# Rashomon Code Flow

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All code can be found on Github. The links below lead to the function line that performs each action.

## 1 Active Learning Procedure

Main Function: One Iteration Function

- 1. Set Up:
  - (a) Set seed
  - (b) Load Dataset
  - (c) Train Test Candidate Split Data

■ df\_Test: 20%

• df\_Candidate: 80%

Initial df\_Train: Remaining

(d) (Batch): Calculate distance/diversity metric

$$d_n^x = \min_m ||x_n - x_m|| \tag{1}$$

This is the distance from an unlabeled observation n to its nearest labeled neighbor.

#### 2. Learning Procedure

For i = 0 to len(df\_Train):

- (a) Prediction Method:
  - i. Train TreeFarms model on df\_Train
    - Results in K number of trees
  - ii.  $\operatorname{Predict\ label}$  for  $\operatorname{df}_{\operatorname{Test\ for\ all\ }}K$  tree in  $\operatorname{TreeFarms}$
  - iii. Calculate F1 score (micro average) from each tree in TreeFarms model for the df\_Test
    - Note that the F1 score is over all K trees, including the duplicate trees, even if we are only using the set of unique trees for the selection process (Line 51).
    - Note that my TestErrorFunction still stores both F1 scores: (1) using the duplicate trees and (2) using only the unique trees (Line 31-55).
- (b) Selection Query
  - i. (UNREAL) Restrict ourselves to only the unique trees (Lines 53 56).
  - ii. Predict the labels of df Candidate for each (unique) tree in TreeFarms (Lines 40 51).
  - iii. Calculate recommendation metric (Vote Entropy) for each observation in the candidate set based off of the (unique/duplicate) trees (Lines 74 83):

$$\mathsf{VoteEntropy}(y,x) = -\sum_{y \in \{0,1\}} \frac{\mathsf{vote}_{\mathcal{C}}(y,x)}{|\mathcal{C}|} \log \frac{\mathsf{vote}_{\mathcal{C}}(y,x)}{|\mathcal{C}|} \tag{2}$$

where

$$\mathsf{vote}_{\mathcal{C}} = \sum_{c \in \mathcal{C}} \mathbb{I}\{c(x) = y\} \tag{3}$$

is the number of "votes" that label y receives for x amongst the models in the Rashomon set of trees  $\mathcal C$ .

iv. Weight VoteEntropy (2) with Diversity Metric 1 with Diversity weight w. (Line 86):

$$UncertaintyMetric(y, x; w) = (1 - w) \cdot VoteEntropy + w \cdot Diversity$$
 (4)

v. Recommend the top k candidate observations with the highest vote entropy (Lines 77 - 81):

 $rg \max { t Uncertainty Metric}$ 

- (c) Update (Lines 67-69)
  - i. Add that observation df\_Training
  - ii. Remove that observation from df\_Candidate
- (d) Repeat Steps (a) (c)

#### Find Optimal Rashomon Threshold $\mathbf{2}$

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Main Function: OptimalThresholdSimulation
(a) Set Up:
      i. Load dataset (Line45)
      ii. Set seed (Lines 46-47)
      iii. Train Test Split Data (Lines 49-57)
           • df_Test: 25\%
           • Initial df_Train: 75%
      iv. Train TreeFarms (Line 60 - 65)
      v. Compute training accuracy for each tree in TreeFarms (Line 78)
      vi. Select threshold values

    Note the discrepancy between accuracy and objective function here
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- (b) For each threshold value in Step 2(a)vi
  - i. Filter out models with training accuracy  $\leq$  threshold (Line 102)
  - ii. Calculate test set accuracy and F1 score
    - A. Predict test set labels (Lines 111-114)
    - B. Compute ensemble prediction as majority (Lines 116-119)
    - C. Compute test set accuracy and F1 score (Lines 121- 123)
    - D. Store indices of models and their accuracy metrics (Lines 125 128)

### Analyze Results [Notebook]

- (a) Average F1 scores across all simulations for each threshold
- (b) Average classification accuracy values across all simulations for each threshold
- (c) Plot average F1 score and accuracy across threshold range
- (d) Find the threshold that has the highest F1/accuracy score