$$\begin{array}{c|c} \Omega(A) & \xrightarrow{\iota_A} & P_A & \xrightarrow{\pi_A} & A \\ \Omega(f) - \Omega(f)' & & \downarrow p_f - p_f' & & \downarrow f - f = 0 \\ \Omega(B) & \xrightarrow{\iota_B} & P_B & \xrightarrow{\pi_B} & B \end{array}$$