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CSC 311  
The Second Semester, 2020/2021  
Homework #2  
Due on March 07, 2021.

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**Q1:**

Consider the following recurrence relation:

$$M(n) = M\left(\frac{n}{2}\right) + n. \quad M(1) = 1.$$

- (a) Solve it using backward substitutions.
- (b) If possible, use the master method to describe the order of growth for  $M(n)$ .

**Q2:**

A SKIP array  $S[0..n-1]$  is an array of  $n$  integers, where  $n > 1$ , in which  $S[0] = 0$  and  $S[n-1] = n$ .  $i$  is a SKIP index in a SKIP array  $S$  if  $n > i > 0$  and  $S[i] > S[i-1] + 1$ .

- (a) Explain why every SKIP array has at least one SKIP index.
- (b) Give the pseudocode of a  $O(\log n)$ -time algorithm that takes as input a SKIP array and returns one of its SKIP indices.

Example: The SKIP array  $\{0, \mathbf{2}, 3, 0, \mathbf{4}, \mathbf{6}\}$  has 3 SKIP indices: 1, 4, and 5.