### ROBUST VISUAL TRACKING USING CORRELATION RESPONSE MAP

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#### **ABSTRACT**

In this paper, we address the problem of heavy occlusion where the negative samples contaminate the translation model. In this setting, we decompose the task of tracking into translation and scale estimation of objects. We use hierarchical convolutional features to estimate target position and update translation model, and we use HOG features for the scale filter. In addition, we evaluate the translation's reliability according to the correlation responses map which is the result of correlation detection. Then we propose a new method to update model according to the reliability. Experiments are performed on 28 benchmark sequences with significant scale variations, it shows that the proposed algorithm performs favorably against state-of-the-art methods in terms of accuracy and robustness.

*Index Terms*— heavy occlusion, negative samples, correlation response, correlation filters

#### 1. INTRODUCTION

Visual tracking is of great importance in security, human computer interaction and auto-control systems. A typical scenario of visual tracking is to track an arbitrary object initialized by position and scale in subsequent image frames and get the positions and scales. In this paper, we aim at using hierarchical convolutional features and correlation responses map to address the problem of heavy occlusion where the negative samples contaminate the translation model.

Correlation filter based trackers [1–7] are ranked top in terms of performances. Bolme et al. [1] propose a correlation filter based tracker, named Minimum Output Sum of Squared Error (MOSSE), which produces stable correlation filters when initialized with a single frame. Henriques et al. [4, 5] provide a link to Fourier analysis that opens up the possibility of extremely fast learning and detection with the fast Fourier transforms. They also propose a kernelized correlation filter (KCF) which uses a single kernel and enables fast learning with fast Fourier transforms instead of costly matrix operation, providing the highest tracking speed in benchmark [8]. Danelljan et al. [3] extend the KCF with low-dimensional adaptive color channels and suggest that color attributes provides superior performance for visual tracking. To better



**Fig. 1**. An example of our approach in challenging situations of fast motion, significant deformation and occlusion on the Lemming sequence [8]. At frame 333, our approach dynamically updates the learning rate rather than a constant one. The learning rate is set to 0 using our approach.

solve the partial occlusion issue, Liu et al. [6] propose a novel tracking method which track objects based on parts with multiple correlation filters. Ma et al. [7] exploit features extracted from deep convolutional neural networks trained on object recognition datasets to improve tracking accuracy and robustness. Then they adaptively learned correlation filters on each convolutional layer to encode the target appearance. Danelljan et al. propose the DSST tracker [2] learning adaptive multi-scale correlation filters using HOG features as target representation to handle the problem of scale change. Note that our proposed algorithm differs from existing methods based on correlation filters for the reason that we use hierarchical convolutional features to update translation model and we use HOG features for the scale filter.

As we need feature extractor to represent the target, feature representation is of prime importance in visual object tracking with the goal of discriminating the target from the background context. Feature representation has received considerable attention. In [9], discriminative local patches are selected to compute the target displacement using the Lucas-Kanade method. Similarly, Collins et al. [10] propose an

online ranking mechanism for feature selection by measuring the variance ratio between object and background pixels. Grabner et al. use key points to describe the regions containing targets and surrounding context. Several hand-crafted local descriptors, such as SIFT [11], SURF [12] and orientation gradients(HOG) [13], have also been exploited as target representation. However, learning features form raw image pixels on large-scale dataset to deal with computer vision problems has made impressive progress compared with handcrafted features. In this paper, we use hierarchical convolution features for translation model and HOG features for scale model respectively for the reason of computing efficiency and accuracy. For object visual tracking, the first step is to find out the most reliable positions. On this basis, we can estimate an appropriate scale. Also we find that the HOG feature is robust in scale estimating.

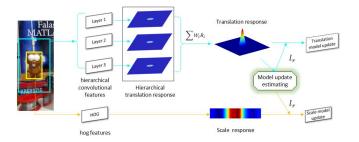
Our approach also builds on the observation based on prior work. It is critical to enhance the detection module to dynamically update the translation model and scale model. However, almost all correlation filter based trackers [1–7] simply update the model wiht a learning rate which is invariant during tracking. For model update, therefor, these method with constant learning rate is not adaptive. When the target is occluded or missing, as shown in Figure 1, this method contaminates the translation model and leads to a risk of drifting. We instead update the models depending on the correlation response which is the result of correlation detection. When the target is occluded, the learning rate is set to a small value or even zero.

#### 2. PROPOSED ALGORITHM

As we aim to address the problem of heavy occlusion where the negative samples contaminate the translation model, we decompose the task of tracking into translation and scale estimation of objects. Also, we evaluate the translation's reliability according to the correlation responses map which is the result of a correlation filter (See Figure 2).

# 2.1. correlation tracking

Here we provide a brief overview of the correlation tracking. A correlation filter is a kind of template to model the appearance of the target. Firstly, an image patch x which is centered around the target is used to extract the original positive sample and the size is  $[M,N]=(1+padding)\times size(target)$ . The patch x contains the target and some background. A training sample is defined as F(x), and F is a feature extractor. The tracker uses all cyclic shifts of x:  $x_{m,n}=circshift(x,[m,n]),(m,n)\in\{0,...,M-1\}\times\{0,...,N-1\}$  to extract training samples. Each sample has a expected regression value  $y_{m,n}$ . For kernelized correlation filter, it is constructed by two parts: one is the feature template  $F(x_{m,n})$ , the other is coefficient  $\alpha_i$ . A typical way to



**Fig. 2**. We use hierarchical convolutional features to estimate target position and update translation model, and we use HOG features for the scale filter. The three convolutional layers extract features and generate responses map respectively. Then the three hierarchical translation responses generate a translation map by (Eq. 9). We dynamically get a learning rate for the translation model and the scale model depending on this translation response.

train a kernelized correlation filter is to get a function  $f(z) = \sum_{m,n=1}^{M,N} \alpha_i k(F(z),F(x_{m,n}))$  that minimizes the cost function (Eq. 1) which is a kernelized ridge regression.

$$\min_{\alpha} \sum_{m,n} \left| f\left(F\left(x_{m,n}\right)\right) - y_{m,n} \right|^{2} + \lambda \left| \sum_{m,n} \alpha_{i} \phi\left(F\left(x_{m,n}\right)\right) \right|^{2}$$
(1)

 $\lambda$  is a regularization parameter. The solution includes two parts: feature template F(x) and coefficient  $\alpha$  as

$$A = \mathcal{F}(\alpha) = \frac{\mathcal{F}(y)}{\mathcal{F}(\phi(F(x)) \cdot \phi(F(x))) + \lambda}$$
 (2)

The  $\mathcal F$  denotes the discrete Fourier operator. The  $\phi$  is the mapping to the Hilbert space induced by the kernel k, defining the inner product as  $\langle \phi(f), \phi(g) \rangle = k(f,g)$ . The  $\lambda$  is same as Eq. 1 that controls overfitting. The first detection step is performed by cutting out a patch z of the same size and position in the new frame. The detection scores are calculated as

$$\mathcal{F}(y_{m,n}) = \sum_{i=1}^{n} \alpha_i k(F(z_{m,n}), F(x_i))$$
 (3)

where  $z_{m,n} = circshift(z, [m, n])$  y. This can be simplified as

$$R = y = \mathcal{F}^{-1}(A \odot \mathcal{F}(\phi(F(z)) \cdot \phi(F(x)))) \tag{4}$$

Then we get a response matrix (Eq. 5). The target position in the new frame is estimated by finding the maximum of the response matrix. For example, given a response matrix

$$R = \begin{bmatrix} r_{0,0} & r_{0,1} & r_{0,2} & \dots & r_{0,n-1} \\ r_{1,0} & r_{1,1} & r_{1,2} & \dots & r_{1,n-1} \\ r_{2,0} & r_{2,1} & r_{2,2} & \dots & r_{2,n-1} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ r_{m-1,0} & r_{m-1,1} & r_{m-1,2} & \dots & r_{m-1,n-1} \end{bmatrix}$$
(5)

Suppose  $r_{i,j}$  is the maximum of the response matrix. The relative displacement of object in vertical direction and horizontal direction [ $vert\_delta$ ,  $horiz\_delta$ ] is defined as

$$vert\_delta = \begin{cases} i & , & \text{if } i < \frac{m-1}{2} \\ i - m + 1 & , & \text{else} \end{cases}$$
 (6)

$$horiz\_delta = \begin{cases} j &, & \text{if } j < \frac{n-1}{2} \\ j - n + 1 &, & \text{else} \end{cases}$$
 (7)

### 2.2. hierarchical convolutional representations

We use hierarchical convolutional features which come from VGG-Net [14] to estimate target position and update translation model. For correlation trackers, target representation must be a matrix retaining spatial resolution. For example, a  $M \times N$  patch's feature should be  $\frac{M}{4} \times \frac{N}{4} \times C$ . As the fully-connected layers show little spatial resolution(i.e.1 × 1), we use three layers of intermediate representations to encode target appearance.

Due to the pooling and convolution operators used in the CNNs, spatial resolution is much smaller in the deeper convolutional layers. For example, the convolutional feature maps of pool5 in the VGG-Net are of spatial size  $7\times 7$ , which is  $\frac{1}{32}$  of the input image size  $224\times 224$ . To unify different layers' convolutional features to same size and locate targets accurately, we resize each feature map to a fixed larger size with bilinear interpolation. The feature is defined as  $F_{l_i}(x), l_i \in \{l_1, l_2, l_3\}, \ l_1, l_2, l_3$  denote the three layers of intermediate representations.

$$F(x) = [F_{l_1}(x), F_{l_2}(x), F_{l_2}(x)]$$
(8)

$$R = \sum_{l} w_{l} R_{l} \tag{9}$$

The interpolation weight  $w_l$  depends on the layer and  $w_1 > w_2 > w_3$ . The  $R_l$  (see Eq. 4) is generated by  $F_l$  feature respectively and R is finally used to determinate the position.

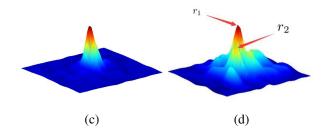
Let  $M \times N$  be the target size in the first frame and S indicate the scales of target. We extract a scale patch  $P_s$  of size  $sM \times sN$  centered around the estimated location. Here s denotes one scale of S and we resize all patches with size  $M \times N$ . In this paper, we use HOG features to construct the scale feature pyramid. Let  $R_s$  denote the correlation response of the target regressor to patch  $P_s$ , the optimal scale s of target is

$$s = \operatorname*{argmax}_{s_i} \{ R_{s_1}, R_{s_2}, R_{s_3} \cdots \}, s_i \in S$$
 (10)

#### 2.3. model update

Adaptability is important for the regression model to estimate the target positions. Unlike prior work which simply update model with constant learning rate, we propose a method





**Fig. 3**. (a) and (b) are the tracking frames and their corresponding response maps (c) and (d). The target in (b) is heavy occluded and its response performs abnormal: the response at the second highest extreme of response  $r_2$  is half of the maximum of response map.

to evaluate the translation's reliability according to the correlation responses (Eq. 5)(Eq. 9). According to this approach, we can find out whether the target is occluded or missing (see Figure 3). Then we dynamically adjust the learning rate. Therefore, our approach effectively adapts to appearance change and alleviates the risk of drifting.

In this paper, the peak-to-sidelobe ratio (PSR) (Eq. 11) is used to quantify the sharpness of the response peak and so evaluate the translation's reliability. The higher PSR value means more confident detection. Therefore, the PSR can be adopted to our approach.

$$PSR_i = \frac{r_i - \mu_i}{\sigma_i} \tag{11}$$

In this paper, we define the highest extreme value as  $r_1$  and the second highest extreme value  $r_2$  (see Figure 3). Then the response matrix  $11 \times 11$  which is centered around the extreme value is used to calculate the PSR. Thus, the PSR can describe the highest extreme value  $PSR_1$  as well as the second highest extreme value  $PSR_2$ .  $\mu_i$  and  $\sigma_i$  are the mean and the standard deviation of the  $11 \times 11$  response matrix. z We then dynamically get the learning rate  $l_r$  and update model as

$$l_r = \begin{cases} \eta r_1 &, & \text{if } psr > \tau \text{ and } r_1 > wr_2 \\ 0 &, & \text{else} \end{cases}$$
 (12)

$$M^{t} = (1 - l_{r})M^{t-1} + l_{r}T^{t}$$
(13)

|                    | boy                       | car4                         | carScale                            | couple              | crossing                   | david                             | dog1                      | doll                                | dudek                              | fleetface                         | freeman1                          | freeman3                            | freeman4                  | girl                                |
|--------------------|---------------------------|------------------------------|-------------------------------------|---------------------|----------------------------|-----------------------------------|---------------------------|-------------------------------------|------------------------------------|-----------------------------------|-----------------------------------|-------------------------------------|---------------------------|-------------------------------------|
| Ours               | 100                       | 97.9                         | 56                                  | 81.4                | 98.3                       | 72.1                              | 100                       | 99.6                                | 100                                | 64.8                              | 54.9                              | 29.6                                | 45.9                      | 100                                 |
| DSST               | 100                       | 100                          | 84.5                                | 10.7                | 100                        | 100                               | 100                       | 99.6                                | 98.1                               | 66.5                              | 36.8                              | 31.3                                | 41.7                      | 24.2                                |
| DLT                | 100                       | 100                          | 70.6                                | 28.6                | 99.2                       | 27                                | 88.4                      | 96                                  | 97.8                               | 42.1                              | 33.4                              | 85.2                                | 15.5                      | 66.6                                |
| KCF                | 99.2                      | 36.7                         | 44.4                                | 24.3                | 92.5                       | 62.2                              | 65.3                      | 55.2                                | 97.6                               | 66.9                              | 16                                | 27.4                                | 18.4                      | 75.6                                |
| Struck             | 97.5                      | 39.9                         | 43.3                                | 60.7                | 95.8                       | 23.6                              | 65.2                      | 68.9                                | 98.1                               | 78.1                              | 20.2                              | 17.6                                | 18.7                      | 97                                  |
| LSHT               | 50.7                      | 27.6                         | 44.8                                | 9.29                | 40                         | 28.2                              | 54.3                      | 23                                  | 89.9                               | 65.5                              | 18.4                              | 15.7                                | 20.1                      | 14.4                                |
| TLD                | 82.9                      | 24                           | 68.7                                | 22.9                | 45.8                       | 61.1                              | 75.6                      | 69.3                                | 67                                 | 44.1                              | 23.3                              | 64.6                                | 21.6                      | 72.6                                |
|                    |                           |                              |                                     |                     |                            |                                   |                           |                                     |                                    |                                   |                                   |                                     |                           |                                     |
|                    | ironman                   | lemming                      | liquor                              | matrix              | mRolling                   | shaking                           | singer1                   | skating1                            | skiing                             | soccer                            | trellis                           | walking                             | walking2                  | woman                               |
| Ours               | ironman<br>55.4           | lemming 94.2                 | liquor<br>52.5                      | matrix<br>25        | mRolling<br>42.7           | shaking<br>98.9                   | singer1                   | skating1<br>30.3                    | skiing<br>9.88                     | soccer<br>34.2                    | trellis<br>92.8                   | walking<br>83.5                     | walking2                  | woman<br>93.1                       |
| Ours<br>DSST       |                           |                              |                                     |                     |                            |                                   |                           |                                     |                                    |                                   |                                   |                                     |                           |                                     |
|                    | 55.4                      | 94.2                         | 52.5                                | 25                  | 42.7                       | 98.9                              | 100                       | 30.3                                | 9.88                               | 34.2                              | 92.8                              | 83.5                                | 100                       | 93.1                                |
| DSST               | <b>55.4</b> 13.3          | <b>94.2</b> 26.9             | 52.5<br>40.9                        | 25                  | <b>42.7</b> 6.71           | 98.9<br><b>100</b>                | 100<br>100                | 30.3<br><b>54.8</b>                 | 9.88<br>4.94                       | 34.2<br><b>52.8</b>               | 92.8<br><b>96.8</b>               | 83.5<br><b>99.8</b>                 | 100<br>100                | 93.1<br>93.3                        |
| DSST<br>DLT        | 55.4<br>13.3<br>6         | 94.2<br>26.9<br>24.3         | 52.5<br>40.9<br>36.3                | 25<br>18<br>1       | <b>42.7</b><br>6.71<br>7.3 | 98.9<br><b>100</b><br>92.6        | 100<br>100<br>100         | 30.3<br><b>54.8</b><br>48.5         | 9.88<br>4.94<br><b>11.1</b>        | 34.2<br><b>52.8</b><br>13.8       | 92.8<br><b>96.8</b><br>31.8       | 83.5<br><b>99.8</b><br>46.4         | 100<br>100<br>100         | 93.1<br>93.3<br>80.2                |
| DSST<br>DLT<br>KCF | 55.4<br>13.3<br>6<br>15.7 | 94.2<br>26.9<br>24.3<br>43.1 | 52.5<br>40.9<br>36.3<br><b>98.2</b> | 25<br>18<br>1<br>13 | <b>42.7</b> 6.71 7.3 7.9   | 98.9<br><b>100</b><br>92.6<br>1.4 | 100<br>100<br>100<br>27.6 | 30.3<br><b>54.8</b><br>48.5<br>36.3 | 9.88<br>4.94<br><b>11.1</b><br>6.2 | 34.2<br><b>52.8</b><br>13.8<br>39 | 92.8<br><b>96.8</b><br>31.8<br>84 | 83.5<br><b>99.8</b><br>46.4<br>51.5 | 100<br>100<br>100<br>37.8 | 93.1<br>93.3<br>80.2<br><b>93.6</b> |

**Table 1**. Per-video overlap precision (OP) in percent on the 28 sequences. The best results are reported in bold. Our approach performs favourably compared to existing trackers.

where  $\tau$  is the threshold and w in this paper is set to 4.  $r_1 > wr_2$  means that  $r_1$  is four times more than  $r_2$ . t is the index of the current frame. M denotes the translation model and scale model and  $T^t$  denotes the template in frame T which is used to update models, such as A (Eq. 2) and  $\mathcal{F}(F(x))$ ). Contrary to traditional correlation filter based trackers, due to our adaptive model update method, even when the target is occluded at one frame, our approach can still maintain the accuracy of the classifier by slightly updating the model. Hence, it is able to relocate the occluded target when it appears in the following frames.

#### 3. EXPERIMENTS

### 3.1. experimental settings

We employ all the 28 sequences annotated with the scale variation attribute in the benchmark [8]. We compare our approach with 6 state-of-art trackers, including DSST [2], DLT [15], KCF [5], Struck [16], LSHT [17], TLD [18], in benchmark [8]. We choose VGG-Net to extract hierarchical convolutional features and HOG descriptors to extract scale features. We use distance precision (DP) at a threshold of 0.5 to evaluate trackers' performance.

Our regularization parameter is set to  $\lambda$  =0.0001 in Eq. 1. As shown in Figure 2, the filter size is set to 2.5 times the initial target size. We use S=33 number of scales with a scale factor of a=1.02. The base learning rate is set to 0.02 for the translation model an 0.025 for the scale model. We use the same parameter values for all the sequences. The convolutional features are extracted from VGG-Net's layer 37, layer 28 and layer 19.

### 3.2. robust estimation with occlusion

In this section, we evaluate our approach in challenging situations of occlusion, such as Lemming, walking 2 and girl. Ta-

ble 1 shows the results of our approach. It is worth mentioning that for the most challenging Lemming sequence, none of the other 6 state-of-the-art methods are able to track targets well whereas our method achieves the distance precision rate of 94.2%. For the reason that the model update in this paper using dynamical learning rate, our approach can be highly adaptive. The model is updated in a comprehensive way, so our tracker achieves the best performance in these sequences.

### 3.3. overall performance evaluation

We evaluate the overall performance on the 28 sequences. Tabel 1 provides a per-video comparison with the top 6 existing trackers in our evaluation. The per-video results are presented using overlap precision (OP). Our approach provides better or competitive performance on 14 out of the 28 sequences. The 14 sequences are reported in bold. Our method provides a OP of 71.9% compared to 64.3% obtained by the method DSST [2]. Compared to DSST and the other trackers, our approach makes a significant improvement on overlap precision.

## 4. CONCLUSION

In this paper, we propose an effective algorithm for visual object tracking. Our approach decomposes the task of tracking into translation and scale estimation of objects. Also, we indicate that a dynamically updated model is comprehensive and adaptive for challenging situations of occlusion. The proposed tracker based on these findings achieves high performance on a large tracking benchmark. In future, we plan to further explore the potential of response map to other tracking difficulties.

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