

## MATH 151 – PYTHON LAB 7

**Directions:** Use Python to solve each problem. ([Template link](#))

1. Given  $f(x) = \begin{cases} 8 - x^2 & \text{if } x < 0 \\ 5e^{-((x-2)/2)^2} + x & \text{if } x \geq 0 \end{cases}$ 
  - (a) Find the critical values of the function.
  - (b) Find the absolute extrema of  $f$  on the interval  $[-5, 5]$ .
  - (c) Use the method to find the absolute extrema on  $[-10, 10]$ .
  - (d) Plot  $f$  on the interval  $[-10, 10]$ . Choose a **ylim** that allows you to see the graph accurately.

2. When a foreign object lodged in the trachea forces a person to cough, the velocity of the air stream is related to the radius of the trachea by the equation:

$$v(r) = k(r_0 - r)r^2$$

where  $r_0$  is the normal radius of the trachea and  $k$  is a constant.

- (a) Determine the value of  $r$  in the interval  $[\frac{1}{2}r_0, r_0]$  at which  $v$  has an absolute maximum.
  - (b) What is the absolute maximum value of  $v$  on the interval?
  - (c) Let  $r = 0.65$  inches and  $k = 15000$ . What is the maximum value of the function and where does it occur?
  - (d) Sketch the graph of  $v$  with the conditions from part (c) on the interval  $[0, r_0]$
3. Given  $f(x) = \arctan(x)$  and  $g(x) = \operatorname{arccot}(x)$ :
  - (a) Find the derivative of  $f(x)$  and  $g(x)$  separately, then simplify the derivative of  $f(x) + g(x)$ .
  - (b) In a print command, explain what this tells you about  $f(x) + g(x)$ .
  - (c) Plot  $f(x) + g(x)$  and, in a print statement, specifically define the simplified function. (Hint: consider using a piecewise function)
  - (d) In a print statement, explain why this makes sense for  $x > 0$ . (HINT: consider using a cofunction identity)