

6-4.1

$$p(a_{ij}=1) = \frac{\# \text{links}}{\# \text{possible links}} = \frac{L}{\binom{N}{2}} = \frac{2L}{N(N-1)}$$

6-4.2

$$p(a_{ij}=1 | a_{xy}=0) = \frac{L}{\binom{N}{2} - 1}$$

since for one of all possible links we know that there is no link. Therefore, #possible links - 1 in the denominator but L links in the numerator.

$$p(a_{ij}=0 | a_{xy}=1) = \frac{L-1}{\binom{N}{2} - 1}$$

since one link is already taken

6-4.3

$$r_c = \frac{p(a_{ij}=1 | a_{xy}=0)}{p(a_{ij}=1)} = \frac{L}{\left(\frac{N(N-1)}{2} - 1\right)} \cdot \frac{N(N-1)}{2L} = \frac{N(N-1)}{N(N-1) - 2}$$

$$r_n = \frac{(L-1)}{\left(\frac{N(N-1)}{2} - 1\right)} \cdot \frac{N(N-1)}{2L} = \frac{(L-1)}{L} \cdot \frac{N(N-1)}{(N(N-1) - 2)}$$

$$\Rightarrow \frac{r_c}{r_n} = \frac{L}{L-1}$$

6-4.4 For $G(N, p) \Rightarrow p(a_{ij}=1) = p$

$$\text{and } p(a_{ij}=1 | a_{xy}=0) = p(a_{ij}=0 | a_{xy}=1) = p$$

$$\Rightarrow r_c^i = 1 \text{ and } r_n^i = 1 \Rightarrow \frac{r_c^i}{r_n^i} = 1$$

6-4.5 For $G(N, p)$ the probability of setting a link is not influenced.

For $G(N, L)$ the number of nodes and links is fixed. Therefore, for small N and L the ~~number of~~ the probability of assigning a new link strongly depends on previous settled links