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## Algorithms - HW#2

## Algorithm 1

a) Assume:  $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ ,  $B = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$   
 $C = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$ ,  $n = 2$

Output:  $C = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}$  at  $i=0, k=0$ ,  $C = \begin{bmatrix} 2 & 0 \\ 0 & 0 \end{bmatrix}$  at  $k=1$

$C = \begin{bmatrix} 2 & 4 \\ 0 & 0 \end{bmatrix}$  at  $k=0$ ,  $C = \begin{bmatrix} 2 & 8 \\ 0 & 0 \end{bmatrix}$  at  $k=1$

$C = \begin{bmatrix} 2 & 4 \\ 9 & 0 \end{bmatrix}$  at  $k=0$ ,  $C = \begin{bmatrix} 2 & 4 \\ 18 & 0 \end{bmatrix}$  at  $k=1$

$C = \begin{bmatrix} 2 & 4 \\ 18 & 10 \end{bmatrix}$  at  $k=0$ ,  $C = \begin{bmatrix} 2 & 4 \\ 18 & 32 \end{bmatrix}$  at  $k=1$

~~Basic~~B) Basic operation:  $C[i,j] \leftarrow C[i,j] + A[i,j] \oplus B[i,j]$ 

c)  $\sum_{i=0}^{n-1} \sum_{j=0}^{n-1} \sum_{k=0}^{n-1} 1 = n^3 = \Theta(n^3)$



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### -Algorithm 2

a) Assume:  $n \leq 3$

Output:  $S \leq 0 + 1 + 1 \leq 2$  at  $i \leq 1$   
 $S \leq 2 + 2 + 2 \leq 6$  at  $i \leq 2$   
 $S \leq 6 + 3 + 3 \leq 12$  at  $i \leq 3$   
Return  $\rightarrow (12)$

b) Basic operation:  $S \leftarrow S + 1 + 1$

$$c) C(n) = \sum_{i=1}^n 1 \leq n - 1 + 1 = n \rightarrow \Theta(n)$$

d) no worst case, because it's gonna always take  $n$  times

### -Algorithm 3

a) Assume:  $A[1, 3, 5]$ ,  $n = 3$

Output:  $V \leq 1$ ,  $S \leq 5$ , returns  $5 - 1 \leq 4$

b) Basic operation: if  $A[i] \leq y$ , if  $A[i] \leq y$

$$c) C(n) = \sum_{i=1}^n n - 1 = n - 1 \rightarrow \Theta(n)$$

d) all of cases will take  $n$  times

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is it a LeetCode problem?

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- Algorithm 4

a) Assume:  $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$

output: return  $\rightarrow$  False  $1 \neq 3$

b) Basic operation:  $\neq$

$$c) c(n) = \sum_{i=1}^{n-2} \sum_{j=i+1}^{n-1} 1 = \sum_{i=1}^{n-2} (n-1-i) = n-1-i$$

$$= \sum_{i=1}^{n-2} (n-1-i) = \sum_{i=1}^{n-2} (n-1) - \sum_{i=1}^{n-2} i = (n-1) \sum_{i=1}^{n-2} 1 - \sum_{i=1}^{n-2} i$$

$$= (n-1) \cdot (n-2) - \frac{(n-1) \cdot (n-2)}{2} \rightarrow \Theta(n^2)$$

d) Best case  $O(1)$ , Worst case  $O(n^2)$



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let  $n = 0, 1, 2, \dots, 14$   
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2-  $A = \langle E, X, A, M, P, L, E \rangle$

$$\begin{array}{ccccccc} E & | & X & A & M & P & L & E \\ \uparrow & & \downarrow & & & & & \\ E & X & | & A & M & P & L & E \\ \uparrow & & \downarrow & & & & & \\ A & E & X & | & M & P & L & E \\ & & & & \uparrow & & & \\ A & E & M & X & | & P & L & E \\ \uparrow & & & & \downarrow & & & \\ A & E & M & P & X & | & L & E \\ \uparrow & & & & & & \downarrow & \\ A & E & L & M & P & X & L & E \\ A & E & E & L & M & P & X & \rightarrow A = \langle A, E, E, L, M, P, X \rangle \end{array}$$

3-  $A = \langle 3, 41, 52, 25, 38, 57, 9, 49 \rangle$

$$\begin{array}{cccccccc} 3 & | & 41 & 52 & 25 & 38 & 57 & 9 & 49 \\ \uparrow & & \downarrow & & & & & & \\ 3 & 41 & | & 52 & 25 & 38 & 57 & 9 & 49 \\ \uparrow & & \downarrow & & & & & & \\ 3 & 41 & 52 & | & 25 & 38 & 57 & 9 & 49 \\ \uparrow & & & & \downarrow & & & & \\ 3 & 25 & 41 & 52 & | & 38 & 57 & 9 & 49 \\ \uparrow & & & & \downarrow & & & & \\ 3 & 25 & 38 & 41 & 52 & | & 57 & 9 & 49 \\ \uparrow & & & & & & \downarrow & & \\ 3 & 25 & 38 & 41 & 52 & 57 & | & 9 & 49 \\ \uparrow & & & & & & & \downarrow & \\ 3 & 9 & 25 & 38 & 41 & 52 & 57 & 1 & 49 \\ \uparrow & & & & & & & & \\ 3 & 9 & 25 & 38 & 41 & 49 & 52 & 57 & \end{array}$$

$A = \langle 3, 9, 25, 38, 41, 49, 52, 57 \rangle$

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4. Consider the following version

$$C(n) \leq \sum_{i=1}^{n-1} 1 \leq n-1-1+1 \leq n-1 \rightarrow \Theta(n)$$

Worst case is  $O(n^2)$  if it's reverse

The difference between the 2 versions is that this version uses swap not shifting

5. insertion sort best case  $\rightarrow \Theta(n)$

Bubble sort best case  $\rightarrow \Theta(n^2)$

- So insertion sort is better.

6. both of them has the same time complexity  $\Theta(n^2)$