$$\begin{CD}
\Omega(A) @>\iota_A>> P_A @>>\pi_A>> A \\
@V\Omega(f)VV @Vp_fVV @VfVV \\
\Omega(B) @>\iota_B>> P_B @>>\pi_B>> B
\end{CD}$$