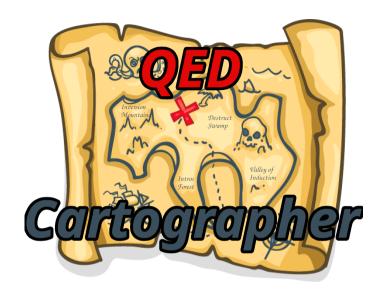
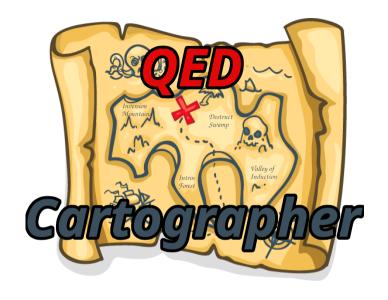


Alex Sanchez-Stern, Abhishek Varghese, Zhanna Kaufman, Dylan Zhang, Talia Ringer, Yuriy Brun



Automating Formal Verification with Reward-Free Reinforcement Learning



Automating Formal Verification with Reward-Free Reinforcement Learning







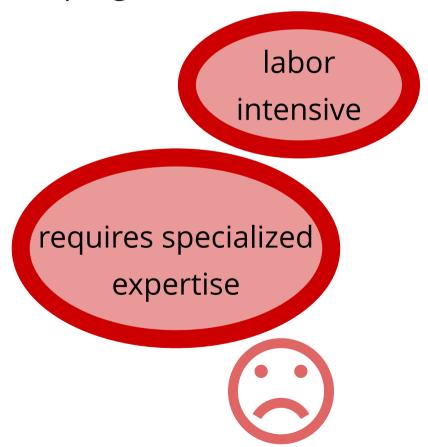








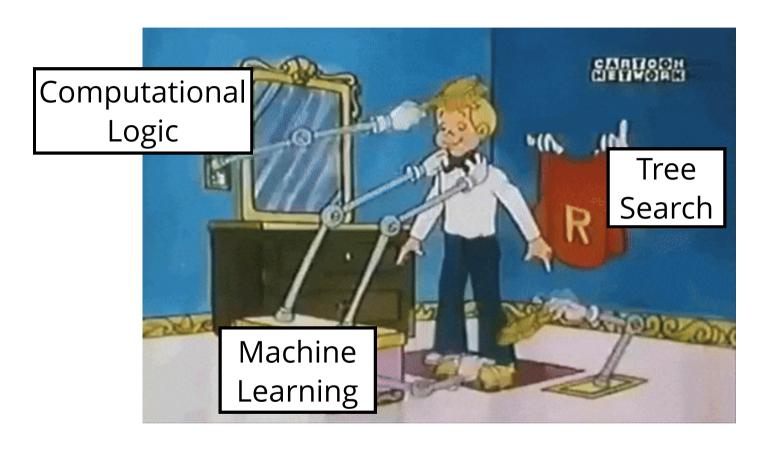


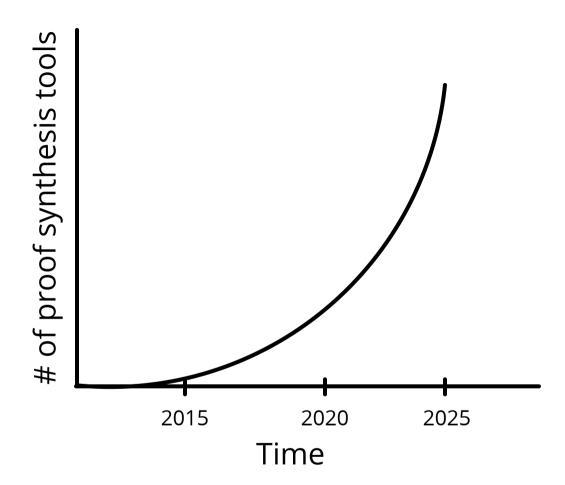


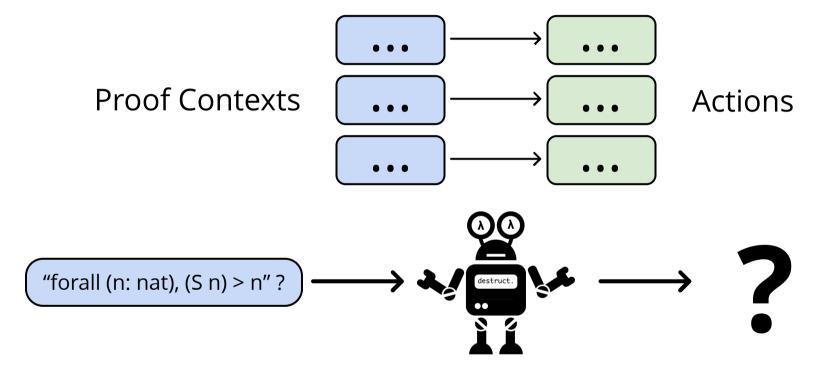


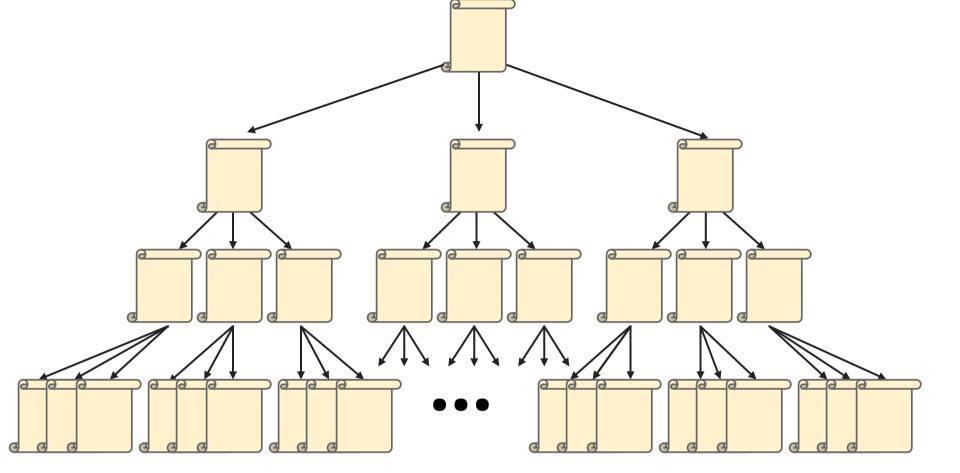


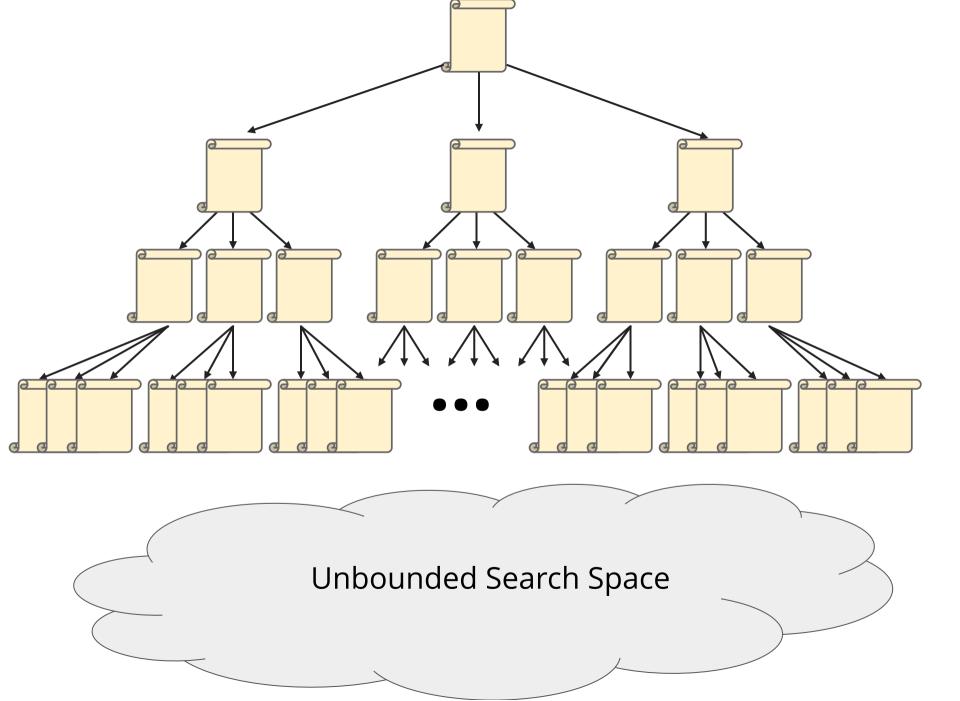












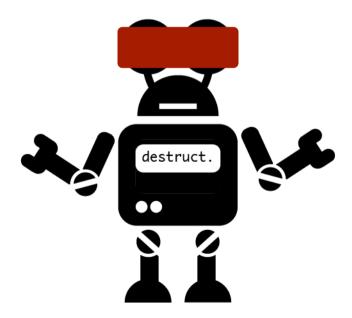
There are some techniques that can help us prune the search tree

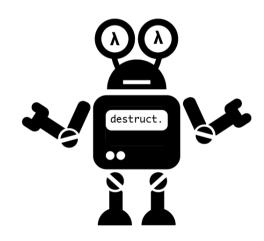


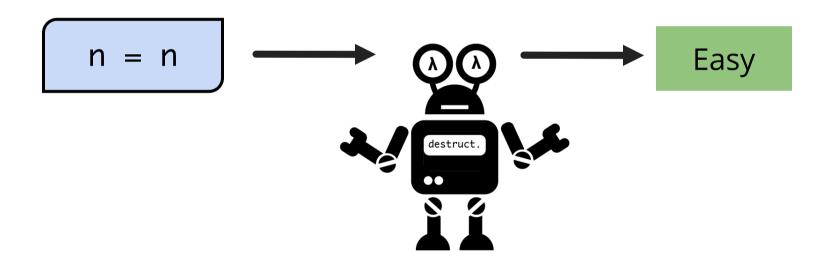
There are some techniques that can help us prune the search tree

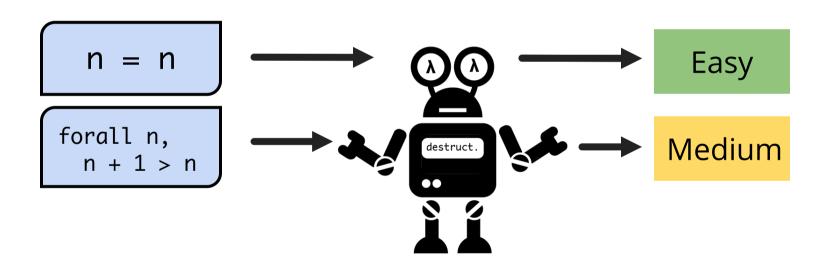


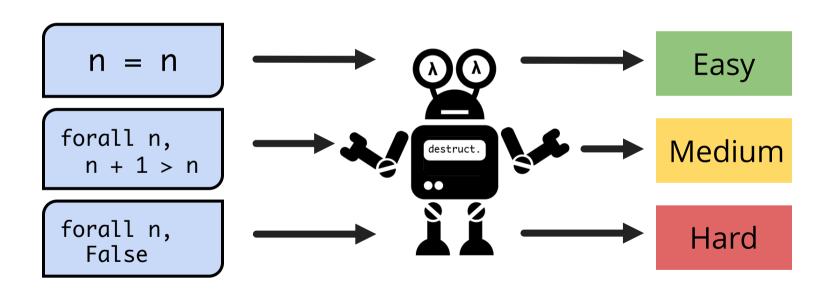
It's hard to explore when you don't know where you are!

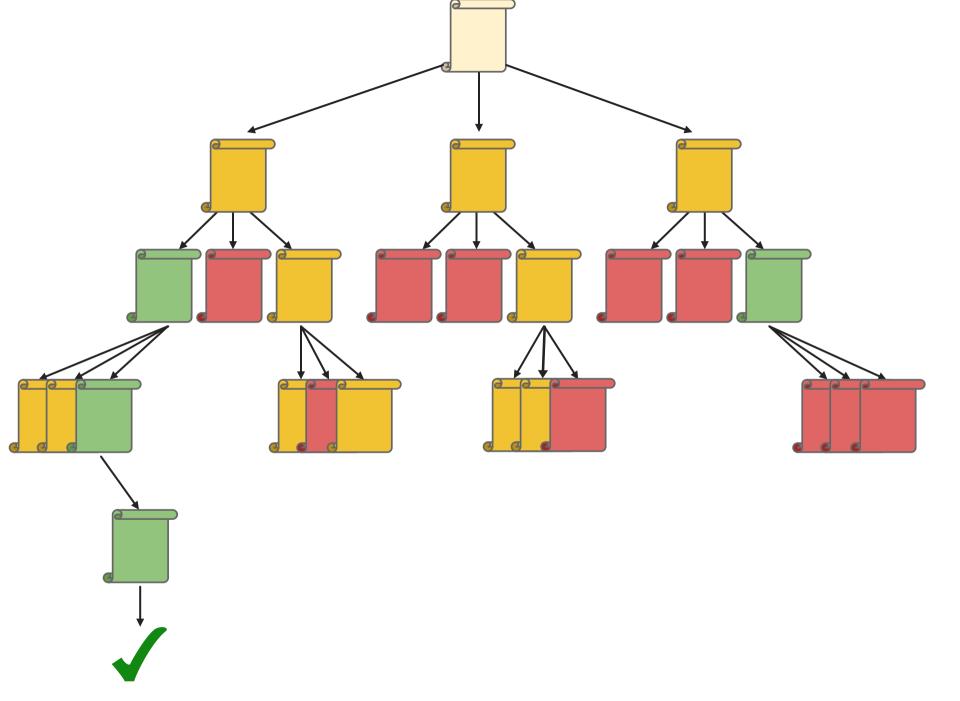


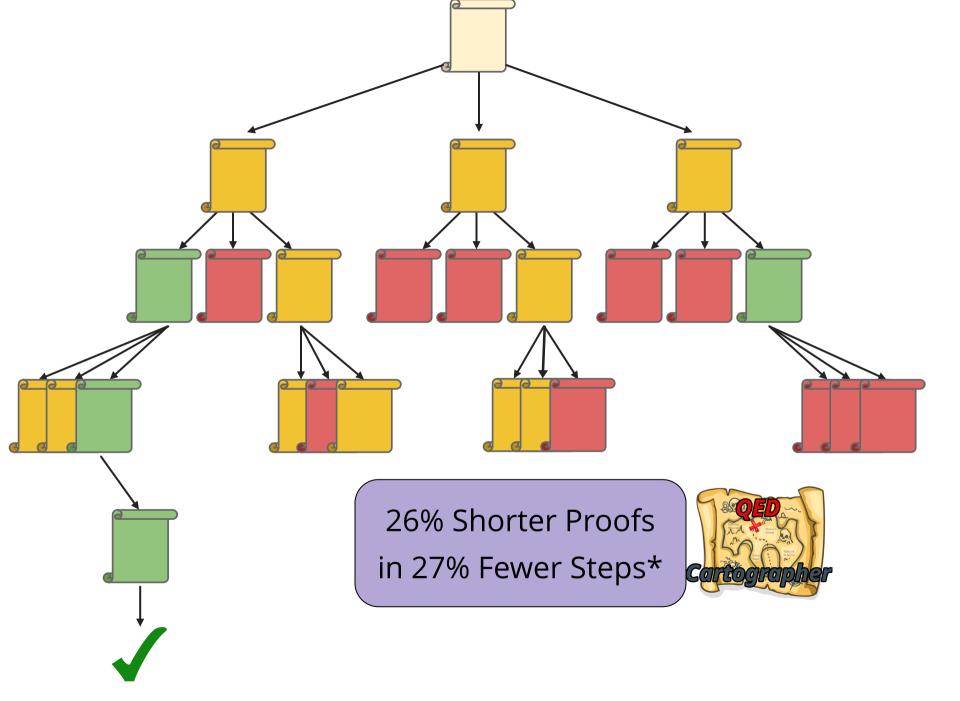


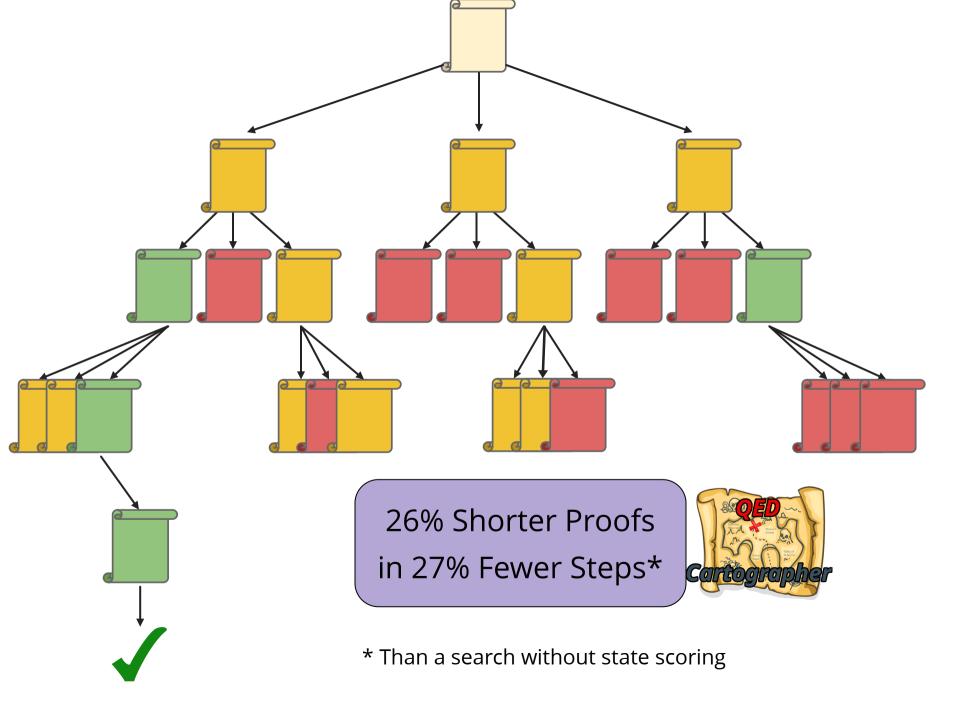


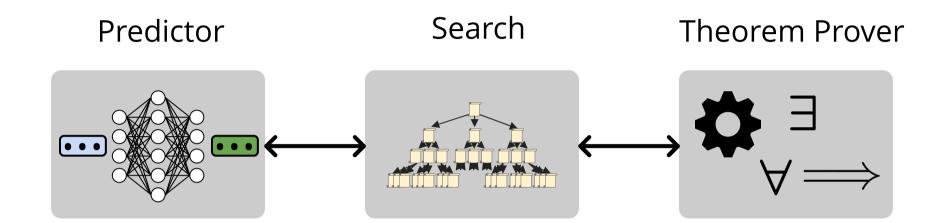


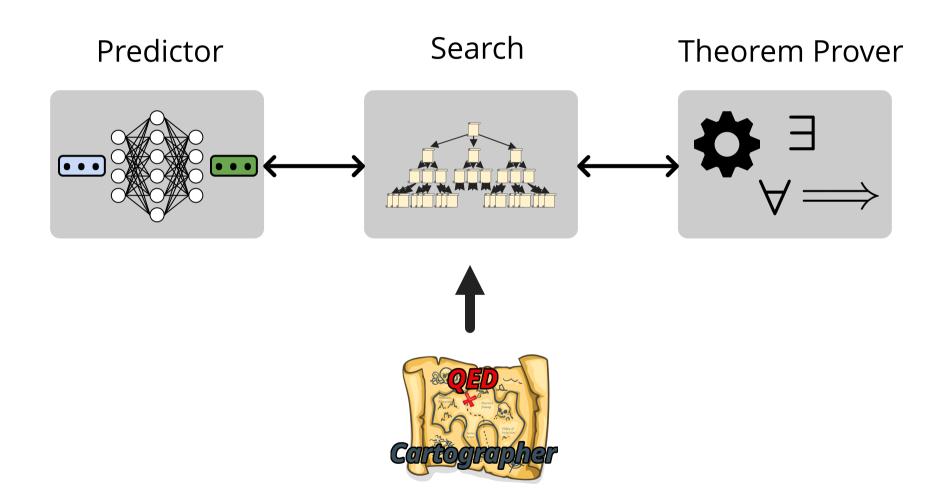










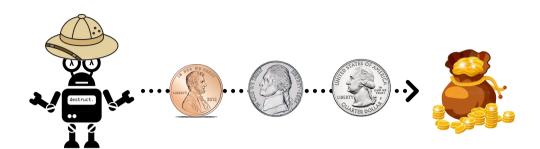


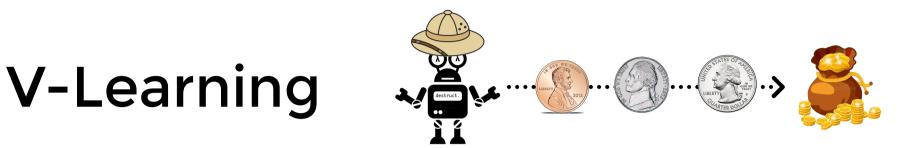
"Reward-free Reinforcement Learning"

"Reward-free Reinforcement Learning"

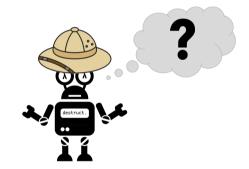
In particular, V-learning

V-Learning

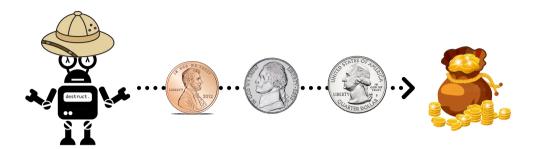




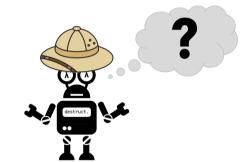
Limitations in Proofs



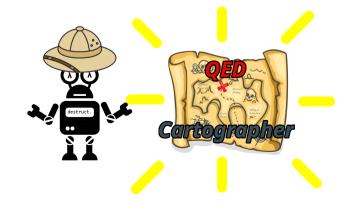
V-Learning

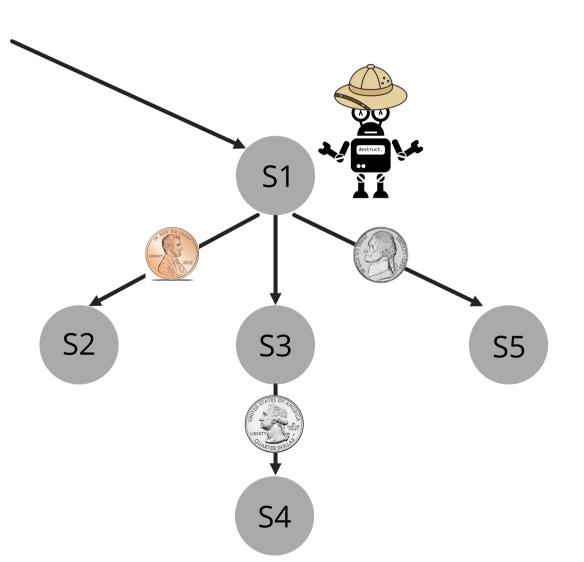


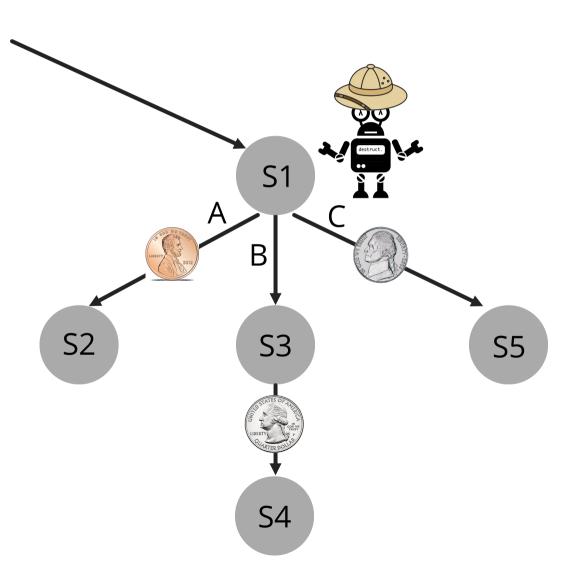
Limitations in Proofs

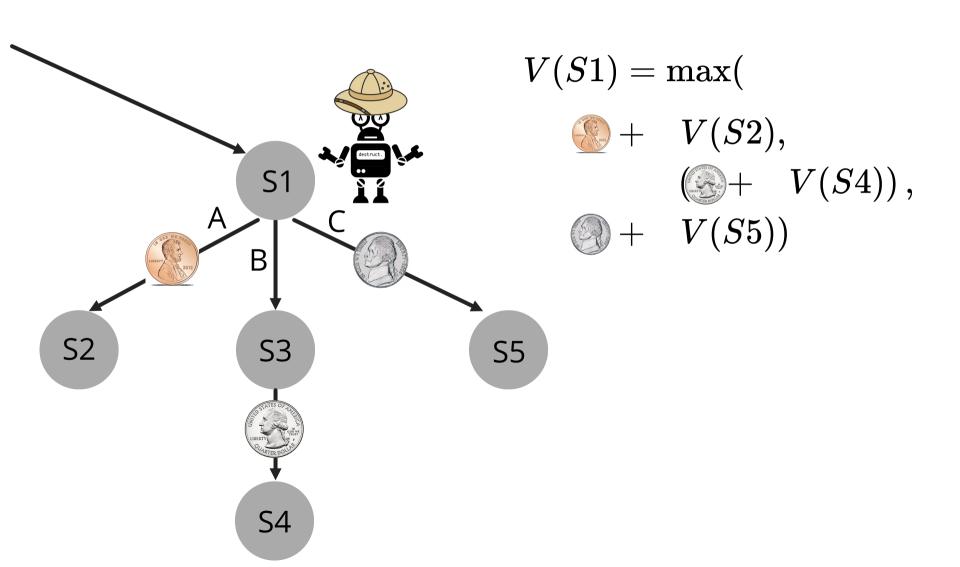


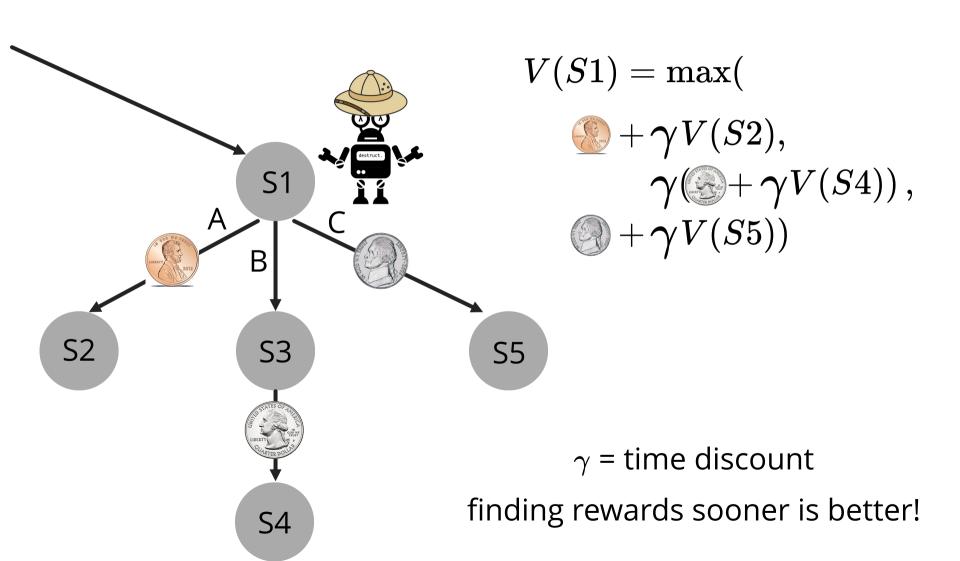
Adapting to Proofs











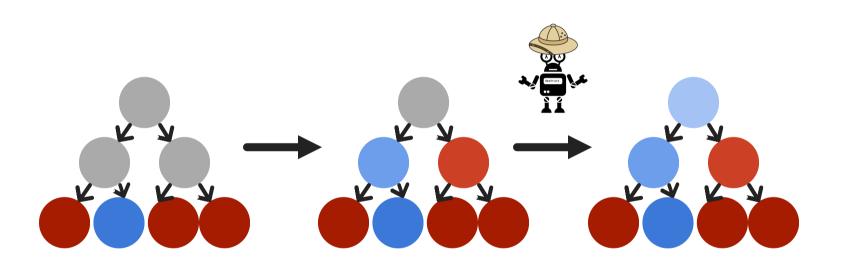
$$V(S1) = \max(\bigcirc + \gamma V(S2), \ \gamma \bigcirc + \gamma V(S4)), \bigcirc + \gamma V(S5))$$

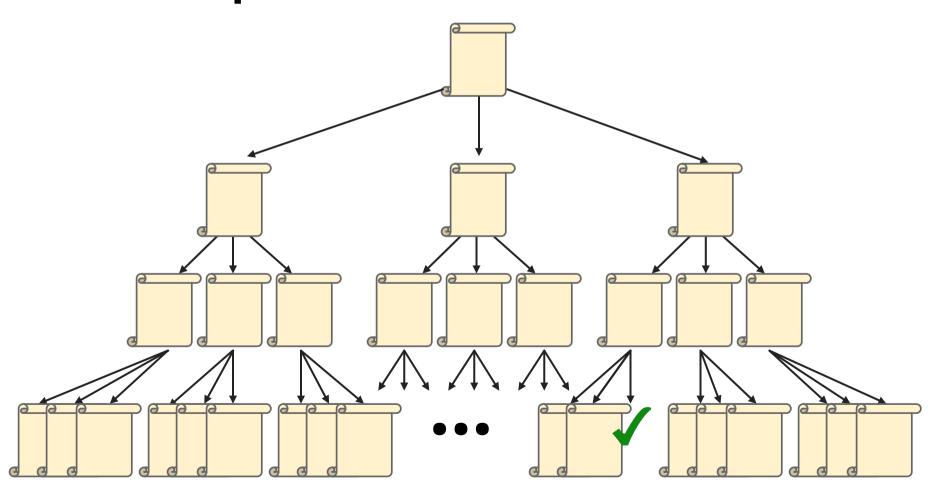
$$V(S1) = \max(\bigcirc + \gamma V(S2), \ \gamma \bigcirc + \gamma V(S4)), \bigcirc + \gamma V(S5))$$

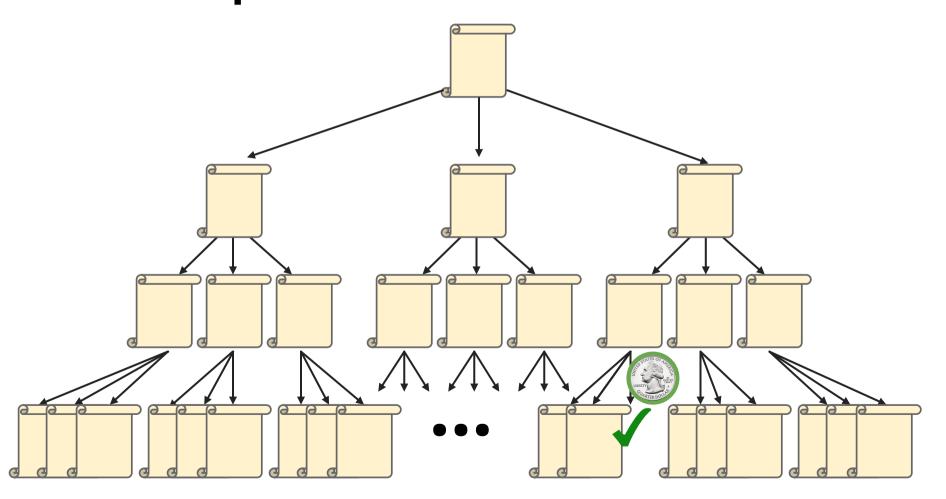


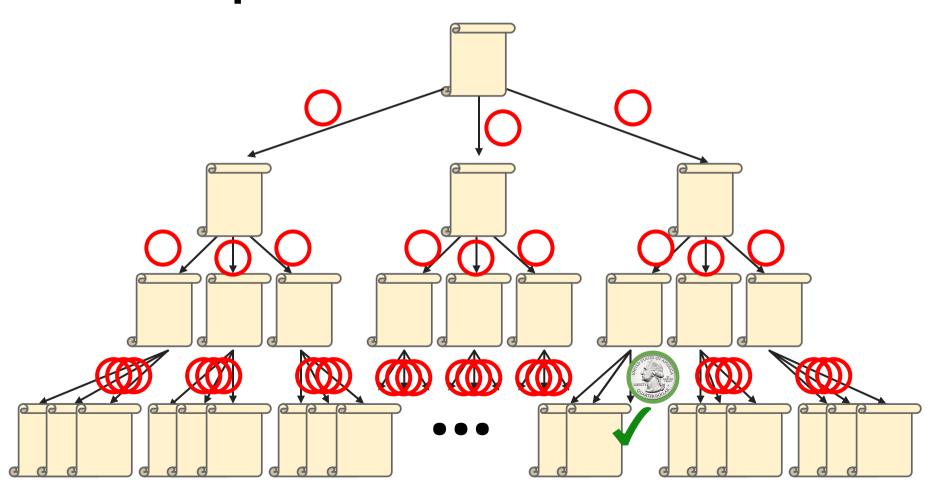
$$V(S) = \max_{a \in \operatorname{actions}(S)} (R(S, a) + \gamma V(\operatorname{next-state}(S, a)))$$

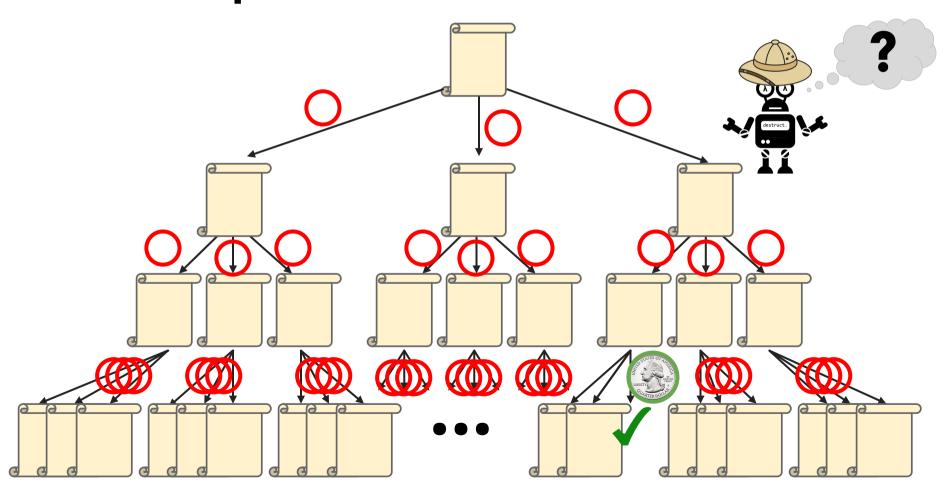
V-Learning in Practice: Iterative Updates





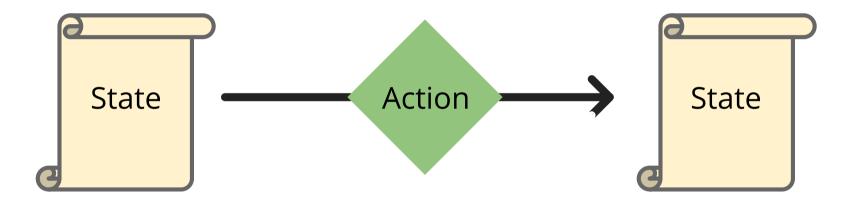






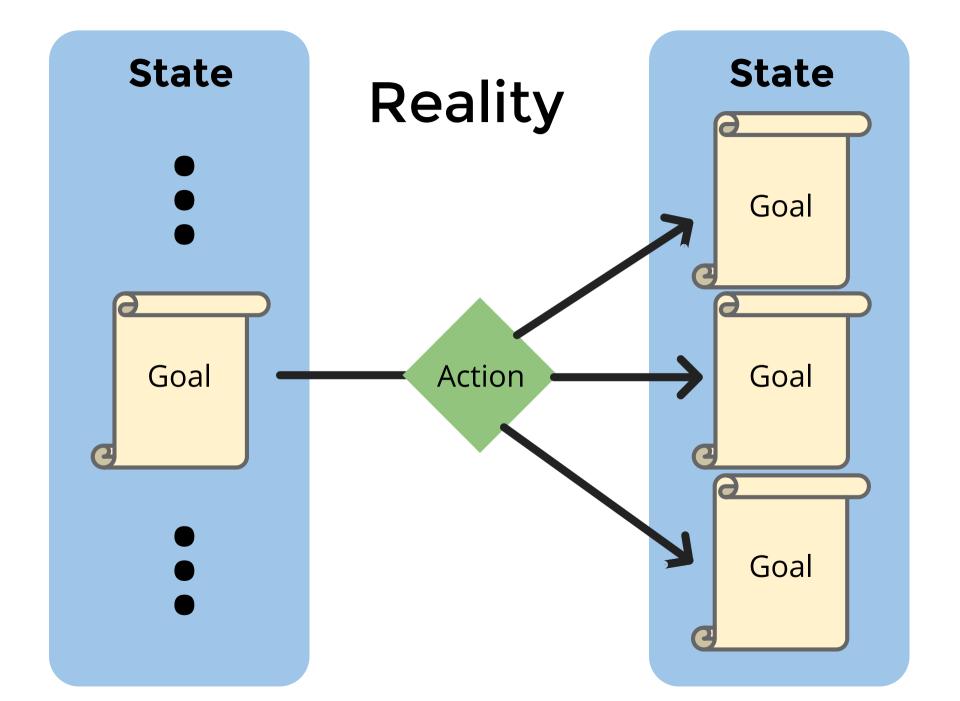
Insight: Proofs have Useful Structure

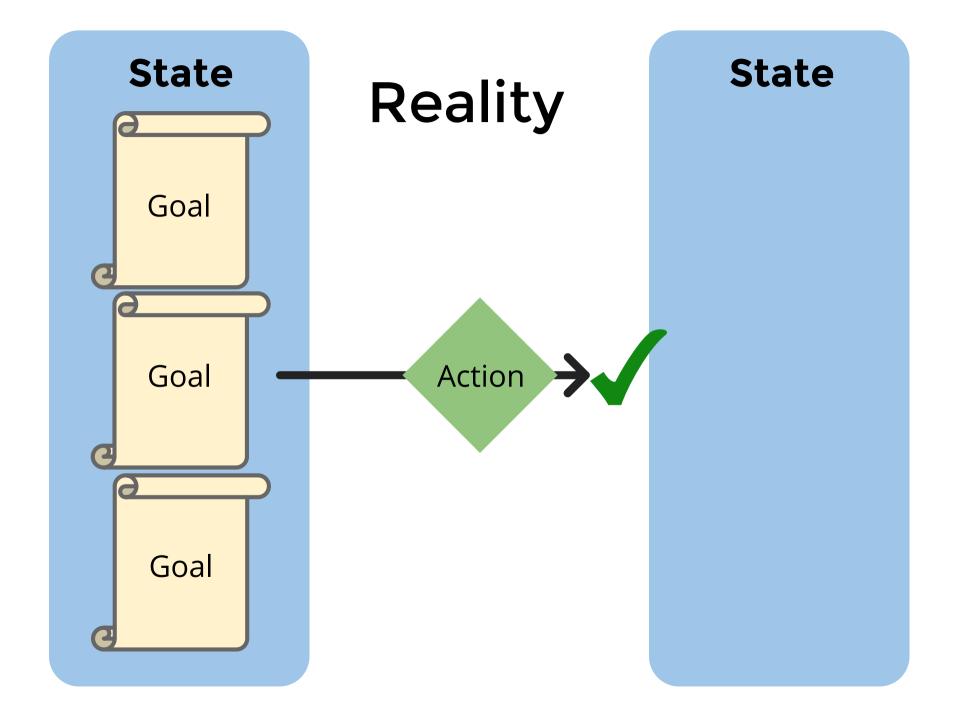
Abstraction

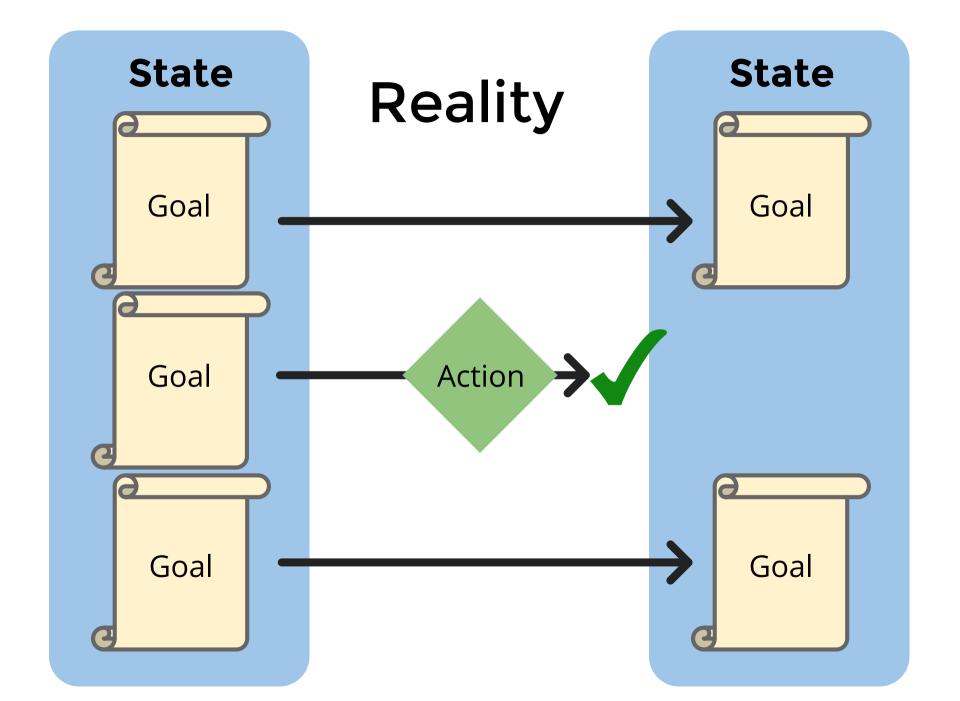


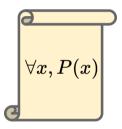
State Reality Action Goal

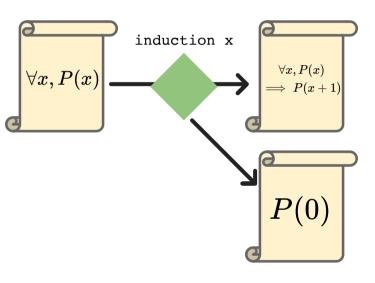
State

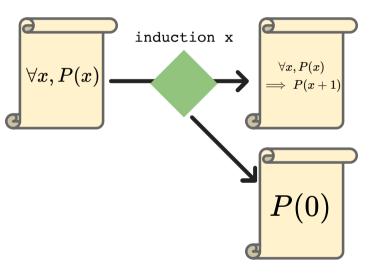




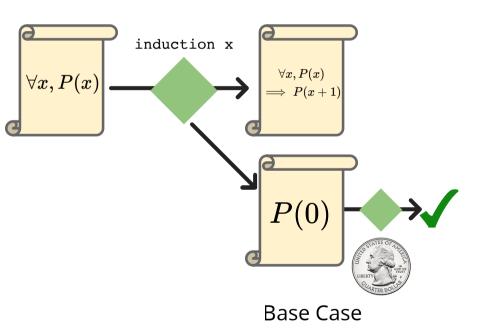


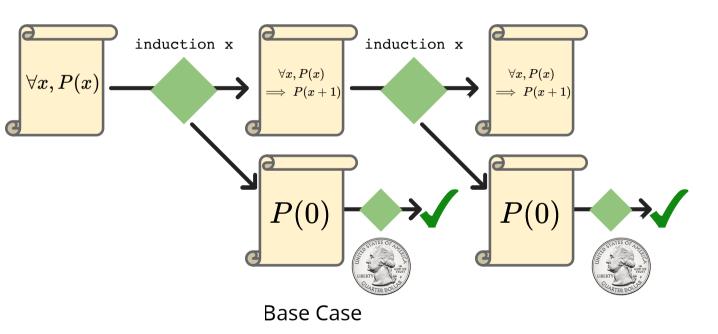


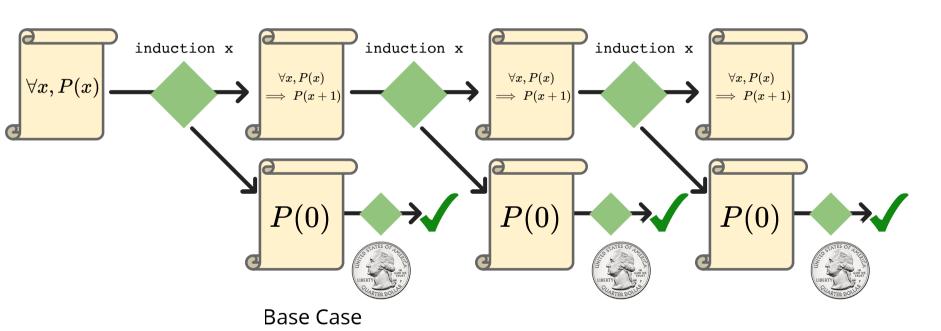


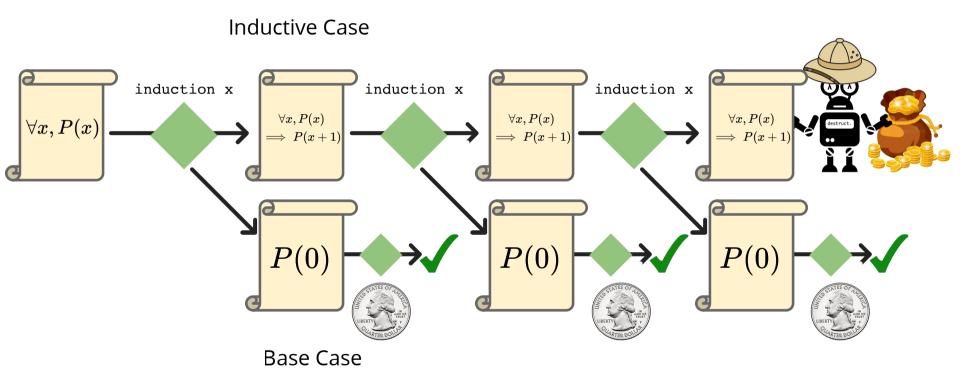


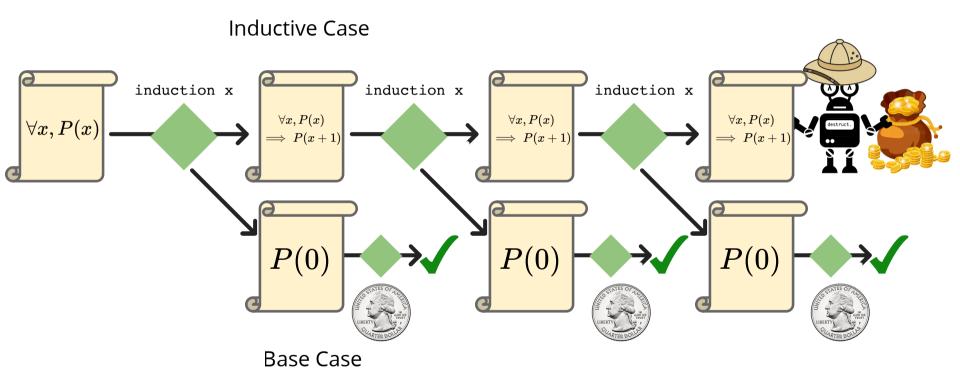
Base Case









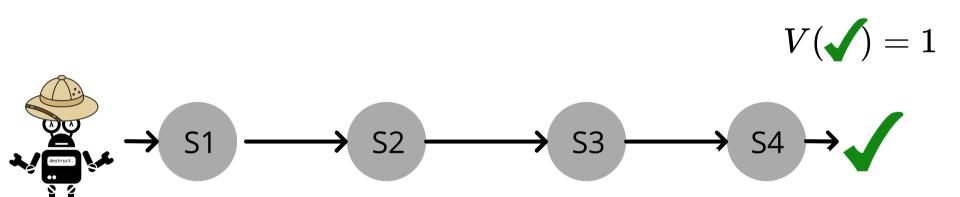


Reward-free doesn't have this problem!

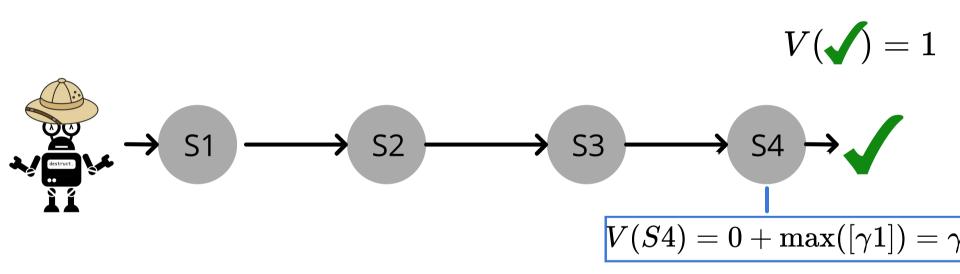
What We Need

A new update equation that accounts for the branching structure of proofs

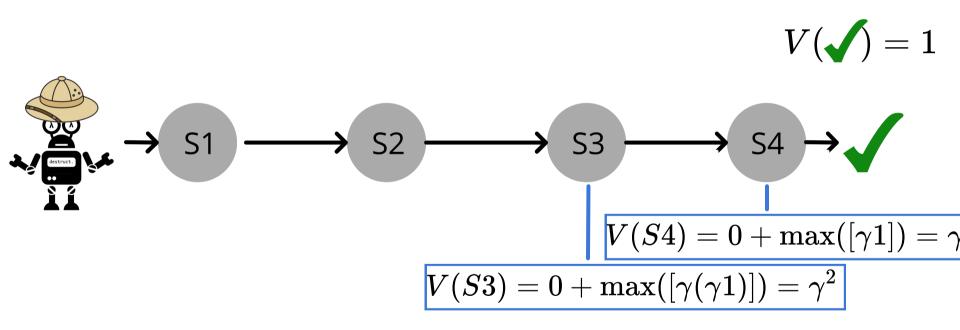
• The state of a completed proof has value 1



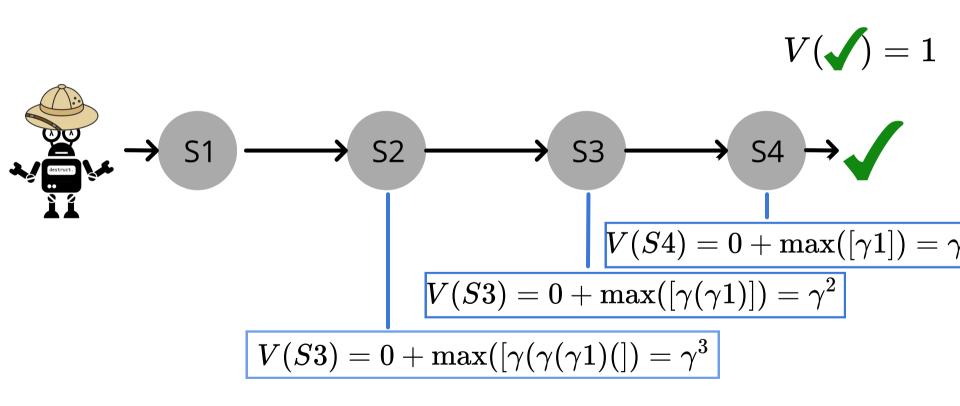
• The state of a completed proof has value 1



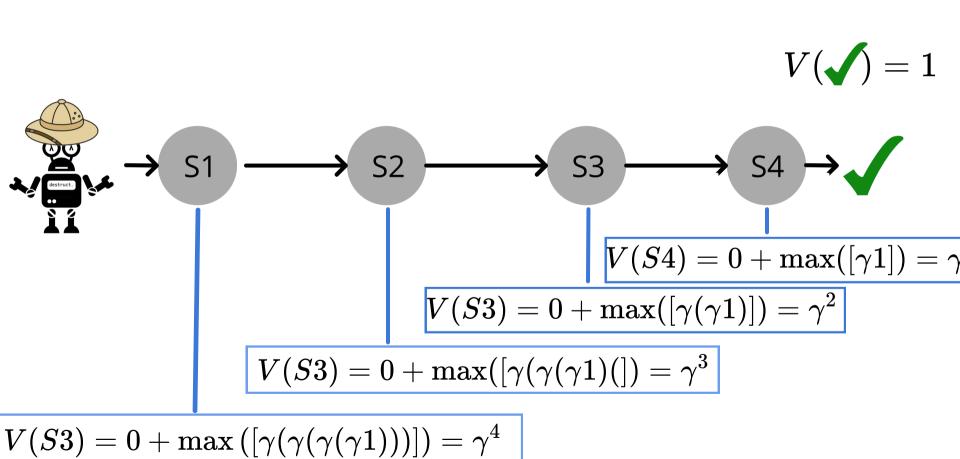
The state of a completed proof has value 1



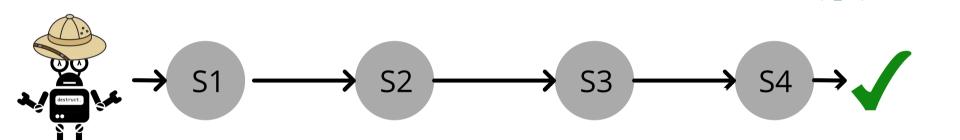
The state of a completed proof has value 1



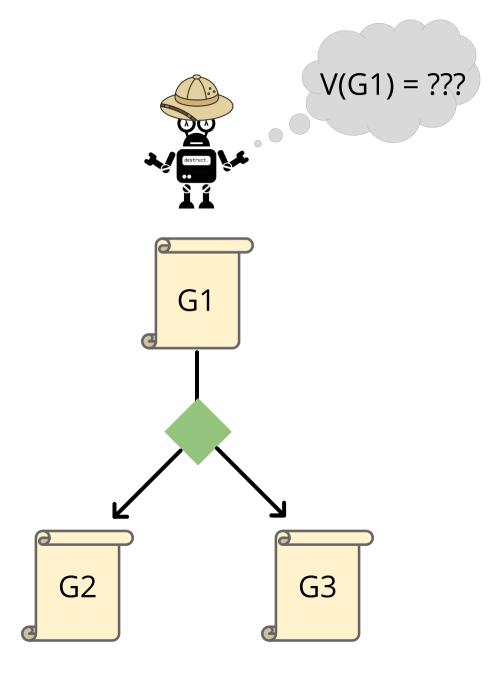
• The state of a completed proof has value 1



Assumption: The state of a completed proof has value 1



$$V(S) = \gamma^{
m (number\ of\ steps\ left)}$$



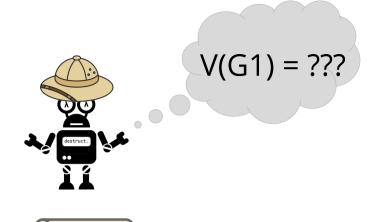


G1 G3

G2

m = Steps to complete proof from G2

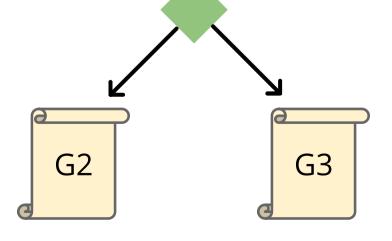
n = Steps to complete proof from G3



m = Steps to complete proof from G2

n = Steps to complete proof from G3

Steps to complete proof from G1 = m + n + 1



G1

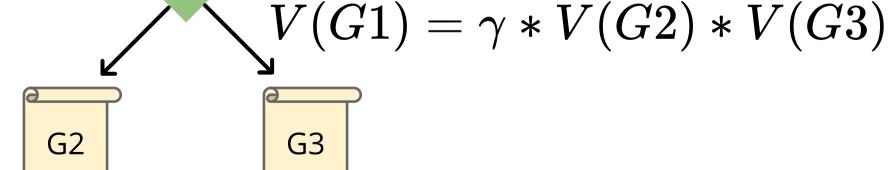


G1

m = Steps to complete proof from G2

n = Steps to complete proof from G3

Steps to complete proof from G1 = m + n + 1



Update Equation for Branch-Structured Proofs

$$V(G) = \max_{a \in \operatorname{actions}(G)} \left(\gamma \prod_{G' \in \operatorname{next-states}(G,a)} V(G')
ight)$$

Update Equation for Branch-Structured Proofs

$$V(G) = \overline{\max_{a \in \operatorname{actions}(G)}} \Big(\gamma \prod_{G' \in \operatorname{next-states}(G,a)} V(G') \Big)$$

Update Equation for Branch-Structured Proofs

$$V(G) = \max_{a \in \operatorname{actions}(G)} \left(\gamma \prod_{G' \in \operatorname{next-states}(G,a)} V(G')
ight)$$

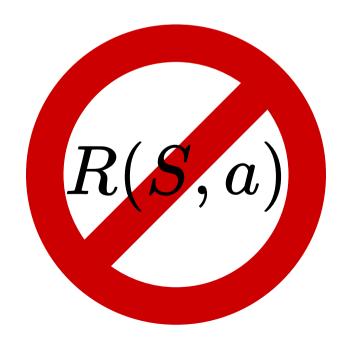
$$V(G) = \max_{a \in \operatorname{actions}(G)} \left(\gamma \overline{\prod_{G' \in \operatorname{next-states}(G,a)} V(G')}
ight)$$

$$V(G) = \max_{a \in \operatorname{actions}(G)} \left(\overline{\gamma} \prod_{G' \in \operatorname{next-states}(G,a)} V(G')
ight)$$

$$V(G) = \max_{a \in \operatorname{actions}(G)} \left(\gamma \prod_{G' \in \operatorname{next-states}(G,a)} V(G')
ight)$$

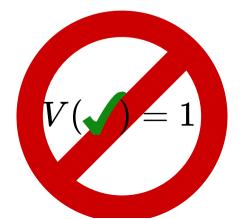
$$V(G) = \max_{a \in \operatorname{actions}(G)} \left(\gamma \prod_{G' \in \operatorname{next-states}(G,a)} V(G')
ight)$$

Where's the Reward?



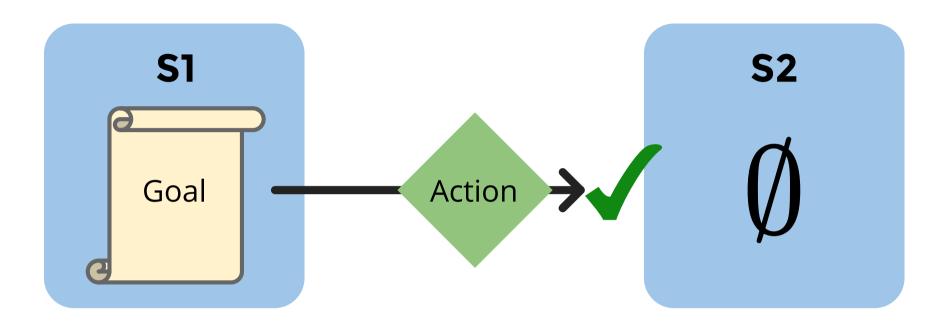
$$V(G) = \max_{a \in \operatorname{actions}(G)} \left(\gamma \prod_{G' \in \operatorname{next-states}(G,a)} V(G')
ight)$$

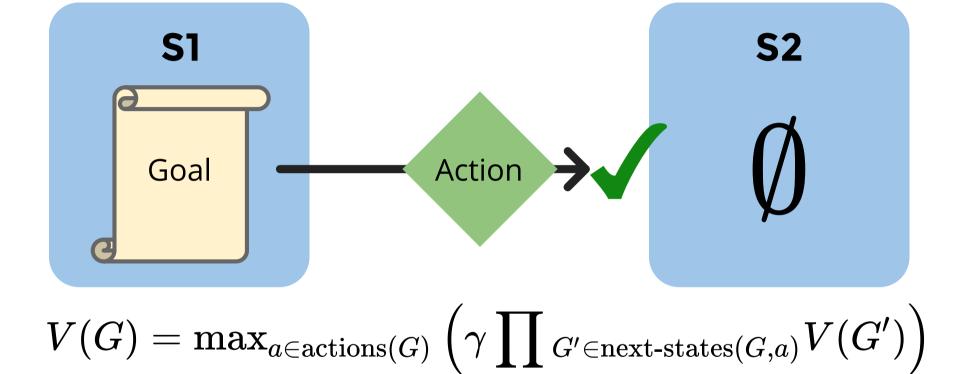
Where's the Reward?

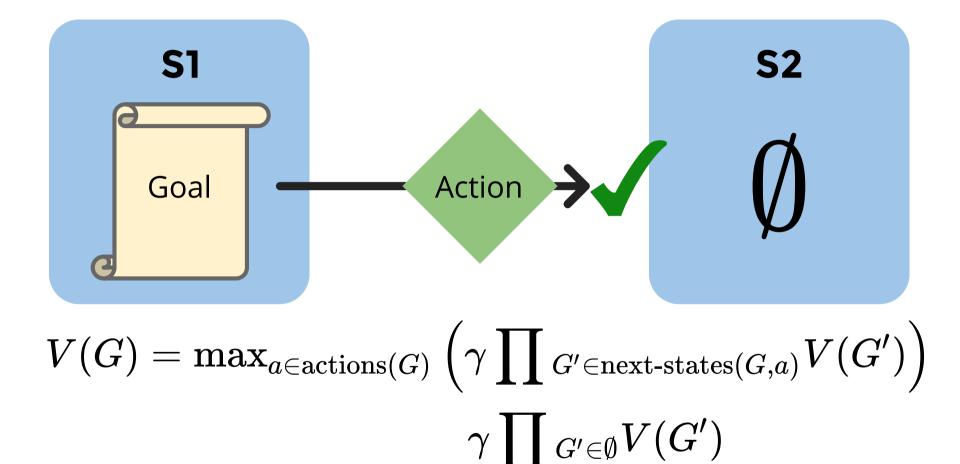


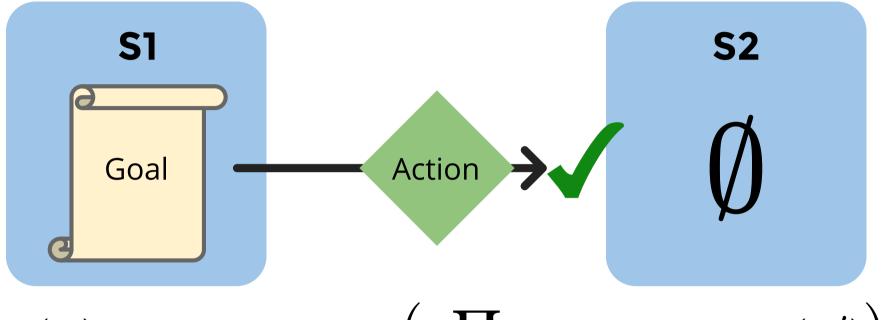




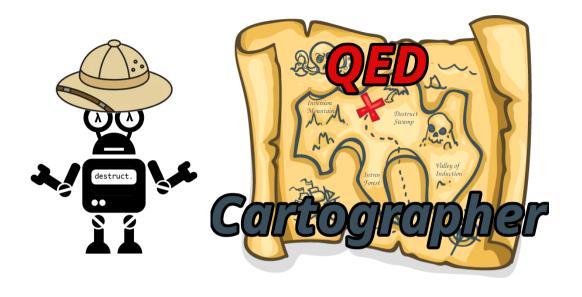




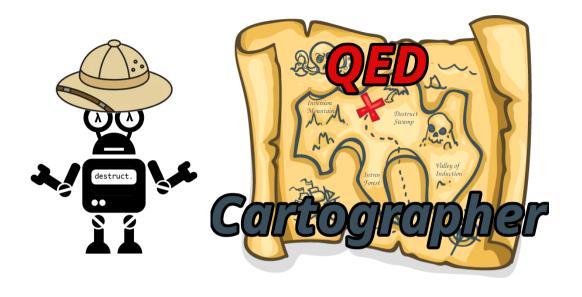




$$egin{aligned} V(G) &= \max_{a \in ext{actions}(G)} \left(\gamma \prod_{G' \in ext{next-states}(G,a)} V(G')
ight) \ & \gamma \prod_{G' \in \emptyset} V(G') \ & \gamma(1) \end{aligned}$$



Automating Formal Verification with Reward-Free Reinforcement Learning



Automating Formal Verification with Reward-Free Reinforcement Learning

26% Shorter Proofs in 27% Fewer Steps

Benchmark: CoqGym



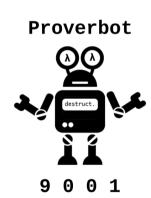
124 Coq Projects

68,501 Theorems

85/15 train-test split

Baseline: Proverbot9001 (updated)

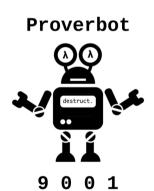
QEDCartographer, except without state scoring-based search

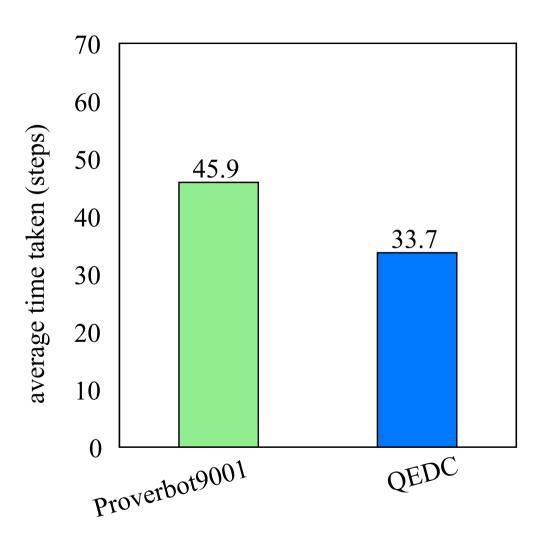


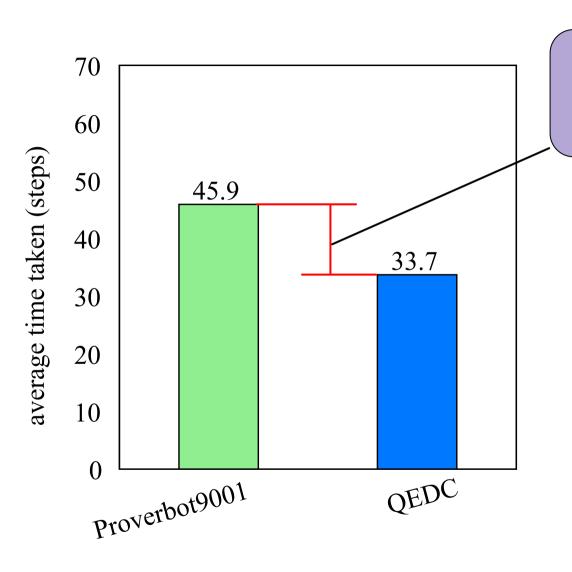
Baseline: Proverbot9001 (updated)

QEDCartographer, except without state scoring-based search

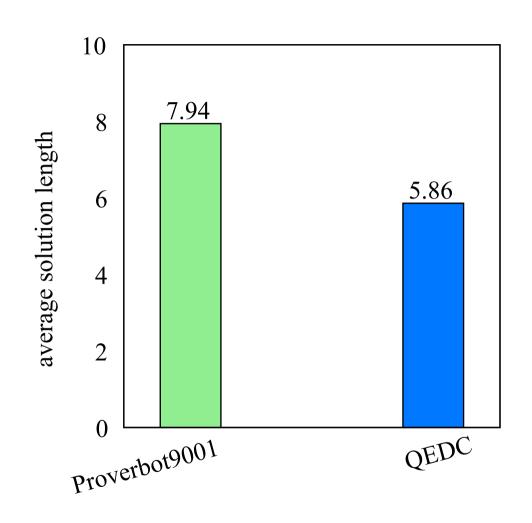
Uses a variant of depth-first search instead

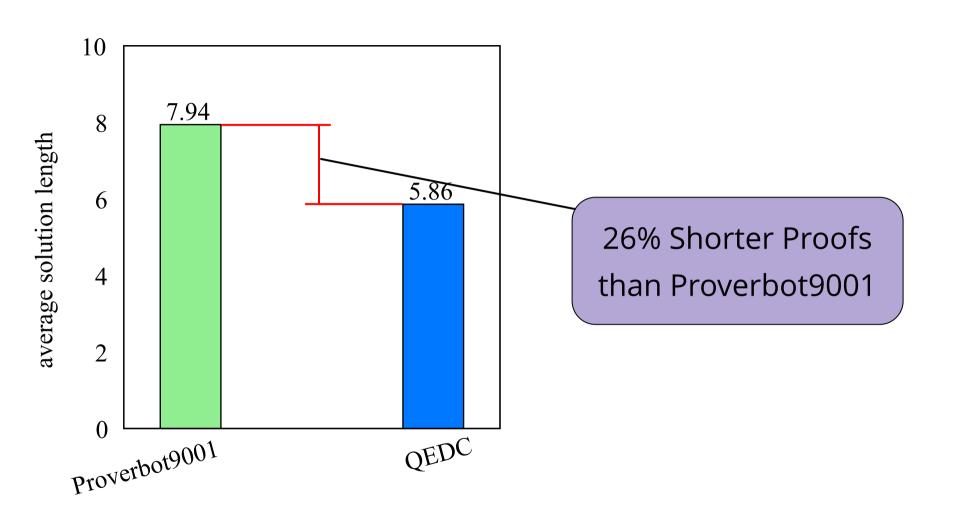


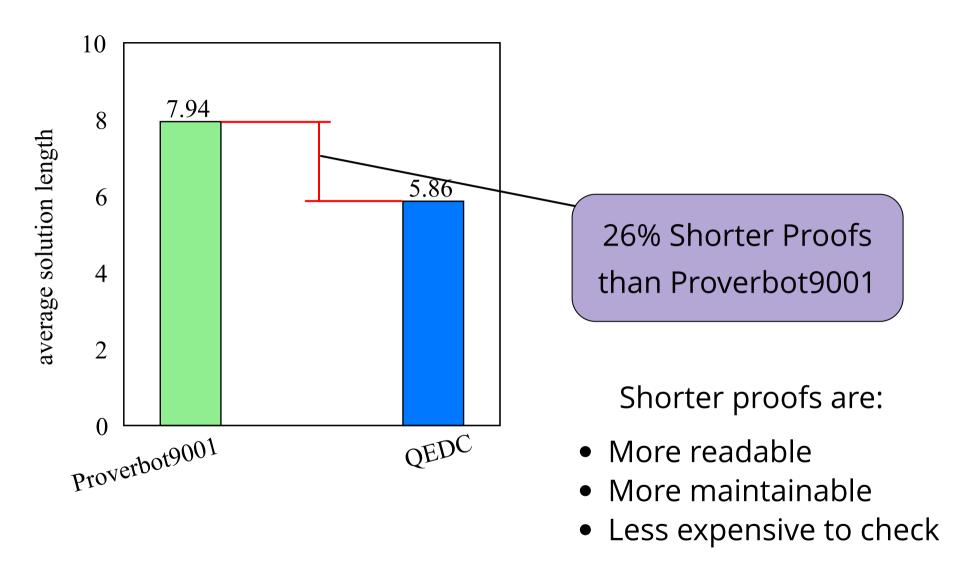


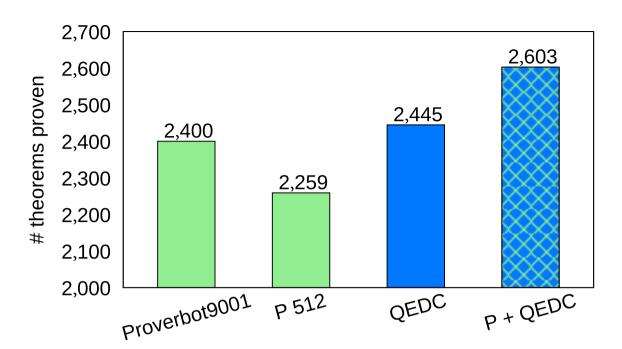


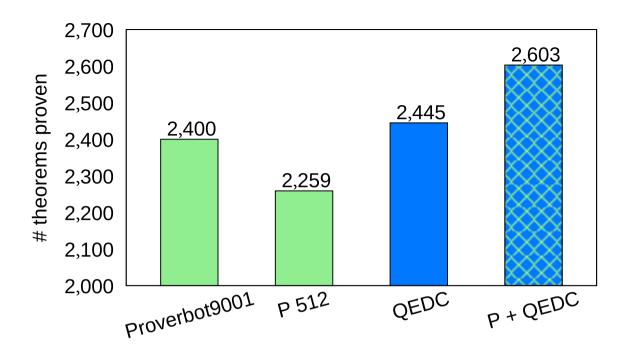
27% faster than Proverbot9001



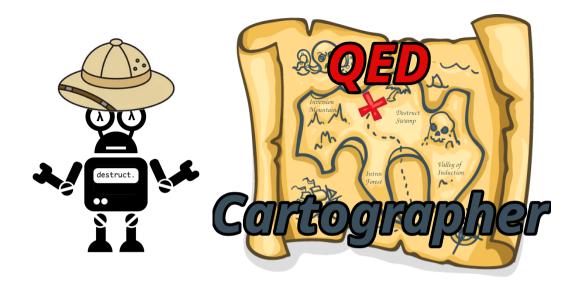








Proves slightly more theorems, and proves complementary theorems



Automating Formal Verification with Reward-Free Reinforcement Learning

Uses a new V-value equation for branching goal structure

Makes producing verified-correct code easier and faster

Preprint available at alexsanchezstern.com