MSE 160 Lecture Notes

Hei Shing Cheung Molecules and Materials, Winter 2024

MSE 160

"In this class we are mostly understanding solids"
- Prof. Scott Ramsay

1 Mechanical Behavior

Classes of Materials In this class, we look at three classes of materials (non-exhaustive):

- Metal held together with metallic bonds, typically ductile and conductive.
- Ceramics (often metal oxides [excp: diamond]) held together via covalent & ionic bonds, typically brittle and insulating.
- Polymers Molecules (often hydrocarbons) typically ductile and insulating

Engineering Stress For normal stress, we know that:

$$\sigma = \frac{F}{A_0} \tag{1}$$

Engineering Strein Also:

$$\epsilon = \frac{\Delta l}{l_0} \tag{2}$$

Young's Moduclus For elastic deformation, E, is given, by Hooke's Law, as follows:

$$\sigma = E\epsilon \tag{3}$$

Tensile Test We apply force as to the ends of a dogbone-sample, with l_0 being the gauge length and A_0 being the area of the cross-section at the middle.

Tensile Strein Maximum tensile strain on the engineeging stress-strain curve.

1.1 Understanding Elastic Properties in terms of Atomic Configuration

Atomic Configuration We can understand the elastic properties of a material by looking at the atomic configuration. Skemetically, we can represent the atomic configuration as a spring system:

- 1. **Intial Before Loading** Atoms are in equilibrium, with the interatomic forces being balanced.
- 2. **Loading** We apply a force to the material, causing the atoms to move from their equilibrium positions. The bond stretches and the atoms move further apart.
- 3. Unloading We remove the force, causing the atoms to return to their equilibrium positions.

Atom Positions Elastic modulus is dependent on the atomic interatomic bonding force. Thus, The elastic modulus is prootionally to the slope of the interatomic force-seperation curve.

Force-Seperation Curve The force-seperation curve is a plot of the force between two atoms as a function of the distance between them. The slope of the curve is proportional to the elastic modulus near the equilibrium position.

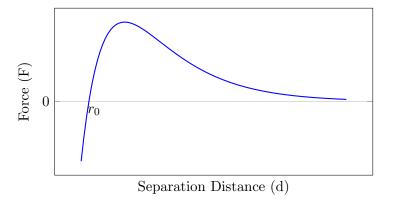


Figure 1: Force-Separation Curve (Lennard-Jones Force)

$$E \propto \left. \frac{dF}{dr} \right|_{r_0}$$
 (4)

Definiton 1.1.1 (Equilibrium interatomic seperation distance). The equilibrium interatomic seperation distance, r_0 , is the distance between two atoms at which the interatomic force is zero. This is due to the interatomic forces being the sum of attractive and repulsive forces.

Elastic Modulus Thus, strongly bonded materials have a higher elastic modulus and the slope of the force-separation curve is steeper at r_0 .

1.2 Understanding Other Properties in terms of Atomic Configuration

Potential Energy-Separation Curve The potential energy-separation curve is a plot of the potential energy between two atoms as a function of the distance between them. The potential energy is the area under the force-separation curve.

Depth of the Minimum Energy Well The depth of the minimum energy well, E_0 , is the energy required to break the bond between two atoms. This is the energy required to move the atoms from the equilibrium position to infinity. It is proportional to the melting temperature of the material.

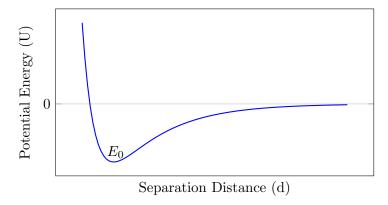


Figure 2: Potential Energy-Separation Curve

Coefficient of Thermal Expansion The coefficient of thermal expansion, α , is the fractional change in length per degree change in temperature.

Depth of Potential Energy Curve The deeper the potential energy curve, the higher the melting temperature and more symetric the curve near E_0 . This would give the following three properties:

- 1. **Higher Melting Temperature** The higher the melting temperature, the deeper the potential energy curve.
- 2. **Higher Elastic Modulus** The steeper the slope of the force-seperation curve at r_0 , the higher the elastic modulus.
- 3. Lower Coefficient of Thermal Expansion The more symetric the potential energy curve near E_0 , the lower the coefficient of thermal expansion.

1.3 Shear and Tensile Stress

1.3.1 Shear

Shear Stress Shear stress is the force per unit area acting parallel to the surface. It is given by:

$$\tau = \frac{F}{A_0} \tag{5}$$

Shear Strain Shear strain is the change in angle between two lines originally perpendicular to each other. It is given by:

$$\gamma = \frac{\Delta l}{l_0} \approx \tan \theta \approx \theta = \frac{\pi}{2} - \phi \tag{6}$$

Shear Modulus The shear modulus, G, is the ratio of shear stress to shear strain. It is given by:

$$\tau = G\gamma \tag{7}$$

Relationship between Shear and Tensile Modulus The shear modulus is related to the tensile modulus by the following equation:

$$G = \frac{E}{2(1+\nu)} \tag{8}$$

where ν is the Poisson's ratio.

Poisson's Ratio Poisson's ratio, ν , is the ratio of lateral strain to axial strain. It is given by:

$$\nu = -\frac{\epsilon_{\text{lat}}}{\epsilon_{\text{axial}}} \tag{9}$$

1 atm = 101.325 kPa = 1.01325 bar = 14.696 psi $6.022 \times 10^{23} \, \mathrm{mol}^{-1}$

 $1.602 \times 10^{-19} \,\mathrm{C}$

 $1.602 \times 10^{-19} \,\mathrm{J}$ 1 eV

 $8.854 \times 10^{-12} \,\mathrm{F}\,\mathrm{m}^{-1}$ $8.314\,\mathrm{J}\,\mathrm{mol}^{-1}\,\mathrm{K}^{-1}$

 $0.082\,067\,\mathrm{L\,atm\,mol^{-1}\,K^{-1}}$

 $273.15\,\mathrm{K}$ $0^{\circ}C$

 $8.62\times 10^{-5}\,{\rm eV\,atom^{-1}\,K^{-1}}$ $1.38 \times 10^{-23} \, \mathrm{J} \, \mathrm{atom}^{-1} \, \mathrm{K}^{-1}$

 $96486 \,\mathrm{C}\,\mathrm{mol}^{-1}$

 $4.136 \times 10^{-15} \, \mathrm{eV} \, \mathrm{s}$ $6.626 \times 10^{-34} \,\mathrm{J\,s}$

 $2.99\times 10^8\,{\rm m\,s^{-1}}$

 $9.81\,\mathrm{m\,s^{-2}}$

Microstructure

 $LPF = \frac{\text{length of atoms}}{\text{length of vector}}$ $PPF = \frac{\text{area of atoms}}{\text{area of plane}}$ $A = \pi r^2$ $n\lambda = 2d_{\rm hkl}\sin\theta$ $N_V = N \exp(-1)$ $\rho = \frac{nA}{V_C N_A}$ $APF = \frac{V_S}{V_C}$ $a = \frac{4}{\sqrt{3}}R$ $n_w = \overline{\frac{M_w}{\overline{m}}}$ $d_{\rm hkl} = \frac{1}{\sqrt{h^2 + k^2 + l^2}}$ $\rho = \frac{n_A A_A + \bar{n}_C A_C}{V_C N_A}$ $A_{\text{triangle}} = \frac{1}{2}bh$ $LD = \frac{\#}{\text{Length}}$ $PD = \frac{\#}{\text{Area}}$ $V = \frac{4}{3}\pi r^3$ $a = 2\sqrt{2}R$ $N = \frac{N_A \rho}{M_A \rho}$ $n_n = \frac{\overline{N_n}}{\overline{m}}$

Mechanical Behaviour

$\epsilon = rac{\Delta l}{l_0}$	$\sigma_{3 ext{-point}} = rac{3FL}{2wh^2}$	$\epsilon_T = \ln(1 + \epsilon)$		$\nu = -\frac{\epsilon_x}{\epsilon_z} = -\frac{\epsilon_y}{\epsilon_z}$
$\sigma=rac{F}{A_0}$	$\sigma = E\epsilon$	$\sigma_T = \sigma(1+\epsilon)$	$\sigma_T = rac{F}{A_i}$	$E = 2G(1 + \nu)$

Magnetic Behaviour

$B_0=\mu_0 H$	$B=\mu_0 H + \mu_0 M$	$\mu_B = rac{e\hbar}{2m_e} = eta$	
$H = rac{NI}{L}$	$M = \chi_m H$	$\chi_m)\mu_0$	$\beta = 9.27 \times 10^{-24} Am^2$

Electrical Behaviour

 $\sigma = n|e|\mu_e$ $\sigma = n|e|\mu_e + p|e|\mu_h$ $\sigma = p|e|\mu_h$

Electrochemistry

 $E_{\rm at\ 25\,\circ C} = E^{\circ} - \frac{0.0592}{n} \ln Q$ $E = E^{\circ} - \frac{RT}{nF} \ln Q$ $w = nFE^{\circ}$

Thermodynamics

 $H \equiv U + PV$ $\Delta U = q + w$ $q=nC_P\Delta T$ $\Delta S = \frac{q_{\rm rev}}{T}$ constant T: $\Delta G = \Delta H - T\Delta S$ $\Delta U = q - P_{\rm ext} \Delta V$ $G \equiv H - TS$ $q = mc\Delta T$ PV = nRT

For $aA + bB \to cC + dD$, $Q = \frac{a_C^c a_D^d}{a_A^d a_B^D}$

 $\Delta_{\rm r}G = \Delta G^\circ + RT \ln Q$

 $\Delta_{\rm r} H^{\circ} = (\Sigma v_i \Delta_{f,i} H^{\circ})_{\rm prod.} - (\Sigma v_i \Delta_{f,i} H^{\circ})_{\rm react.}$

 $\Delta_{\rm r} S^{\circ} = (\Sigma v_i \Delta_{f,i} S^{\circ})_{\rm prod.} - (\Sigma v_i \Delta_{f,i} S^{\circ})_{\rm react.}$ $W_{\rm phase} = \frac{\text{length of opp. side of lever}}{\text{total leneth of lever}}$ total length of lever

Specific heats and heat capacities

Substance	$c \left(\frac{J}{g \cdot K} \right)$	$C_P \left(\frac{J}{mol \cdot K} \right)$
$\operatorname{Air}(g)$	1.0	ı
$CO_2(g)$	0.843	37.1
$H_2(g)$	14.304	28.836
$H_2O(g)$	2.03	36.4
$H_2O(l)$	4.184	75.3
$H_2O(s)$	2.09	37.7
NaCl	0.853	50.5
$O_2(g)$	0.918	29.378

Temperatures and enthalpies of phase changes

Substance	M.P.	$\Delta_{fus}H$	B.P.	$\Delta_{vap}H$
	$(_{\circ}C)$	$\frac{kJ}{mol}$	$(_{\circ}C)$	$\frac{kJ}{mol}$
Al	658	10.6	2467	284
Ca	851	9.33	1487	162
CH_4	-182	0.92	-164	8.18
H_2O	0	6.01	100	40.7
Fe	1530	14.9	2735	354

Standard formation enthalpy, standard entropy and standard formation Gibbs energy at $298.15\,\mathrm{K}$

$\Delta_f G^{\circ} \\ (\frac{kJ}{mol})$	0 -50.75	-23.49	1 1	-1162	-394.4	1 1	ı	0	1 1	-228.6	. 0
$S^{\circ} \left(\frac{J}{mol \cdot K} \right)$	5.74	200.93 269.9	70.3	68.87 92.6	83.0	93.1	33.2	27.3	87.4 130.68	188.7	$69 \\ 205.0$
$\frac{\Delta_f H^{\circ}}{(\frac{kJ}{mol})}$	0 -74.81	-83.9 -103.8	-59.8 -635	-1225	-987.0 -393.5	-168.6 -154.79	ı	0	-824.2	-241.8	-285.8 0
Species	$C \\ CH_4(g)$	$egin{aligned} C_2H_2(g) \ C_3H_8(g) \end{aligned}$	$CaC_2(s)$ CaO(s)	$CaF_2(s) \ CaF_2(l)$	$Ca(OH)_2(s)$ $CO_2(q)$	$Cu_2O(s) \ Cu_2O(l)$	Cu(s)	Fe(s)	$Fe_2O_3(s) \ H_2(g)$	$H_2O(g)$	$H_2O(l) \ O_2(g)$

Miscellaneous enthalpies

$\Delta H(rac{kJ}{mol})$	157	-328	1734		3.9
Reaction	$F_2 \to F(g)$	$F(g) \to F^-(g)$	$Ca(g) \to Ca^{2+}(g)$	$NaCl(s) \rightarrow$	$Na^+(aq) + Cl^-(aq)$
Substance	F_2	ĹΉ	Ca	NaCl	

Scott Ramsay, December 2024

IUPAC Periodic Table of the Elements

18 2 P Helium Helium 4.0026	10 10 10 10 10 10 10 10 10 10 10 10 10 1	18 argon 39.95 ±0.16	36 Kr krypton 83.798 ±0.002	54 Xenon xenon 131.29 ± 0.01	86 radon	118 Og oganesson [294]
7	9 fluorine 18.998 ± 0.001	17 Chlorine 35.45 ± 0.01	35 Br bromine 79.904 ± 0.003	53 lodine 126.90 ± 0.01	At At astatine	TS TS tennessine [294]
4	8 0xygen 15.999 ± 0.001	16 Sulfur 32.06 ± 0.02	34 Se selenium 78.971 ± 0.008	52 Te tellurium 127.60 ± 0.03	84 Po polonium [209]	116 LV Iivermorium [293]
<u>ر</u> بر	7 nitrogen 14.007	15 phosphorus 30.974 ± 0.001	33 AS arsenic 74.922 ± 0.001	\$50 antimony 121.76 ± 0.01	83 Dismuth 208.98 ± 0.01	Mc moscovium [290]
-	6 Carbon 12.011	28.085 ± 0.001	32 Ge germanium 72.630 ± 0.008	50 Sn tin 118.71 ± 0.01	82 Pb lead 207.2 ± 1.1	114 FI flerovium [290]
ç	5 Doron boron ± 0.02	13 AI aluminium 26.982 ± 0.001	31 Ga gallium 69.723 ± 0.001	49	### ##################################	Nh nihonium [286]
		25	30 Zn zinc 65.38 ± 0.02	48 Cadmium 112.41 ± 0.01	## 80 mercury 200.59 # 0.01	112 Cn copernicium [285]
		E	29 Cu copper 63.546 ± 0.003	47 Silver 107.87	79 Au gold 196.97 ± 0.01	Rg roentgenium
		10	28 Ni nickel 58.693	46 Pd palladium 106.42 ± 0.01	78 platinum 195.08 ± 0.02	DS darmstadfium
		0	27 Co cobalt 58.933 ± 0.001	45 Rh rhodium 102.91 ± 0.01	77 	109 Mt meitnerium
		∞	26 Fe iron 55.845 ± 0.002	Ru ruthenium 101.07 ± 0.02	76 Osmium 190.23 ± 0.03	108 HS hassium [269]
		~	25 Wn manganese 54.938 ± 0.001	Tc Tc technetium	75 Re rhenium 186.21 ± 0.01	107 Bh bohrium [270]
		9	24 Cr chromium 51.996 ± 0.001	42 Mo molybdenum 95.95 ± 0.01	74 tungsten 183.84 ± 0.01	Sg seaborgium
	oer I	ω	23 V vanadium 50.942 ± 0.001	Nb niobium 92.906 ± 0.001	73 Ta tantalum 180.95 ± 0.01	105 Db dubnium [268]
	atomic number Symbol name abridged standard atomic weight	4	22 Ti titanium 47.867 ± 0.001	40 Zr zirconium 91.224 ± 0.002	72 Hf hafnium 178.49 ± 0.01	104 Rf rutherfordium
		ო	21 Scandium 44.956 ± 0.001	39 Yttrium 88.906 ± 0.001	57-71 lanthanoids	89-103 actinoids
c	4 Be beryllium 9.0122 ± 0.0001	12 Mg magnesium 24.305 ± 0.002	20 Ca calcium 40.078 ± 0.004	38 Sr strontium 87.62 ± 0.01	56 Ba barium 137.33 ± 0.01	88 Ra radium [226]
1 T hydrogen 1,0080	3 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	22.990 ± 0.001	19 K potassium 39.098 ± 0.001	37 Rb rubidium 85.468 ± 0.001	55 CS caesium 132.91 ± 0.01	87 Fr francium [223]



103 Lr lawrencium [262]
102 No nobelium [259]
Md mendelevium [258]
100 Fm fermium [257]
99 ES einsteinium [252]
98 Cf californium [251]
97 BK berkelium [247]
96 Cm curium
95 Am ameridum [243]
94 Pu plutonium [244]
Np neptunium
92 uranium 238.03 ± 0.01
91 Pa protactinium 231.04 ± 0.01
90 Th thorium 232.04 ± 0.01
89 Ac actinium

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