# CS 6110 Software Correctness, Spring 2022 (edited from a previous class; look for bugs!)

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URL: bit.ly/cs6110s22



### Slides for Lec4: Agenda

- Logic readings
  - Discussions
- FSM material
  - Not familiar to many
    - Not taught as a practical tool in most courses
    - Not taught as the first real formal methods in most courses
      - E.g. context-free parsing is really the first dramatically successful FV tool
        - The horrible bugs in them
          - Fortran missing comma -> spacecraft in a coma ☺
          - The )))\*((( rule for parsing!
      - Knuth's article on how bad compilers were in the 1960s!!
        - Youtube version is pretty good (how he got his honeymoon paid for!)
        - <a href="https://archive.computerhistory.org/resources/text/Oral\_History/Knuth\_Don\_1/Knuth\_Don.oral\_history.2007.102658053\_all.pdf">https://archive.computerhistory.org/resources/text/Oral\_History/Knuth\_Don\_1/Knuth\_Don\_oral\_history.2007.102658053\_all.pdf</a>
  - OpSem basics → Sutter

### Slides for Lec4: Agenda

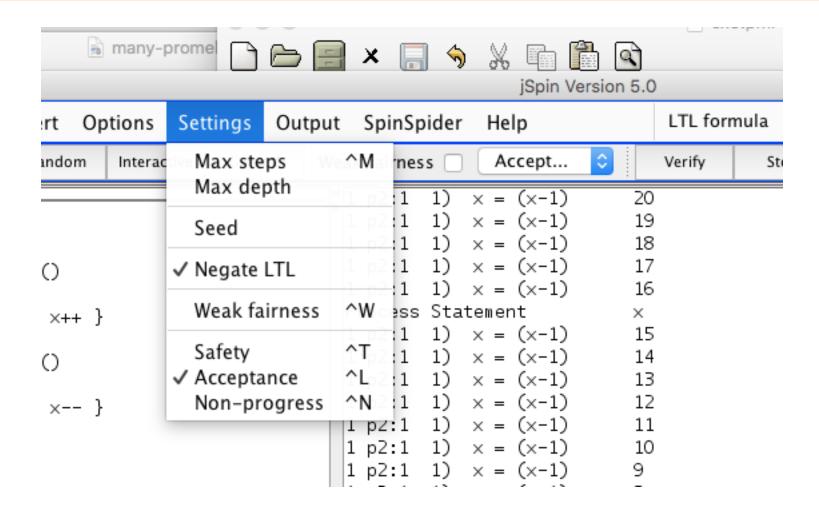
- How the project discussions are proceeding
  - Notes being taken
  - References being catalogued
  - Not all are at the same point in learning about Logic, Automata, ...
    - But they are all important to learn properly!
- We will go through the Bradley/Manna book Ch 1,2
  - Discussion of readings from Ch1
- SPIN Usage
  - Long trace
    - Search depth control

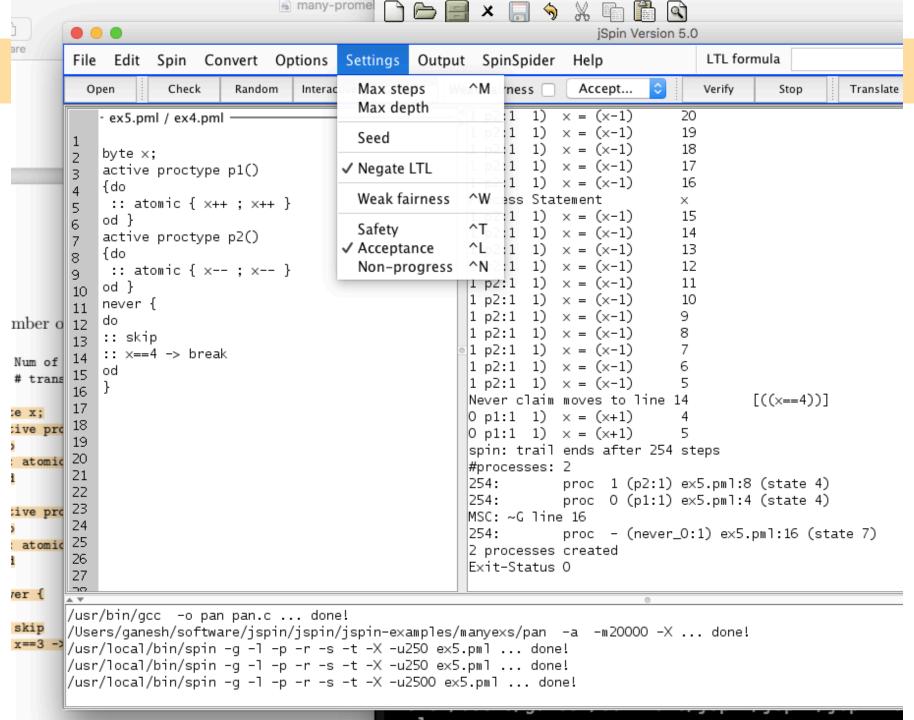
### Slides for Lec4: Agenda

- Readings for next week + Asg-2
  - Posted tomorrow (1/21) evening
  - From Ben-Ari's book
  - From CEATL
    - About NBA != DBA
    - About LTL
    - Nested DFS
    - How we can show LTL validity by creating the right Kripke Structure!
      - Reinforces idea of validity
- Distributed Locking Protocol
  - In Promela
  - In Murphi

### How SPIN helps

- Helps you quickly model "situations"
  - See SPIN-Soldiers + SpinTutorialby Ruys
- Debug your thoughts
- Find flaws in design
- Has a lot of power and will NEVER become irrelevant
  - The more complex a system gets, the less you need to get fancy wrt verification
- (after a 1-month training), you can do this
  - When in doubt, whip up a SPIN model and find bugs (in system or in your head)
- Has worked for large systems
  - Recent correctness workshop -> entire new Pthreads implementation modeled!
- We don't have the full month to train you
  - This is the last SPIN week ... but I'll give you a REAL protocol verif to read on Thu!





```
/* Smart reductions saved states */
byte x,y;
active proctype p1()
{do
 :: atomic { x++ ; x++ }
 od
active proctype p2()
{do
 :: atomic { y++ ; y++ }
 od
never {
do
:: skip
:: (x==3) -> break
od
```

```
/* Smart reductions saved states */
byte x,y;
active proctype p1()
{do
    :: atomic { x++ ; x++ }
    od
}
active proctype p2()
{do
    :: atomic { y++ ; y++ }
    od
}
never {
do
    :: skip
    :: (x==3) -> break
od
}
```

```
+ Partial Order Reduction
Full statespace search for:
       never claim
                                  + (never 0)
       assertion violations

    + (if within scope of claim)

       acceptance cycles - (not selected)
       invalid end states - (disabled by never claim)
State-vector 36 byte, depth reached 255, ••• errors: 0 •••
     128 states, stored
     129 states, matched
     257 transitions (= stored+matched)
       O atomic steps
hash conflicts:
                      0 (resolved)
Stats on memory usage (in Megabytes):
   0.008
                equivalent memory usage for states (stored*(State-vector + overhead))
   0.290
                actual memory usage for states
 128.000
                memory used for hash table (-w24)
   1.068
               memory used for DFS stack (-m20000)
 129.264
               total actual memory usage
unreached in proctype p1
       ex6.pml:6, state 7, "-end-"
       (1 of 7 states)
unreached in proctype p2
       ex6.pml:10, state 7, "-end-"
       (1 of 7 states)
unreached in claim never 0
       ex6.pml:16, state 7, "-end-"
       (1 of 7 states)
pan: elapsed time O seconds
```

```
/* Reductions don't work */
byte x,y;
active proctype p1()
{do
:: atomic { x++ ; x++ }
od }
active proctype p2()
{do
:: atomic { y++ ; y++ }
od }
never {
do
:: skip
:: (x==3)&&(y==2) \rightarrow break
od
```

ex7
do the
right depth
setting!

```
/* Reductions don't work */
byte x,y;
active proctype p1()
{do
    :: atomic { x++ ; x++ }
od }
active proctype p2()
{do
    :: atomic { y++ ; y++ }
od }
never {
do
    :: skip
    :: (x==3)&&(y==2) -> break
od
}
```

```
Full statespace search for:
       never claim
                                  + (never_0)
        assertion violations
                                  + (if within scope of claim)
       acceptance cycles - (not selected)
       invalid end states - (disabled by never claim)
State-vector 36 byte, depth reached 32767, ••• errors: 0 •••
    16384 states, stored
    16385 states, matched
    32769 transitions (= stored+matched)
       O atomic steps
hash conflicts:
                       3 (resolved)
Stats on memory usage (in Megabytes):
    1.000
                equivalent memory usage for states (stored*(State-vector + overhead))
    1.072
                actual memory usage for states
  128.000
                memory used for hash table (-w24)
   10.681
                memory used for DFS stack (-m200000)
                total actual memory usage
  139.658
unreached in proctype p1
       ex7.pml:6, state 7, "-end-"
        (1 of 7 states)
unreached in proctype p2
       ex7.pml:10, state 7, "-end-"
        (1 of 7 states)
unreached in claim never O
        ex7.pml:16, state 7, "-end-"
        (1 of 7 states)
pan: elapsed time 0.03 seconds
pan: rate 546133.33 states/second
```

ex8 do the right depth setting!

```
/* Smart reductions saved states */
byte x,y;
active proctype p1()
{do
 :: atomic { x++ ; x++ }
 od
active proctype p2()
{do
 :: atomic { y++ ; y++ }
 od
never {
do
:: skip
:: (x==232)\&\&(y==2) -> break /* observe both vars to introduce
                               * state explosion
                               */
od
```

ex8
do the
right depth
setting!

```
1 p2:1 1) y = (y+1)
                       253
0 p1:1 1) \times = (\times +1)
                           254
Process Statement
                           X
0 p1:1 1) \times = (\times +1)
                                      254
1 p2:1 1) y = (y+1)
                                      254
spin: ex8.pml:9, Error: value (256->0 (8)) truncated in assignment
1 p2:1 1) y = (y+1)
                                      255
1 p2:1 1) y = (y+1)
1 p2:1
       1) y = (y+1)
|1 p2:1 1) y = (y+1)
|1 p2:1 1) y = (y+1)
1 p2:1 1) y = (y+1)
1 p2:1 1) v = (v+1)
```

```
byte pid1, pid2;
proctype p1()
{byte x; /* Also init to 0 */
 do
 :: x++ ; x++
 od
proctype p2()
{byte y; /* Also init to 0 */
 do
 :: y++ ; y++
 od
init {
 atomic {
pid1 = run p1();
 pid2 = run p2();
never {
do
:: skip
:: (p1:x==2)&&(p2:y==232) -> break
od
```

```
/* Channels */
chan ch = [0] of { byte }; /* rendezvous channel */
active proctype p1()
{byte x; /* local var x init to 0 */
 do
 :: x++ -> ch!x
 od
active proctype p2()
{byte y,z;
 do
 :: ch?y \rightarrow z++ /* z tries to keep track of the value of x */
od
never {
do
:: skip
:: (p2:y - p2:z) > 1 -> break
od
```

```
/* Channels */
chan ch = [0] of { byte }; /* rendezvous channel */
active proctype p1()
{byte x; /* local var x init to 0 */
 do
 :: x++ -> ch!x /*; and -> are the same */
 od
}
active proctype p2()
{byte y,z; /* can be named x, but keeping distinct names */
 do
 :: ch?y -> z++ /* z tracks value of x */
 od
never {
do
:: skip
:: (p1:x - p2:z) > 1 -> break
od
}
```

```
/* set depth-bound of DFS to around 20 */
chan ch = [1] of { byte }; /* buffering (non-rendezvous) channel */
active proctype p1()
{byte x; /* local var x init to 0 */
 do
 :: x++ -> ch!x /*; and -> are the same */
 od
active proctype p2()
{byte y,z; /* can be named x, but keeping distinct names */
 do
 :: ch?y -> z++ /* z tracks value of x */
 od
never {
do
:: skip
:: (p1:x - p2:z) > 2 -> break
od
```

#### ex12b

```
    ex12b.pml / ex12.pml -

/* set depth-bound of DFS to around 20 */
chan ch = [1] of { byte }; /* buffering (non-rendezvous) channel */
byte x, z;
active proctype p1()
 do
 :: x++ -> ch!x /*; and -> are the same */
 od
active proctype p2()
{byte y; /* can be named x, but keeping distinct names */
 :: ch?y -> z++ /* z tracks value of x */
 od
never {
do
:: skip
:: (x - z) > 2 -> break
od:
accept: goto accept
```

```
warning: for p.o. reduction to be valid the never claim must be
stutter-invariant
(never claims generated from LTL formulae are stutter-invariant)
pan:1: acceptance cycle (at depth 4082)
pan: wrote ex12b.pml.trail
(Spin Version 6.4.5 -- 1 January 2016)
Warning: Search not completed
        + Partial Order Reduction
Full statespace search for:
        never claim
                                  + (never 0)
        assertion violations + (if within scope of claim)
        acceptance cycles + (fairness disabled)
        invalid end states - (disabled by never claim)
State-vector 44 byte, depth reached 6129. ••• errors: 1 •••
     3074 states, stored
     514 states, matched
     3588 transitions (= stored+matched)
        O atomic steps
hash conflicts:
                       0 (resolved)
Stats on memory usage (in Megabytes):
                equivalent memory usage for states
    0.211
(stored*(State-vector + overhead))
    0.388
                actual memory usage for states
  128.000
                memory used for hash table (-w24)
 1068.115
                memory used for DFS stack (-m20000000)
 1196.408 total actual memory usage
pan: elapsed time 0.05 seconds
pan: rate
             61480 states/second
```

```
active proctype p1()
{byte x;
 do
 :: x = x + 3 /* USER BEWARE: this statement is atomic, unlike in C !! */
 od
active proctype p2()
{byte y;
 do
 :: y = y + 5
 od
never {
do
:: skip
:: (p1:x == p2:y) -> break
od;
accept: goto accept; /* not needed but looks Buchi */
```

```
active proctype p1()
{byte x;
 do
 :: x = x + 3 /* USER BEWARE: this statement is atomic, unlike in C !! */
 od
active proctype p2()
{byte y;
 do
 :: y = y + 5
 od
never {
do
:: skip
:: (p1:x == p2:y) -> break
od;
accept: goto accept; /* not needed but looks Buchi */
```

http://spinroot.com/spin/Man/Pan.html suggests using -DNOREDUCE
PO reductions not safe with remote references (must be stutter invariant)

```
active proctype p1()
{byte x;
 do
 :: x = x + 3 /* USER BEWARE: this statement is atomic, unlike in C !! */
 od
active proctype p2()
{byte y;
 do
 :: y = y + 5
 od
never {
do
:: skip
:: (p1:x == p2:y) -> break
od;
accept: goto accept; /* not needed but looks Buchi */
```

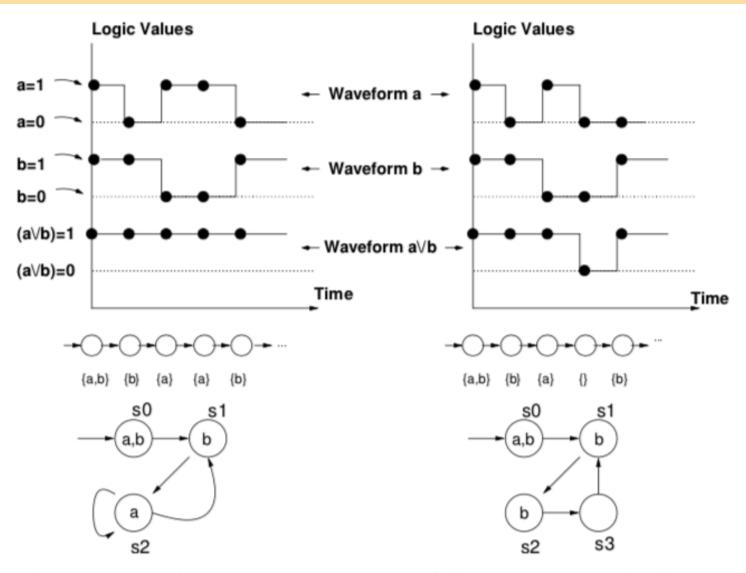
```
mtype = {are_you_free, yes, no, release}
byte progress; /* SPIN initializes all variables to 0 */
proctype phil(chan lf, rf; int philno)
{ do
  :: do
     :: lf!are_you_free ->
       if
       :: lf?yes -> break
       :: lf?no
       fi
     od;
     do
     :: rf!are_you_free ->
       if
       :: rf?yes -> progress = 1 -> progress = 0
                  -> lf!release -> rf!release -> break
       :: rf?no -> lf!release -> break
       fi
     od
  od
proctype fork(chan lp, rp)
  :: rp?are_you_free -> rp!yes ->
     do
     :: lp?are_you_free -> lp!no
                       -> break
     :: rp?release
     od
  :: lp?are_you_free -> lp!yes ->
     :: rp?are_you_free -> rp!no
     :: lp?release
                       -> break
     od
  od
init {
  chan c0 = [0] of { mtype }; chan c1 = [0] of { mtype };
   chan c2 = [0] of { mtype }; chan c3 = [0] of { mtype };
   chan c4 = [0] of { mtype }; chan c5 = [0] of { mtype };
   atomic {
    run phil(c5, c0, 0); run fork(c0, c1);
     run phil(c1, c2, 1); run fork(c2, c3);
    run phil(c3, c4, 2); run fork(c4, c5); }
never { /* Negation of []<> progress */
do
:: skip
:: (!progress) -> goto accept;
 accept: (!progress) -> goto accept;
```

#### Question: What is the theory behind this checking? Answer: On-the-fly LTL Model Checking using Buchi Automata!

```
    ex12b.pml / ex12.pml -

/* set depth-bound of DFS to around 20 */
chan ch = [1] of { byte }; /* buffering (non-rendezvous) channel */
byte x, z;
active proctype p1()
 :: x++ -> ch!x /* : and -> are the same */
 od
active proctype p2()
{byte y; /* can be named x, but keeping distinct names */
 do
 :: ch?v -> z++ /* z tracks value of x */
 od
never {
do
:: skip
:: (x - z) > 2 -> break
od:
accept: goto accept
```

```
warning: for p.o. reduction to be valid the never claim must be
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(never claims generated from LTL formulae are stutter-invariant)
pan:1: acceptance cycle (at depth 4082)
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(Spin Version 6.4.5 -- 1 January 2016)
Warning: Search not completed
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Full statespace search for:
       never claim
                                  + (never_0)
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State-vector 44 byte, depth reached 6129. ••• errors: 1 •••
     3074 states, stored
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     3588 transitions (= stored+matched)
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hash conflicts:
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Stats on memory usage (in Megabytes):
                equivalent memory usage for states
    0.211
(stored*(State-vector + overhead))
   0.388
                actual memory usage for states
  128.000
                memory used for hash table (-w24)
 1068.115
                memory used for DFS stack (-m20000000)
 1196.408
                total actual memory usage
pan: elapsed time 0.05 seconds
pan: rate 61480 states/second
```



**Fig. 22.1.** Two Kripke structures and some of their computations. In the Kripke structure on the left, the assertion 'Henceforth  $(a \lor b)$ ' is true.

#### **22.1.5** LTL syntax

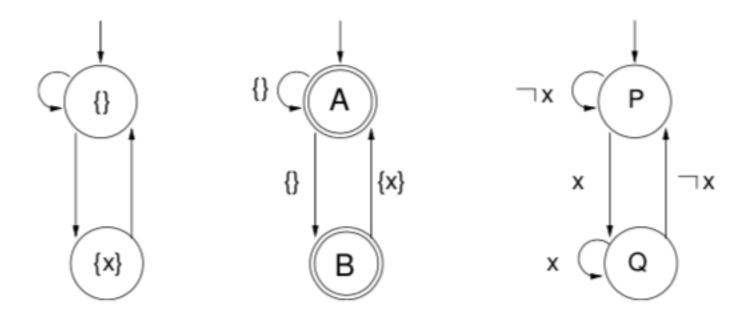
LTL formulas  $\varphi$  are inductively defined as follows, through a context-free grammar:

```
\begin{array}{lll} \varphi \to x, & \text{a propositional variable} \\ & | \neg \varphi & \text{negation of an LTL formula} \\ & | (\varphi) & \text{parenthesization} \\ & | \varphi_1 \lor \varphi_2 & \text{disjunction} \\ & | G\varphi & \text{henceforth } \varphi \\ & | F\varphi & \text{eventually } \varphi \text{ ("future")} \\ & | X\varphi & \text{next } \varphi \\ & | (\varphi_1 \mathbf{U} \ \varphi_2) & \varphi_1 \text{ until } \varphi_2 \\ & | (\varphi_1 \mathbf{W} \ \varphi_2) & \varphi_1 \text{ weak-until } \varphi_2 \end{array}
```

Here is the inductive definition for the semantics of LTL:

```
\sigma \models x iff x is true at s_0 (written s_0(x))
\sigma \models \neg \varphi iff \sigma \not\models \varphi
\sigma \models (\varphi) iff \sigma \models \varphi
\sigma \models \varphi_1 \lor \varphi_2 \quad \text{iff } \sigma \models \varphi_1 \lor \sigma \models \varphi_2
\sigma \models G\varphi iff \sigma^i \models \varphi for every i \ge 0
\sigma \models F\varphi iff \sigma^i \models \varphi for some i \ge 0
\sigma \models X\varphi iff \sigma^1 \models \varphi
\sigma \models (\varphi_1 \cup \varphi_2) iff \sigma^k \models \varphi_2 for some k \geq 0 and \sigma^j \models \varphi_1 for all j < k
\sigma \models (\varphi_1 W \varphi_2) iff \sigma \models G\varphi_1 \vee \sigma \models (\varphi_1 U \varphi_2)
```

$$re \rightarrow \emptyset \mid \varepsilon \mid a \in \Sigma \mid (re) \mid re_1 + re_2 \mid re_1 re_2 \mid re^*$$
  
 $ore \rightarrow re^{\omega} \mid re \ ore \mid ore_1 + ore_2$ 



**Fig. 23.10.** A Kripke structure (left), its corresponding Büchi automata (middle), and a property automaton expressing GFx (right)

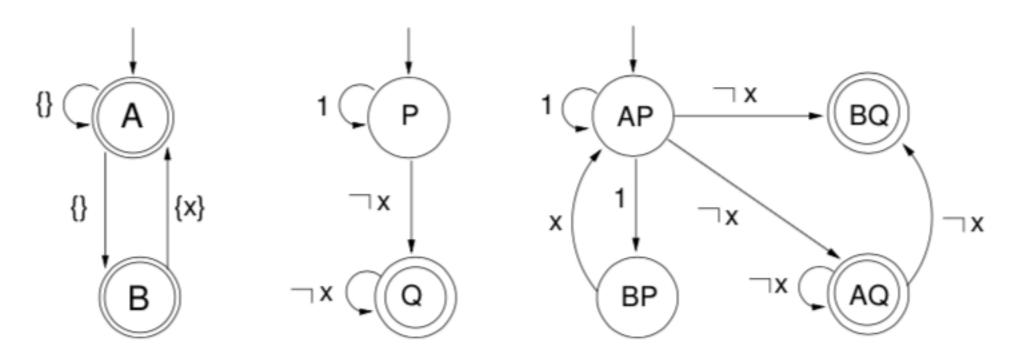


Fig. 23.11. System automaton (left), complemented property automaton (middle), and product automaton (right)

Notice that the "property automaton" (P) on the right-hand side of Figure 23.10 includes all runs that satisfy GFx. Therefore, to determine whether a given Kripke structure ("system" S) satisfies a property P, we can check whether

$$L(S) \subseteq L(P)$$
.

This check is equivalent to

$$L(S) \cap \overline{L(P)} = \emptyset.$$

$$L(S) \cap \overline{L(P)} \neq \emptyset.$$

