Bit Masking

• **Practice 1:** write an expression that, given a 32-bit integer j, sets its least-significant byte to all 1s, but preserves all other bytes.

• **Practice 2:** write an expression that, given a 32-bit integer j, flips ("complements") all but the least-significant byte, and preserves all other bytes.

### Powers of 2

Without using loops, how can we detect if a binary number is a power of 2? What is special about its binary representation and how can we leverage that?

# Demo: Powers of 2



### Lecture Plan

- Casting and Combining Types (cont'd.)
- Bitwise Operators
- Bitmasks
- Bit Shift Operators

# Left Shift (<<)

The LEFT SHIFT operator shifts a bit pattern a certain number of positions to the left. New lower order bits are filled in with 0s, and bits shifted off the end are lost.

```
x << k;  // evaluates to x shifted to the left by k bits
x <<= k;  // shifts x to the left by k bits</pre>
```

#### 8-bit examples:

```
00110111 << 2 results in 11011100
01100011 << 4 results in 00110000
10010101 << 4 results in 01010000
```

The RIGHT SHIFT operator shifts a bit pattern a certain number of positions to the right. Bits shifted off the end are lost.

```
x >> k;  // evaluates to x shifted to the right by k bits
x >>= k;  // shifts x to the right by k bits
```

Question: how should we fill in new higher-order bits?

Idea: let's follow left-shift and fill with 0s.

```
short x = 2; // 0000 0000 0000 0010
x >>= 1; // 0000 0000 0000 0001
printf("%d\n", x); // 1
```

The RIGHT SHIFT operator shifts a bit pattern a certain number of positions to the right. Bits shifted off the end are lost.

```
x >> k;  // evaluates to x shifted to the right by k bit
x >>= k;  // shifts x to the right by k bits
```

Question: how should we fill in new higher-order bits?

Idea: let's follow left-shift and fill with 0s.

```
short x = -2; // 1111 1111 1111 1110
x >>= 1; // 0111 1111 1111 1111
printf("%d\n", x); // 32767!
```

The RIGHT SHIFT operator shifts a bit pattern a certain number of positions to the right. Bits shifted off the end are lost.

```
x >> k;  // evaluates to x shifted to the right by k bit
x >>= k;  // shifts x to the right by k bits
```

Question: how should we fill in new higher-order bits?

Problem: always filling with zeros means we may change the sign bit.

Solution: let's fill with the sign bit!

The RIGHT SHIFT operator shifts a bit pattern a certain number of positions to the right. Bits shifted off the end are lost.

```
x >> k;  // evaluates to x shifted to the right by k bit
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Question: how should we fill in new higher-order bits?

Solution: let's fill with the sign bit!

```
short x = 2; // 0000 0000 0000 0010
x >>= 1; // 0000 0000 0000 0001
printf("%d\n", x); // 1
```

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```
x >> k;  // evaluates to x shifted to the right by k bit
x >>= k;  // shifts x to the right by k bits
```

Question: how should we fill in new higher-order bits?

Solution: let's fill with the sign bit!

```
short x = -2; // 1111 1111 1110 x >>= 1; // 1111 1111 1111 1111 1111 1111 printf("%d\n", x); // -1!
```

There are two kinds of right shifts, depending on the value and type you are shifting:

- Logical Right Shift: fill new high-order bits with 0s.
- Arithmetic Right Shift: fill new high-order bits with the most-significant bit.

Unsigned numbers are right-shifted using Logical Right Shift.

Signed numbers are right-shifted using Arithmetic Right Shift.

This way, the sign of the number (if applicable) is preserved!

# Shift Operation Pitfalls

- Technically, the C standard does not precisely define whether a right shift for signed integers is logical or arithmetic. However, almost all compilers/machines use arithmetic, and you can most likely assume this.
- 2. Operator precedence can be tricky! For example:

1<<2 + 3<<4 means 1 << (2+3) << 4 because addition and subtraction have higher precedence than shifts! Always use parentheses to be sure:

$$(1<<2) + (3<<4)$$

# Bit Operator Pitfalls

- The default type of a number literal in your code is an int.
- Let's say you want a long with the index-32 bit as 1:

```
long num = 1 << 32;
```

• This doesn't work! 1 is by default an **int**, and you can't shift an int by 32 because it only has 32 bits. You must specify that you want 1 to be a **long**.

```
long num = 1L << 32;
```

### Recap

- Bitwise Operators
- Bitmasks
- Bit Shift Operators

Next time: How can a computer represent floating point numbers?