

ASTR 5463 Final Project: Title

Authors

1 Introduction

2 Methods

For $i = 2, \dots, N - 1$,

$$\begin{aligned}\alpha_i^- &= e_{0,i} + \frac{e_{2,i} - (\Delta\tau_i + 2\Delta\tau_{i-1})e_{1,i}}{\Delta\tau_{i-1}(\Delta\tau_i + \Delta\tau_{i-1})}, \\ \beta_i^- &= \frac{(\Delta\tau_i + \Delta\tau_{i-1})e_{1,i} - e_{2,i}}{\Delta\tau_{i-1}\Delta\tau_i} \\ \gamma_i^- &= \frac{e_{2,i} - \Delta\tau_{i-1}e_{1,i}}{\Delta\tau_i(\Delta\tau_i + \Delta\tau_{i-1})} \\ \alpha_i^+ &= \frac{e_{2,i+1} - \Delta\tau_i e_{1,i+1}}{\Delta\tau_{i-1}(\Delta\tau_i + \Delta\tau_{i-1})} \\ \beta_i^+ &= \frac{(\Delta\tau_i + \Delta\tau_{i-1})e_{1,i+1} - e_{2,i+1}}{\Delta\tau_{i-1}\Delta\tau_i} \\ \gamma_i^+ &= e_{0,i+1} + \frac{e_{2,i+1} - (\Delta\tau_{i-1} + 2\Delta\tau_i)e_{1,i+1}}{\Delta\tau_i(\Delta\tau_i + \Delta\tau_{i-1})},\end{aligned}$$

where

$$\begin{aligned}e_{0,i} &= 1 - e^{-\Delta\tau_{i-1}}, \\ e_{1,i} &= \Delta\tau_{i-1} - e_{0,i} \\ e_{2,i} &= (\Delta\tau_{i-1})^2 - 2e_{1,i}.\end{aligned}$$

$$\begin{aligned}\mathbf{i}_{i-1}^-(\mu, \nu) &= \Delta\mathbf{i}_{i-1}^-(S, \mu, \nu) \\ &= \gamma_{i-1}^-, \\ \mathbf{i}_i^-(\mu, \nu) &= \mathbf{i}_{i-1}^-(\mu, \nu)e^{-\Delta\tau_{i-1}} + \Delta\mathbf{i}_i^-(S, \mu, \nu) \\ &= \gamma_{i-1}^-e^{-\Delta\tau_{i-1}} + \beta_i^-, \\ \mathbf{i}_{i+1}^-(\mu, \nu) &= \mathbf{i}_i^-(\mu, \nu)e^{-\Delta\tau_{i-1}} + \Delta\mathbf{i}_{i+1}^-(S, \mu, \nu) \\ &= [\gamma_{i-1}^-e^{-\Delta\tau_{i-1}} + \beta_i^-]e^{-\Delta\tau_i} + \alpha_{i+1}^-, \end{aligned}$$

$$\begin{aligned}
i_{i+1}^+(\mu, \nu) &= \Delta i_{i+1}^+(S, \mu, \nu) \\
&= \alpha_{i+1}^+, \\
i_i^+(\mu, \nu) &= i_{i+1}^+(\mu, \nu)e^{-\Delta\tau_i} + \Delta i_i^+(S, \mu, \nu) \\
&= \alpha_{i+1}^+e^{-\Delta\tau_i} + \beta_i^+, \\
i_{i-1}^+(\mu, \nu) &= i_i^+(\mu, \nu)e^{-\Delta\tau_{i-1}} + \Delta i_{i-1}^+(S, \mu, \nu) \\
&= [\alpha_{i+1}^+e^{-\Delta\tau_i} + \beta_i^+]e^{-\Delta\tau_{i-1}} + \gamma_{i-1}^+.
\end{aligned}$$

3 Results

4 Conclusion

References