

# Homework 1

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**Question 1.** *Their* vs *There*

**Answer a):** Unigram model

The probability of a sentence,  $w_1, w_2, \dots, w_n$  is given by:

$$p(w_1, w_2, \dots, w_n) = \prod_{i=1}^n p(w_i | w_1^{i-1})$$

In the unigram model we assume  $p(w_i | w_1^{i-1}) = p(w_i)$ , i.e. we assume that words are independent of each other. Therefore,

$$p(w_1, w_2, \dots, w_n) = \prod_{i=1}^n p(w_i)$$

The approach to attempt to solve the *their* vs *there* in terms of a unigram model is a bad idea for the following reason. When evaluating a probability of a sentence;  $p(w_1, w_2, \dots, w_n)$  which contains either *their* or *there* and we want to see which sentence is more likely, we compare their probabilities and choose the one with higher probability. Namely:

$$\operatorname{argmax}_{\text{their,there}} \{p(w_1, w_2, \dots, w_{n-1}) * p(\text{their}), p(w_1, w_2, \dots, w_{n-1}) * p(\text{there})\} = \operatorname{argmax}_{\text{their,there}} \{p(\text{their}), p(\text{there})\}$$

That is, we always pick the word (out of there/their) which has higher probability. That is, the more occurring word will always be considered the "correct" word.

**Answer b):** Bigram model

When using a bigram we assume;  $p(w_i | w_1^{i-1}) = p(w_i | w_{i-1})$ , that is, the probability of a word depends on the preceding word. Thus, the formula is:

$$p(w_1, w_2, \dots, w_n) = \prod_{i=1}^n p(w_i | w_{i-1})$$

The bigram model would do a lot better as it can account for the fact that a noun is more frequently preceded by *their*, rather than *there*. Similarly, a verb is more frequently preceded by *there*, rather than *their*. The language model does not know what a "noun" or a "verb" is, but it knows the probability over all words preceding *their* and *there*, which will have this structure.

**Question 2.** Independence assumption

**Answer a):** The strange man

**Answer b):**

**Answer c):**

**Question 3.** Hidden Markov Model and Named Entity Recognition

**Answer a):** Transition matrix

The matrix is represented s.t. we go from row to column, therefore if we sum up the probabilities of a row we get 1.

Table 1: Transition matrix

	Per	Org	end
start	$\frac{3}{4}$	$\frac{1}{4}$	0
Per	$\frac{3}{6}$	$\frac{3}{6}$	0
Org	0	$\frac{11}{15}$	$\frac{4}{15}$

**Answer b):**

**Answer c):**

**Answer d):**