

Assignment - 3

Q1 Compare PDA and FSM

Soln:-

FSM	PDA
<ul style="list-style-type: none">- FSM stands for Finite Machine.- It does not have capability to remember previous input.- Constructed for type-3 grammar.- NFSM and FSM are equivalent.	<ul style="list-style-type: none">- PDA stands for push Down Automata.- contains stack, it can already read input.- Constructed for type-2 grammar.- NPDA has more capability than PDA.

Q2: Design and draw Deterministic PDA Accepting "Balance string of Bracket" which are accepted by following CFG.

$$S \rightarrow SS | [S] | \{S\} | \wedge$$

$$\delta(w_0, [, z_0) = (w_1, [z_0)$$

$$\delta(w_0, \{ , z_0) = (w_1, \{z_0)$$

$$\delta(w_0, [, [) = (w_1, [[)$$

$$\delta(w_0, \{ , \{) = (w_1, \{\{)$$

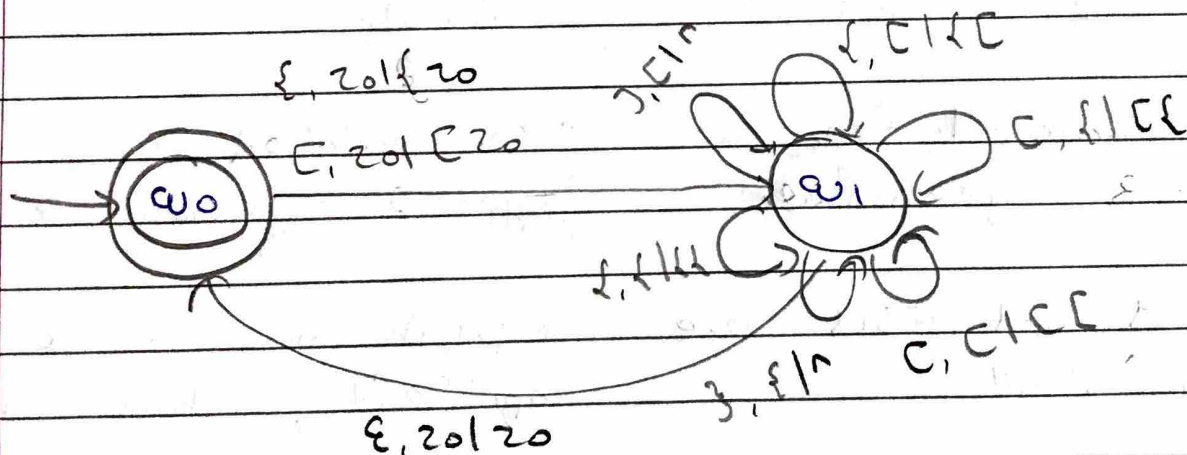
$$\delta(w_0, [, \downarrow) = (w_1, [\downarrow)$$

$$\delta(w_0, \{ , [) = (w_1, \{\downarrow)$$

$$\delta(w_0,] , [) = (w_1, \epsilon)$$

$$\delta(w_0, \} , \downarrow) = (w_1, \epsilon)$$

$$\delta(w_1, \epsilon, z_0) = (w_0, z_0)$$



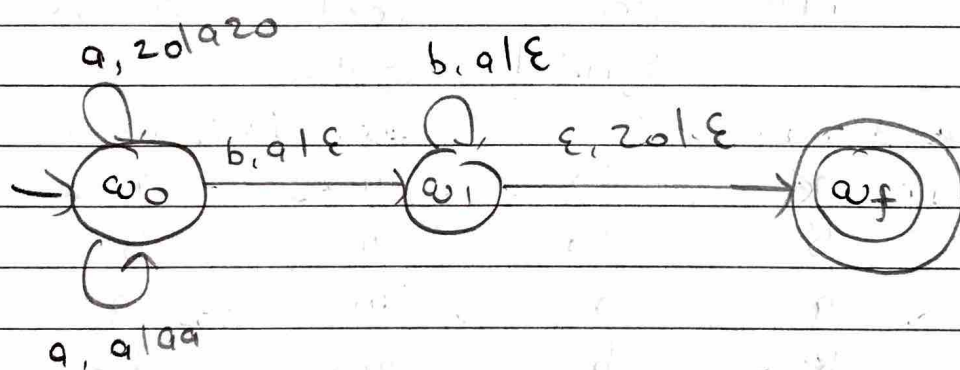
Q3 Design a PDA to accept

$$L = \{a^n b^n \mid n \geq 0\}$$

Soln:-

This is a language in which equal number of a's are followed by equal number of b's. The logic is: first we push all a's onto the stack. Then on reading every single b each a is popped. And at last if stack is empty then string will be accepted.

$$\begin{aligned} \Rightarrow \quad & \delta(q_0, a, z_0) = (q_0, az_0) \\ & \delta(q_0, a, a) = (q_0, aa) \\ & \delta(q_0, b, a) = (q_1, \epsilon) \\ & \delta(q_1, b, a) = (q_1, \epsilon) \\ & \delta(q_1, \epsilon, z_0) = (q_f, \epsilon) \end{aligned}$$



Q4 Give Transition tables for Deterministic PDA recognizing following language.

$$L = \{ x \in \{a, b\}^* \mid n_a(x) \neq n_b(x) \}$$

Trace it for the string abbaababbb

Soln:-

$$\delta(q_0, a, z_0) = (q_0, az_0)$$

$$\delta(q_0, b, z_0) = (q_0, bz_0)$$

$$\delta(q_0, a, a) = (q_0, aa)$$

$$\delta(q_0, b, b) = (q_0, bb)$$

$$\delta(q_0, a, b) = (q_0, \epsilon)$$

$$\delta(q_0, b, a) = (q_0, \epsilon)$$

$$\delta(q_0, \epsilon, a) = (q_f, a)$$

$$\delta(q_0, \epsilon, b) = (q_f, b)$$

current state	input	stack symbol	next state	move
q_0	a	z_0	q_0	az_0
q_0	b	z_0	q_0	bz_0
q_0	a	a	q_0	aa
q_0	b	b	q_0	bb
q_0	b	a	q_0	\wedge
q_0	a	b	q_0	\wedge
q_0	ϵ	a	q_f	a
q_0	ϵ	b	q_f	b

Trace it for the string $abb aababbb$.

$$\delta(q_0, \underline{a}bb aababbb, \underline{z_0}) = \delta(q_0, \underline{b}ba aababbb, \underline{a}z_0)$$

$$- \delta(q_0, \underline{b}a aababbb, \underline{z_0})$$

$$- \delta(q_0, \underline{a}a aabbb, \underline{b}z_0)$$

$$- \delta(q_0, \underline{a}babbb, \underline{z_0})$$

$$- \delta(q_0, \underline{b}abbb, \underline{a}z_0)$$

$$- \delta(q_0, \underline{a}bbb, \underline{z_0})$$

$$- \delta(q_0, \underline{b}bb, \underline{a}z_0)$$

$$- \delta(q_0, \underline{b}b, \underline{z_0})$$

$$- \delta(q_0, \underline{b}, \underline{b}z_0)$$

$$- \delta(q_0, \underline{\epsilon}, \underline{b}b z_0)$$

$$- \delta(q_f, b) - \text{Accepted.}$$

Q5 For the PDA, $(\{q_0, q_1\}, \{0, 1\}, \{0, 1, z_0\}, \delta, q_0, z_0, \phi)$, where δ is

$$\delta(q_0, \epsilon, z_0) = \{(q_1, \epsilon)\}$$

$$\delta(q_0, 0, z_0) = (q_0, 0z_0)$$

$$\delta(q_0, 0, 0) = (q_0, 00)$$

$$\delta(q_0, 1, 0) = (q_0, 10)$$

$$\delta(q_0, 1, 1) = (q_0, 11)$$

$$\delta(q_0, 0, 1) = (q_1, \epsilon)$$

$$\delta(q_1, 0, 1) = (q_1, \epsilon)$$

$$\delta(q_1, 0, 0) = (q_1, \epsilon)$$

$$\delta(q_1, \epsilon, z_0) = (q_1, \epsilon)$$

obtain CFG accepted by the above PDA.

$S \Rightarrow^*$

$$1) \quad S \rightarrow (q_0, z_0, q_0) \\ S \rightarrow (q_0, z_0, q_1)$$

$$2) \quad \text{For } \delta(q_0, \epsilon, z_0) = (q_0, \epsilon)$$

$$(q_0, z_0, q_0) \rightarrow \epsilon$$

$$3) \quad \text{For } \delta(q_0, 0, z_0) = (q_0, 0z_0)$$

$$(q_0, z_0, q_0) \rightarrow 0 (q_0, 0, q_0) (q_0, z_0, q_0)$$

$$(q_0, z_0, q_0) \rightarrow 0 (q_0, 0, q_1) (q_1, z_0, q_0)$$

$$(q_0, z_0, q_1) \rightarrow 0 (q_0, 0, q_0) (q_0, z_0, q_1)$$

$$(q_0, z_0, q_1) \rightarrow 0 (q_0, 0, q_1) (q_1, z_0, q_1)$$

$$4) \quad \text{For } \delta(q_0, 0, 0) = (q_0, 00)$$

$$(q_0, 0, q_0) = 0 (q_0, 0, q_0) (q_0, 0, q_0)$$

$$(q_0, 0, q_0) = 0 (q_0, 0, q_1) (q_1, 0, q_0)$$

$$(q_0, 0, q_1) = 0 (q_0, 0, q_0) (q_0, 0, q_1)$$

$$(q_0, 0, q_1) = 0 (q_0, 0, q_1) (q_1, 0, q_1)$$

$$5) \quad \text{For } \delta(q_0, 1, 0) = (q_0, 10)$$

$$(q_0, 0, q_0) = 1 (q_0, 1, q_0) (q_0, 0, q_0)$$

$$(q_0, 0, q_0) = 1 (q_0, 1, q_1) (q_1, 0, q_0)$$

$$(q_0, 0, q_1) = 1 (q_0, 1, q_0) (q_0, 0, q_1)$$

$$(q_0, 0, w_1) \rightarrow 1 (q_0, 1, w_1) (w_1, 0, w_1)$$

$$6) \text{ For } \delta(q_0, 1, 1) = (w_0, 1)$$

$$(w_0, 1, w_0) = 1 (w_0, 1, w_0) (w_0, 1, w_0)$$

$$(w_0, 1, w_0) = 1 (w_0, 1, w_1) (w_1, 1, w_0)$$

$$(w_0, 1, w_1) = 1 (w_0, 1, w_0) (w_0, 1, w_1)$$

$$(w_0, 1, w_1) = 1 (w_0, 1, w_1) (w_1, 1, w_1)$$

\Rightarrow

$$7) \text{ For } \delta(q_0, 0, 1) = (w_1, \epsilon)$$

$$(w_0, 1, w_1) \rightarrow 0$$

$$8) \text{ For } \delta(w_1, 0, 1) = (w_1, \epsilon)$$

$$(w_1, 1, w_1) \rightarrow 0$$

$$9) \text{ For } \delta(q_1, 0, 0) = (q_1, \epsilon)$$

\Rightarrow

$$(q_1, 0, w_1) \rightarrow 0$$

$$10) \text{ For } \delta(q_1, \epsilon, z_0) = (q_1, \epsilon)$$

$$(q_1, z_0, w_1) \rightarrow \epsilon$$

Now,

$$(w_0, z_0, w_0) - A$$

$$(w_0, z_0, w_1) - B$$

$$(w_1, z_0, w_0) - C$$

$$(w_1, z_0, w_1) - D$$

$$(w_0, 0, w_0) - E$$

$$(w_0, 0, w_1) - F$$

$$(w_1, 0, w_0) - G$$

$$(w_1, 0, w_1) - H$$

$$(w_0, 1, w_0) - I$$

$$(w_0, 1, w_1) - J$$

$$(w_1, 1, w_0) - K$$

$$(w_1, 1, w_1) - L$$

Now,

$$S \rightarrow A \mid B$$

$$A \rightarrow \epsilon$$

$$A \rightarrow 0 \mid E \mid A$$

$$A \rightarrow 0 \mid F \mid C$$

$$B \rightarrow 0 \mid E \mid B$$

$$B \rightarrow 0 \mid F \mid D$$

$$E \rightarrow 0 \mid E \mid E$$

$$E \rightarrow 0 \mid F \mid G$$

$$F \rightarrow 0 \mid E \mid F$$

$$F \rightarrow 0 \mid F \mid H$$

$$E \rightarrow 1 \mid I \mid E$$

$$E \rightarrow 1 \mid J \mid G$$

$$F \rightarrow 1 \mid I \mid F$$

$$F \rightarrow 1 \mid J \mid H$$

$$I \rightarrow 1 \mid I \mid I$$

$$I \rightarrow 1 \mid J \mid K$$

$$J \rightarrow 1 \mid I \mid J$$

$$J \rightarrow 1 \mid J \mid L$$

$$J \rightarrow 0$$

$$L \rightarrow 0$$

$$H \rightarrow 0$$

$$0 \rightarrow \epsilon$$

So simplified CFG is:

$$S \rightarrow A|B$$

$$A \rightarrow \emptyset EA | \emptyset FC | \epsilon$$

$$B \rightarrow \emptyset EB | \emptyset FD | \epsilon$$

$$E \rightarrow \emptyset EE | \emptyset FG | IIE | IJG$$

$$F \rightarrow \emptyset EF | \emptyset FH | IIF | IJH$$

$$I \rightarrow III | IJK$$

$$J \rightarrow IIT | IJL | \emptyset$$

$$L \rightarrow \emptyset$$

$$H \rightarrow \emptyset$$

$$D \rightarrow \emptyset \epsilon$$