# An introduction to machine learning for fMRI

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 how to build computer systems that automatically improve with experience

#### what is machine learning?

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- building models of data for
  - predicting numeric variables (regression)
  - predicting categoric variables (classification)
  - grouping data points (clustering)
  - ...

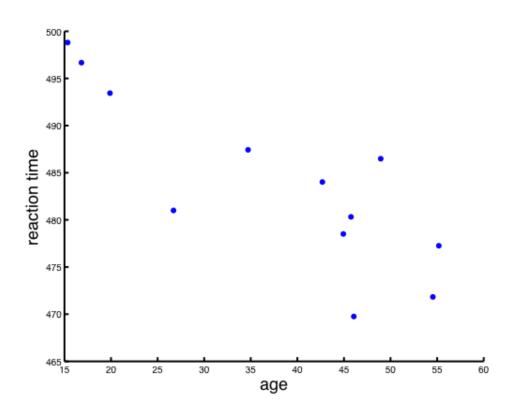
#### what is machine learning?

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  - ...
- overlaps with applied statistics

#### why use it at all?

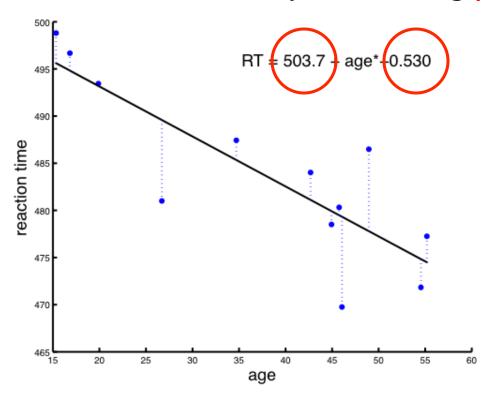
to tell a story about data

#### once upon a time there was a sample...

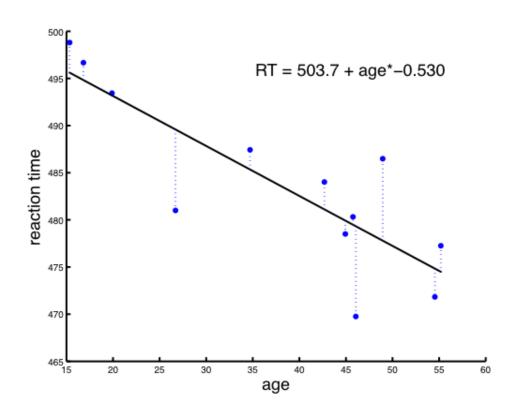


#### ... and then came a beautiful model...

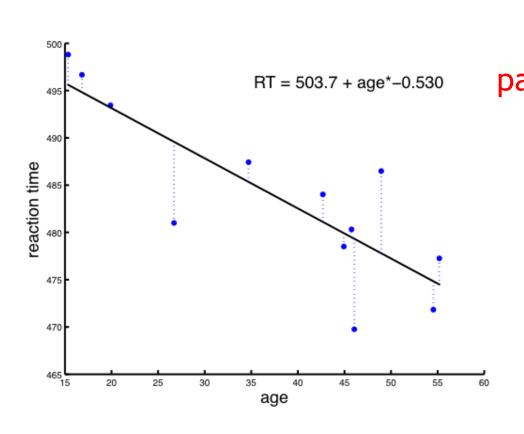
#### fit model by estimating parameters



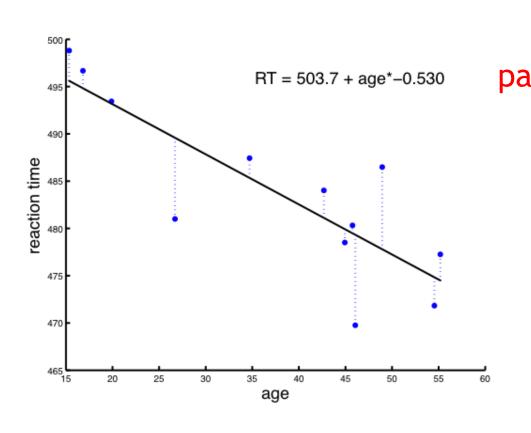
### very suggestive, but...



Is RT really related to age?



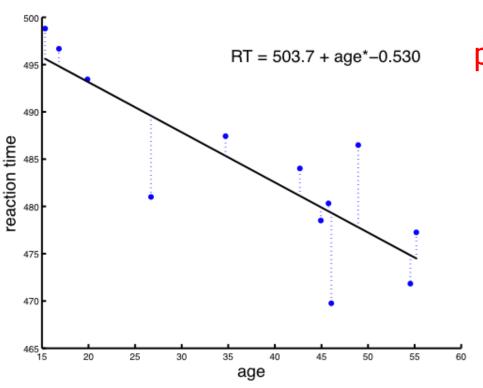
Model: RT =  $b_0$  +  $b_1$ \*age + e parameters in the population



Model:  $b_0$  )+(  $b_1$ \*)age + e parameters in the population

> parameters estimated from the sample

$$b_{est} = (X'X)^{-1}X'y$$



Model:

$$RT = b_0 + b_1 * age + e$$

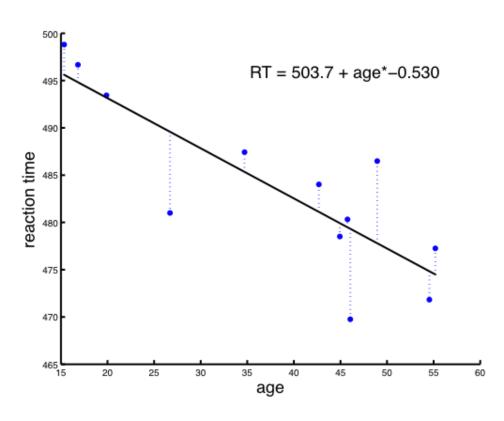
parameters in the population

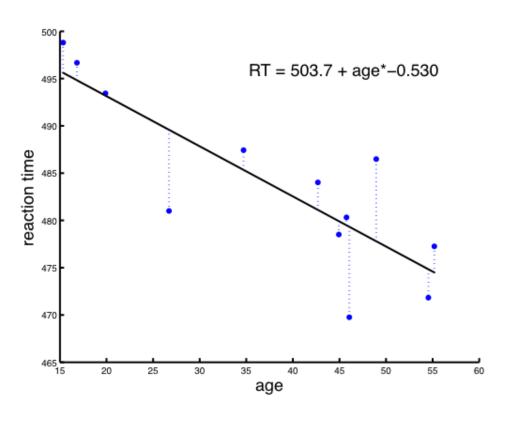
parameters estimated from the sample

$$b_{est}=(X'X)^{-1}X'y$$

Hypothesis: Is by different from 0?

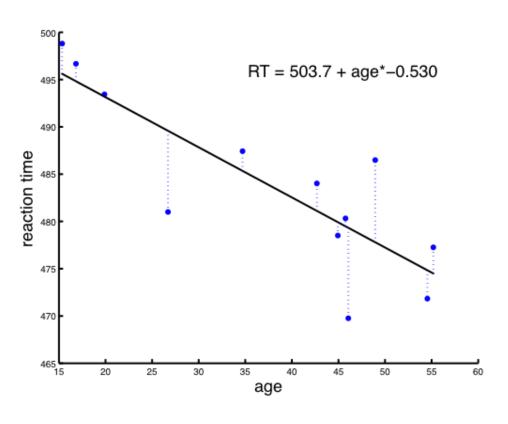
Null hypothesis:  $b_1 = 0$ Alternative:  $b_1 \sim = 0$ 





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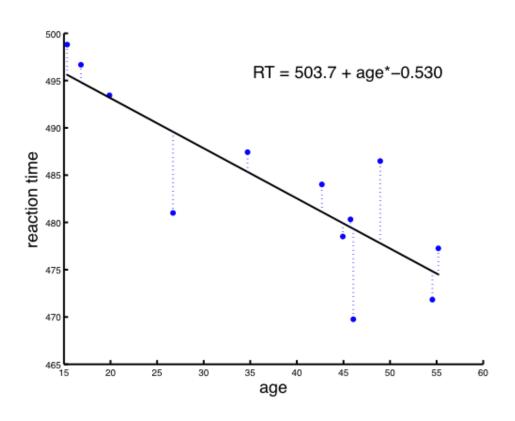
How likely is the parameter estimate  $(b_1 = -0.53)$  if the null hypothesis is true?



Null hypothesis:  $b_1 = 0$ Alternative:  $b_1 \sim = 0$ 

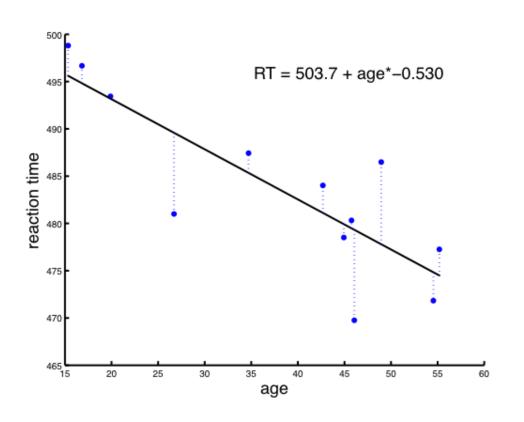
How likely is the parameter estimate  $(b_1 = -0.53)$  if the null hypothesis is true?

We need a statistic with a known distribution to determine this!



#### the CLT tells us

$$\hat{eta}_1 \sim N(eta_1, Var(\hat{eta}_1))$$
 but we don't know  $Var(\hat{eta}_1)$ 



#### the CLT tells us

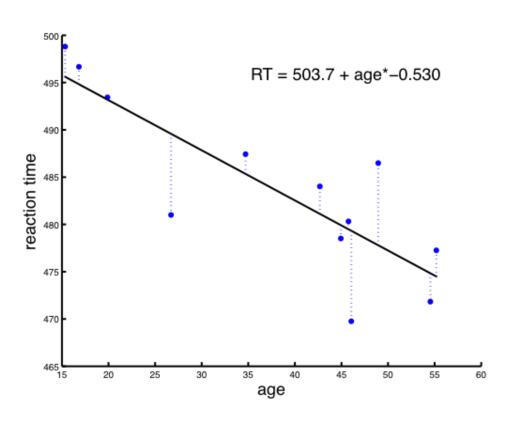
$$\hat{\beta}_1 \sim N(\beta_1, Var(\hat{\beta}_1))$$

#### but we don't know

$$Var(\hat{\beta}_1)$$

#### we do know

$$t = \frac{\hat{\beta}_1}{\sqrt{\hat{Var}(\hat{\beta}_1)}} \sim T_{N-p}$$



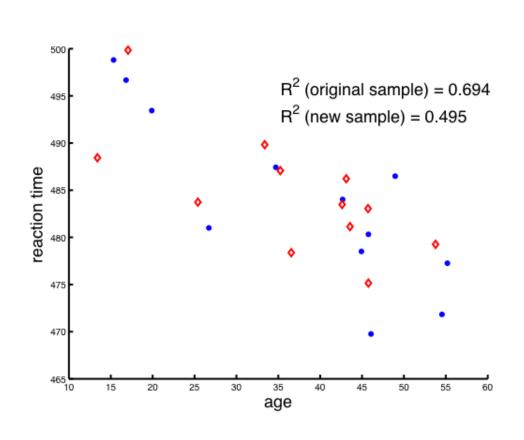
$$t(10) = -4.76$$

How likely is this value in this t distribution?

#### what can we conclude?

- in this sample
  - p < 0.001 there is a relationship between age and RT</p>
  - R2 age accounts for 69% of variance in RT
- very unlikely if no relationship in the population
- the test does not tell us how well we can predict RT from age in the population

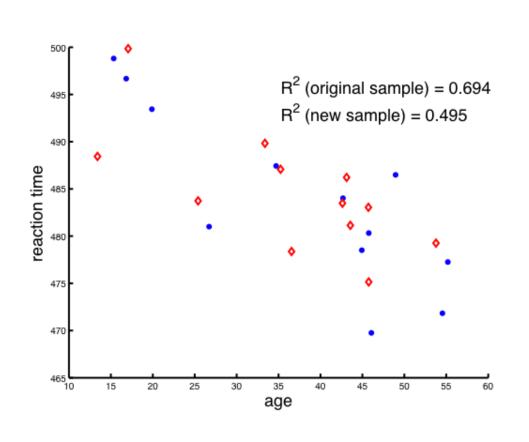
### what happens with a new sample?



draw a new sample from the same population

compute the R2 using parameters estimated in the original sample

#### what happens with a new sample?



repeat this 100 times... using model parameters estimated from the original sample

average R2 = 0.578

a measure of how good the model learned from a single sample is

### the learning perspective

When we estimate parameters from a sample, we are learning about the population from training data.

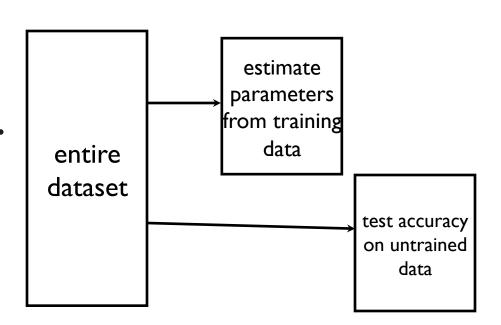
### the learning perspective

When we estimate parameters from a sample, we are learning about the population from training data.

How well can we measure the prediction ability of our learned model? Use a new sample as test data.

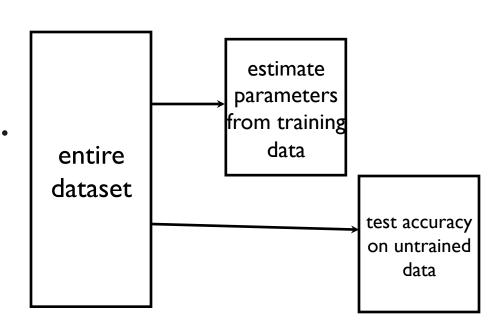
#### test data and cross-validation

If you can't collect more split your sample in two...



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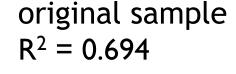


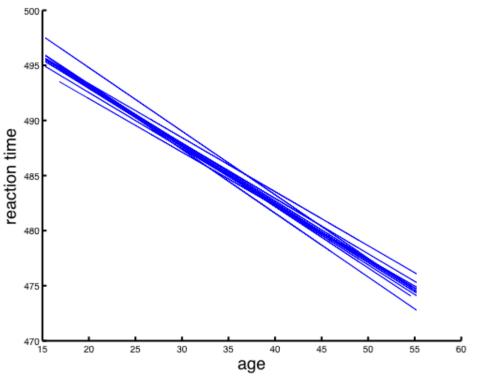
#### k-fold cross-validation:

- split into k folds
- train on k-1, test on the left out
- average prediction measure on all k folds
- several variants: all possible splits, leave-one-out

#### leave-one-out cross-validation

#### regression lines on each training set



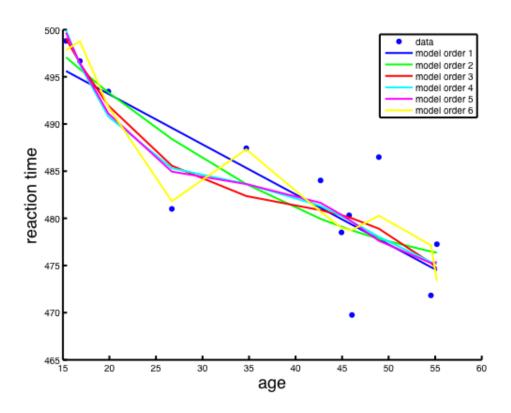


leave-one-out on original  $R^2 = 0.586$ 

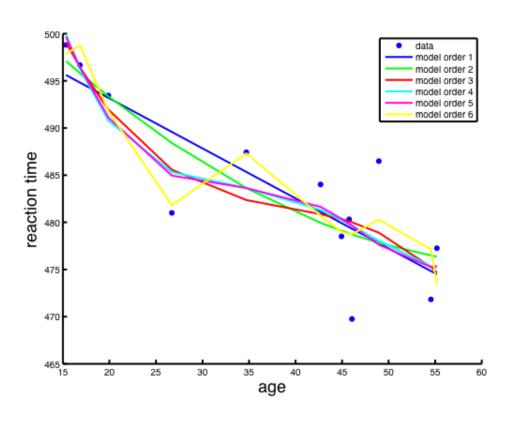
mean over 100 new samples  $R^2 = 0.591$ 

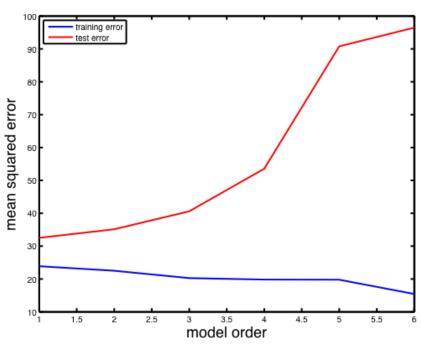
As model complexity goes up, we can always fit the training data better

What does this do to our predictive ability?



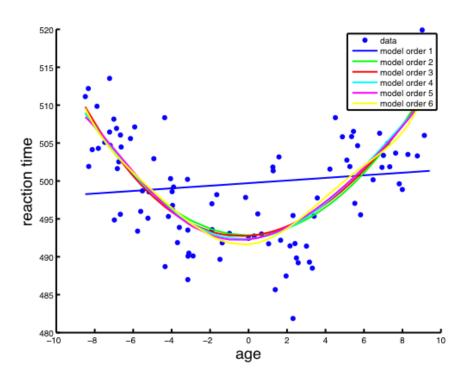
polynomials of higher degree fit the training data better...



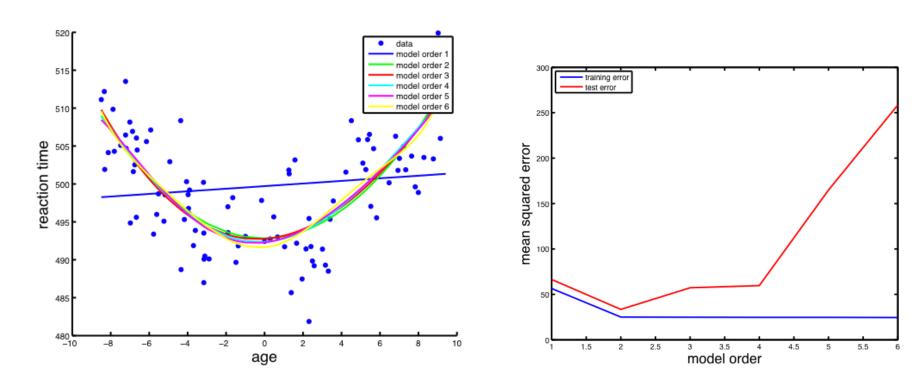


polynomials of higher degree fit the training data better...

... but they do worse on test data: overfitting



if the relationship in the population were more complicated



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we could use CV to determine adequate model complexity

(this would need to be done with nested CV, CV inside the training set)

#### what is machine learning, redux

- generalization: make predictions about a new individual
- a model that generalizes captures the relationship between the individual and what we want to predict
- cross-validation is a good way of
  - measuring generalization
  - doing model selection (there are others)

#### what is machine learning, redux

- generalization: make predictions about a new individual
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- cross-validation is a good way of
  - measuring generalization
  - doing model selection (there are others)
- "all models are wrong but some are useful"
   George Box

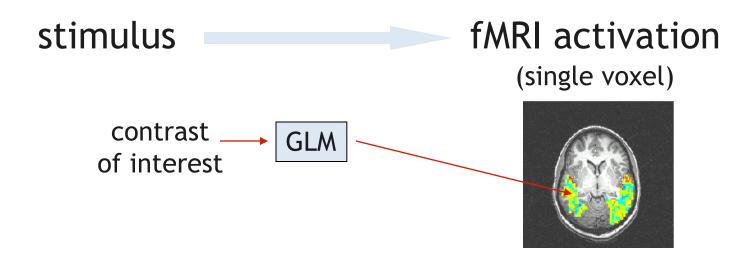
#### what does this have to do with fMRI?

#### In this talk:

- prediction is classification
- generalization is within subject (population of trials)
- how to draw conclusions with statistical significance
- what has it been used for?

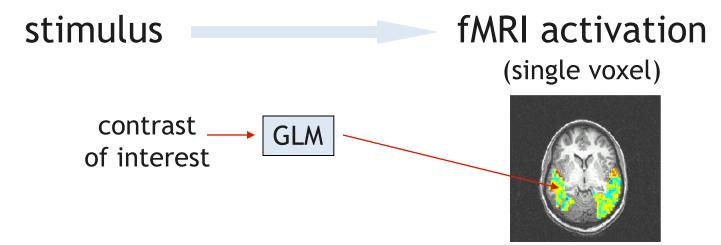
# two questions

**GLM:** are there voxels that reflect the stimulus?

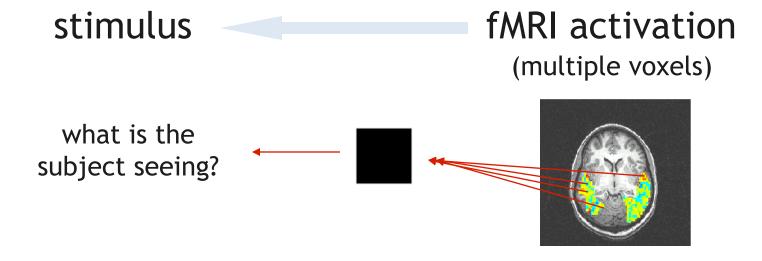


## two questions

**GLM:** are there voxels that reflect the stimulus?



Classifier: do voxels contain information to predict?



#### case study: two categories

[data from Rob Mason and Marcel Just, CCBI, CMU]

- subjects read concrete nouns in 2 categories
  - words name either tools or building types
  - trial:

see a word
think about properties, use, visualize
blank

8 seconds

# case study: two categories

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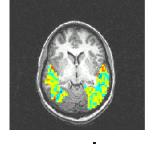
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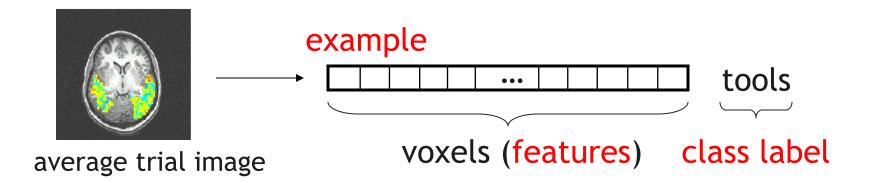
3 seconds 8 seconds

goal: can the two categories be distinguished?

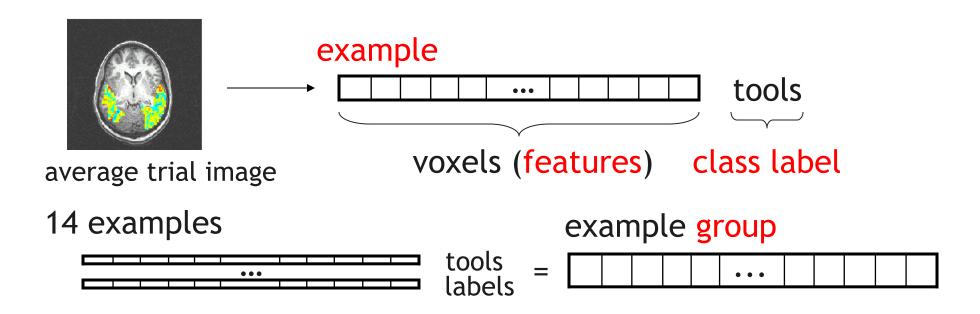
 average images around trial peak to get one labelled image



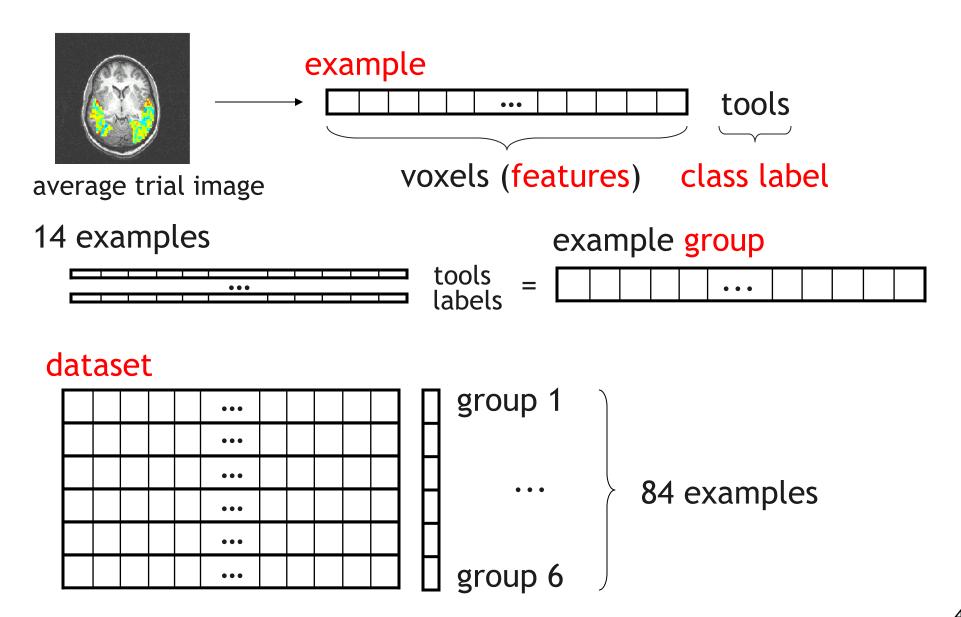
# the name(s) of the game

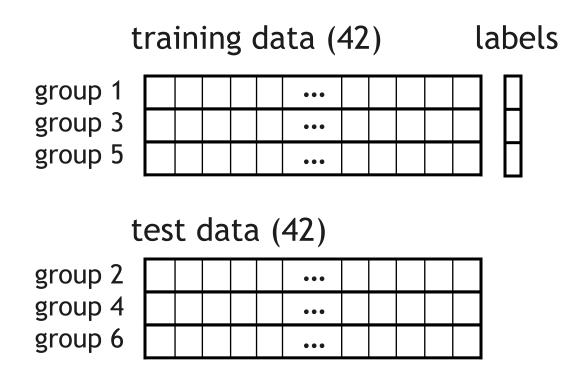


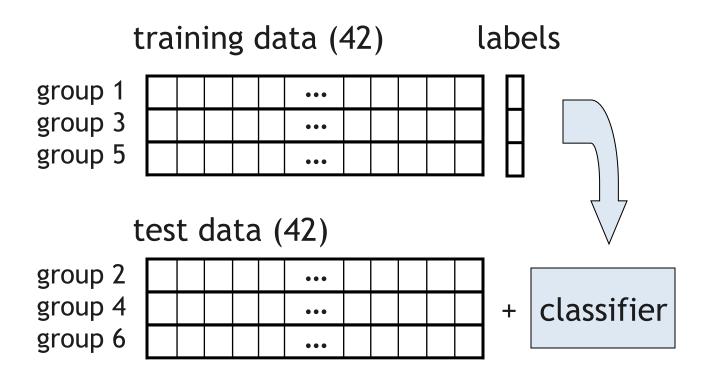
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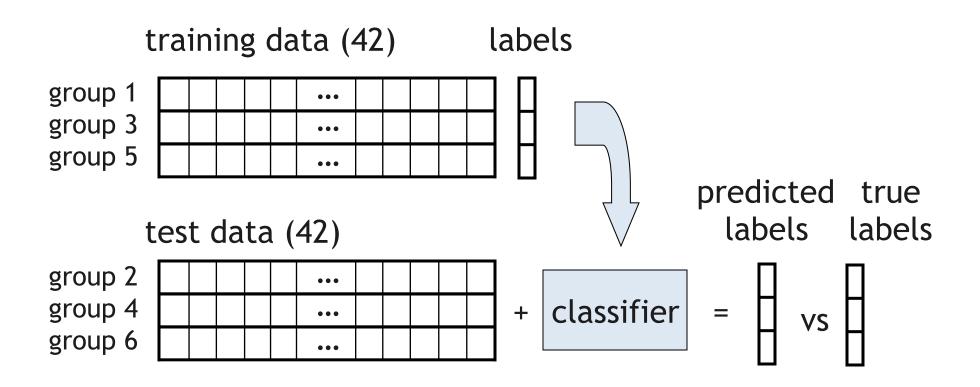


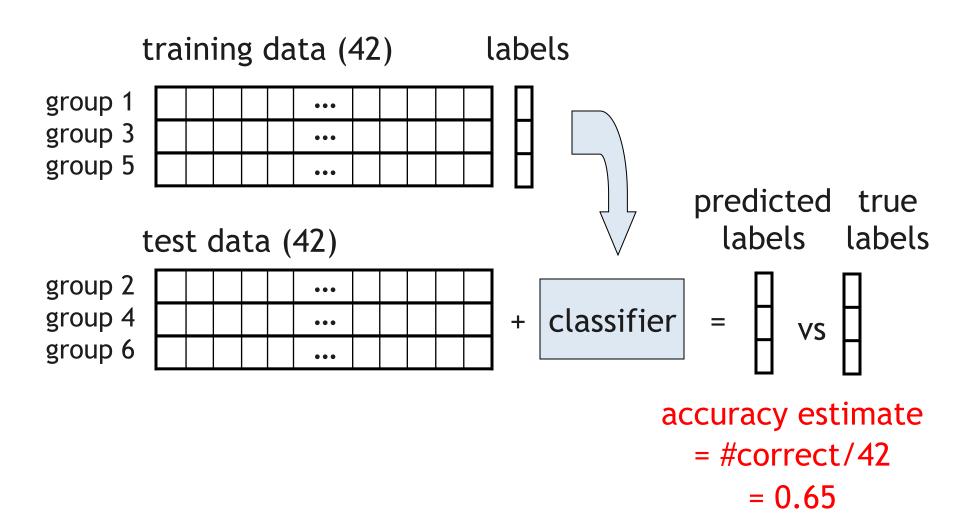
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- estimation is done on the test data
  - it is finite, hence an estimate with uncertainty
- null hypothesis: "the classifier learned nothing"

# what questions can be tackled?

- is there information? (pattern discrimination)
- where/when is information present? (pattern localization)
- how is information encoded? (pattern characterization)

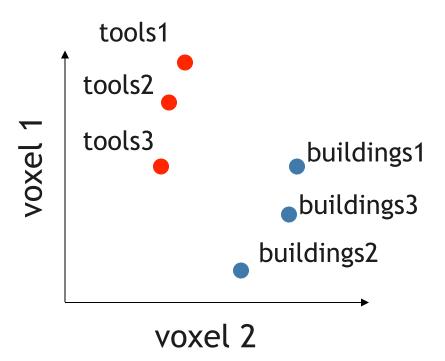
## "is there information?"

• what is inside the black box?

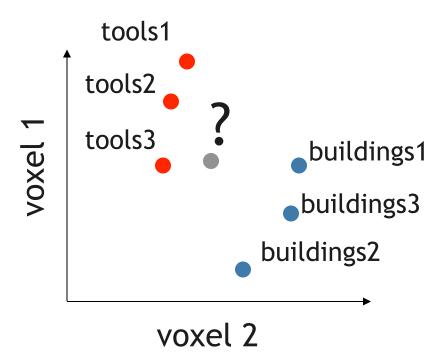
how to test results?

from a study to examples

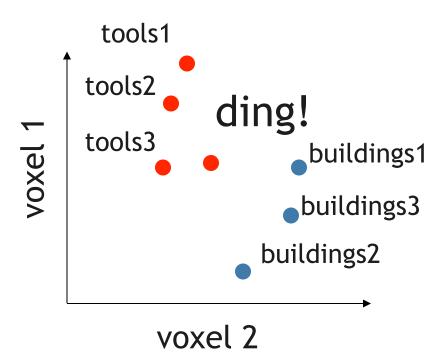
- simplest function is no function at all
- "nearest neighbour"



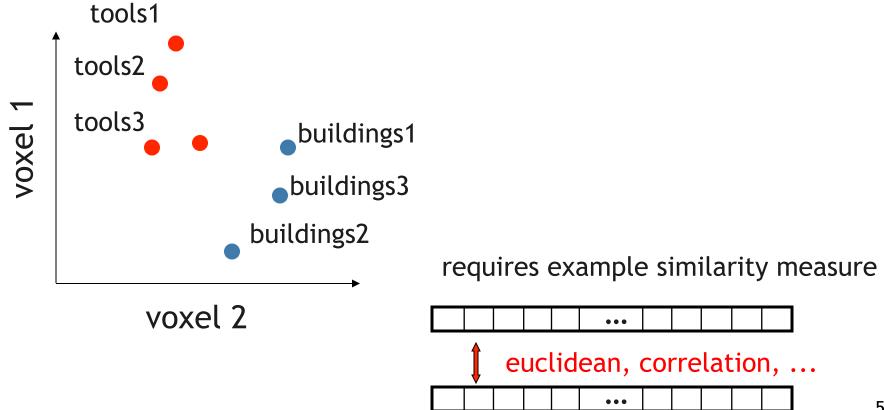
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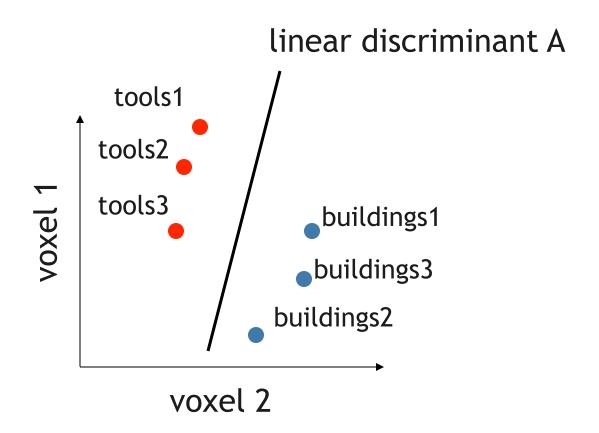
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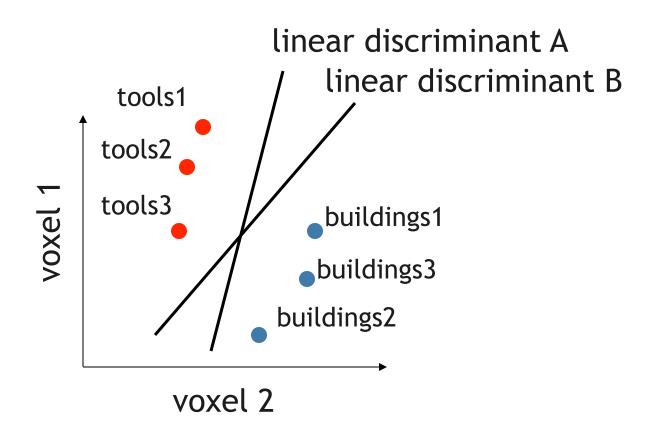
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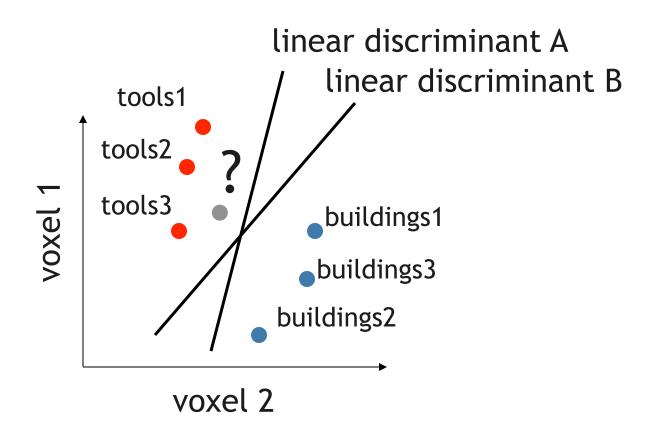
next simplest: learn linear discriminant



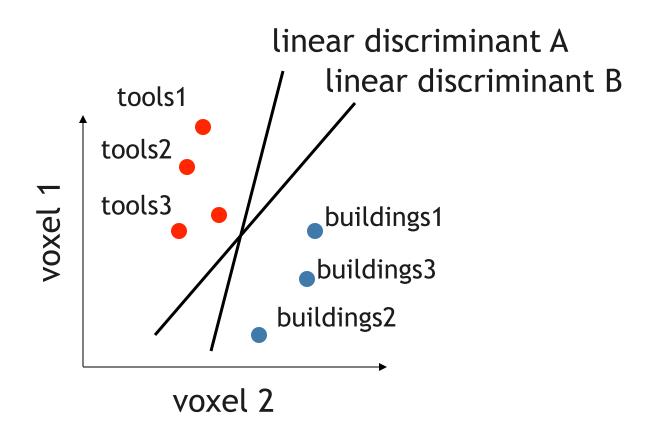
- next simplest: learn linear discriminant
- note that there are many solutions...

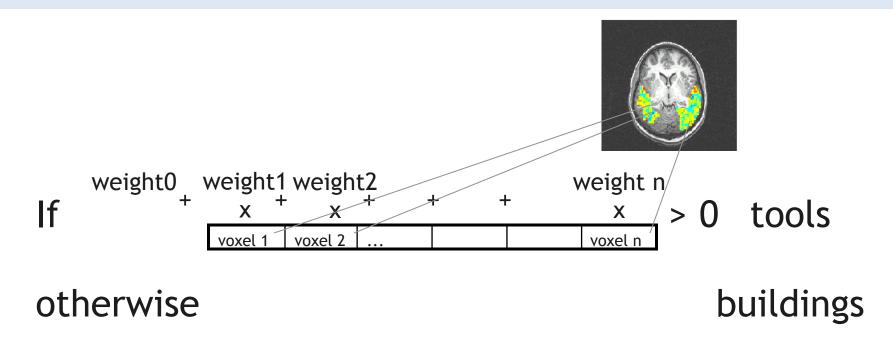


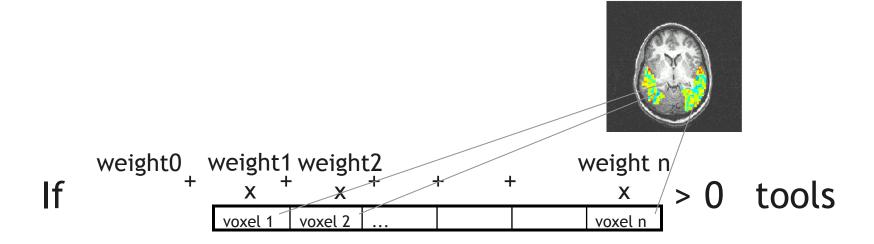
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otherwise buildings

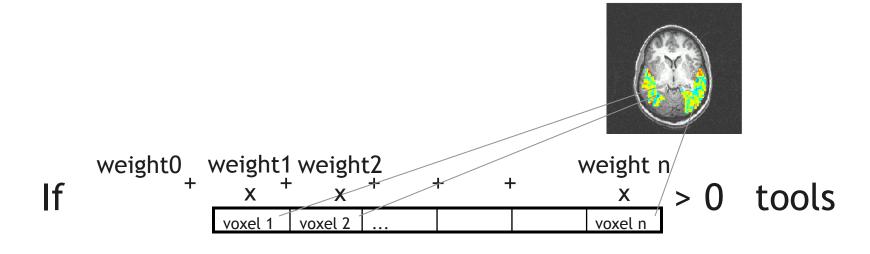
#### various kinds

Gaussian Naive Bayes

Logistic Regression

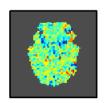
Linear SVM

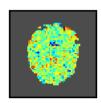
differ on how weights are chosen

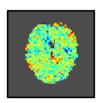


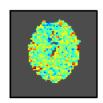
otherwise buildings

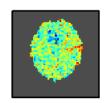
## linear SVM weights:

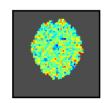


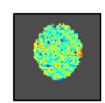


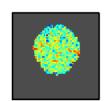


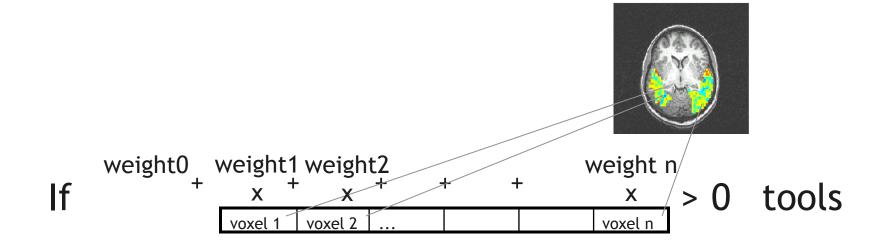










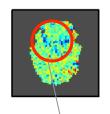


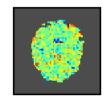
otherwise

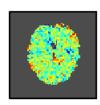
buildings

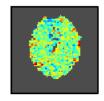
weights pull towards tools

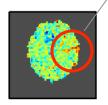
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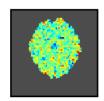


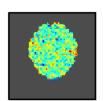


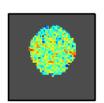








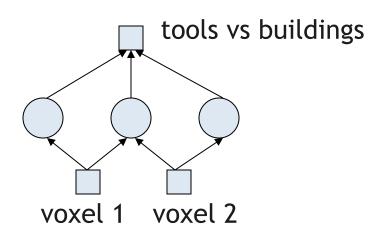




weights pull towards buildings

linear on a transformed feature space

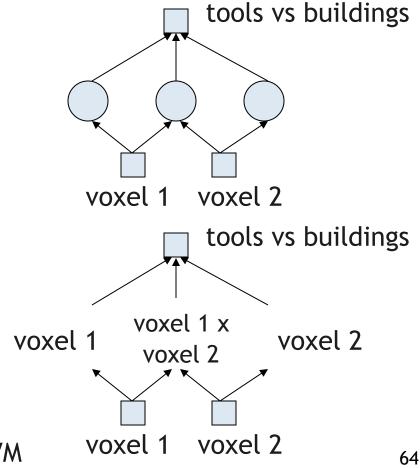
- linear on a transformed feature space
- neural networks:new features are learnt



linear on a transformed feature space!

neural networks:new features are learnt

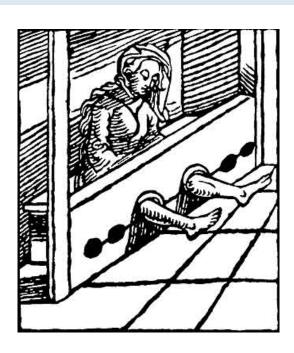
SVMs
 new features are (implicitly)
 determined by a kernel



quadratic SVM

#### reasons to be careful:

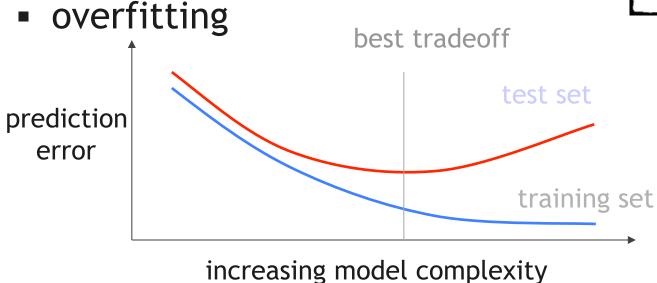
- too few examples, too many features
- harder to interpret



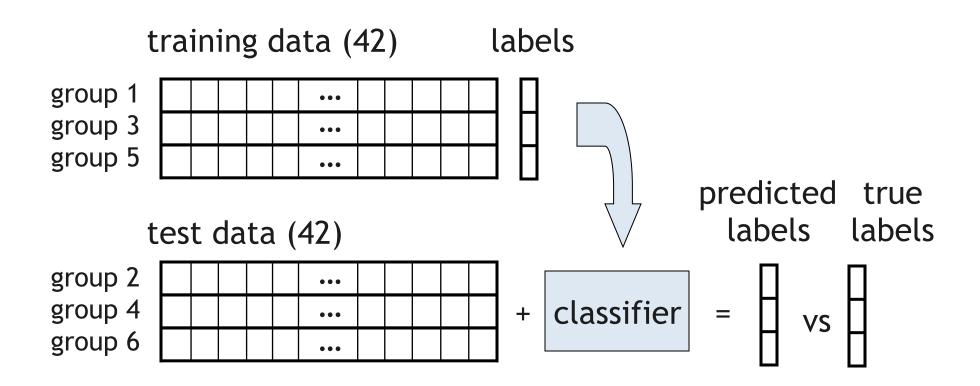
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[from Hastie et al,2001]



#### Predicted labels

```
tools
buildings
buildings
```

• • •

tools buildings tools

True labels	Predicted labels		
tools tools buildings	tools buildings buildings	error	#correct out of #test
buildings buildings tools	tools buildings tools	error	

#### True labels Predicted labels tools tools tools buildings error buildings buildings #correct out of buildings tools error #test buildings buildings tools tools

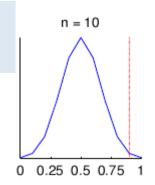
null hypothesis:

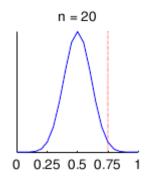
"classifier learnt nothing" ---- "predicts randomly"

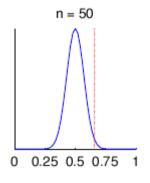
#### True labels Predicted labels tools tools tools buildings error buildings buildings #correct out of buildings tools error #test buildings buildings tools tools

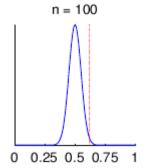
- null hypothesis:
  - "classifier learnt nothing" --- "predicts randomly"
- intuition:
  - a result is significant if very unlikely under null

- X = #correct
- P(X|null) is binomial(#test,0.5)
- p-value is P(X>=result to test|null)







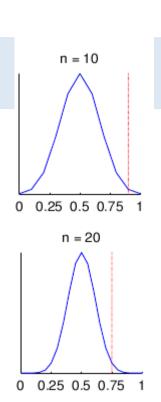


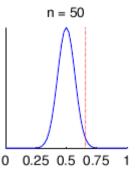
distribution under null (0.05 p-value cut-off)

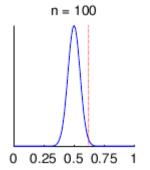
# how do we test predictions?

- X = #correct
- P(X|null) is binomial(#test,0.5)
- p-value is P(X>=result to test|null)
- lots of caveats:
  - accuracy is an estimate
  - few examples very uncertain
  - can get a confidence interval
  - must correct for multiple comparisons

distribution under null (0.05 p-value cut-off)





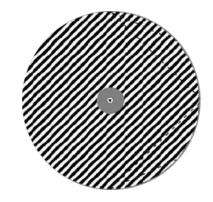


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- how is information encoded? (pattern characterization)

# case study: orientation

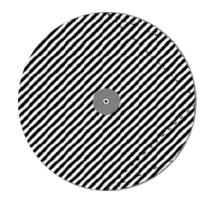
[Kamitani&Tong, 2005]

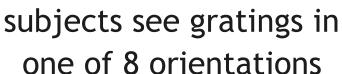


subjects see gratings in one of 8 orientations

#### case study: orientation

[Kamitani&Tong, 2005]



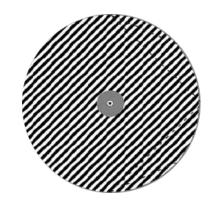




voxels in visual cortex respond similarly to different orientations

#### case study: orientation

[Kamitani&Tong, 2005]

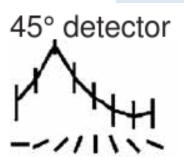


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voxels in visual cortex respond similarly to different orientations

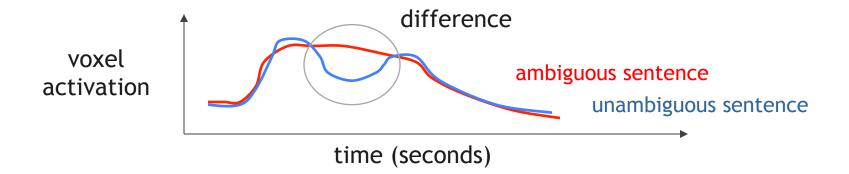
linear SVM

yet, voxels can be combined to predict the orientation of the grating being seen!

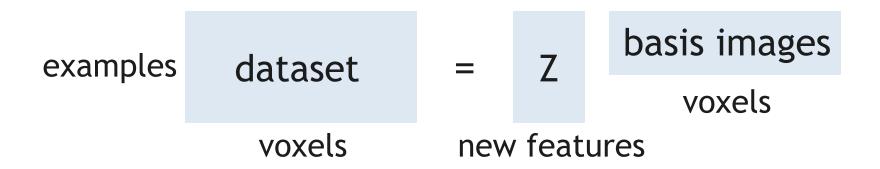


- case study #1, features are voxels
- case study #2, features are voxels in visual cortex

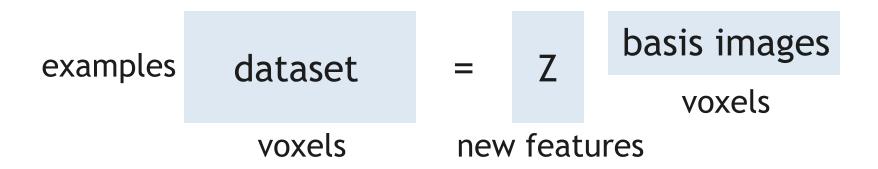
- case study #1, features are voxels
- case study #2, features are voxels in visual cortex
- what else could they be?
   voxels at particular times in a trial,
   syntactic ambiguity study



- you can also synthesize features
  - Singular Value Decomposition (SVD)
  - Independent Component Analysis (ICA)



- you can also synthesize features
  - Singular Value Decomposition (SVD)
  - Independent Component Analysis (ICA)



- reduces to #features < #examples</p>
- a feature has a spatial extent: basis image
- learn on the training set, convert the test set

# example construction

- an example
  - can be created from one or more brain images
  - needs to be amenable to labelling

#### example construction

- an example
  - can be created from one or more brain images
  - needs to be amenable to labelling
- some possibilities
  - the brain image from a single TR
  - the average image in a trial or a block
  - the image of beta coefficients from deconvolution

# example construction

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  - can be created from one or more brain images
  - needs to be amenable to labelling
- some possibilities
  - the brain image from a single TR
  - the average image in a trial or a block
  - the image of beta coefficients from deconvolution
- caveats
  - remember the haemodynamic response time-to-peak
  - images for two examples not separate "enough"
    - in test set, lowers the effective #examples in statistical test
    - in between train and test set, "peeking"/"circularity"
  - read [Kriegeskorte et al. 2009] ("double dipping")

## localization

key idea #1
 test conclusions pertain to whatever is fed to the classifier

#### localization

- key idea #1
   test conclusions pertain to whatever is fed to the classifier
- key idea #2
   one can predict anything that can be lated

```
one can predict anything that can be labelled: stimuli, subject percepts, behaviour, response, ...
```

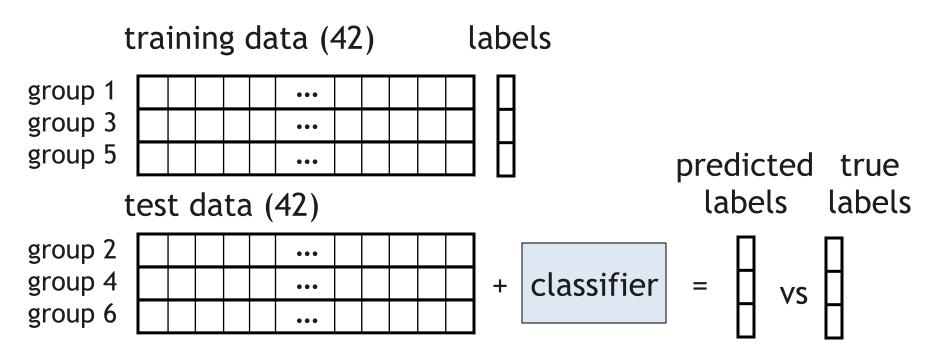
#### localization

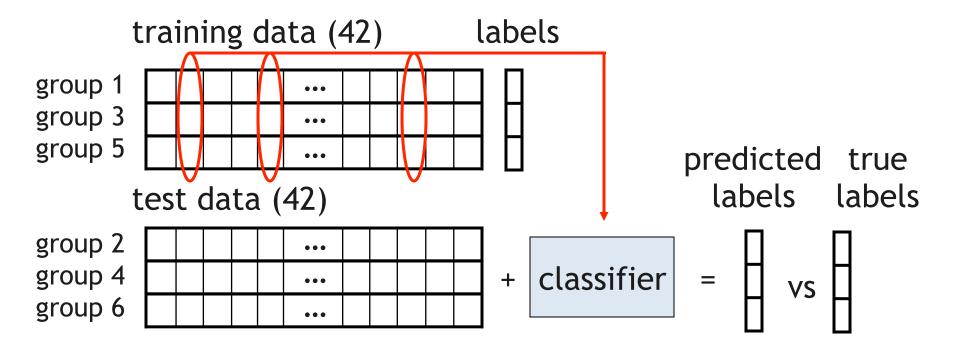
- key idea #1
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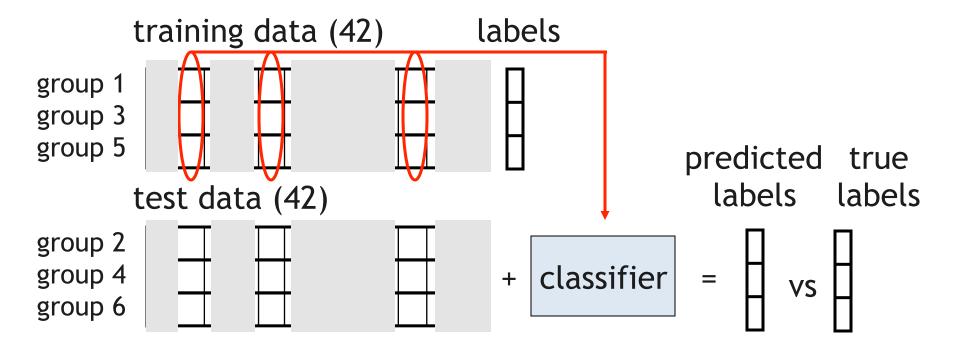
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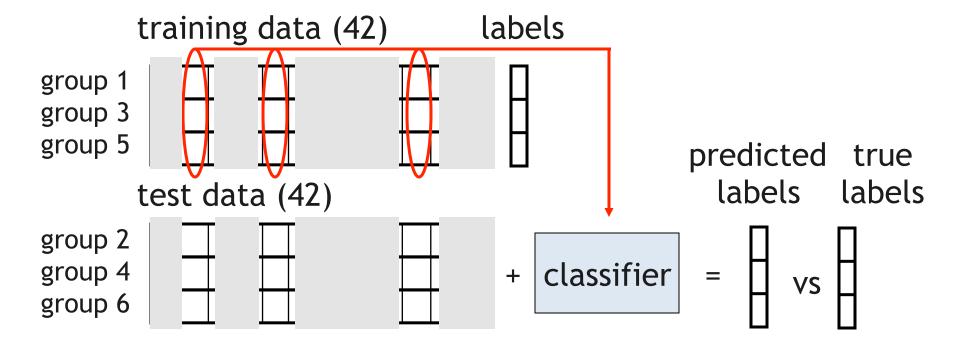
#### so what criteria can we use?

- location
- time
- voxel behaviour or relationship to label
  - aka "feature selection"





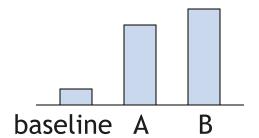




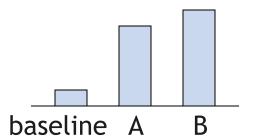
- great for improving prediction accuracy
- but
  - voxels often come from all over the place
  - very little overlap in selected across training sets

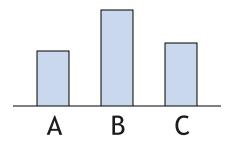
look at the training data and labels

- look at the training data and labels
- a few criteria:
  - difference from baseline

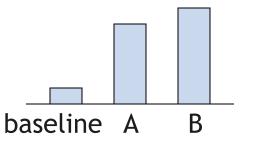


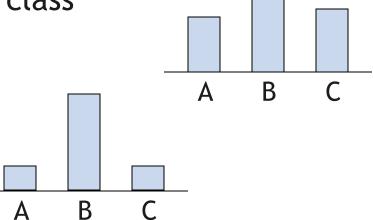
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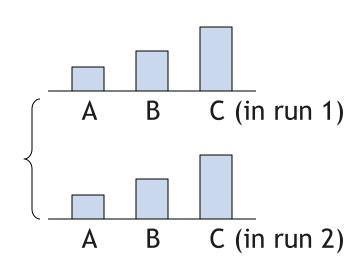


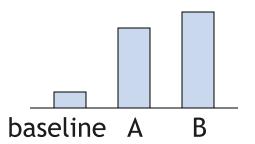
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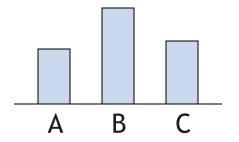




- look at the training data and labels
- a few criteria:
  - difference from baseline
  - difference between classes (e.g. ANOVA)
  - preferential response to one class
  - stability
  - ...



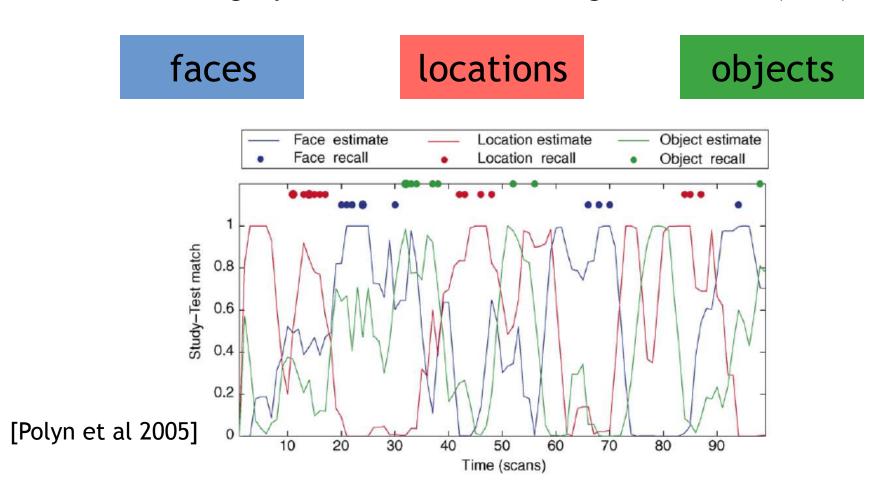




В

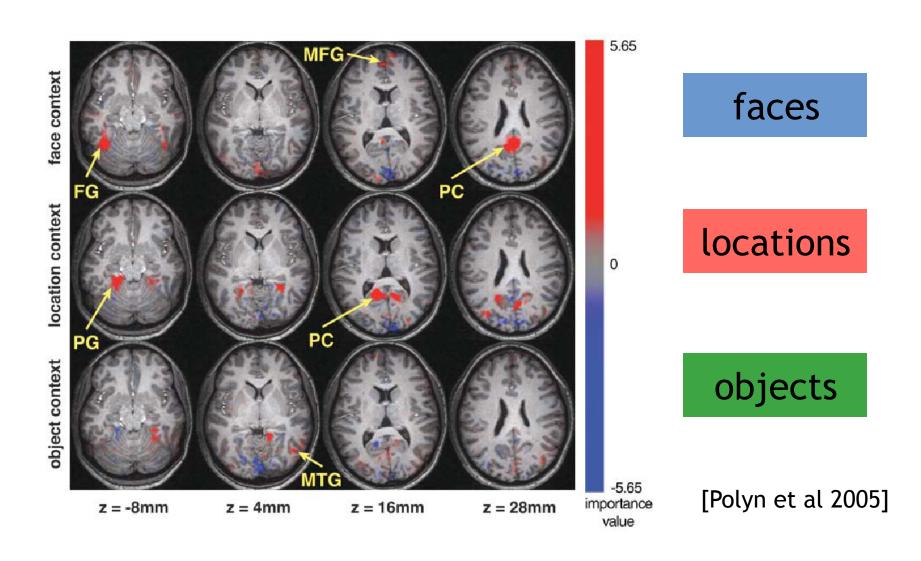
#### case study: category reinstatement

- items from 3 categories: faces, locations, objects
- classifier trained during study of the grouped items
- detect category reinstatement during free recall (test)



## temporal localization

#### voxel influence on reinstatement estimate



### temporal localization

#### key ideas:

- trained classifiers may be used as detectors
   to localize the time at which information is present
- test examples can be temporally overlapping
- it is feasible to decode endogenous events

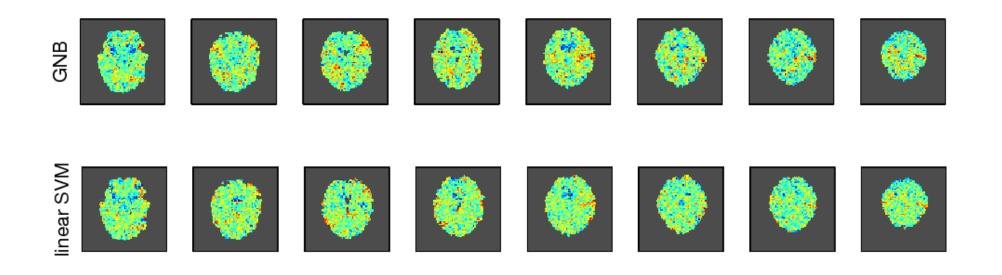
# what questions can be tackled?

- is there information?(pattern discrimination)
- where/when is information present? (pattern localization)
- how is information encoded?(pattern characterization)

- a classifier learns to relate features to labels
- we can consider not just what gets selected but also how the classifier uses it
- in linear classifiers, look at voxel weights

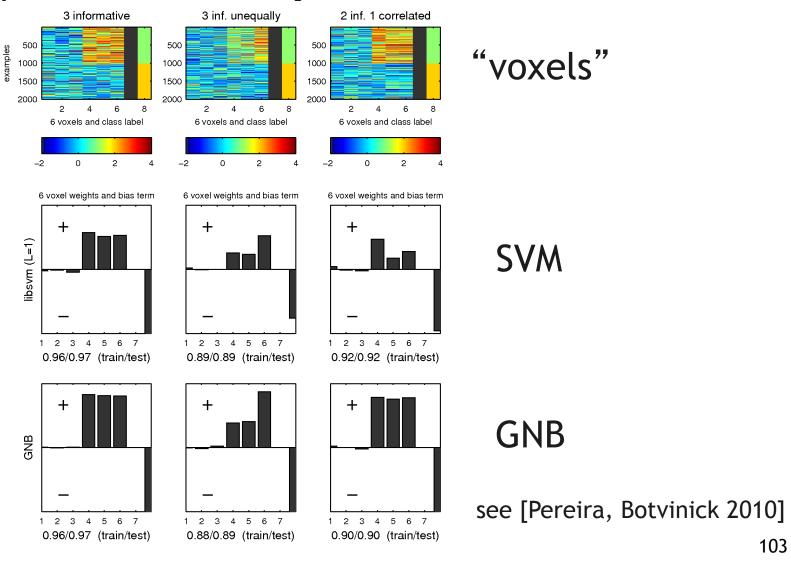


- weights depend on classifier assumptions
- less of an issue if feature selection is used



weights are similar, but accuracy difference 15%

assumption effects on synthetic data



# case study: 8 categories

[Haxby et al., 2001]

# subjects see photographs of objects in 8 categories

- faces, houses, cats, bottles,
   scissors, shoes, chairs, scrambled
- block: series of photographs of the same category



# case study: 8 categories

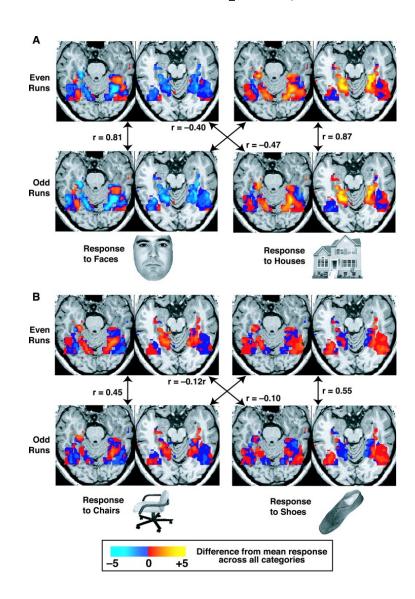
[Haxby et al., 2001]

#### nearest neighbour classifier

- all category pair distinctions
- selects voxels by location
  - fusiform gyrus
  - rest of temporal cortex
- selects voxels by behaviour
  - responsive to single category
  - responsive to multiple

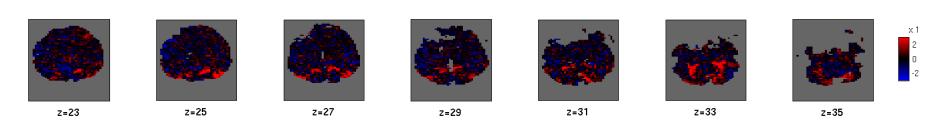
#### logic:

- restrict by location/behaviour
- see if there is still information



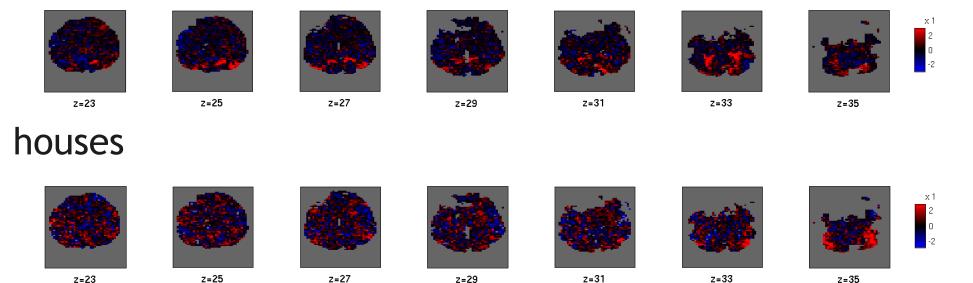
1) whole-brain logistic regression weights

#### faces



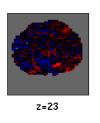
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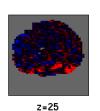
#### faces

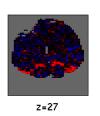


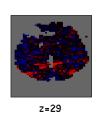
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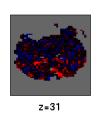
#### faces

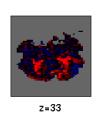


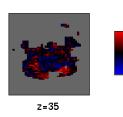




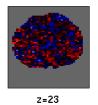


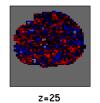


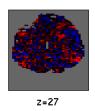


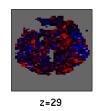


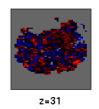
#### houses

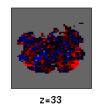


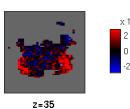




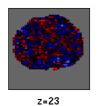


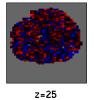


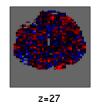


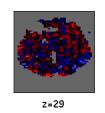


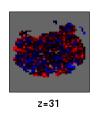
chairs

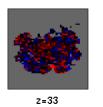


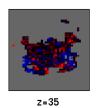


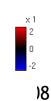






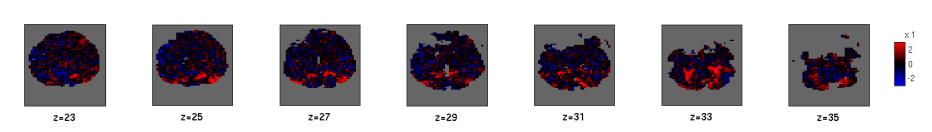






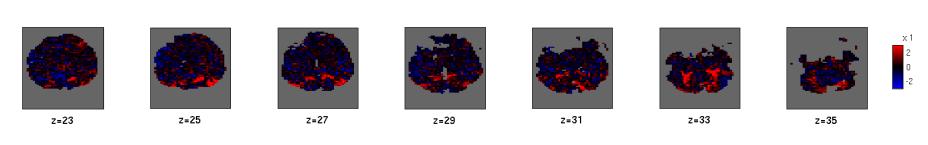
## 2) feature selection

#### faces

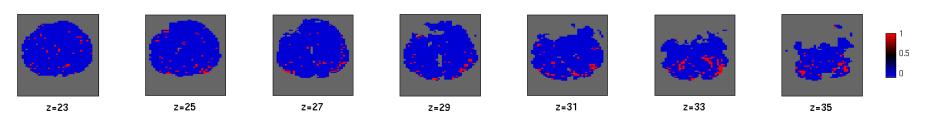


## 2) feature selection

#### faces



## top 1000 voxels



#### whole brain classifier

- accuracy 40% in this case
- many more features than examples => simple classifier
- messy maps (can bootstrap to threshold)

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#### a lot of work

[Mitchell et al 2004], [Norman et al 2006], [Haynes et al 2006], [Pereira 2007], [De Martino et al 2008], [Carrol et al 2009], [Pereira et al 2009]

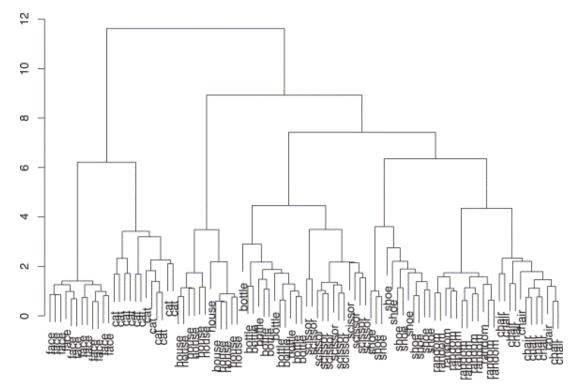
#### neural network

- one-of-8 classifier
- temporal cortex

#### learned model

- hidden units
- activation patterns across units reflect category similarity

distance [Hanson et al., 2004]



face cat house bottle scissor shoe chair

#### neural network

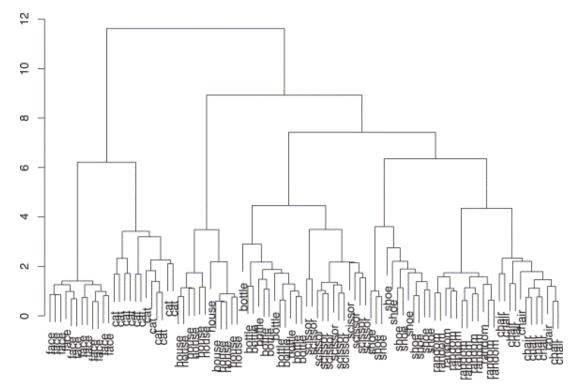
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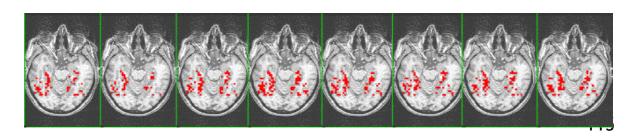
- hidden units
- activation patterns across units reflect category similarity
- sensitivity analysis
  - add noise to voxels
  - which ones lead to classification error?

[Hanson et al., 2004]

#### distance



face cat house bottle scissor shoe chair



## classifier dissection conclusions

- if linear works, you can look at weights
  - but know what your classifier does (or try several)
  - read about bootstrapping (and [Strother et al. 2002])

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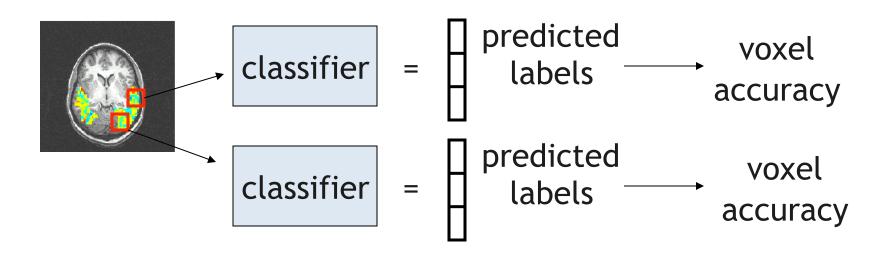
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  - try multiple methods and look at the voxels they pick
  - voxels picked may be a small subset of informative ones
  - report all #s of voxels selected or use cross-validation on training set to pick a # to use
- nonlinear classifiers
  - worth trying, but try linear + voxel selection first
  - look at [Hanson et al. 2004] and [Rasmussen et al. 2011]
     for ways of gauging voxel influence on classifier

# information-based mapping (searchlights)

[Kriegeskorte 2006]

- focus the classifier on small voxel neighbourhoods
- more examples than features
- can learn voxel relationships (e.g. covariance matrix)
- can train nonlinear classifiers

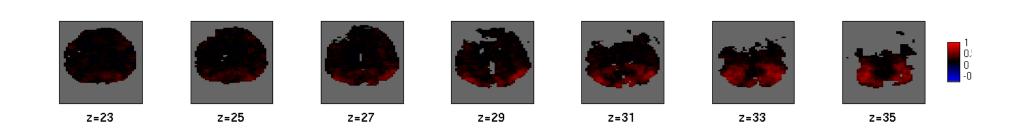


on 8 categories, yields an accuracy map

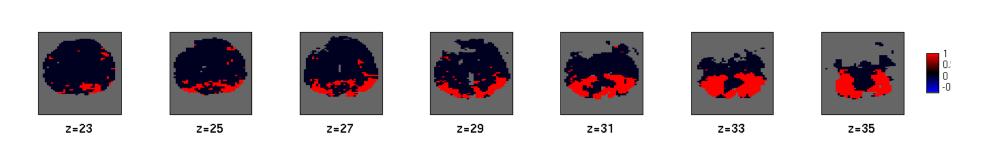


also local information: covariance, voxel weights

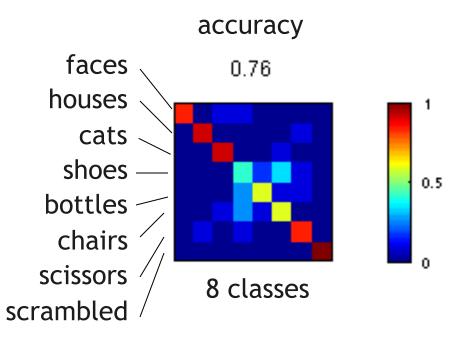
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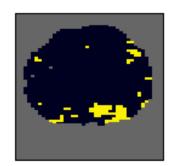
- also local information: covariance, voxel weights
- can be thresholded for statistical significance

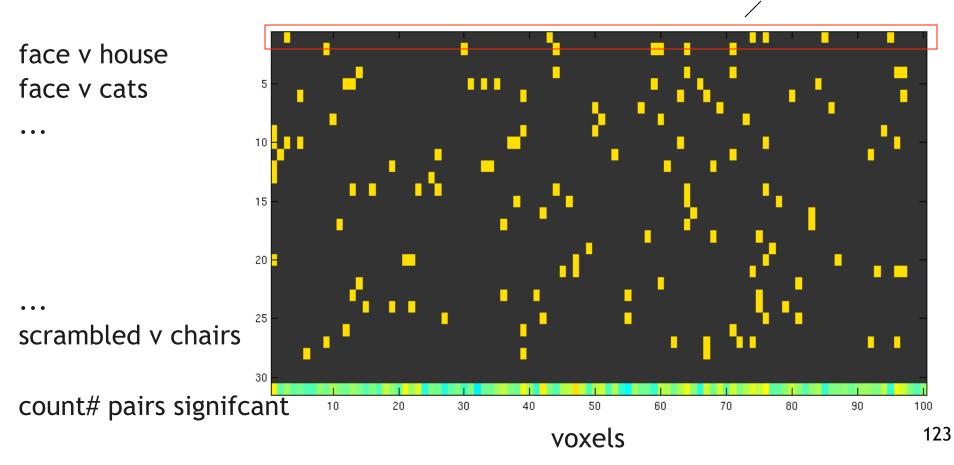


- "H0: chance level" deems many voxels significant
- what does accuracy mean in multi-class settings?
  - confusion matrix
  - for each class, what do examples belonging to it get labelled as?

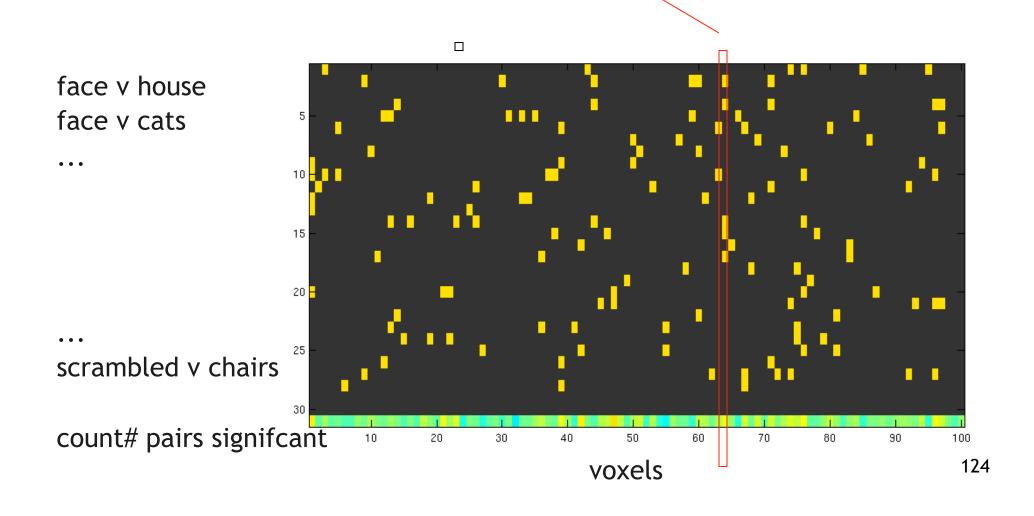


- contrast each pair of classes directly
- threshold accuracy to a binary image





- each voxel has a binary profile across pairs
- how many different ones?



[Pereira&Botvinick, KDD 2011]

- a binary profile is a kind of confusion matrix
- only a few hundred profiles, many similar
- cluster them!





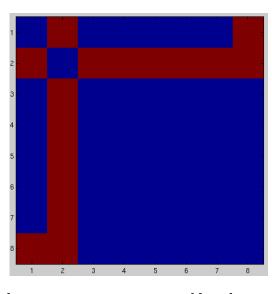




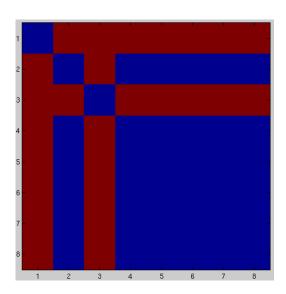








houses versus all else



faces and cat versus all else

- 1 face
- 2 house
- 3 cat
- 4 bottle
- 5 scissors
- 6 chairs
- 7 shoes
- 8 scrambled

- a map of accuracy works well in 2 class situation
- some classifiers seem consistently better
   see [Pereira&Botvinick 2010] for details
- easy to get above chance with multiway prediction so reporting accuracy or #significant is not enough
- consider reporting common profiles or grouping classes into distinctions to test

# what questions can be tackled?

- is there information?(pattern discrimination)
- where/when is information present? (pattern localization)
- how is information encoded? (pattern characterization)

## to get started

- MVPA toolbox (in MATLAB)
  - http://code.google.com/p/princeton-mvpa-toolbox
- PyMVPA (in Python)
  - http://www.pymvpa.org
- support the whole workflow
  - cross-validation, voxel selection, multiple classifiers,...
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- Searchmight (in MATLAB, shameless plug)
  - http://minerva.csbmb.princeton.edu/searchmight
  - special purpose toolbox for information mapping
  - can be used with MVPA toolbox

# Thank you! questions?