

King Saud University

College of Computer and Information Sciences

Department of Computer Science

Data Structures CSC 212

Final Exam - Fall 2017

Date: 30/12/2017 Duration: 3 hours

Guidelines

•No calculators or any other electronic devices are allowed in this exam.

•Use a pencil in choice questions.

Student ID: Name:												
Section: Instructor:												
1	2.1	2.2	3.1	3.2	4	5	6	7	8	Total		

(a) Choose the correct frequency for every line as well as the total O of the following code:

```
1    sum = 1;
2    for (i = 1; i <= n; i++) {
3        sum+= i;
4        for (j = i; j >= 2; j--)
5        sum--;}
```

- 1. Line 1: (\widehat{A}) 1 (\widehat{B}) 2 (\widehat{C}) 3 (\widehat{D}) n (\widehat{E}) 2n
- 2. Line 2: (A) n (B) n+1 (C) n-1 (D) n+2 (E) n-2
- 3. Line 3: (\widehat{A}) n (\widehat{B}) n+1 (\widehat{C}) n-1 (\widehat{D}) n+2 (\widehat{E}) n-2
- 4. Line 4: (A) n^2 (B) n(n-1)/2 (C) (2n+1)/2 (D) (2n-1)/2 (E) n(n+1)/2
- 5. Line 5: (A) n^2 (B) n(n-1)/2 (C) (2n+1)/2 (D) (2n-1)/2 (E) n(n+1)/2
- 6. Total O: (A) 1 (B) n (C) n^2 (D) $n \log(n)$ (E) n^3

(b) Choose the correct frequency for every line as well as the total O of the following code:

```
count = 0;
for (i = 1; i < n+1; i++)
count ++;
for (j = 0; j <= count; j++)
k = j+1;</pre>
```

- 1. Line 1: (A) 0 (B) 1 (C) 2 (D) n (E) n^2
- 2. Line 2: (A) n (B) n+1 (C) n-1 (D) n+2 (E) n-2
- 3. Line 3: (\widehat{A}) n (\widehat{B}) n+1 (\widehat{C}) n-1 (\widehat{D}) n+2 (\widehat{E}) n-2
- 4. Line 4: (A) count + 2 (B) n + 1 (C) n 1 (D) n + 2 (E) n(n + 1)/2
- 5. Line 5: (A) count + 1 (B) n + 1 (C) n 1 (D) n + 2 (E) n(n 1)/2
- 6. Total O: (A) 1 (B) n (C) n^2 (D) $n \log(n)$ (E) n^3

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(c) Choose the correct answer:	
1. $n^2 + n \log n^4$ is : (A) $O(n)$ (B) $O(n^2)$ (C) $O(n \log(n))$ (D) $O(n^4)$ (E) None	
2. $n^2 + 1000n$ is : (A) $O(n)$ (B) $O(n^2)$ (C) $O(n\log(n))$ (D) $O(nn^2)$ (E) None	
3. $n^4 \log n + n!$ is : (A) $O(n!)$ (B) $O(n^4)$ (C) $O(n^5)$ (D) $O(\log(n))$ (E) None	
4. Algorithm A is $O(n)$, and Algorithm B is $O(2n)$. Given the same input:	
(A) A always finishes before B. (B) B always finishes before A. (C) A and B finish at the same	ne
time.	
Question 2	$_{ m its}$
(a) Given a queue of time intervals represented as pairs of integers, write the method public static Queue	ıe<
Pair <integer, integer="">> getIntervals(Queue<pair<integer, integer="">> q, int start, int end), which return</pair<integer,></integer,>	ns
all intervals of ${\tt q}$ intersecting the interval [start, end]. The input ${\tt q}$ must not change. Assume that	all
intervals in q are valid (that is first <= second), non-overlapping and ordered in chronological ordered	er.
The class Pair is given below.	
<pre>public class Pair<u, v=""> { public U first; public V second; Pair(U first, V second) { this.first = first; this.second = second; } }</u,></pre>	

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(b) Consider a stack of decreasing time intervals, that is, starting from the top, each interval contains the next. Write the method public static Pair<Integer, Integer> smallest(Stack<Pair<Integer, Integer>> st, int t), which returns the smallest interval containing t if it exists, null otherwise. Assume that all intervals in st are valid (that is first <= second).</p>

Example 0.1. If $st : \{[0,8], [1,6], [1,5], [2,4]\}$, then smallest(st, 1) returns [1,5], smallest(st, 3) returns [2,4], smallest(st, 9) returns null.

Complete the code below by choosing the correct answer:

```
public static Pair<Integer, Integer>smallest(Stack<Pair<Integer, Integer>> st, int t){
2
3
      Pair < Integer , Integr > itm = null;
4
      while (!st.empty()) {
        Pair < Integer , Integr > it = st.pop();
5
6
        if (...)
7
8
          itm = it;
9
        else
10
11
12
      while (...) {
13
14
15
      return itm; }
```

- 1. Line 2:
 - A Queue<Pair<Integer, Integer>> r = new
 LinkedQueue<Pair<Integer, Integer>>();
 - B Stack<Integer> r = new LinkedStack<
 Integer>();
 - C List<Pair<Integer, Integer>> r = new
 LinkedList<Pair<Integer, Integer>>();
 - D Stack<Pair<Integer, Integer>> r = new
 LinkedStack<Pair<Integer, Integer>>();
 - (E) None
- 2. Line 6:
 - (A) r.push(it.first);
 - (B) r.insert(it);
 - (C) r.enqueue(it);
 - (D) r.push(it);
 - (E) None
- 3. Line 7:
 - (A) if (it.first < t && t <= it.second)
 - $\stackrel{\textstyle igoreal}{igorplus}$ if (it.first <= t && t <= it.second)
 - (C) if (it.first < t || it.second > t)

- $\stackrel{\textstyle \frown}{
 m (D)}$ if (it.first <= t && it.second <= t)
- (E) None
- 4. Line 10:
 - (A) r.serve();
 - B break;
 - (C) r.pop();
 - (D) r.findNext();
 - (E) None
- 5. Line 12:
 - (A) while (r.empty()){
 - (B) while (!r.empty()){
 - (C) while (r.pop()!= null){
 - (D) while (r.length()!= 0){
 - (E) None
- 6. Line 13:
 - (A) st.push(r.pop());
 - (B) st.push(r.serve());
 - (C) st.push(r.retrieve()); r.findNext();
 - (D) st.push(r.push());
 - (E) None

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(a) The method **private** BTNode<T> mirrorCopy(BTNode<T> t) creates **recursively** a mirror copy of the subtree

```
t. Choose the correct option to complete the code of this method:
```

- 1. Line 2:
 - (A) if (t.left == null || t.right == null)
 - (B) if (t.left == null && t.right == null)
 - (C) if (t == null)
 - (D) if (root != null)
 - (E) None
- 2. Line 3:
 - (A) return null;
 - (B) return root;
 - (C) return mirrorCopy(root);
 - (D) return mirrorCopy(t);
 - (E) None
- 3. Line 4:
 - (A) BTNode<T> p = new BTNode<T>(t.data);
 - (B) BTNode<T> p = new BTNode<T>(root);
 - (C) BTNode<T> p = new BTNode<T>(t);
 - (D) BTNode<T> p = new BTNode<T>(root.data);
 - (E) None

- 4. Line 5:
 - (A) p.right = mirrorCopy(t.left);
 - (B) t.left = mirrorCopy(t.left);
 - (C) p.right = mirrorCopy(t.right);
 - (D) t.left = mirrorCopy(t.right);
 - (E) None
- 5. Line 6:
 - (A) t.right = mirrorCopy(t.left);
 - (B) p.left = mirrorCopy(t.left);
 - (C) p.left = mirrorCopy(t.right);
 - (D) t.right = mirrorCopy(t.right);
 - (E) None
- 6. Line 7:
 - (A) return p;
 - (B) return mirrorCopy(t);
 - (C) mirrorCopy(t.left); mirrorCopy(t.right);
 - (D) return t;
 - (E) None
- (b) Consider the function f below, member of DoubleLinkedList:

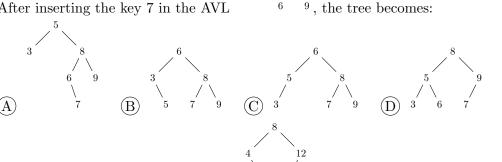
```
public void f(int n) {
  Node<T> p = head; Node<T> q = null;
  for (int i = 0; i < n; i++) {
     q = p;
     p = p.next;
  }
  if (p != null) {
     p.previous = null;
     while (p.next != null)
          p = p.next;
     p.next = head;
     head = q.next;
     q.next = null;
  }
}</pre>
```

Choose the correct result in each of the following cases:
1. The list 1: A, B, C, D, E , after calling 1.f(2), 1 becomes:
2. The list 1: A, B, C, D, E , after calling 1.f(0), 1 becomes:
3. The list 1: A, B, C, D, E , after calling 1.f(5), 1 becomes:
4. The list 1: A, B, C, D, E , after calling 1.f(1), 1 becomes:
Question 4
(a) Consider the following heap represented as an array: 3, 7, 9, 13, 8, 11. Choose the correct answer for every operation (all operations are done on the above heap).
1. Heap after inserting 5: (A) 2.7.0.12.8.11.5 (D) 2.7.7.12.8.11.0 (O) 2.7.0.12.8.5.11 (D) 5.7.2.12.8.11.0 (E) November 1. Heap after inserting 5:
A 3,7,9,13,8,11,5 B 3,5,7,13,8,11,9 C 3,7,9,13,8,5,11 D 5,7,3,13,8,11,9 E None
2. Heap after inserting 10: (A) 2.7.10.12.8.11.0 (B) 2.7.0.12.8.10.11 (C) 2.7.0.12.8.11.10 (D) 2.7.0.10.8.11.12 (E) November 11.12 (E) November 1
(A) 3,7,10,13,8,11,9 (B) 3,7,9,13,8,10,11 (C) 3,7,9,13,8,11,10 (D) 3,7,9,10,8,11,13 (E) None
3. Heap after inserting 2:
A 3,7,9,13,8,11,2 B 3,7,2,13,8,11,9 C 2,7,3,13,8,9,11 D 2,7,3,13,8,11,9 E None
4. Heap after deleting one key: (A) 7,13,9,11,8 (B) 7,8,9,13,11 (C) 9,7,11,13,8 (D) 7,9,8,11,13 (E) None
5. Heap after deleting two keys: (A) 7,13,9,11 (B) 8,11,9,13 (C) 7,8,9,13 (D) 13,9,8,11 (E) None
(b) What is the result of a bottom-up min-heap construction of the following array: 2,4,6,3,5,1?
(A) $1,2,3,5,4,6$ (B) $2,1,3,4,5,6$ (C) $1,3,2,4,5,6$ (D) $1,3,2,5,6,4$ (E) None.
(c) Choose the correct answer:
1. What is the height of a heap of size k ?
(A) $\log \log k$ (B) $k/2$ (C) $k \log k$ (D) $\log k$ (E) None.
2. Bottom-up heap construction is:
$igotimes_{O}O(n)$ $igotimes_{O}O(\log n)$ $igotimes_{O}O(n\log n)$ $igotimes_{O}O(n^2)$ $igotimes_{O}O(n^2)$ $igotimes_{O}O(n^2)$ $igotimes_{O}O(n^2)$
3. The enqueue operation in a heap priority queue is:
$igain O(1)$ $igotimes O(\log n)$ $igotimes O(n)$ $igotimes O(n\log n)$ $igotimes$ None.

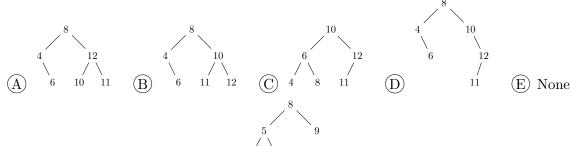
Choose the correct result in each of the following cases:



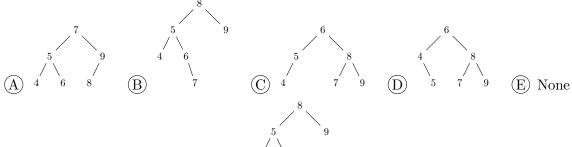
1. After inserting the key 7 in the AVL



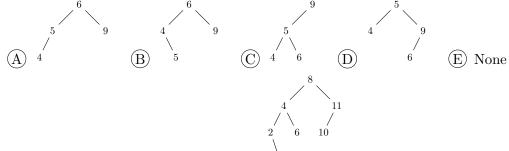
2. After inserting the key 11 in the AVL , the tree becomes:



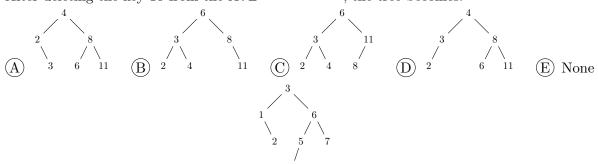
3. After inserting the key 7 in the AVL 4 , the tree becomes:



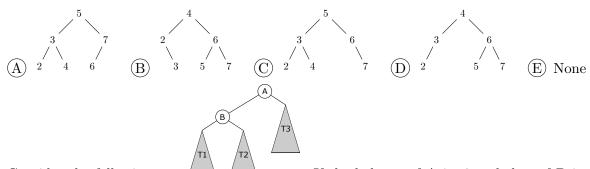
4. After deleting the key 8 from the AVL ⁴ , the tree becomes:



5. After deleting the key 10 from the AVL , the tree becomes:



6. After deleting the key 1 from the AVL , the tree becomes:



7. Consider the following tree _____ . If the balance of A is -2 and that of B is 0, then after performing a single right rotation at A, then:

(a) The balance of A becomes: L	
---------------------------------	--

(b) The balance of B becomes	:
------------------------------	---

the hash table. Use the following collision resolution strategies:

1. Linear rehashing (c=1). Fill in the following table:

Key	16	14	27	5	21	43	10	38	19	18	20
Position											
Number of probes											

2. External chaining. Fill in the following table:

Key	16	14	27	5	21	43	10	38	19	18	20
List position											

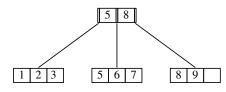
3. Coalesced chaining with cellar size 2 (do not change the hash function). Fill in the following table (put -1 if there is no next element):

Key	16	14	27	5	21	43	10	38	19	18	20
Position											
Next											

Choose the correct result in each of the following cases:

1. After inserting the key 6 in the B+ tree , the **root** of tree becomes:

(A) (B) (5 6 (C) (D) (T) (E) None



2. After inserting the key 4 in the B+ tree

, the **root** of the tree becomes:

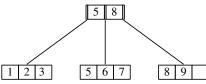




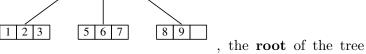




(E) None



3. After inserting the key 10 in the B+ tree becomes:



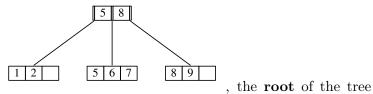
5 10











4. After deleting the key 2 from the B+ tree becomes:

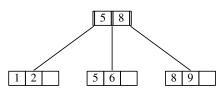










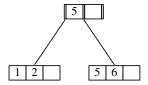


5. After deleting the key 5 from the B+ tree becomes:





(E) None



6. After deleting the key 5 from the B+ tree

, the **root** of the tree becomes:

, the **root** of the tree





2 (D)

(E) None

7. A B+ tree of order 3 containing n keys has a height that is:

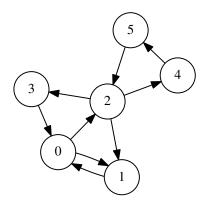
$$\widehat{A}$$
 $O(n)$

$$\bigcirc$$
 $O(n/3)$

$$\bigcirc$$
 $O(n^3)$

$$\bigcirc$$
 $O(\log n)$

Consider the following graph.



1.	Giv	e t	he	a	dj	a	е	n	c;	y	n	na	at	r	ix	(oi	f ·	tl	16	9	g	r	$a_{ m j}$	p	h						
													•								•							 				
							•						•								•							 	•			
									•	•			•			•				•	•			•						•	•	•
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												•			•				•	•				•		•		 •	•	•	•	•
												•			•	•	•			•				•			•	 •	•	•		•

2.	Give	the	adjac	ency	list	repre	esent	ation	of	the	;
	graph	1.									
3.	What	is t	the nu	ımbeı	c of	edges	in t	he su	ıbgr	aph	l
	conta	ining	g the	nodes	{1,	$2, 3$ }.					
4.	What	is t	he ma	aximu	m ni	umbe	r of e	$_{ m dges}$	in a	a di-	
	rected	d gra	ph w	ith n	node	es (lo	ops,	edges	fro	m a	J
	node	to it	self, a	are no	t all	owed)?				

ADT Queue Specification

- enqueue (Type e): **requires**: Queue Q is not full. **input**: Type e. **results**: Element e is added to the queue at its tail. **output**: none.
- serve (Type e): **requires**: Queue Q is not empty. **input**: none. **results**: the element at the head of Q is removed and its value assigned to e. **output**: Type e.
- length (int length): requires: none. input: none. results: The number of elements in the Queue Q is returned. output: length.
- full (boolean flag): requires: none. input: none. results: If Q is full then flag is set to true, otherwise flag is set to false. output: flag.

ADT Stack Specification

- push(Type e): requires: Stack S is not full.
 input: Type e. results: Element e is added to
 the stack as its most recently added elements.
 output: none.
- pop(Type e): requires: Stack S is not empty.
 input: results: the most recently arrived element in S is removed and its value assigned to
 e. output: Type e.
- empty(boolean flag): **requires**: none. **input**: none. **results**: If Stack S is empty then flag is true, otherwise false. **output**: flag.
- full(boolean flag): **requires**: none. **input**: none. **results**: If S is full then Full is true, otherwise Full is false. **output**: flag.