

4.3) Determine the level curve(s) of $f(x, y) = x^3 - 3xy^2$ through the stationary point.

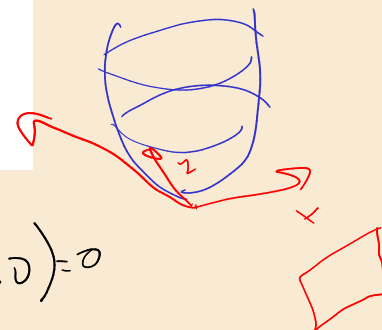
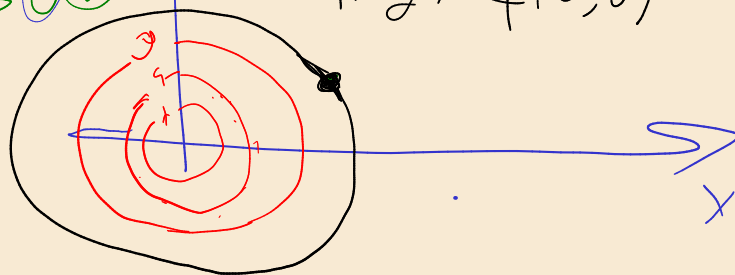
$$\begin{bmatrix} 3x^2 - 3y^2 \\ -6xy \end{bmatrix}$$

$$\frac{x^3 - 3xy^2}{x^2 + y^2}$$

$$\frac{0,0}{f(0,0)=0}$$

$x=y \rightarrow (0,0)$

$f(x,y) = f(0,0) = 0$



$$x^3 - 3xy^2 = 0$$

$$x(x^2 - 3y^2) = 0$$

$$a \cdot b = 0$$

$$a = b \rightarrow (a-b)(a+b)$$

$$a = 0$$

$$\begin{bmatrix} a=0 \\ b=0 \end{bmatrix}$$

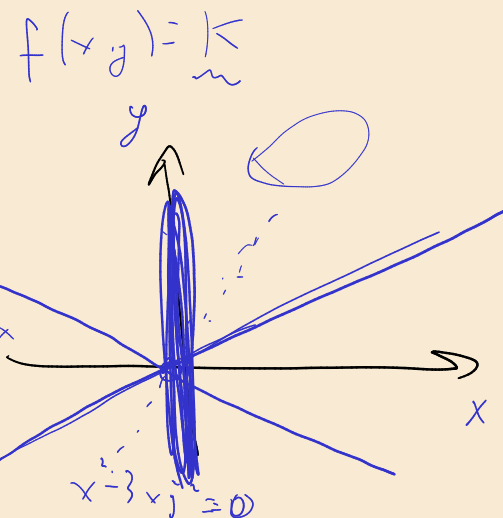
$$\begin{bmatrix} x=0 \\ x^2 - 3y^2 = 0 \end{bmatrix}$$

$$\begin{bmatrix} x=0 \\ (x - \sqrt{3}y)(x + \sqrt{3}y) = 0 \end{bmatrix}$$

$$\begin{bmatrix} x=0 \\ x = \sqrt{3}y \\ x = -\sqrt{3}y \end{bmatrix}$$

$$y = \frac{1}{\sqrt{3}}x$$

$$x^2 - 3y^2 = 0$$



$$f(x) = F'(x)$$

$$\begin{array}{ccc} \int^2 & & x^3 \\ \log & \nearrow & \frac{x}{1} \\ \textcircled{\frac{1}{x}} & & \\ e^x & (l_g)' = \frac{1}{x} e^x & \sin \rightarrow \cos \\ & & -\cos \rightarrow \underline{+\sin} \end{array}$$

$$\int (fg)' - \int f'g = \underline{\int fg'}$$

$$\begin{array}{l} \int f dg = \underline{fg} - \underline{\int g df} = xe^x \Big|_1^2 - \int_1^2 e^x \cdot 1 dx = \\ 14.2.2 \quad \int_1^2 xe^x dx \quad \downarrow \\ (e^x)' = \underline{e^x} \cdot x + e^x \cdot 1 \\ \downarrow \\ \boxed{\begin{array}{l} f = \textcircled{x} \\ dg = e^x \end{array}} \rightarrow df = 1 \cdot dx \\ \quad \quad \quad y = se^x = (e^x) \end{array}$$

$$= xe^x - e^x \Big|_1^2$$

$$2e^2 -$$

$$\int x^2 \ln x dx$$

$$\begin{array}{l|l} f = \ln x & df = \frac{1}{x} dx \\ dg = x^2 dx & g = \frac{x^3}{3} \end{array}$$

$$\ln x \cdot \frac{x^3}{3} - \frac{1}{3} \int x^2 dx \quad \text{LIAT}$$

$$\left(\ln x \cdot \frac{x^3}{3} - \frac{1}{9} \frac{x^3}{3} + C \right) \cdot \sin e^{x^2}$$

$$\int x^2 e^x dx \quad \text{b) } \int_a^b g df$$

$$\begin{array}{l|l} f = x^2 & df = 2x dx \\ dg = e^x dx & g = e^x \end{array}$$

$$x^2 e^x - 2 \int x e^x dx$$

$$(fg)' \quad \uparrow$$

$$e^{x^2} = e^x (x^2)'$$

$$f(g(x))' = f'(x) \cdot g'$$

$$\int_1^2 2x e^{x^2} dx$$

$u = x^2 \rightarrow du = 2x dx$
 $dx = \frac{du}{2x}$

$$\int_1^2 2x e^u \frac{du}{2x} = \int_1^4 e^u du$$

$$e^4 - e^1$$

$$(e^{x^2})' = e^{x^2} \cdot 2x$$