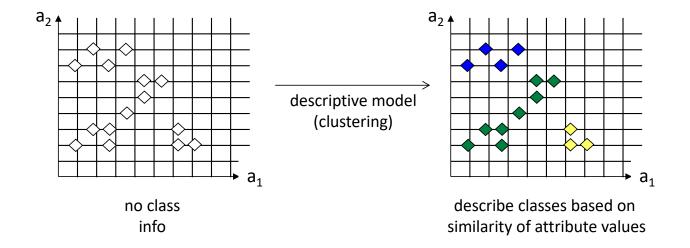
## 4. CLASSIFICATION

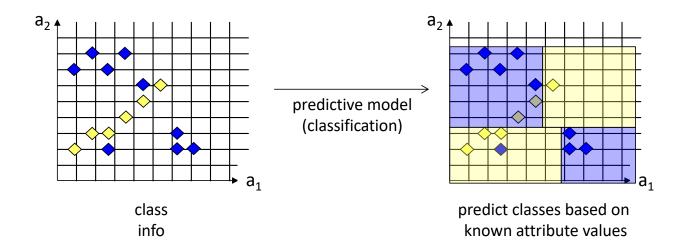
## **Clustering and Classification**

Given a dataset of *objects* described by *attributes*, build a model that assigns objects to a *class* (or label)



## **Clustering and Classification**

Given a dataset of *objects* described by *attributes*, build a model that assigns objects to a *class* 



#### **Classification Problem**

**Input**: set of objects with categorical/numerical attributes and one class label

**Output**: A model that returns the class label given the object attributes

 Model is a function represented as rules, decision trees, formulae

Classification belongs to supervised ML

Objects have class information

## **Classification: General Approach**

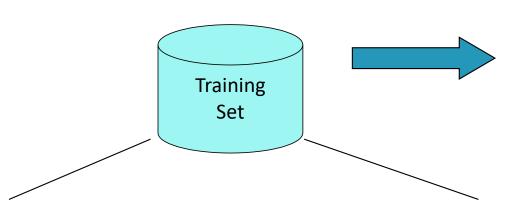
Model is learnt from a set of objects with known labels: **training set** 

The quality of the model is evaluated by comparing the predicted class labels with those from a set of objects with known labels: **test set** 

Test set is independent of training set,
 otherwise over-fitting will occur

The model is applied to data with unknown labels: **prediction** 

## **Classification: Training**



NAME	RANK	YEARS	TENURED
Mike	Assistant Prof	3	no
Mary	Assistant Prof	7	yes
Bill	Professor	2	yes
Jim	Associate Prof	7	yes
Dave	Assistant Prof	6	no
Anne	Associate Prof	3	no

Categorical attribute

Numerical Class label attribute

Classification
Algorithms

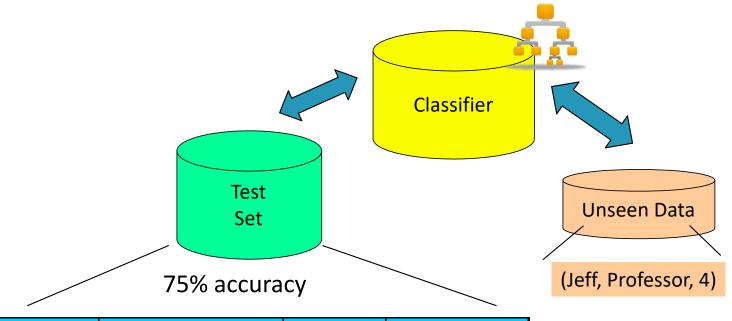
Classifier
(Model)

IF rank = 'professor'
OR years > 6
THEN tenured = 'yes'

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Classification - 6

## **Classification: Model Test and Usage**



NAME	RANK	YEARS	TENURED
Tom	Assistant Prof	2	no
Merlisa	Associate Prof	7	no
George	Professor	5	yes
Joseph	Assistant Prof	7	yes

Tenured?



YES

#### Classification: Problem Formulation

#### **Problem**

Given a database D with n data items described by d categorical/numerical attributes and one categorical attribute (class label C)

**Find** 

A function  $f: X^d \rightarrow C$ 

rules decision tree formula

Such that

classifies *accurately* the items in the *training* set *generalises* well for the (unknown) items in the *test* set

### **Characteristics of Classification Methods**

#### Predictive accuracy

#### Speed and scalability

- Time to build the model
- Time to use the model
- In memory vs. on disk processing

#### Robustness

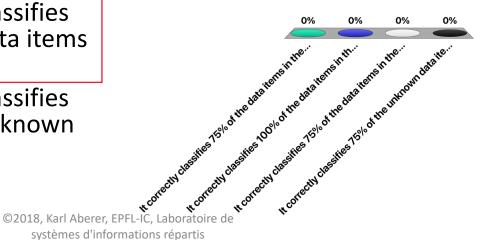
Handling noise, outliers and missing values

#### Interpretability

- Understanding the model and its decisions (black box)
   vs. white box
- Compactness of the model

## If a classifier has 75% accuracy, it means that ...

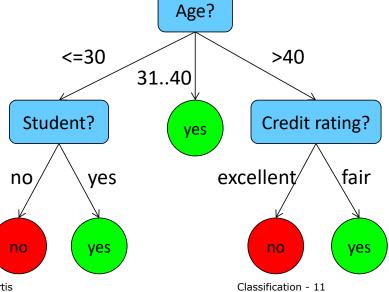
- A. It correctly classifies75% of the data items in the training set
- B. It correctly classifies 100% of the data items in the training set but only 75% in the test set
- C. It correctly classifies 75% of the data items in the test set
- D. It correctly classifies 75% of the unknown data items



### **Decision Trees**

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

- Nodes are tests on a single attribute
- Branches are attribute values
- Leaves are marked with class labels



some columns are not used

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## **Decision Tree Induction: Algorithm**

Tree construction (top-down divide-and-conquer strategy)

- At the beginning, all training samples belong to the root
- Examples are partitioned recursively based on a selected "most discriminative" attribute
- Discriminative power determined based on information gain (ID3/C4.5)

#### Partitioning stops if

- All samples belong to the same class → assign the class label to the leaf
- There are no attributes left → majority voting to assign the class label to the leaf
- There are no samples left

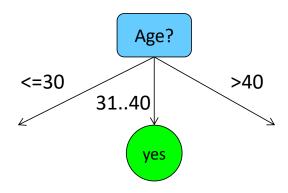
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## **Example: Decision Tree Induction**

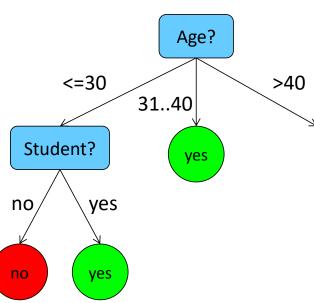
age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
≥40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

buys\_computer is always yes if 31 < age < 40



## **Example: Decision Tree Induction**

44	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
	88		559	
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
			638696	
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
	555555		9449399Y	
	7787		599	
>40	medium	no	excellent	no

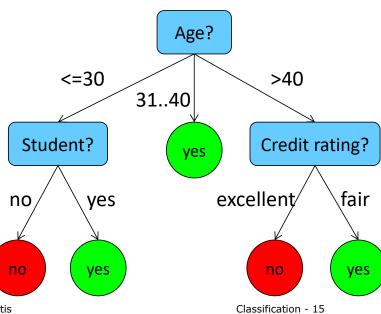


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Classification - 14

## **Example: Decision Tree Induction**

385	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
	898		199	
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
88.88	888		e5x 63655X	
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
38.48	9999999		errellen	
38.48	8988		Sast	
>40	medium	no	excellent	no



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### **Attribute Selection**

At a given branch in the tree, the set of samples S to be classified has P positive and N negative instances

The entropy of the set S is

$$H(P, N) = -\frac{P}{P+N} \log_2 \frac{P}{P+N} - \frac{N}{P+N} \log_2 \frac{N}{P+N}$$

Note

$$H(P, N) = 0 \rightarrow \text{no uncertainty}$$

$$H(P, N) = 1 \rightarrow maximal uncertainty$$

## **Attribute Selection: Example**

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

$$H_S = H(9, 5) = 0.94$$

entropy of label (buys\_computer)

Age 
$$[<=30]$$
  $H(2, 3) = 0.97$ 

Age 
$$[31...40]$$
  $H(4, 0) = 0$ 

Age 
$$[>40]$$
  $H(3, 2) = 0.97$ 

Income [high] 
$$H(2, 2) = 1$$

Income [med] 
$$H(4, 2) = 0.92$$

Income [low] 
$$H(3, 1) = 0.81$$

Student [yes] 
$$H(6, 1) = 0.59$$

Student [no] 
$$H(3, 4) = 0.98$$

Rating [fair] 
$$H(6, 2) = 0.81$$

Rating 
$$[exc]$$
  $H(3, 3) = 1$ 

## **Attribute Selection: Example**

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
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3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

$$H_S = H(9, 5) = 0.94$$

conditional entropy probability of being in that subgroup x entropy of subgroup

$$H_{Age} = p([<=30]) \cdot H(2, 3) + p([31...40]) \cdot H(4, 0) + p([>40]) \cdot H(3, 2) =$$
  
= 5/14 \cdot 0.97 + 4/14 \cdot 0 + 5/14 \cdot 0.97 = 0.69

$$H_{Income}$$
 = p([high]) · H(2, 2) + p([med]) · H(4, 2) + p([low]) · H(3, 1) =   
= 4/14 · 1 + 6/14 · 0.92 + 4/14 · 0.81 = 0.91

$$H_{Student} = p([yes]) \cdot H(6, 1) + p([no]) \cdot H(3, 4) = 7/14 \cdot 0.59 + 7/14 \cdot 0.98 = 0.78$$

$$H_{Rating} = p([fair]) \cdot H(6, 2) + p([exc]) \cdot H(3, 3) = 8/14 \cdot 0.81 + 6/14 \cdot 1 = 0.89$$

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Classification - 18

we split using the attribute with the smallest uncertainty.

#### **Attribute Selection: Information Gain**

Attribute A partitions S into  $S_1$ ,  $S_2$ , ...  $S_v$ Entropy of attribute A is

$$H(A) = \sum_{i=1}^{\nu} \frac{P_{i} + N_{i}}{P + N} H(P_{i}, N_{i})$$

sum through all partition

The information gain obtained by splitting S using A is

$$Gain(A) = H(P, N) - H(A)$$

H(P,N) = total / true uncertainty H(A) = uncertainty of category

$$Gain(Age) = 0.94 - 0.69 = 0.25$$

$$Gain(Income) = 0.94 - 0.91 = 0.03$$

$$Gain(Student) = 0.94 - 0.78 = 0.16$$

$$Gain(Rating) = 0.94 - 0.89 = 0.05$$

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entropy before splitting - entropy after splitting

## ← split on age

if H(A) = H(P,N), then gain = 0

if the uncertainty of the attribute is equal to the uncertainty of S, then gain is 0

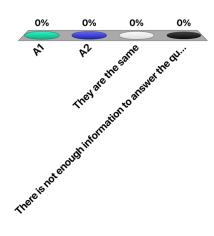
the attribute has no impact on classification

# Given the distribution of positive and negative samples for attributes $A_1$ and $A_2$ , which is the best attribute for splitting?

$A_1$	Р	N
a	2	2
b	4	0
A <sub>2</sub>	Р	N
x	3	1
y y	3	1

- A. A1
- B. A2
- C. They are the same
- D. There is not enough information to answer the question

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Druning	
Pruning	PRUNING

## The construction phase does not filter out noise → **overfitting**

#### Pruning strategies

- Stop partitioning a node when large majority of samples is positive or negative, i.e., N/(N+P) or P/(N+P) > 1 - ε
- Build the full tree, then replace nodes with leaves labelled with the majority class, if classification accuracy does not change ask: build full tree?
- Apply Minimum Description Length (MDL) principle

## **Minimum Description Length Pruning**

Let  $M_1$ ,  $M_2$ , ...,  $M_n$  be a list of candidate models (i.e., trees). The best model is the one that minimizes

$$L(M) + L(D|M)$$

#### where

- L(M) is the length in bits of the description of the model (#nodes, #leaves, #arcs ...)
- L(D|M) is the is the length in bits of the description of the data when encoded with the model (#misclassifications)

## **Extracting Classification Rules from Trees**

Represent the knowledge in the form of IF-THEN rules

- One rule is created for each path from the root to a leaf
- Each attribute-value pair along a path forms a conjunction
- The leaf node holds the class prediction

## Rules are easier for humans to understand Example

```
IF age = "<=30" AND student = "no"

IF age = "<=30" AND student = "yes"

IF age = "31...40"

IF age = ">40" AND credit_rating = "excellent"

THEN buys_computer = "yes"

THEN buys_computer = "no"
```

#### **Decision Trees: Continuous Attributes**

With continuous attributes we can not have a separate branch for each value

- use binary decision trees

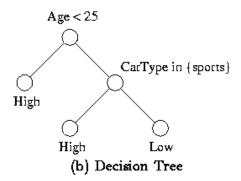
## Binary decision trees

- For continuous attributes A a split is defined by val(A) < X</li>
- For categorical attributes A a split is defined by a subset X ⊆ domain(A)

## **Example: Binary Decision Tree**

rid	Age	Саг Туре	Risk
0	23	family	High
1	17	sports	High
2	43	sports	High
3	68	family	Low
4	32	truck	Low
5	20	family	High

(a) Training Set



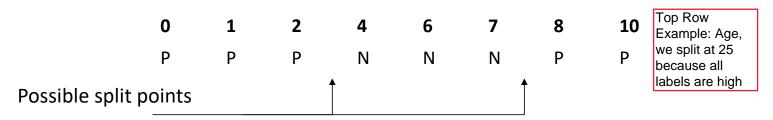
## **Splitting Continuous Attributes**

### **Approach**

- Sort the data according to attribute value
- Determine the value of X which maximizes information gain by scanning through the data items

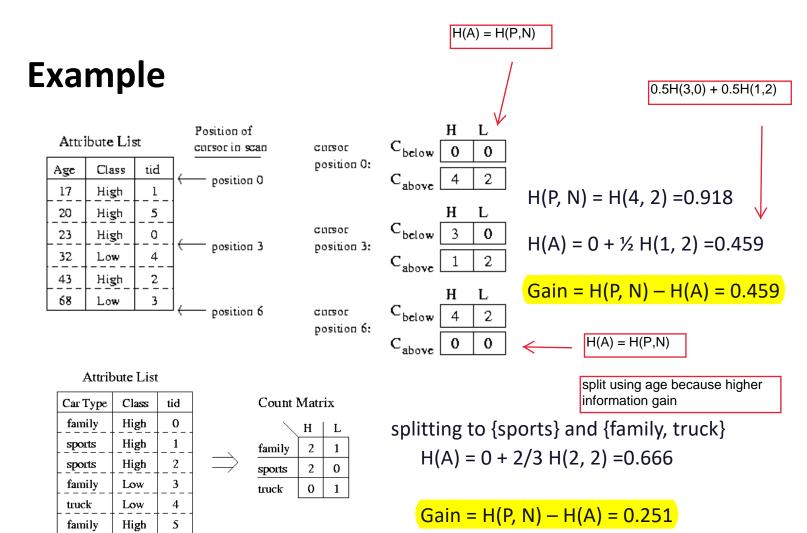
  X is the continuous attribute (eq age)

Only if the class label changes, a relevant decision point exists



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Classification - 26



## **Scalability of Continuous Attribute Splits**

## Naive implementation

 At each step the data set is split in subsets that are associated with a tree node

#### **Problem**

- For evaluating which attribute to split, data needs to be sorted according to these attributes
- Becomes dominating cost

## **Scalability of Continuous Attribute Splits**

Idea: Presorting of data and maintaining order throughout tree construction

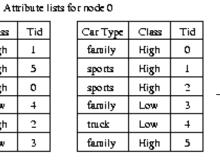
- Requires separate sorted attribute tables for each attribute
   Updating attribute tables
  - Attribute used for split: splitting attribute table straightforward
  - Other attributes
    - Build Hash Table associating tuple identifiers (TIDs) of data items with partitions
    - Select data from other attribute tables by scanning and probing the hash table

ask

## **Example**



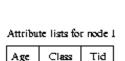
#### Class Tid Age 17 High 1 20 High 23 High Low 43 High 2 3 Low



#### hash table

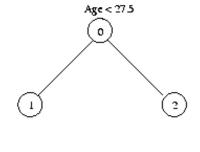
0	L
1	Г
2	R
3	R
4	R
5	L

age hash table



Age	Class	Tid
17	High	1
20	High	5
23	High	0

Car Type	Class	Tid
family	High	0
sports	High	1
family	High	5



#### Attribute lists for node 2

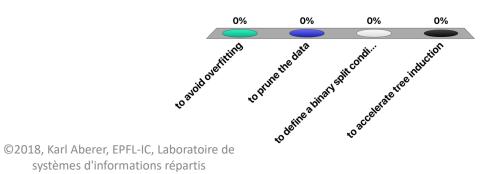
probe

Age	Class	Tid	
32	Low	4	
43	High	2	
68	Low	3	

Car Type	Class	Tid
sports	High	2
family	Low	3
truck	Low	4

## When splitting a continuous attribute, its values need to be sorted ...

- A. to avoid overfitting
- B. to prune the data
- C. to define a binary split condition
- D. to accelerate tree induction



### **Characteristics of Decision Tree Induction**

## Strengths

- Automatic feature selection
- Minimal data preparation
- Non-linear model
- Easy to interpret and explain

#### Weaknesses

- Sensitive to small perturbation in the data
- Tend to overfit
- Have to be re-trained from scratch with new data

## **Decision Tree Induction: Properties**

Model: flow-chart like tree structure

Score function: classification accuracy

Optimisation: top-down tree construction + pruning

Data Management: avoiding sorting during splits

## **Classification Algorithms**

Decision tree induction is a (well-known) example of a classification algorithm

#### **Alternatives**

- Basic methods: Naïve Bayes, kNN, logistic regression, ...
- Ensemble methods: random forest, gradient boosting, ...
- Support vector machines
- Neural networks: CNN, rNN, LSTM, ...

## **Ensemble Methods**

#### Idea

- Take a collection of simple or weak learners
- Combine their results to make a single, strong learner
   Types
- Bagging: train learners in parallel on different samples of the data, then combine outputs through voting or averaging
- Stacking: combine model outputs using a secondstage learner like linear regression
- Boosting: train learners on the filtered output of other learners

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Classification - 35

#### **Random Forests**

Learn K different decision trees from independent samples of the data (bagging)

 vote between different learners, so models should not be too similar

Aggregate output: majority vote

## Why do Ensemble Methods Work?

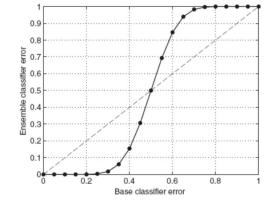
Assume there are 25 base classifiers

- Each classifier has error rate = 0.35
- Assume classifiers are independent

Probability that the ensemble classifier makes a

wrong prediction

$$P(\text{wrong prediction}) = \sum_{i=13}^{25} {25 \choose i} \varepsilon^{i} (1-\varepsilon)^{25-i} = 0.06$$



Tan, Steinbach, Kumar

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## **Sampling Strategies**

Two sampling strategies

## Sampling data

 select a subset of the data → Each tree is trained on different data

## Sampling attributes

 select a subset of attributes → corresponding nodes in different trees (usually) don't use the same feature to split

## **Random Forests: Algorithm**

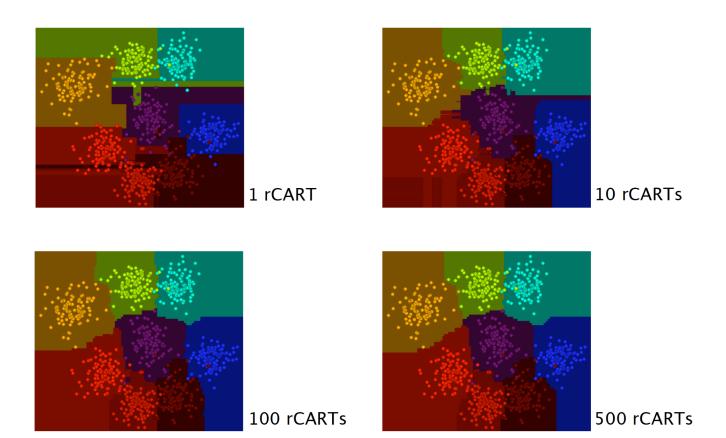
- 1. Draw K bootstrap **samples of size N** from original dataset, with replacement (bootstrapping) [all attributes taken]
- 2. While constructing the decision tree, select a random set of **m attributes** out of the p attributes available to infer split (feature bagging)

  some attributes taken

#### Typical parameters

- m ≈ sqrt(p), or smaller
- K≈500

## **Illustration of Random Forests**



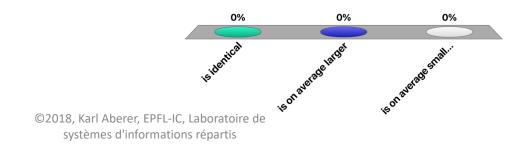
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## The computational cost for constructing a RF with K as compared to constructing K decision trees on the same data

- A. is identical
- B. is on average larger
- C. is on average smaller

we use lesser attributes. lesser branches



#### **Characteristics of Random Forests**

## Strengths

- Ensembles can model extremely complex decision boundaries without overfitting
- Probably the most popular classifier for dense
   data (<= a few thousand features)</li>
- Easy to implement (train a lot of trees)
- Parallelizes easily, good match for MapReduce

#### **Characteristics of Random Forests**

#### Weaknesses

- Deep Neural Networks generally do better
- Needs many passes over the data at least the max depth of the trees
- Relatively easy to overfit hard to balance accuracy/fit tradeoff

#### References

#### **Textbook**

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 Morgan Kaufman, 2000, ISBN 1-55860-489-8

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