#### CS 5/6110, Software Correctness Analysis, Spring 2021

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#### Overview of Lecture 19

- Projects
  - Please fix meeting this week (schedule online) to
    - Select/Refine projects
    - Seek resources
      - Projects will be the central aspect of your class
- Today's topic : Cache Coherence

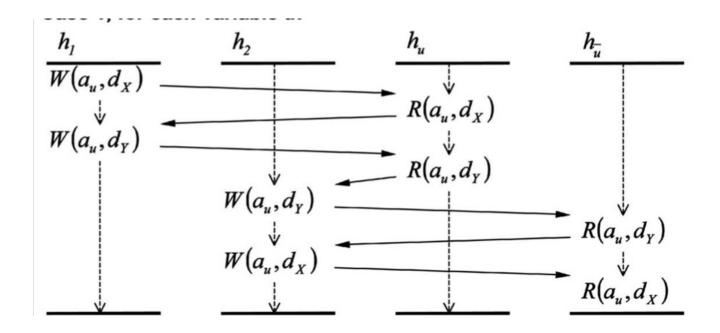
#### What is cache coherence?

- With shared-memory multiprocessors being the norm, we need a notion of sharing memory "as if it were one common area"
  - What does this mean?
    - Every write by Pi is readable by Pi as well as Pj where i != j
  - This is not precise-enough
    - A program can write more times to a location than once ©
    - There could be multiple readers of a line
- So,
  - Formally define when write-events are observable by read-events that match

#### What is cache coherence?

- To define memory views as shared by multiple processors, we need to define a formal shared memory consistency model
- Coherence is one of the basic models
  - Each location has a latest data that every reader agrees on
  - Also known as "per-location sequential consistency"
- There are some interesting complexity results that help us understand coherence
  - Given a "finished execution trace", checking coherence is NP-Complete
    - Very insightful proof by Jason Cantin et al
    - https://ieeexplore.ieee.org/stamp/stamp.jsp?arnumber=1435343

#### How a programmer sees coherence (Cantin paper)



Given four processes (or hardware threads) and reads/writes Per location ("a\_u" in this case) explain read-value outcomes. Here we explain as if this interleaving took place.

The inability find such an explanation means the system is incoherent

# Implementing coherence

- Snoopy-bus protocols (still present at smaller scales)
- Directory-based protocols (more scalable)
- See <a href="https://www.morganclaypool.com/doi/pdf/10.2200/S00962ED2V01Y201910CAC049">https://www.morganclaypool.com/doi/pdf/10.2200/S00962ED2V01Y201910CAC049</a> for Thu's colloq speaker's book

#### Coherence Verification

- Given the complexity of coherence protocols, formal methods (model-checking mainly) is essential
- Let us take a look at an academic protocol called The German Protocol
- How does coherence verification scale?
  - Not well today, large protocols take days to cover for one bit of data and 3 processors
  - Solutions
    - Derive cutoff bounds Emerson and Kahlon
      - The bounds are large (7-8) and automatically computing bounds is not practical for large protocols
    - Do a parametric verification
      - Prove coherence for all "N" N is the number of cores/threads
      - This involves modeling 2-3 nodes explicitly and involves a manual abstraction/refinement loop called CEGAR
        - Counter-Example Guided Abstraction Refinement
      - Involves designer input of non-interference lemmas
    - Do formal synthesis
      - Dr. Nagarajan will be presenting this on Thu

# **Basics about Transition Systems**

 Before we study the German protocol and how the parametric verification method I'm going to present works, let us discuss basic concepts about formal transition systems

#### Almost all specs for safety property checking look like this

Based on Guarded Commands

```
Rule1: g1 ==> a1
Rule2: g2 ==> a2
...
RuleN: gN ==> aN
Invariant P
```

- Supported by tools such as Murphi (Stanford, Dill's group)
- Presents the behavior declaratively
  - Good for specifying "message packet" driven behaviors
  - Sequentially dependent actions can be strung using guards
- "Rule Sets" can specify behaviors across axes of symmetry
  - Processors, memory locations, etc.
- Simple and Universally Understood Semantics

Let us understand how we may safely transform such rule-based specifications (this is what we have to do in the parametric verification approach to be presented). The method is called the CMP method named after its inventors at Intel.

# Let us understand how we may safely transform such rule-based specifications. The first few will be warmups. Then the real thing!

- Observation: Weakening a guard is sound
- Suppose we add a disjunct as below (Cond1) and still manage to show that P is an invariant, then without adding Cond1, the result must still hold

Rule1: g1 \/ Cond1 ==> a1
Rule2: g2 ==> a2
Invariant P

- Reason: Rule1 fires more often with Cond1 added!
- May get false alarms (P may fail if Rule1 fires spuriously)
- For many "weak properties" P, we can "get away" by guard weakening
  - This is a standard abstraction, first proposed by Kurshan (E.g. removing a module that is driving this module, letting inputs "dangle")
- BUT in the CMP method, we won't do this rather we will do guard strengthening!
- Except it is useful to know this disjunction property in thinking about certain steps of CMP

#### But... Guard Strengthening is, by itself, Unsound

Strengthening a guard is not sound

Rule1: g1 /\ Cond1 ==> a1

Rule2: g2 ==> a2

**Invariant P** 

- Reason: Rule1 fires only when g1 /\ Cond1
- So, less behaviors examined in checking P
  - Thus, verifying \_with\_ Cond1 means nothing for verification without Cond1
- But hang on, there is more in the CMP method ©

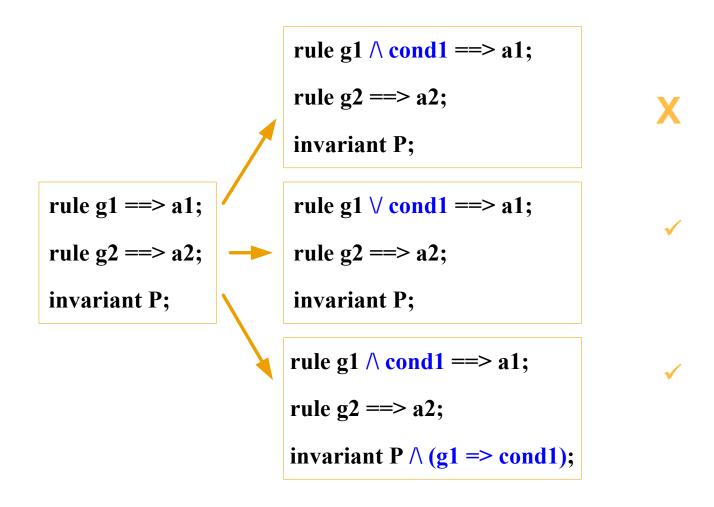
# Guard Strengthening can be made sound, if the conjunct is implied by the guard

This is sound

```
Rule1: g1 /\ Cond1 ==> a1
Rule2: g2 ==> a2
Invariant P /\ (g1 ==> Cond1)
```

- Reason: Rule1 fires only when g1 /\ Cond1
- BUT, Cond1 is always implied by g1; we are showing g1→Cond1 is an invariant also, so no real loss of states over which Rule1 fires...
  - Call this "Guard Strengthening Supported by Lemma"
- Except, you are showing the invariant in the same modified system!
  - This is fine:
    - Initial state satisfies P, and also (g1 → Cond1). Thus, whenever g1 is true in the initial state, Cond1 is an implied fact. So g1 /\ Cond1 is like g1 by itself.
    - Thus "a1" can be conducted in the initial state, to obtain the next set of states. (No change wrt g2 and a2, so they are like before.)
  - In general
    - At state t (by induction over time), we have P true and (g1 → Cond1) true.
    - Thus , g1, when true, implies Cond1 at time t. Thus g1 /\ Cond1 is like g1 (same truth status) at time t
      - Thus we can obtain the state at t+1 safely via "a1"

# Summary of Transformations so far (checkmark shows what's safe)



# The CMP Approach

- Weaken to the Extreme
- Then Strengthen Back Just Enough (to pass all properties)

#### Weaken to the Extreme sounds crazy at first!

Rule1: g1 \/ True ==> a1

Rule2: g2 ==> a2

**Invariant P** 

The transition system above can be transformed to the one below without any issues (except the proof of P being an invariant might not go through) – but that will be fixed momentarily

**Rule1: True ==> a1** 

Rule2: g2 ==> a2

**Invariant P** 

#### Strengthen Back Some

Rule1: True /\ C1 ==> a1

Rule2: g2 ==> a2

Invariant P  $\land$  (g1 => C1)

"Not Enough!" may be the outcome of strengthening. That is, while we added C1 back, it may not be strong-enough.

How to pick C1 will be discussed soon.

#### Strengthen Back More...

Rule1: True /\ C1 ==> a1

Rule2: g2 ==> a2

Invariant P  $\land$  g1 => C1

"Not Enough!"



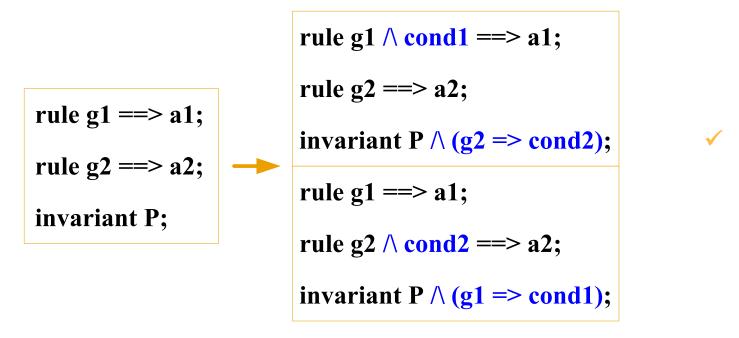
Rule1: True /\ C1 /\ C2 ==> a1

Rule2: g2 ==> a2

Invariant P  $\land$  (g1 => C1)  $\land$  (g1 => C2)

"OK, just right!"

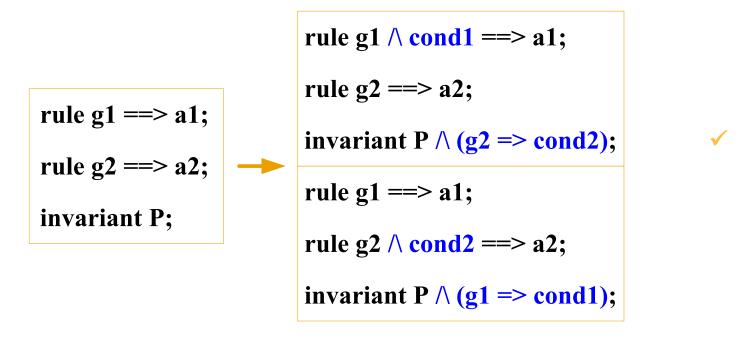
# A Variation of Guard Strengthening Supported by Lemma: Doing it in a meta-circular manner (i.e., the temporal induction I alluded to earlier...)



This is the approach in our work

Now the secret: in the CMP method, the designer decouples all nodes beyond k (typically 2) explicitly modeled nodes. Then, brings back the N-k nodes, but in 'spirit' - i.e., in terms of the non-interference conditions they must obey (note that "N" is a free parameter).

The Ci are thus the non-interference lemmas. Each is discovered upon seeing a counterexample, and then added back into the system! If the coherence invariant is proved (usually this happens), then you ended up having used a model-checker to prove a parametric theorem - which is a big deal!



This is the approach in our work

#### This method has been perfected at Intel and in production use!

- See <u>https://www.cs.utexas.edu/~hunt/FMCAD/FMCAD09/slides/talupur.pdf</u>
- https://dl.acm.org/doi/pdf/10.5555/1517424.1517434
- Designers write "protocol flow" diagrams as part of standard documentation
  - These are mined to obtain the non-interference lemmas
- See http://formalverification.cs.utah.edu/presentations/fmcad04\_tuto rial2/chou/ctchou-tutorial.pdf for details of how this is done
- NOTE the table-style specification recommended in the above tutorial at fmcad04!!

We will now present highlights of the German Protocol to tell you how coherence protocols look like (but this is like a "hello world" of cache protocols)

- See german.m , german.pdf , and abs-german.pdf in the class directory
- We will note down some highlights in the coming slides

```
const -- configuration parameters --
NODE NUM : 6;
DATA_NUM : 2;
type -- type decl --
NODE : scalarset(NODE_NUM);
DATA : scalarset(DATA_NUM);
CACHE_STATE : enum {I, S, E};
CACHE: record State: CACHE_STATE; Data: DATA; end;
MSG_CMD : enum {Empty, ReqS, ReqE, Inv, InvAck, GntS, GntE};
MSG : record Cmd: MSG_CMD; Data : DATA; end;
```

```
var -- state variables --
Cache: array [NODE] of CACHE; -- Caches
Chan1 : array [NODE] of MSG; -- Channels for Req*
Chan2 : array [NODE] of MSG; -- Channels for Gnt* and Inv
Chan3 : array [NODE] of MSG; -- Channels for InvAck
InvSet : array [NODE] of boolean; -- Nodes to be invalidated
ShrSet : array [NODE] of boolean; -- Nodes having S or E copies
                                         — E copy has been granted
ExGntd : boolean;
CurCmd : MSG_CMD;
                                         -- Current request command
                                         -- Current request node
CurPtr : NODE;
MemData : DATA;
                                         — Memory data
                                         -- Latest value of cache line
AuxData : DATA;
```

```
-- Initial States --
ruleset d : DATA do startstate "init"
—— All nodes: init all cmd channels to be empty, Cache States I,
-- the set of nodes to be invalidated is empty
-- and nodes having S or E copies empty
  for i : NODE do
    Chan1[i].Cmd := Empty;
    Chan2[i].Cmd := Empty;
    Chan3[i].Cmd := Empty;
    Cache[i].State := I;
    InvSet[i] := false;
    ShrSet[i] := false;
  end;
  ExGntd := false;
  CurCmd := Empty;
 MemData := d;
  AuxData := d;
end end;
```

```
ruleset i : NODE do
-- Any node with cmd req channel empty and cache I/S can request ReqE
rule "SendReqE"
    Chan1[i].Cmd = Empty &
    (Cache[i].State = I |
        Cache[i].State = S)
    ==>
    Chan1[i].Cmd := ReqE; -- raises "ReqE" semaphore
end
end;
```

```
ruleset i : NODE do
-- For any node that is waiting with ReqS requested, with CurCmd Empty
-- we set CurCmd to ReqS on behalf of node i (setting CurPtr to point to it).
-- Then void Chan1 empty.
—— Now Set the nodes to be invalidated to the nodes having S or E copies.
  rule "RecvReqS" -- prep action of dir ctrlr
   CurCmd = Empty &
   Chan1[i].Cmd = ReqS
   ii
   CurCmd := ReqS;
   CurPtr := i; -- who sent me ReqS
   Chan1[i].Cmd := Empty; -- drain its cmd
   for j : NODE do InvSet[j] := ShrSet[j] end; -- inv = nodes with S/E
 end
end;
```

```
ruleset i : NODE do
-- For any node that is waiting with ReqE requested, with CurCmd Empty
-- we set CurCmd to ReqE on behalf of node i (setting CurPtr to point to it).
-- Then void Chan1 empty.
—— Now Set the nodes to be invalidated to the nodes having S or E copies.
  rule "RecvReqE"
   CurCmd = Empty &
   Chan1[i].Cmd = ReqE
   ii
   CurCmd := ReqE;
   CurPtr := i; -- who sent me ReqE
   Chan1[i].Cmd := Empty; -- drain its cmd
   for j : NODE do InvSet[j] := ShrSet[j] end; -- inv = nodes with S/E
 end
end;
```

```
ruleset i : NODE do
-- For every node with Chan2 Cmd empty and InvSet true (node to be invalidated)
-- and if CurCmd is ReqE or (ReqS with ExGnt true), then
-- void Chan2 Cmd to Inv, and remove node i from InvSet (invalidation already set out)
  rule "SendInv"
   Chan2[i].Cmd = Empty &
   InvSet[i] = true & -- Gnt* and Inv channel
    ( CurCmd = ReqE | -- DC: curcmd = E
     CurCmd = ReqS & ExGntd = true ) -- DC: curcmd = S & ExGntd
   Chan2[i].Cmd := Inv; -- fill Chan2 with Inv
   InvSet[i] := false;
 end
end;
```

```
— When a node gets invalidated, it acks, and when it was E
-- then the node (i) coughs up its cache data into Chan3
— Then cache state is I and undefine Cache Data
ruleset i : NODE do
  rule "SendInvAck"
    Chan2[i].Cmd = Inv &
   Chan3[i].Cmd = Empty
   Chan2[i].Cmd := Empty;
    Chan3[i].Cmd := InvAck;
    if (Cache[i].State = E) then Chan3[i].Data := Cache[i].Data end;
    Cache[i].State := I; undefine Cache[i].Data;
 end
end;
```

```
ruleset i : NODE do
 rule "RecvInvAck"
    Chan3[i].Cmd = InvAck &
    CurCmd != Empty
    ii
    Chan3[i].Cmd := Empty;
   ShrSet[i] := false;
    if (ExGntd = true) then ExGntd := false;
   MemData := Chan3[i].Data;
    undefine Chan3[i].Data end;
 end
end;
```

```
ruleset i : NODE do
  rule "SendGntS"
    CurCmd = ReqS \&
    CurPtr = i \&
    Chan2[i].Cmd = Empty &
    ExGntd = false
   Chan2[i].Cmd := GntS;
    Chan2[i].Data := MemData;
    ShrSet[i] := true;
    CurCmd := Empty;
    undefine CurPtr;
  end
end;
```

```
ruleset i : NODE do
  rule "SendGntE"
   CurCmd = ReqE \&
   CurPtr = i \&
   Chan2[i].Cmd = Empty &
   ExGntd = false &
   forall j : NODE do ShrSet[j] = false end -- nodes having S or E status
   ĺ
   Chan2[i].Cmd := GntE;
   Chan2[i].Data := MemData;
   ShrSet[i] := true;
   ExGntd := true;
   CurCmd := Empty;
   undefine CurPtr;
 end
end;
```

```
ruleset i : NODE do
rule "RecvGntS"
   Chan2[i].Cmd = GntS
   ==>
   Cache[i].State := S;
   Cache[i].Data := Chan2[i].Data;
   Chan2[i].Cmd := Empty;
   undefine Chan2[i].Data;
end
end;
```

```
ruleset i : NODE do
  rule "RecvGntE"
    Chan2[i].Cmd = GntE
    ==>
    Cache[i].State := E;
    Cache[i].Data := Chan2[i].Data;
    Chan2[i].Cmd := Empty;
    undefine Chan2[i].Data;
  end
end;
```

```
ruleset i : NODE; -- for every node i
       d: DATA -- for every data d
 do
   rule "Store"
     Cache[i].State = E -- if node is in E
     Cache[i].Data := d; -- store d into Cache[i].Data
     AuxData := d; -- Also update latest cache line value
                        -- The node in E can get any "D" value
   end
end;
```

#### Invariants of the German protocol

```
---- Invariant properties ----
invariant "CtrlProp"
forall i : NODE do
  forall j : NODE do
  i!=j ->
   (Cache[i].State = E -> Cache[j].State = I) &
    (Cache[i].State = S -> Cache[j].State = I |
                           Cache[j].State = S)
 end
end;
invariant "DataProp"
( ExGntd = false -> MemData = AuxData ) &
forall i : NODE
do Cache[i].State != I ->
    Cache[i].Data = AuxData
end;
```