

MSE 160 Lecture Notes

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MSE 160

The up-to-date version of this document can be found at <https://github.com/HaysonC/skulenotes>

"In this class we are mostly understanding solids"
- Prof. SCOTT RAMSAY

1 Mechanical Behavior

Classes of Materials In this class, we look at three classes of materials (non-exhaustive):

- **Metal** held together with metallic bonds, typically **ductile** and **conductive**.
- **Ceramics** (often metal oxides [excp: diamond]) held together via covalent & ionic bonds, typically **brittle** and **insulating**.
- **Polymers Molecules** (often hydrocarbons) typically **ductile** and **insulating**

Engineering Stress For normal stress, we know that:

$$\sigma = \frac{F}{A_0} \quad (1)$$

Engineering Strein Also:

$$\epsilon = \frac{\Delta l}{l_0} \quad (2)$$

Young's Moduclus For elastic deformation, E , is given, by Hooke's Law, as follows:

$$\sigma = E\epsilon \quad (3)$$

Tensile Test We apply force as to the ends of a dogbone-sample, with l_0 being the gauge length and A_0 being the area of the cross-section at the middle.

Tensile Strein Maximum tensile strain on the engineeing stress-strain curve.

1.1 Understanding Elastic Properties in terms of Atomic Configuration

Atomic Configuration We can understand the elastic properties of a material by looking at the atomic configuration. Schematically, we can represent the atomic configuration as a spring system:

1. **Initial - Before Loading** Atoms are in equilibrium, with the interatomic forces being balanced.
2. **Loading** We apply a force to the material, causing the atoms to move from their equilibrium positions. The bond stretches and the atoms move further apart.
3. **Unloading** We remove the force, causing the atoms to return to their equilibrium positions.

Atom Positions Elastic modulus is dependent on the atomic interatomic bonding force. Thus, The elastic modulus is proportional to the slope of the interatomic force-separation curve.

Force-Separation Curve The force-separation curve is a plot of the force between two atoms as a function of the distance between them. The slope of the curve is proportional to the elastic modulus near the equilibrium position.

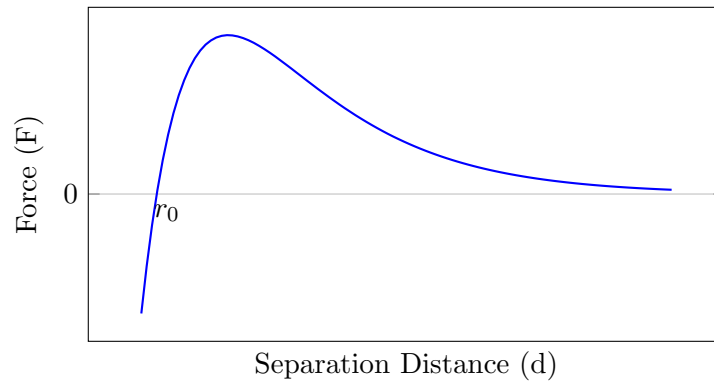


Figure 1: Force-Separation Curve (Lennard-Jones Force)

$$E \propto \left. \frac{dF}{dr} \right|_{r_0} \quad (4)$$

Definition 1.1.1 (Equilibrium interatomic separation distance). The equilibrium interatomic separation distance, r_0 , is the distance between two atoms at which the interatomic force is zero. This is due to the interatomic forces being the sum of attractive and repulsive forces.

Elastic Modulus Thus, strongly bonded materials have a higher elastic modulus and the slope of the force-separation curve is steeper at r_0 .

1.2 Understanding Other Properties in terms of Atomic Configuration

Potential Energy-Separation Curve The potential energy-separation curve is a plot of the potential energy between two atoms as a function of the distance between them. The potential energy is the area under the force-separation curve.

Depth of the Minimum Energy Well The depth of the minimum energy well, E_0 , is the energy required to break the bond between two atoms. This is the energy required to move the atoms from the equilibrium position to infinity. It is proportional to the melting temperature of the material.

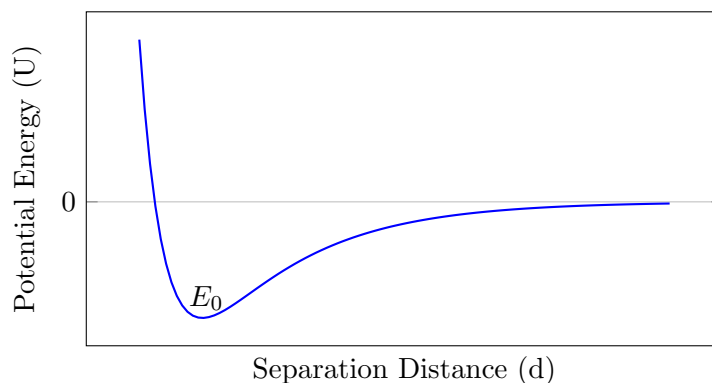


Figure 2: Potential Energy-Separation Curve

Coefficient of Thermal Expansion The coefficient of thermal expansion, α , is the fractional change in length per degree change in temperature.

Depth of Potential Energy Curve The deeper the potential energy curve, the higher the melting temperature and more symmetric the curve near E_0 . This would give the following three properties:

1. **Higher Melting Temperature** The higher the melting temperature, the deeper the potential energy curve.
2. **Higher Elastic Modulus** The steeper the slope of the force-separation curve at r_0 , the higher the elastic modulus.
3. **Lower Coefficient of Thermal Expansion** The more symmetric the potential energy curve near E_0 , the lower the coefficient of thermal expansion.

1.3 Shear and Tensile Stress

1.3.1 Shear

Shear Stress Shear stress is the force per unit area acting parallel to the surface. It is given by:

$$\tau = \frac{F}{A_0} \quad (5)$$

Shear Strain Shear strain is the change in angle between two lines originally perpendicular to each other. It is given by:

$$\gamma = \frac{\Delta l}{l_0} \approx \tan \theta \approx \theta = \frac{\pi}{2} - \phi \quad (6)$$

Shear Modulus The shear modulus, G , is the ratio of shear stress to shear strain. It is given by:

$$\tau = G\gamma \quad (7)$$

Relationship between Shear and Tensile Modulus The shear modulus is related to the tensile modulus by the following equation:

$$G = \frac{E}{2(1 + \nu)} \quad (8)$$

where ν is the Poisson's ratio.

Poisson's Ratio Poisson's ratio, ν , is the ratio of lateral strain to axial strain. It is given by:

$$\nu = -\frac{\epsilon_{\text{lat}}}{\epsilon_{\text{axial}}} \quad (9)$$

1.4 Testing

Definiton 1.4.1 (Gauge Length). The gauge length, l_0 , is the length of the sample over which the strain is measured.

Definiton 1.4.2 (Reduced Section). The reduced section is the part of the sample where the cross-sectional area is reduced to a smaller value.

Gauge length is always no longer than the reduced section. The reduced section is where the sample will likely break.

Testing Ceramics In relation to tensile testing, ceramics have the following properties:

- **Brittle** Ceramics are brittle and will break suddenly.
- **High Strength** Ceramics have high strength and thus difficult to machine the sample.
- **Sample Alignment** The sample must be aligned properly to test for pure tension. Unlike metals and polymers, which are self-aligning.
- **Fracture** Ceramics will fracture while still off-axis. Hence, there would be a large shear component.

Thus, we often approximate tensile behaviour with a point loading on a horizontal beam, with two point support (3 point bending test). Peak stress is given by:

$$\sigma_{\text{peak}} = \frac{3FL}{2bd^2} \quad (10)$$

, where:

- L (span) is the distance between the two supports.
- b is the width of the sample
- d is the thickness/depth of the sample

2 Selection of Materials

2.1 Material Performance

Example 2.1.1 (Aircraft Wing Spar). The aircraft wing spar is beam (loaded in bending) that supports the wing. The spar is made of a material with the objective of minimize mass under the following constraints:

- **Deflection** There is a maximum allowable deflection of the wing.
- There is more..., but for this example, we will only consider the deflection.

The material selection solve for a **light stiff beam**.

Mass The mass of the beam is given by:

$$m = \rho V = \rho AL$$

2.2 Density

Deflection The deflection of the beam is given by:

$$\delta = \frac{FL^3}{48EI} \quad (11)$$

For a beam with a rectangular cross-section, we have:

$$\delta = \frac{FL^3}{48E} \cdot \frac{12}{bh^3} = \frac{FL^3}{4Ebh^3}$$

We can set b proportional to h :

$$\delta = \frac{FL^3}{cE} \cdot \frac{1}{A^2}, \quad \text{for some constant } c$$

We can then isolate for A , the free variable, and minimize the mass via the objective equation $m = \rho AL$:

$$A = \sqrt{\frac{FL^3}{cE\delta}}$$
$$m = \rho L \sqrt{\frac{FL^3}{cE\delta}} = \rho L \sqrt{\frac{FL^3}{cE\delta}}$$

Arrange into the form (functional)(geometric)(material):

$$m = \left(\frac{F}{c\delta}\right)^{\frac{1}{2}} \cdot \left(L^{\frac{5}{2}}\right) \cdot \left(\frac{\rho}{E^{\frac{1}{2}}}\right)$$

Material Performance Index The material performance index is given by:

$$\text{Material Performance Index (MSI)} = \frac{E^{\frac{1}{2}}}{\rho} \quad (12)$$

MPI Graph We plot $\log E$ against $\log \rho$ to get the MPI graph.

Tempered Glass Tempered glass are made to resist tension. It is done by applying a compressive stress to the surface of the glass. This is done by cooling the surface of the glass faster than the core or chemically treating the surface.

2.2 Density

Density The density of a material is given by:

$$\rho = \frac{m}{V} \quad (13)$$

Archimedes' Principle The buoyant force on an object is equal to the weight of the fluid displaced by the object. Derive from that, we have:

$$\rho = \frac{m}{V} = \frac{m_{\text{object}}}{m_{\text{object}} - m_{\text{object in fluid}}} \quad (14)$$

3 Atomic Structures

3.1 General Definitions

Ordered structures We have the following three orders:

1. **Long Range Order (LRO)** Atoms are arranged in a well-defined pattern over long distances in repeating units.
(Example) Diamonds, some polymers, most metals, many ceramics, graphite, quartz, etc.
2. **Short Range Order (SRO)** Periodic arrangement of atoms over a few atomic or molecular spacings.
(Example) Most polymers, glasses, amorphous materials, etc.
3. **No Order (NO)** Atoms are randomly arranged.
(Example) Ideal gases, etc.

Describing Crystal Structures We can describe crystal structures by the following:

- **Unit Cell** The smallest repeating unit of a crystal structure that could be used to represent the entire crystal.
- **Lattice** The repeating arrangement of points that represent the positions of atoms in the unit cell.
(Example) Simple Cubic, Body-Centered Cubic, Face-Centered Cubic, etc.
- **Lattice Plus Basis** *Not required for this course*

Theoretical Density of Metals The theoretical density of metals is given by:

$$\rho = \frac{nM}{V_c N_A} \quad (15)$$

, where:

- n is the number of atoms in the unit cell.
- M is the atomic mass of the element (amu = g/mol).
- V_c is the volume of the unit cell.
- N_A is Avogadro's number ($6.022 \times 10^{23} \text{mol}^{-1}$)

3.2 Describing Basic Unit Cells

Definiton 3.2.1 (Coordination Number (CN)). The coordination number is the number of nearest neighbors an atom has in a crystal structure.

Definiton 3.2.2 (Atomic Packing Factor (APF)). The atomic packing factor is the fraction of the volume of the unit cell that is occupied by hard spheres. It is given by:

$$\text{APF} = \frac{\text{Volume of atoms in unit cell}}{\text{Volume of unit cell}} \quad (16)$$

Simple Cubic (SC) The simple cubic structure has the following properties:

- **Centers of atoms** Located at the eight corners of a cube
- **Rare Packing Density** Due to low packing density (only known example: Polonium, Po)
- **Close-packed directions** As cube edges.
- **Coordination Number** Number of nearest neighbor: 6

Face-Centered Cubic (FCC) The face-centered cubic structure has an atom on the centre of each face of the cube. It has the following properties:

- **Ductile and Malleable** due to the close-packed planes. Common examples include: Al, Cu, Au, Ag.
- **Coordination Number** Number of nearest neighbor: 12
- **Close-packed directions** As cube diagonals.
- **Theoretical Density** The theoretical density of FCC is derived from Equation (15):

$$\rho = \frac{nM}{V_c N_A}$$

With $n = 4$ (8 corners $\times \frac{1}{8}$ atom each + 6 faces $\times \frac{1}{2}$ atom each) and $V_c = a^3$ (where a is the **lattice parameter**):

$$\rho_{\text{FCC}} = \frac{4M}{a^3 N_A}$$

We can then obtain a via the relationship between the atomic radius, r , and the lattice parameter via the geometry on the close-packed direction (face diagonal):

$$a = 2\sqrt{2}r$$

Substitute a back into the equation:

$$\begin{aligned} \rho_{\text{FCC}} &= \frac{4M}{(2\sqrt{2}r)^3 N_A} = \frac{4M}{16\sqrt{2}r^3 N_A} \\ &= \frac{M}{4\sqrt{2}r^3 N_A} \end{aligned} \quad (17)$$

- **Atomic Packing Factor** The atomic packing factor of FCC is given by:

$$\text{APF}_{\text{FCC}} = \frac{\text{Volume of atoms in unit cell}}{\text{Volume of unit cell}} = \frac{4 \times \frac{4}{3}\pi r^3}{a^3} = \frac{4 \times \frac{4}{3}\pi r^3}{(2\sqrt{2}r)^3} = \frac{\pi}{6\sqrt{2}} = \mathbf{0.74} \quad (18)$$

This is the highest possible packing factor for spheres. Thus, no other structure can have a higher packing factor.

- **Stacking** The FCC structure can be thought of as stacking close-packed planes. The stacking sequence is ABCABC... (where A, B, and C describe the orientation hexagonal close-packed planes).

Hexagonal Close-Packed (HCP) The hexagonal close-packed structure is **crystal structure** by stacking close-packed hexagonal planes. It has the following properties:

- **Coordination Number** Number of nearest neighbor: 12
- **Close-packed directions** As cube diagonals.
- **Theoretical Density** The theoretical density of HCP is derived from Equation (15):

$$\rho = \frac{nM}{V_c N_A}$$

With $n = 6$ (12 corners $\times \frac{1}{6}$ atom each) and $V_c = a^3$:

$$\rho_{\text{HCP}} = \frac{6M}{a^3 N_A} \quad (19)$$

- **Atomic Packing Factor** The atomic packing factor of HCP is given by:

$$\text{APF}_{\text{HCP}} = \frac{\text{Volume of atoms in unit cell}}{\text{Volume of unit cell}} = \frac{6 \times \frac{4}{3}\pi r^3}{a^3} = \frac{6 \times \frac{4}{3}\pi r^3}{a^3} = \mathbf{0.74} \quad (20)$$

- **Stacking** The HCP structure can be thought of as stacking close-packed planes. The stacking sequence is ABAB...

Example 3.2.3 (Density of Aluminum). Given that the atomic radius of aluminum is $r = 143$ pm and the atomic mass is $M = 26.98$ g/mol, we can calculate the density of aluminum with FCC structure. We have:

$$\begin{aligned} \rho_{\text{Al}} &= \frac{M}{4\sqrt{2}r^3 N_A} = \frac{26.98}{4\sqrt{2} \times (143 \times 10^{-12})^3 \times 6.022 \times 10^{23}} \\ &= \frac{26.98}{4\sqrt{2} \times (143 \times 10^{-12})^3 \times 6.022 \times 10^{23}} = 2.7 \text{ g/cm}^3 \end{aligned}$$

Body-Centered Cubic (BCC) The body-centered cubic structure has an atom at the centre of the cube. It has the following properties:

1. **Coordination Number** Number of nearest neighbor: 8
2. **Atomic Packing Factor** The atomic packing factor of BCC is given by:

$$\text{APF}_{\text{BCC}} = \frac{\text{Volume of atoms in unit cell}}{\text{Volume of unit cell}} = \frac{2 \times \frac{4}{3}\pi r^3}{a^3} = \frac{2 \times \frac{4}{3}\pi r^3}{(4r/\sqrt{3})^3} = \mathbf{0.68} \quad (21)$$

3. **Close Packed Directions** As cube diagonals.
4. **Theoretical Density** The theoretical density of BCC is derived from Equation (15):

$$\rho = \frac{nM}{V_c N_A}$$

With $n = 2$ (8 corners $\times \frac{1}{8}$ atom each + 1 center atom) and $V_c = a^3$:

$$\rho_{\text{BCC}} = \frac{2M}{a^3 N_A} \quad (22)$$

5. **Stacking** The BCC structure can be thought of as stacking close-packed planes. The stacking sequence is ABAB...

4 Geometric Properties of Crystals

4.1 Crystallographic Directions and Planes

Point Coordinates A lattice position in a unit cell is determined as fractional multiples of the unit cell edge lengths a , b , and c . (Defining the origin at one corner of the unit cell and $a = b = c = 1$)

Crystallographic Directions A crystallographic direction is a line between two points in a crystal. It is denoted by square brackets, $[uvw]$. The direction is determined from the “tail” to the “head” of the vector. Also:

1. It **shall not** include commas; and
2. It **shall be reduced** to the smallest integers; and
3. Negative signs are represented by a bar over the number.

Example 4.1.1. The crystallographic direction from $(0, 0, 0)$ to $(-1, 0, 1/2)$ is $[\bar{2}01]$.

4.2 X-Ray Diffraction

Family of Directions A family of directions is a set of directions that are parallel to each other. It is denoted by $\langle uvw \rangle$.

Example 4.1.2. The family of directions $\langle 100 \rangle$ is the set of directions $[100]$, $[010]$, $[001]$, $[\bar{1}00]$, $[0\bar{1}0]$, and $[00\bar{1}]$.

Angle between Directions The angle between two directions in a **cubic** crystal is given by:

$$\cos \theta = \frac{h_1 h_2 + k_1 k_2 + l_1 l_2}{\sqrt{h_1^2 + k_1^2 + l_1^2} \sqrt{h_2^2 + k_2^2 + l_2^2}} \quad (23)$$

, which is simply the normalized dot product of the two vectors.

Crystallographic Planes A crystallographic plane is a set of parallel planes in a crystal. It is denoted by (hkl) . The plane is determined by the intercepts on the x , y , and z axes.

Generally, we find the intercepts by finding the points where the plane intersects the axes. We then take the reciprocals of the intercepts and multiply by the smallest integer to get the Miller Indices.

Family of Planes A family of planes is a set of planes that are parallel to each other. It is denoted by $\{hkl\}$.

Distance between Planes The distance between two planes with miller indices $(h_1 k_1 l_1)$ and $(h_2 k_2 l_2)$ is given by:

$$d = \frac{a}{\sqrt{h^2 + k^2 + l^2}} \quad (24)$$

, where a is the lattice parameter.

4.2 X-Ray Diffraction

The diffraction pattern is used to determine the crystal structure. By measuring the n^{th} order peak angle θ_c and the wavelength of the X-ray, we can determine the distance between planes:

$$\begin{aligned} 2d \sin \theta &= n\lambda \\ d &= \frac{n\lambda}{2 \sin \theta_c} \end{aligned} \quad (25)$$

Thus, we could determine the lattice parameter a by the following equation:

$$a = \frac{n\lambda}{2 \sin \theta_c} \sqrt{h^2 + k^2 + l^2} \quad (26)$$

4.3 Geometrically Ideal Crystal Structures

Coordination Number and Ratio The coordination number increases with $\frac{r_{\text{cation}}}{r_{\text{anion}}}$ (The ionic radii ratio). It relates to coordination number as follows:

Ionic Radii Ratio	Coord. Number	Name
< 0.155	2	Linear
0.155 - 0.225	3	Trigonal Planar
0.225 - 0.414	4	Tetrahedral
0.414 - 0.732	6	Octahedral
0.732 - 1.0	8	Cubic

Table 1: Coordination Number and Ionic Radii

Definiton 4.3.1 (AX Type). The AX type is a crystal structure where the cation and anion are of the same ratio.

Example 4.3.2 (AX Type: NaCl rock salt). The NaCl structure is an AX type structure. The cation and anion are of the same ratio. Sodium (Cation) has radius $r_{\text{Na}} = 0.102$ nm and Chlorine (Anion) has radius $r_{\text{Cl}} = 0.181$ nm. The ratio is:

$$\frac{r_{\text{cation}}}{r_{\text{anion}}} = \frac{0.102}{0.181} = 0.56$$

Thus, the coordination number is 6.

Additionally, we could calculate its theoretical density. It has 4 cation and 4 anion in the unit cell. The volume of the unit cell is a^3 , and it follows a FCC structure. Thus, the density is:

$$\begin{aligned} \rho &= \frac{4M_{\text{Na}} + 4M_{\text{Cl}}}{a^3 N_A} = \frac{4(22.99) + 4(35.45)}{a^3 N_A} \\ &= \frac{4(22.99) + 4(35.45)}{(2\sqrt{2}r_{\text{Na}})^3 N_A} = \frac{4(22.99) + 4(35.45)}{(2\sqrt{2} \times 0.102)^3 N_A} \\ &= \frac{4(22.99) + 4(35.45)}{(2\sqrt{2} \times 0.102)^3 N_A} = 2.16 \text{ g/cm}^3 \end{aligned}$$

Example 4.3.3 (AX Type: ZnS, Zinc Blende). The ZnS structure is an AX type structure. It has a FCC structure with CN = 4. The radius of Zinc (Cation) is $r_{\text{Zn}} = 0.074$ nm and the radius of Sulfur (Anion) is $r_{\text{S}} = 0.184$ nm. The ratio is:

$$\frac{r_{\text{cation}}}{r_{\text{anion}}} = \frac{0.074}{0.184} = 0.40$$

Example 4.3.4 (AX₂ Type: CaF₂). The CaF₂ structure is an AX₂ type structure. It has a FCC structure with CN = 8. The radius of Calcium (Cation) is $r_{\text{Ca}} = 0.099$ nm and the radius of Fluorine (Anion) is $r_{\text{F}} = 0.133$ nm. The ratio is:

$$\frac{r_{\text{cation}}}{r_{\text{anion}}} = \frac{0.099}{0.133} = 0.74$$

Constants and conversions

1 atm = 101.325 kPa = 1.013 25 bar = 14.696 psi
 N_A 6.022 × 10²³ mol⁻¹
e 1.602 × 10⁻¹⁹ C
1 eV 1.602 × 10⁻¹⁹ J
 ϵ_0 8.854 × 10⁻¹² F m⁻¹
R 8.314 J mol⁻¹ K⁻¹
0.082 067 L atm mol⁻¹ K⁻¹
0 °C 273.15 K
k 8.62 × 10⁻⁵ eV atom⁻¹ K⁻¹
1.38 × 10⁻²³ J atom⁻¹ K⁻¹
F 96 486 C mol⁻¹
h 6.626 × 10⁻³⁴ J s
4.136 × 10⁻¹⁵ eV s
c 2.99 × 10⁸ m s⁻¹
g 9.81 m s⁻²

Microstructure

$LD = \frac{\#}{\text{Length}}$ $LPF = \frac{\text{length of atoms}}{\text{length of vector}}$
 $PD = \frac{\#}{\text{Area}}$ $PPF = \frac{\text{area of atoms}}{\text{area of plane}}$
 $V = \frac{4}{3}\pi r^3$ $A = \pi r^2$
 $A_{\text{triangle}} = \frac{1}{2}bh$ $\rho = \frac{n_A A_A + n_C A_C}{V_{CNA}}$
 $\rho = \frac{n_A}{V_C N_A} \bar{V}_s$ $APF = \frac{V_s}{V_C}$
 $N = \frac{N_A \rho}{A}$ $N_V = N \exp(-\frac{Q_V}{kT})$
 $a = 2\sqrt{2}R$ $a = \frac{4}{\sqrt{3}}R$
 $d_{\text{hkl}} = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$ $n\lambda = 2d_{\text{hkl}} \sin \theta$
 $n_n = \frac{\bar{M}_w}{\bar{m}}$ $n_w = \frac{\bar{M}_w}{\bar{m}}$

Mechanical Behaviour

$\sigma = \frac{F}{A_0}$ $\epsilon = \frac{\Delta l}{l_0}$
 $\sigma = E\epsilon$ $\sigma_{3\text{-point}} = \frac{3FL}{2wh^2}$
 $\sigma_T = \sigma(1 + \epsilon)$ $\epsilon_T = \ln(1 + \epsilon)$
 $\sigma_T = \frac{F}{A_i}$ $\sigma_T = K\epsilon_T^n$
 $E = 2G(1 + \nu)$ $\nu = -\frac{\epsilon_x}{\epsilon_z} = -\frac{\epsilon_y}{\epsilon_z}$

Magnetic Behaviour

$H = \frac{NI}{L}$ $B_0 = \mu_0 H$
 $M = \chi_m H$ $B = \mu_0 H + \mu_0 M$
 $B = (1 + \chi_m)\mu_0 H$ $\mu_B = \frac{eh}{2m_e} = \beta$
 $\beta = 9.27 \times 10^{-24} \text{ Am}^2$

Electrical Behaviour

$\sigma = n|e|\mu_e + p|e|\mu_h$ $\sigma = n|e|\mu_e$
 $\sigma = p|e|\mu_h$

Electrochemistry

$E = E^\circ - \frac{RT}{nF} \ln Q$ $I = \frac{nC}{t}$
 $E_{\text{at } 25^\circ\text{C}} = E^\circ - \frac{0.0592}{n} \ln Q$
 $w = nFE^\circ$

Thermodynamics

$PV = nRT$ $\Delta U = q + w$
 $\Delta U = q - P_{\text{ext}}\Delta V$ $H \equiv U + PV$
 $G \equiv H - TS$ $\Delta S = \frac{q_{\text{rev}}}{T}$
constant T: $\Delta G = \Delta H - T\Delta S$
 $q = mc\Delta T$ $q = nC_P\Delta T$
For $aA + bB \rightarrow cC + dD$, $Q = \frac{a_C^c a_D^d}{a_A^a a_B^b}$
 $\Delta_r G = \Delta G^\circ + RT \ln Q$
 $\Delta_r H^\circ = (\sum v_i \Delta_f H^\circ)_{\text{prod.}} - (\sum v_i \Delta_f H^\circ)_{\text{react.}}$
 $\Delta_r S^\circ = (\sum v_i \Delta_f S^\circ)_{\text{prod.}} - (\sum v_i \Delta_f S^\circ)_{\text{react.}}$
 $W_{\text{phase}} = \frac{\text{length of opp. side of lever}}{\text{total length of lever}}$
 $E = h\nu = \frac{hc}{\lambda}$
Specific heats and heat capacities

Substance	c ($\frac{J}{g\cdot K}$)	C_P ($\frac{J}{mol\cdot K}$)
Air(g)	1.0	-
CO ₂ (g)	0.843	37.1
H ₂ (g)	14.304	28.836
H ₂ O(g)	2.03	36.4
H ₂ O(l)	4.184	75.3
H ₂ O(s)	2.09	37.7
NaCl	0.853	50.5
O ₂ (g)	0.918	29.378

Temperatures and enthalpies of phase changes

Substance	M.P. (°C)	$\Delta_{fus}H$ ($\frac{kJ}{mol}$)	B.P. (°C)	$\Delta_{vap}H$ ($\frac{kJ}{mol}$)
Al	658	10.6	2467	284
Ca	851	9.33	1487	162
CH ₄	-182	0.92	-164	8.18
H ₂ O	0	6.01	100	40.7
Fe	1530	14.9	2735	354

Standard formation enthalpy, standard entropy and standard formation Gibbs energy at 298.15 K

Species	$\Delta_f H^\circ$ ($\frac{kJ}{mol}$)	S° ($\frac{J}{mol\cdot K}$)	$\Delta_f G^\circ$ ($\frac{kJ}{mol}$)
C	0	5.74	0
CH ₄ (g)	-74.81	186.2	-50.75
C ₂ H ₂ (g)	-83.9	200.93	-
C ₃ H ₈ (g)	-103.8	269.9	-23.49
CaC ₂ (s)	-59.8	70.3	-
CaO(s)	-635	38.1	-
CaF ₂ (s)	-1225	68.87	-1162
CaF ₂ (l)	-1186	92.6	-
Ca(OH) ₂ (s)	-987.0	83.0	-
CO ₂ (g)	-393.5	213.6	-394.4
Cu ₂ O(s)	-168.6	93.1	-
Cu ₂ O(l)	-154.79	-	-
Cu(s)	-	33.2	-
Fe(s)	0	27.3	0
Fe ₂ O ₃ (s)	-824.2	87.4	-
H ₂ (g)	-	130.68	-
H ₂ O(g)	-241.8	188.7	-228.6
H ₂ O(l)	-285.8	69	-
O ₂ (g)	0	205.0	0

Miscellaneous enthalpies

Substance	Reaction	ΔH ($\frac{kJ}{mol}$)
F ₂	F ₂ → F(g)	157
F	F(g) → F ⁻ (g)	-328
Ca	Ca(g) → Ca ²⁺ (g)	1734
NaCl	NaCl(s) → Na ⁺ (aq) + Cl ⁻ (aq)	3.9

IUPAC Periodic Table of the Elements

1																	18																																																																																																																																																																																																																																																																																																																																																															
1 H hydrogen 1.0080 ± 0.0002																	2 He helium 4.0026 ± 0.0001																																																																																																																																																																																																																																																																																																																																																															
3 Li lithium 6.94 ± 0.06	4 Be beryllium 9.0122 ± 0.0001															9 F fluorine 18.998 ± 0.001	10 Ne neon 20.180 ± 0.001																																																																																																																																																																																																																																																																																																																																																															
11 Na sodium 22.990 ± 0.001	12 Mg magnesium 24.305 ± 0.002															16 S sulfur 32.06 ± 0.02	17 Cl chlorine 35.45 ± 0.01	18 Ar argon 39.95 ± 0.16																																																																																																																																																																																																																																																																																																																																																														
19 K potassium 39.098 ± 0.001	20 Ca calcium 40.078 ± 0.004	21 Sc scandium 44.956 ± 0.001	22 Ti titanium 47.867 ± 0.001	23 V vanadium 50.942 ± 0.001	24 Cr chromium 51.996 ± 0.001	25 Mn manganese 54.938 ± 0.001	26 Fe iron 55.845 ± 0.002	27 Co cobalt 58.933 ± 0.001	28 Ni nickel 58.693 ± 0.001	29 Cu copper 63.546 ± 0.003	30 Zn zinc 65.38 ± 0.02	31 Ga gallium 69.723 ± 0.001	32 Ge germanium 72.630 ± 0.008	33 As arsenic 74.922 ± 0.001	34 Se selenium 78.971 ± 0.008	35 Br bromine 79.904 ± 0.003	36 Kr krypton 83.798 ± 0.002	37 Rb rubidium 85.468 ± 0.01	38 Sr strontium 87.62 ± 0.01	39 Y yttrium 88.906 ± 0.001	40 Zr zirconium 91.224 ± 0.002	41 Nb niobium 92.906 ± 0.001	42 Mo molybdenum 95.95 ± 0.01	43 Tc technetium [97]	44 Ru ruthenium 101.07 ± 0.02	45 Rh rhodium 102.91 ± 0.01	46 Pd palladium 106.42 ± 0.01	47 Ag silver 107.87 ± 0.01	48 Cd cadmium 112.41 ± 0.01	49 In indium 114.82 ± 0.01	50 Sn tin 118.71 ± 0.01	51 Sb antimony 121.76 ± 0.01	52 Te tellurium 127.60 ± 0.03	53 I iodine 126.90 ± 0.01	54 Xe xenon 131.29 ± 0.01	55 Cs caesium 132.91 ± 0.01	56 Ba barium 137.33 ± 0.01	lanthanoids		58 Ce cerium 140.12 ± 0.01	59 Pr praseodymium 140.91 ± 0.01	60 Nd neodymium 144.24 ± 0.01	61 Pm promethium [145]	62 Sm samarium 150.36 ± 0.02	63 Eu europium 151.96 ± 0.01	64 Gd gadolinium 157.25 ± 0.03	65 Tb terbium 158.93 ± 0.01	66 Dy dysprosium 162.50 ± 0.01	67 Ho holmium 164.93 ± 0.01	68 Er erbium 167.26 ± 0.01	69 Tm thulium 168.93 ± 0.01	70 Yb ytterbium 173.05 ± 0.02	71 Lu lutetium 174.967 ± 0.01	72 Hf hafnium 178.49 ± 0.01	73 Ta tantalum 180.95 ± 0.01	74 W tungsten 183.84 ± 0.01	75 Re rhenium 186.21 ± 0.01	76 Os osmium 190.23 ± 0.03	77 Ir iridium 192.22 ± 0.01	78 Pt platinum 195.08 ± 0.02	79 Au gold 196.97 ± 0.01	80 Hg mercury 200.59 ± 0.01	81 Tl thallium 204.38 ± 0.01	82 Pb lead 207.2 ± 1.1	83 Bi bismuth 208.98 ± 0.01	84 Po polonium [209]	85 At astatine [210]	86 Rn radon [222]	87 Fr francium [223]	88 Ra radium [226]	89-103 actinoids	104 Rf rutherfordium [261]	105 Db dubnium [268]	106 Sg seaborgium [269]	107 Bh bohrium [270]	108 Hs hassium [269]	109 Mt meitnerium [271]	110 Ds darmstadtium [281]	111 Rg roentgenium [282]	112 Cn copernicium [285]	113 Nh nihonium [286]	114 Fl flerovium [290]	115 Mc moscovium [290]	116 Lv livermorium [293]	117 Ts tennessine [294]	118 Og oganesson [294]	119 Uut ununtrium [295]	120 Uub ununbium [295]	121 Uuq ununquadium [295]	122 Uuh ununhexium [295]	123 Uus ununseptium [295]	124 Uuo ununoctium [295]	125 Uut ununtrium [295]	126 Uub ununbium [295]	127 Uuq ununquadium [295]	128 Uuh ununhexium [295]	129 Uus ununseptium [295]	130 Uuo ununoctium [295]	131 Uut ununtrium [295]	132 Uub ununbium [295]	133 Uuq ununquadium [295]	134 Uuh ununhexium [295]	135 Uus ununseptium [295]	136 Uuo ununoctium [295]	137 Uut ununtrium [295]	138 Uub ununbium [295]	139 Uuq ununquadium [295]	140 Uuh ununhexium [295]	141 Uus ununseptium [295]	142 Uuo ununoctium [295]	143 Uut ununtrium [295]	144 Uub ununbium [295]	145 Uuq ununquadium [295]	146 Uuh ununhexium [295]	147 Uus 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