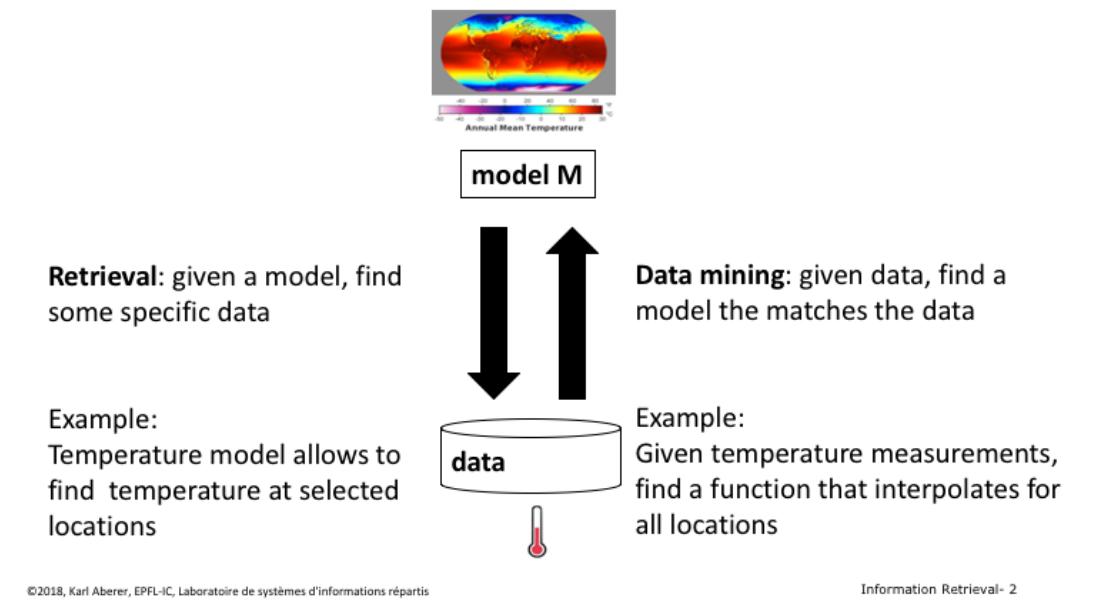


# **Information Retrieval – Vector Space Retrieval**

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Information Retrieval- 1

# Information Management Tasks



Since the central role of an information system is to support a model of a real-world phenomenon based on data, the key information management tasks are related to the interplay between data and models. We can identify two directions for this interplay: from models to data, and from data to models. From models to data is commonly what we understand by **retrieval**, or information retrieval.

Given a model, we would like to learn about specific aspects of reality. If we have a model of the temperature distribution in the world, we would like to retrieve the temperature at a specific location or the global average temperature. For Web search we would use a model of how search terms provided by user to a Web search engine relate to documents considered as being relevant by the user, to retrieve the results of a user query.

Going from data to models is what is commonly called data mining. Often we find big data collections for which we do not have a proper or only incomplete interpretation. For example, we might have temperature measurements at given points, but do not understand the correlations among those measurements or the values at locations without measurements. If we have large document collections, we do not understand which are the topics that are covered by those documents. Data mining deals with the problem of providing algorithms that reveal hidden structures in data in order to create new models. Both information retrieval and data mining will be central topics that will be covered in this course.

## **What do you think ?**

How is a Web search engine working ?

## **Overview**

1. Information Retrieval
2. Text-Based Information Retrieval
3. Vector Space Retrieval
4. Probabilistic Information Retrieval
5. Query Expansion
6. Inverted Index
7. Distributed Retrieval
8. Latent Semantic Indexing
9. Word Embeddings
10. Link-Based Ranking

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Information Retrieval- 4

# **1. INFORMATION RETRIEVAL**

## What is Information Retrieval?

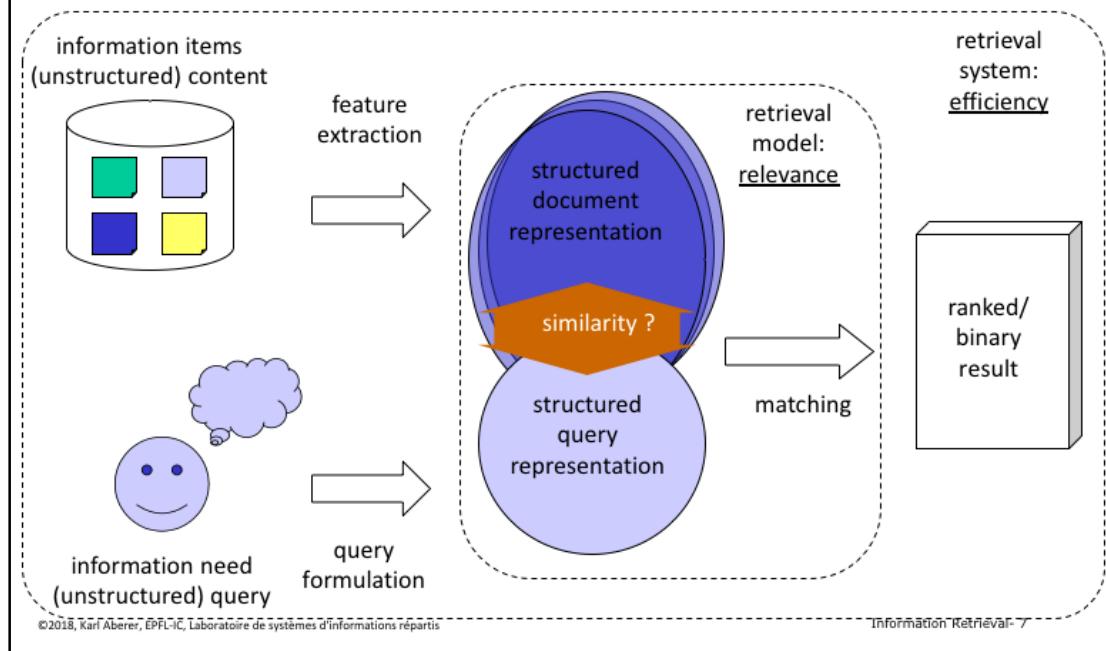
Information retrieval (IR) is the task of finding in a large collection of documents those that satisfy the information needs of a user

- Documents are mostly unstructured data
- Most of the time text documents are considered

Information retrieval deals with the problem of matching information needs of human users with information provided in large document collections. Important aspects of this definition are:

- Documents are largely unstructured data; documents can be based on different media, including text, images, videos
- Document collections are generally large, with the Web being a prime example of a very large document collection
- Information needs are user-driven; there exists no formal (mathematical) definition of the information retrieval task

# Information Retrieval



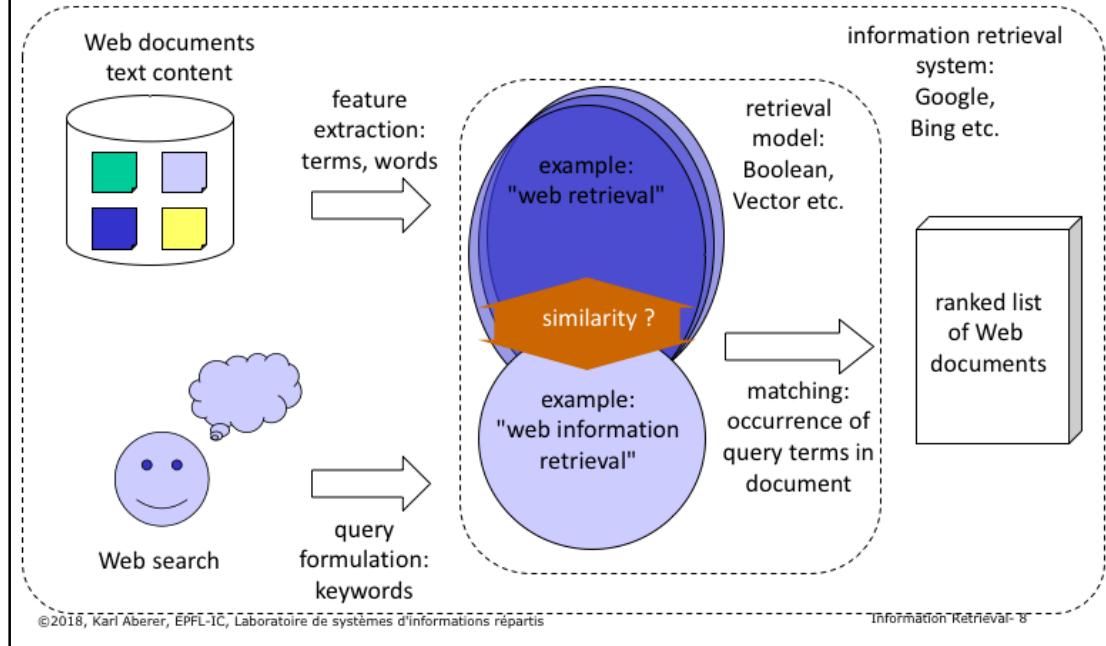
An information retrieval system has to deal with the following tasks:

- Generating structured representations of information items: this process is called **feature extraction** and can include simple tasks, such as extracting words from a text as well as complex methods, e.g., for image or video analysis.
- Generating structured representations of information needs: often this task is solved by providing users with a query language and leave the formulation of structured queries to them. This is the case, for example, for simple keyword based query languages, as used in Web search engines. Some information retrieval systems also support the user in the **query formulation**, e.g., through visual interfaces.
- Matching of information needs with information items: this is the algorithmic task of computing similarity of information items and retrieval queries. The heart of this step is the **information retrieval model**. Similarity measures on the structured representations of queries and documents are used to model **relevance** of information for users. As a result, a selection of relevant information items or a ranked result can be presented to the user.

Since information retrieval systems deal usually with large information collections and/or large user communities, the **efficiency** of an information retrieval system is crucial. This imposes fundamental constraints on the retrieval model. Retrieval models that would capture relevance very well, but are computationally prohibitively expensive, are not suitable for an information retrieval system.



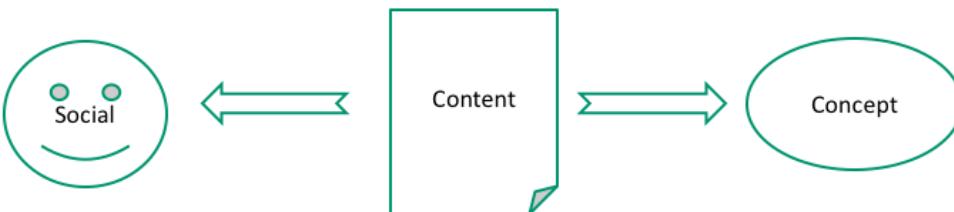
## Example: Text Retrieval



The most popular information retrieval system are Web search engines. To a large degree, they are text retrieval systems, since they exploit mainly the textual content of Web documents for retrieval. However, current Web search engines also exploit link information and even image information. The three tasks of a Web search engine for retrieval are:

1. extracting the textual features, which are the words or terms that occur in the documents. We assume that the web search engine has already collected the documents from the Web using a Web crawler.
2. support the formulation of textual queries. This is usually done by allowing the entry of keywords through Web forms.
3. computing the similarity of documents with the query and producing from that a ranked result. Here Web search engines use standard text retrieval methods, such as Boolean retrieval and vector space retrieval. We will introduce these methods in detail in this lecture later.

# What are the constituents of a document?



People can be

- Authors of documents
- Consumers of documents
- Mentioned within the documents
- Explicitly annotated or automatically extracted

Content consists of the text, and possibly other media, such as images, videos

Concepts are general ideas mentioned, they can be

- Explicitly annotated, e.g., hashtags, keywords
- Automatically extracted, e.g., entities, concepts

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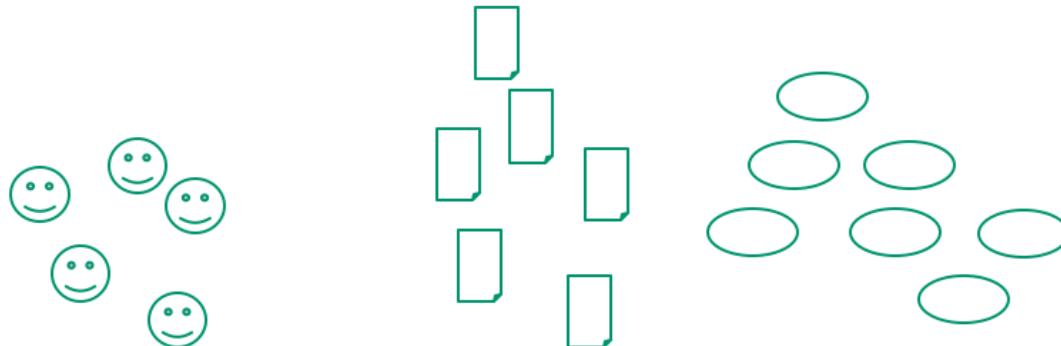
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In general, there are **three types of features** that can be associated with a document:

1. The document **content**: depending on the media this is the characters of text, the pixels of an image, the images of a video. In information retrieval features extracted of the content are the main source of input for retrieval methods to create structured representations of the documents. It is important to note that these structured representations are only used internally to the retrieval system and not visible to the human user. We will first strongly focus on content-based information retrieval for text documents.
2. The **authors** of the document: documents are authored, referenced and consumed by people. This social context can provide very useful to enhance the performance of information retrieval algorithms
3. The **concepts** mentioned in document: concepts are general ideas that have a specific meaning to humans and thus are – different to content features – visible to human users. They can be either manually annotated or automatically extracted, and also help in the retrieval task. Since they are human-understandable, they can

be in fact explicitly used in order to perform structured searches for documents. We will see in the last part of the lecture (extracting knowledge from documents) how automated methods can extract concepts from documents.

# Relationships!



People interact among each other through documents:  
SOCIAL NETWORKS / COMMUNITIES / INFLUENCE

Documents share similar content:  
SEARCH / CLUSTERING / TOPICS / CLASSIFICATION

Concepts have relationships:  
TAXONOMIES / ONTOLOGIES

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Information Retrieval- 10

Each type of the aforementioned features is used to create relationships:

- Content-based features are used to compute document similarity, one of the basic approaches in information retrieval, this part of the lecture. Document similarity allows to search, cluster or classify documents
- Social features are used to create social networks, which can then be analyzed for influence (used in information retrieval) or communities (we will see in the lecture part on data mining how to extract communities)
- Concept features can be organized through semantic relationships in taxonomies and ontologies, which allow to classify and search documents (we will see in the lecture part on knowledge extraction how to infer such relationships)

## Retrieval Model

The retrieval model determines

- the structure of the document representation
- the structure of the query representation
- the similarity matching function

Relevance

- determined by the similarity matching function
- should reflect right topic, user needs, authority, recency
- no objective measure

The heart of an information retrieval system is its retrieval model. The retrieval model is used to capture the meaning of documents and queries, and determine from that the relevance of documents with respect to queries. Although there exist a number of intuitive notions of what determines relevance one must keep clearly in mind that it is not an objective measure.

## Evaluating a Retrieval Model

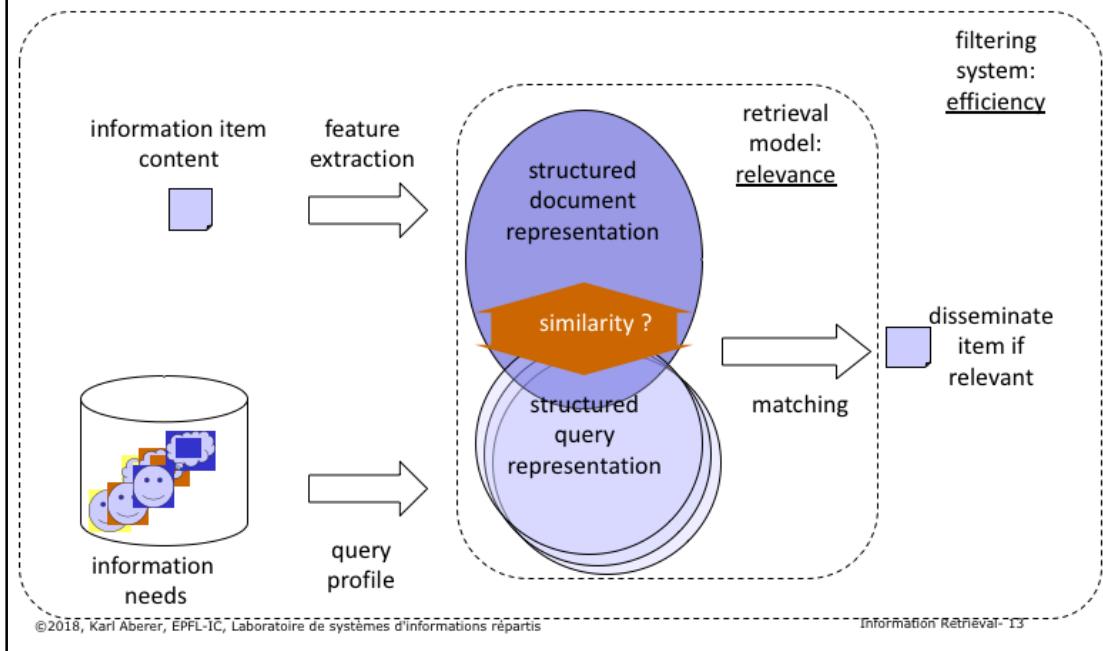
Quality of a retrieval model depends on how well it matches user needs!

Comparison to database querying

- correct evaluation of a class of query language expressions
- can be used to implement a retrieval model

The quality of a retrieval system can principally only be determined through the degree of satisfaction of its users. This is fundamentally different to database querying, where there exist criteria for correct query answering that can be formally verified, e.g., whether a result set retrieved from a database matches the logical conditions specified in a query.

# Information Filtering



The roles of documents and queries can be swapped in an information retrieval system. As a result one obtains an information filtering system. Information filtering systems can be based on the same retrieval models as standard information retrieval systems for ad-hoc query access.

retrieval model stays the same but does not output a ranked list.

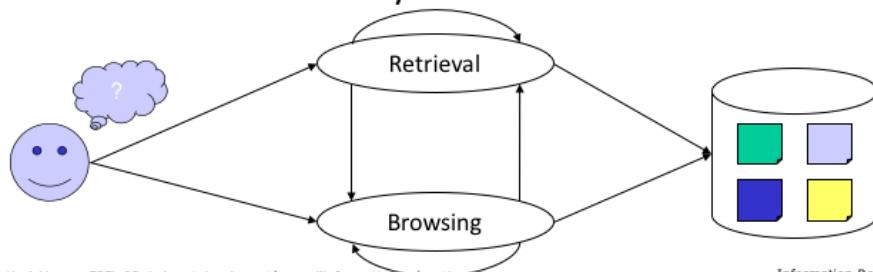
# Information Retrieval and Browsing

## Retrieval

- Produce a ranked result from a user request
- Interpretation of the information by the system

## Browsing

- Let the user navigate in the information set
- Relevance feedback by the human



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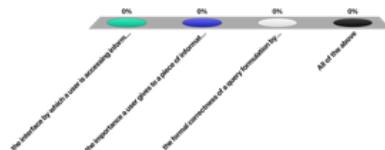
Information Retrieval- 14

Information retrieval is usually closely connected to the task of browsing. Browsing is the explorative access by users to large document collections. By browsing a user implicitly specifies his/her information needs through selection of documents. This feedback can be used by an information retrieval system in order to improve its query representation and thus the retrieval result. One example of such an approach we will see when introducing relevance feedback. On the other hand, results returned by information retrieval systems are usually large, and therefore browsing is needed by users in order to explore the results. Both activities, retrieval and browsing thus can be combined into an iterative process.

relevance feedback

## A retrieval model attempts to model ...

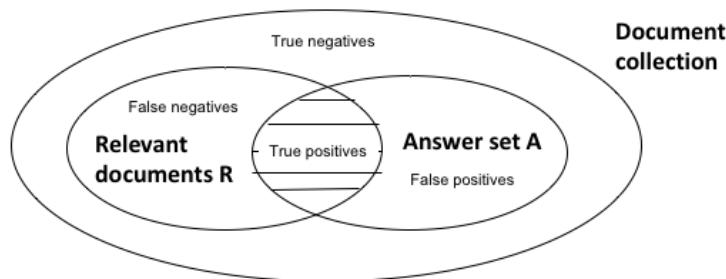
1. the interface by which a user is accessing information
2. the importance a user gives to a piece of information
3. the formal correctness of a query formulation by user
4. All of the above



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# Evaluating Information Retrieval

Test collections, where the relevant documents are identified manually are used to determine the quality of an IR system (e.g. TREC)



Since there exists no objective criterion whether an information retrieval query is correctly answered, other means for evaluating the quality of an information retrieval system are required. The approach is to compare the performance of a specific system to human performance in retrieval. For that purpose test collections of documents, such as TREC (<http://trec.nist.gov/>), are created and for selected queries human experts select the relevant documents. Note that this approach assumes that humans have an agreed-upon, objective notion of relevance, an assumption that can be easily challenged of course.

## Recall and Precision

*Recall* is the fraction of relevant documents retrieved from the set of total relevant documents collection-wide

*Precision* is the fraction of relevant documents retrieved from the total number retrieved (answer set)

	Relevant	Non-relevant
Retrieved	True positives (tp)	False positives (fp)
Not Retrieved	False negatives (fn)	True negatives (tn)

$$R = \frac{tp}{tp + fn} = P(\text{retrieved}|\text{relevant})$$

$$P = \frac{tp}{tp + fp} = P(\text{relevant}|\text{retrieved})$$

The results of IR systems are compared to the expected result in two ways:

1. **Recall** measures how large a fraction of the expected results is actually found.
2. **Precision** measures how many of the results returned are actually relevant.

Important note: This measure evaluates an **unranked** result set. All elements of the result are considered as equally important.

## A simple example of recall and precision

Suppose you search for “Theory of Relativity”.

Recall: Imagine all pages mentioning “theory” and “relativ\*” are returned. We will have probably most documents talking about the topic

Precision: We might have results such as, “In theory, I feel relatively good”, “Relative to the theory of evolution ...” etc.

Thus high recall hurts precision

This example expands upon the point that we made in the previous slide. Simply recalling all web pages that match the search query does not ensure precision—in other words relevance to user needs is not a simple matter.

## Combined Measures

Sometimes we want to characterize the performance of a retrieval system by one number

F-Measure: weighted harmonic mean

$$F = \frac{1}{\alpha \frac{1}{P} + (1 - \alpha) \frac{1}{R}}, \quad \alpha \in [0,1]$$

$$\text{F1: balanced F-Measure with } \alpha = \frac{1}{2}: \quad F1 = \frac{2PR}{P+R}$$

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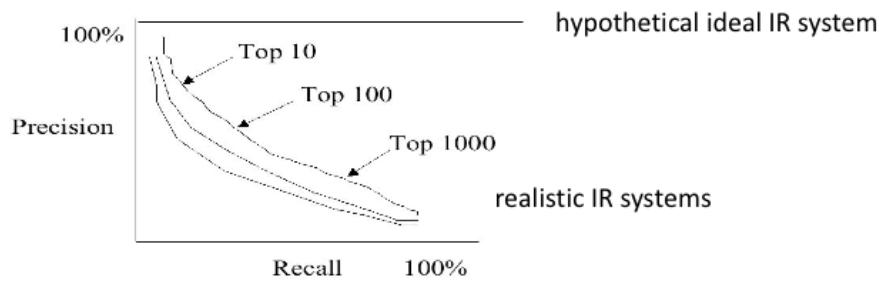
Sometimes one wants to characterize the performance of a retrieval system by a single measures. Different types of means could be considered, e.g., the arithmetic mean or the accuracy measure, i.e.  $(tp + tn) / (tp + tn + fp + fn)$ . Accuracy, which is used in evaluating quality of classifiers could be considered, as retrieval can be understood as the problem of classifying into two sets, relevant and non-relevant. However, since the set of relevant documents is usually much smaller than the set of non-relevant documents, the measure could be optimized by declaring all documents non-relevant.

Arithmetic mean is also no suitable, since when choosing 100% recall we would always have at least 50% of arithmetic mean between recall and precision. Therefore in practice the harmonic mean is used. It can be tuned by the parameter alpha. Larger values of alpha emphasize the importance of precision and smaller ones the importance of recall

## Precision/Recall Tradeoff

An IR system ranks documents by a similarity coefficient, allowing the user to trade off between precision and recall by choosing the cutoff level

Precision depends on the number of results retrieved:  
 $P@k$  = precision for the top-k documents



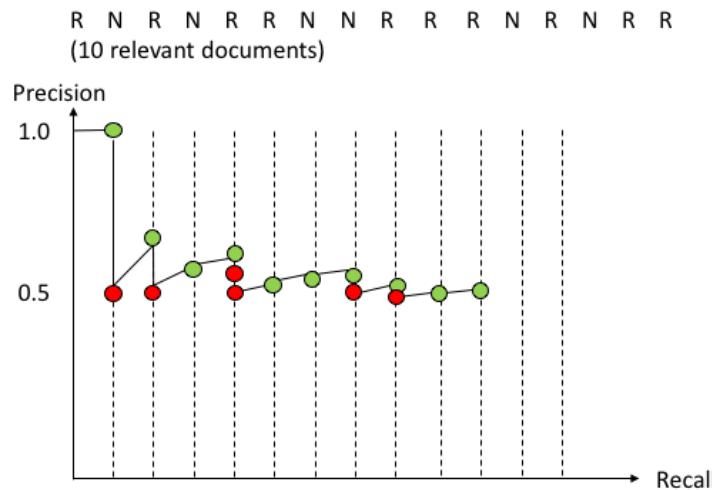
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Information Retrieval- 20

One of the two measures of recall and precision can always be optimized. Recall can be optimized by simply returning the whole document collection, whereas precision can be optimized by returning only very few results. Important is the trade-off: the higher the precision for a specific recall, the better the information retrieval system. A hypothetical, optimal information retrieval system would return results with 100% percent precision always. If a system ranks the results according to relevance the user can control the relation between recall and precision by selecting a threshold of how many results he/she inspects.

## Evaluating Ranked Retrieval

Recall-Precision Plot



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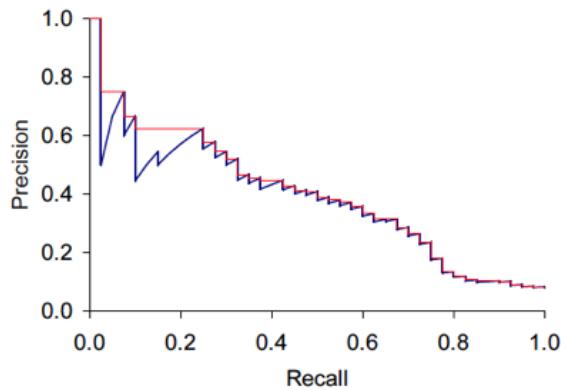
Information Retrieval- 21

If we draw precisely the Recall-Precision graph for a ranked retrieval result, we will find the following picture. The precision will always drop when non-relevant documents are returned and increase when relevant documents are returned.

R - relevant

N - not relevant

## Evaluating Ranked Retrieval



$$\text{Interpolated precision: } P_{int}(R) = \max_{R' \geq R} R'$$

In order to smooth this behavior the interpolated precision is often used which returns always the highest level of precision achieved up to a given recall level.

## Mean Average Precision (MAP)

Given a set of queries Q

For each  $q_j \in Q$  the set of relevant documents  $\{d_1, \dots d_{m_j}\}$

$R_{jk}$  the top k documents for query  $q_j$

$P(R_{jk})$  precision of result  $R_{jk}$

$$MAP(Q) = \frac{1}{|Q|} \sum_{j=1}^{|Q|} \frac{1}{m_j} \sum_{k=1}^{m_j} P(R_{jk})$$

Mean Average Precision has been shown to be a robust measure for evaluating the quality of a ranked retrieval system for a query collection Q. When a relevant document is not retrieved at all, the precision value in the MAP is 0.

## Example

Assume 4 results are returned for a query q:

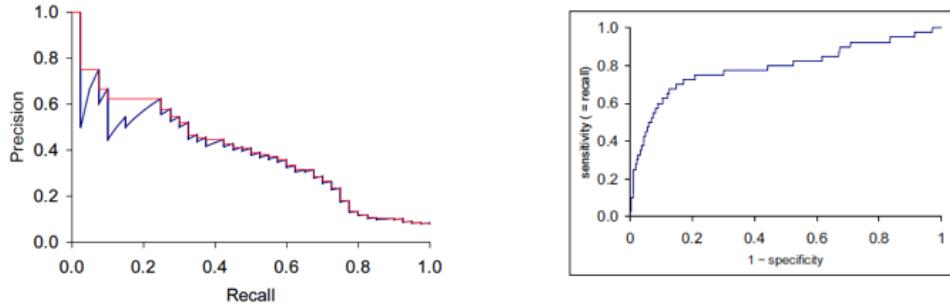
R N R N

$P@1 = 1, P@2 = 0.5, P@3 = 2/3, P@4 = 0.5$

Then  $MAP(\{q\}) = \frac{1}{4} (1 + 0.5 + 2/3 + 0.5) = 2/3$

A simple example where the query set Q to be evaluated consists of a single query q. For multiple queries the results would be averaged.

## ROC Curve



$$\text{Specificity: } 1 - S = \frac{fp}{fp + tn} = P(\text{retrieved} | \text{not relevant})$$

Specificity gives information about how many of the true negatives have been retrieved as false positives

- The steeper the curve rises at the beginning, the better
- The larger the area under the curve, the better

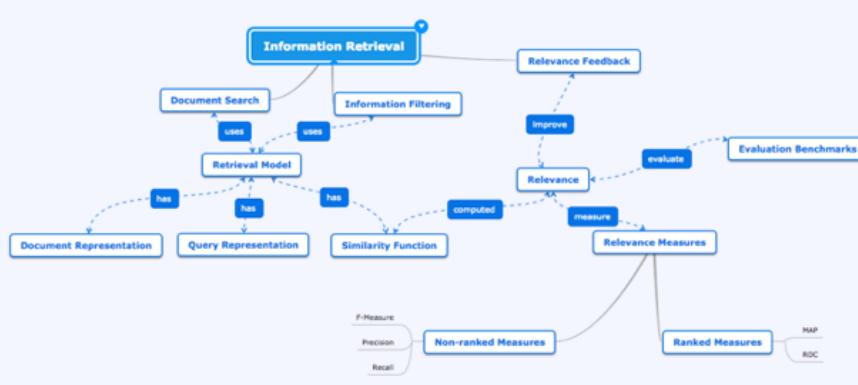
Another frequently used approach to globally evaluate ranked retrieval is the ROC curve. The ROC curve is frequently loosely called a recall-precision curve, which is not accurate (as the figure shows).

The ROC curve relates specificity (on the x-axis) to recall (on the y-axis). Specificity measures the fraction of true negatives that are detected in proportion to all negatives. Thus 1 – specificity is the rate of false positives that have been retrieved, the so-called **false positive rate (FPR)**. In other words, it is the fraction of non-relevant documents among all non-relevant documents that occur in the result. The desired behavior of an IR system is that the curve raises quickly at the beginning, which means that many relevant results are retrieved without having a high fraction of non-relevant documents. This is also equivalent to saying that the area under the curve should be large. Therefore, the area under the ROC curve is sometimes considered similarly as an evaluation of the overall retrieval quality of a retrieval system, analogous to the MAP measure.

Example:

- When the recall is at 0.5 then  $1-S$  is at 0.1. This implies that  $S$  is 0.9. Then we can conclude that  $fp = 1/9 tn$ , or in other words when retrieving half of the relevant documents, then we have also retrieved about 10% of the non-relevant documents.

# Summary of Concepts

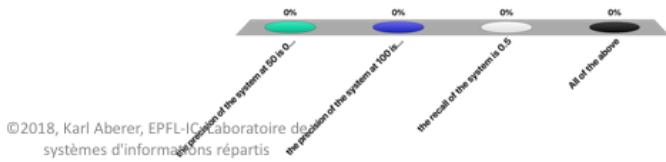


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Q: If the top 100 documents contain 50 relevant documents ...

1. the precision of the system at 50 is 0.25
2. the precision of the system at 100 is 0.5
3. the recall of the system is 0.5
4. All of the above



## If retrieval system A has a higher precision than system B ...

1. the top k documents of A will have higher similarity values than the top k documents of B
2. the top k documents of A will contain more relevant documents than the top k documents of B
3. A will recall more documents above a given similarity threshold than B
4. relevant documents in A will have higher similarity values than in B



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## **2. TEXT-BASED INFORMATION RETRIEVAL**

## Text-based Information Retrieval

Most of the information needs and content are expressed in natural language

- Library and document management systems
- Web (Search Engines)

Basic approach: use the words that occur in a text as *features* for the interpretation of the content

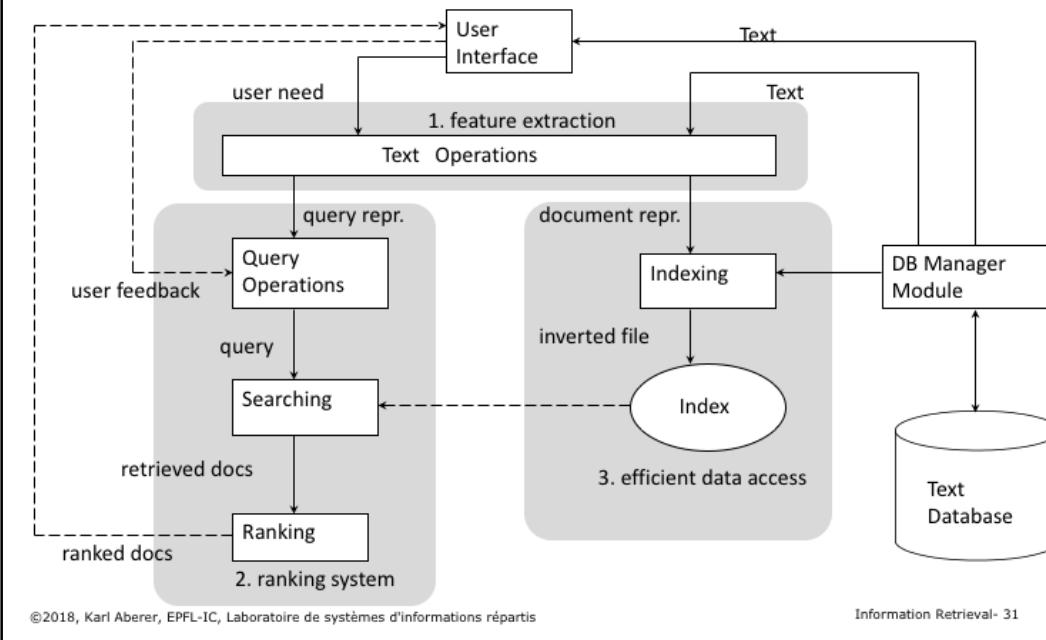
- This is called the "full text" retrieval approach
- Ignore grammar, meaning etc.
- Simplification that has proven successful
- Document structure, layout and metadata may be taken into account additionally (e.g. PageRank/Google)

Traditional information retrieval has been primarily concerned over many years with the problem of retrieving information from large bodies of documents with mostly textual content, as they were typically found in library and document management systems. The problems addressed were classification and categorization of documents, systems and languages for retrieval, user interfaces and visualization. The area was perceived as being one of narrow interest for a highly specialized user community, mainly librarians. The advent of the WWW changed this perception completely, as the web is a universal repository of documents with universal access.

Since nowadays most of the information content is still available in textual form, text is an important basis for information retrieval. Natural language text carries a lot of meaning, which still cannot fully be captured computationally. The research in cognitive science, especially linguistics suggests that perhaps this can never be done. Therefore information retrieval systems are based on strongly simplified models of text, ignoring most of the grammatical structure of text and reducing texts essentially to the terms they contain. This approach is called full text retrieval and is a simplification that has proven to be very successful. Nowadays, this approach is gradually

extended by taking into account other features of documents, such as the document or link structure.

# Architecture of Text Retrieval Systems

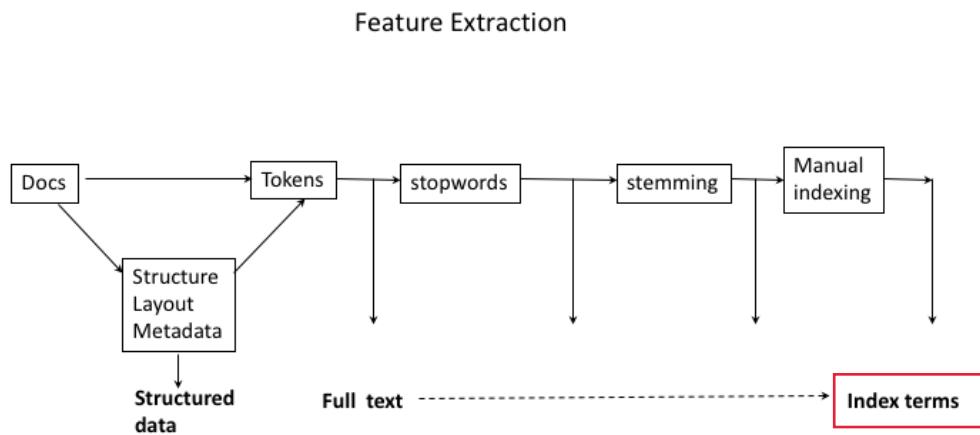


This figure illustrates the basic architecture with the different functional components of a text retrieval system. We can distinguish three main groups of components:

1. the **feature extraction component**: it performs text processing to turn queries and text documents into a keyword-based representation
2. the **ranking system**: it implements the retrieval model. In a first step user queries are potentially modified (in particular if user relevance feedback is used), then the documents required for producing the result are retrieved from the database and finally the similarity values are computed according to the retrieval model in order to compute the ranked result.
3. the **data access system**: it supports the ranking system by **efficiently retrieving documents** containing specific keywords from large document collections. The standard technique to implement this component is called **inverted files**.

In addition we recognize two components to interface the system to the user on the one hand, and to the data collection on the other hand.

# Pre-Processing Text for Text Retrieval



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In full text retrieval each document is represented by a set of representative keywords or index terms. Using index terms is an ancient concept that has been used in books. The earliest example of an index is from a temple library in Babylon, cataloging the subjects of the cuneiforms. An index term is a document word useful for capturing the document's main topics. Often, index terms are only nouns, because nouns carry meaning by themselves, whereas verbs express relationships between words. These relationships are more difficult to extract.

When using words as text features normally a stepwise processing approach is taken: in a first step, the document structure, e.g., from XML, is extracted and if required stored for further processing. The remaining text is stripped of special characters, producing the full text of the document as a sequence of tokens. Then very frequent words which are not useful for retrieval, so-called "stopwords", are eliminated (e.g. "a", "and" etc.). As the same word can occur in natural language in different forms, usually stemming is used: Stemming eliminates grammatical variations of the same word by reducing it to a word root, e.g., the words connecting, connection, connections would be reduced to the same "stem" connect. This step

can be followed by a manual intervention, where humans can select or add index terms based on their understanding of the semantics of the document. The result of the process is a set of index terms which represents the document.

## Text Retrieval - Basic Concepts and Notations

*Document d:* expresses ideas about some topic in a natural language

*Query q:* expresses an information need for documents pertaining to some topic

*Index term:* a semantic unit, a word, short phrase, or potentially root of a word

*Database DB:* collection of  $n$  documents  $d_j \in DB, j=1, \dots, n$

*Vocabulary T:* collection of  $m$  index terms  $k_i \in T, i=1, \dots, m$

A document is represented by a set of index terms  $k_i$

The importance of an index term  $k_i$  for the meaning of a document  $d_j$  is represented by a weight  $w_{ij} \in [0,1]$ ; we write  $d_j = (w_{1j}, \dots, w_{mj})$

The IR system assigns a *similarity coefficient*  $sim(q, d_j)$  as an estimate for the relevance of a document  $d_j \in DB$  for a query  $q$ .

We introduce the precise terminology we will use in the following for text retrieval systems. Note that the way of how specific weights are assigned to an index term with respect to a document and of how similarity coefficients are computed are part of the definition of the text retrieval model.

## Example: Documents

- B1 A Course on Integral Equations
- B2 Attractors for Semigroups and Evolution Equations
- B3 Automatic Differentiation of Algorithms: Theory, Implementation, and Application
- B4 Geometrical Aspects of Partial Differential Equations
- B5 Ideals, Varieties, and Algorithms: An Introduction to Computational Algebraic Geometry and Commutative Algebra
- B6 Introduction to Hamiltonian Dynamical Systems and the N-Body Problem
- B7 Knapsack Problems: Algorithms and Computer Implementations
- B8 Methods of Solving Singular Systems of Ordinary Differential Equations
- B9 Nonlinear Systems
- B10 Ordinary Differential Equations
- B11 Oscillation Theory for Neutral Differential Equations with Delay
- B12 Oscillation Theory of Delay Differential Equations
- B13 Pseudodifferential Operators and Nonlinear Partial Differential Equations
- B14 Sinc Methods for Quadrature and Differential Equations
- B15 Stability of Stochastic Differential Equations with Respect to Semi-Martingales
- B16 The Boundary Integral Approach to Static and Dynamic Contact Problems
- B17 The Double Mellin-Barnes Type Integrals and Their Applications to Convolution Theory

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This is an example of a (simple) document collection that we will use in the following as running example.

# Term-Document Matrix

Matrix of weights  $w_{ij}$

Terms	Documents																
	B1	B2	B3	B4	B5	B6	B7	B8	B9	B10	B11	B12	B13	B14	B15	B16	B17
algorithms	0	0	1	0	1	0	1	0	0	0	0	0	0	0	0	0	0
application	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1
delay	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0
differential	0	0	0	1	0	0	0	1	0	1	1	1	1	1	1	0	0
equations	1	1	0	1	0	0	0	1	0	1	1	1	1	1	1	0	0
implementation	0	0	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0
integral	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1
introduction	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0
methods	0	0	0	0	0	0	0	1	0	0	0	0	0	1	0	0	0
nonlinear	0	0	0	0	0	0	0	0	1	0	0	0	1	0	0	0	0
ordinary	0	0	0	0	0	0	0	1	0	1	0	0	0	0	0	0	0
oscillation	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0
partial	0	0	0	1	0	0	0	0	0	0	0	0	1	0	0	0	0
problem	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	1	0
systems	0	0	0	0	0	1	0	1	1	0	0	0	0	0	0	0	0
theory	0	0	1	0	0	0	0	0	0	0	1	1	0	0	0	0	1

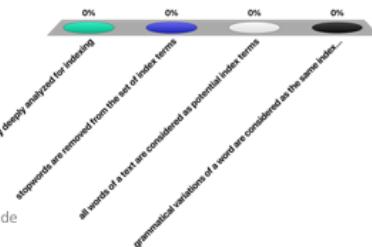
## Example

- Vocabulary (contains only terms that occur multiple times, no stop words)
- all weights are set to 1 (equal importance)

In text retrieval we represent the relationship between the index terms and the documents in a term-document matrix. In this example only a selected vocabulary is used for retrieval, consisting of all index terms that occur in more than one document and only weights of 1 are assigned, indicating that the term occurs in the document.

## Full-text retrieval refers to the fact that ...

1. the document text is grammatically deeply analyzed for indexing
2. stopwords are removed from the set of index terms
3. all words of a text are considered as potential index terms
4. grammatical variations of a word are considered as the same index terms

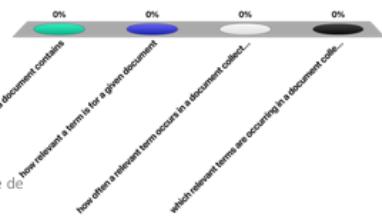


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The entries of a term-document matrix indicate ...

1. how many relevant terms a document contains
2. how relevant a term is for a given document
3. how often a relevant term occurs in a document collection
4. which relevant terms are occurring in a document collection

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## Boolean Retrieval

Users specify which terms should be present in the documents

- Simple, based on set-theory, precise meaning
- Frequently used in (old) library systems
- Still many applications, e.g., web harvesting

Example query

- "application" AND "theory" → answer: B3, B17

### Retrieval Language

$\text{expr} ::= \text{term} \mid (\text{expr}) \mid \text{NOT expr} \mid \text{expr AND expr} \mid \text{expr OR expr}$

### Weights for index terms appearing in documents

$w_{ij} = 1$  if  $k_i \in d_j$  and 0 otherwise

Early information retrieval systems (as well as many search systems in use today, such as spotlight and windows search) use the Boolean retrieval model. This model is actually more similar to database querying, as requests are specified as first order (Boolean) expressions. Term weights are set to 1 when a term occurs in a document, just as in the term-document matrix on the previous slide.

## "Similarity" Computation in Boolean Retrieval

### Step 1:

Determine the disjunctive normal form of the query  $q$

- A disjunction of conjunctions
- Using distributivity and Morgans laws, e.g.  $\text{NOT}(s \text{ AND } t) \equiv \text{NOT } s \text{ OR NOT } t$
- Thus  $q = ct_1 \text{ OR } \dots \text{ OR } ct_l$  where  $ct = \underline{t}_1 \text{ AND } \dots \text{ AND } \underline{t}_k$  and  $\underline{t} \in \{t, \text{NOT } t\}$

### Step 2:

For each conjunctive term  $ct$  create its weight vector  $\text{vec}(ct)$

- $\text{vec}(ct) = (w_1, \dots, w_m)$  :
  - $w_i = 1$  if  $k_i$  occurs in  $ct$
  - $w_i = -1$  if  $\text{NOT } k_i$  occurs in  $ct$
  - $w_i = 0$  otherwise

Computing the similarity of a document with a query reduces in Boolean retrieval to the problem of checking whether the term occurrences in the document satisfy the Boolean condition specified by the query. In order to do this in a systematic manner, a Boolean query is first normalized into **disjunctive normal form**. Using this equivalent representation, checking whether a document matches the query reduces to the problem of checking whether the document vector, i.e., the column of the term-document matrix corresponding to the document, matches one of the conjunctive terms of the query.

## "Similarity" Computation in Boolean Retrieval

Step 3:

If one weight vector of a conjunctive term  $ct$  in  $q$  matches the document weight vector  $d_j = (w_{1j}, \dots, w_{mj})$  of a document  $d_j$ , then the document  $d_j$  is relevant, i.e.,

$$sim(d_j, q) = 1$$

–  $vec(ct)$  matches  $d_j$  if:

$$w_i = 1 \wedge w_{ij} = 1$$

$$w_i = -1 \wedge w_{ij} = 0$$

A match is established if the document vector contains all the terms of the query vector in the correct form, i.e., if the term occurs positively in the query the term has to occur in the document, if the term occurs in the negated form in the query the term must not occur, and if the term does not occur in the query it may or may not occur in the document.

## Example

Index terms       $\{application, algorithm, theory\}$

Query             $"application" \text{ AND } ("algorithm" \text{ OR NOT } "theory")$

Disjunctive normal form of query

$("application" \text{ AND } "algorithm" \text{ AND } "theory") \text{ OR }$

$("application" \text{ AND } "algorithm" \text{ AND NOT } "theory") \text{ OR }$

$("application" \text{ AND NOT } "algorithm" \text{ AND NOT } "theory")$

Query weight vectors       $q=\{(1,1,1), (1,1,-1), (1,-1,-1)\}$

Documents             $d_1=\{algorithm, theory, application\} \quad (1,1,1)$

$d_2=\{algorithm, theory\} \quad (0,1,1)$

$d_3=\{application, algorithm\} \quad (1,1,0)$

Result             $sim(d_1, q) = sim(d_3, q) = 1, sim(d_2, q) = 0$

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This example illustrates a complete Boolean retrieval process for our sample document collection.

The transformation from the original query to the disjunctive normal form proceeds in the following steps:

application AND (algorithm OR NOT theory) ->

(application AND algorithm) OR

(application AND NOT theory)->

(application AND algorithm AND (theory OR NOT theory) OR

(application AND (algorithm or NOT algorithm) AND NOT theory) -

>

(application AND algorithm AND theory) OR

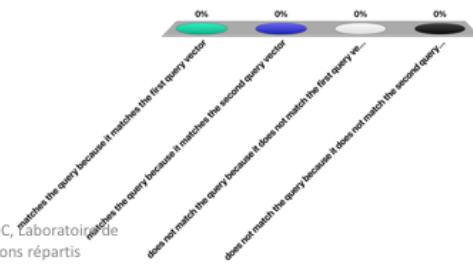
(application AND algorithm AND NOT theory) OR

(application AND algorithm AND NOT theory) OR  
(application AND NOT algorithm AND NOT theory) ->

(application AND algorithm AND theory) OR  
(application AND algorithm AND NOT theory) OR  
(application AND NOT algorithm AND NOT theory)

Let the query be represented by  $\{(1, 0, -1), (0, -1, 1)\}$   
and the document by  $(1, 0, 1)$ . The document ...

1. matches the query because it  
matches the first query vector
2. matches the query because it  
matches the second query  
vector
3. does not match the query  
because it does not match the  
first query vector
4. does not match the query  
because it does not match the  
second query vector



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## **3. VECTOR SPACE RETRIEVAL**

# Vector Space Retrieval

## Limitations of Boolean Retrieval

- No ranking: problems with handling large result sets
- Queries are difficult to formulate
- No tolerance for errors
- Queries either return far too many results, or none

## Key Idea of Vector Space Retrieval

- represent both the document and the query by a weight vector in the m-dimensional keyword space assigning non-binary weights
- determine their distance in the m-dimensional keyword space

The main limitation of the Boolean retrieval model is its incapability to rank the result and to match documents that do not contain all the keywords of the query. More complex requests become very difficult to formulate. Finally it is hard to predict for the user whether a query would produce a reasonably sized set of results. Often either no results are returned, if the query is too restrictive or very large numbers of results are produced in the opposite case.

The vector space retrieval model addresses these issues by supporting non-binary weights, i.e., real numbers in [0,1], both for documents and queries, and producing continuous similarity measures in [0,1]. The similarity measure is derived from the geometrical relationship of vectors in the m-dimensional space of document/query vectors.

## Similarity Computation in Vector Space Retrieval

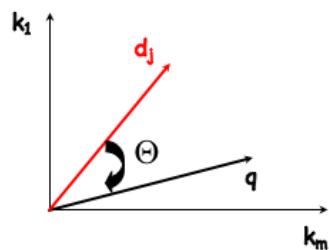
$$\vec{d}_j = (w_{1j}, w_{2j}, \dots, w_{mj}), w_{ij} > 0 \quad \text{if } k_i \in d_j$$

$$\vec{q} = (w_{1q}, w_{2q}, \dots, w_{mq}), w_{iq} \geq 0$$

$$\text{sim}(\vec{q}, \vec{d}_j) = \cos(\theta) = \frac{\vec{d}_j \cdot \vec{q}}{\|\vec{d}_j\| \|\vec{q}\|} = \frac{\sum_{i=1}^m w_{ij} w_{iq}}{\|\vec{d}_j\| \|\vec{q}\|}$$

$$\|v\| = \sqrt{\sum_{i=1}^m v_i^2}$$

Since  $w_{ij} > 0$  and  $w_{iq} \geq 0$ ,  $0 \leq \text{sim}(q, d_j) \leq 1$



The distance measure for vectors has to satisfy the following properties:

- If two vectors coincide completely their similarity should be maximal, i.e., equal to 1.
- If two vectors have no keywords in common, i.e., if wherever the query vector has positive weights the document vector has weight 0, and vice versa – or in other words if the vectors are orthogonal – the similarity should be minimal, i.e., equal to 0.
- in all other cases the similarity should be between 0 and 1.

The scalar product (which is equivalent to the cosine of the angle of two vectors) has exactly these properties and is therefore (normally) used as similarity measure for vector space retrieval.

# Vector Space Retrieval - Properties

## Properties

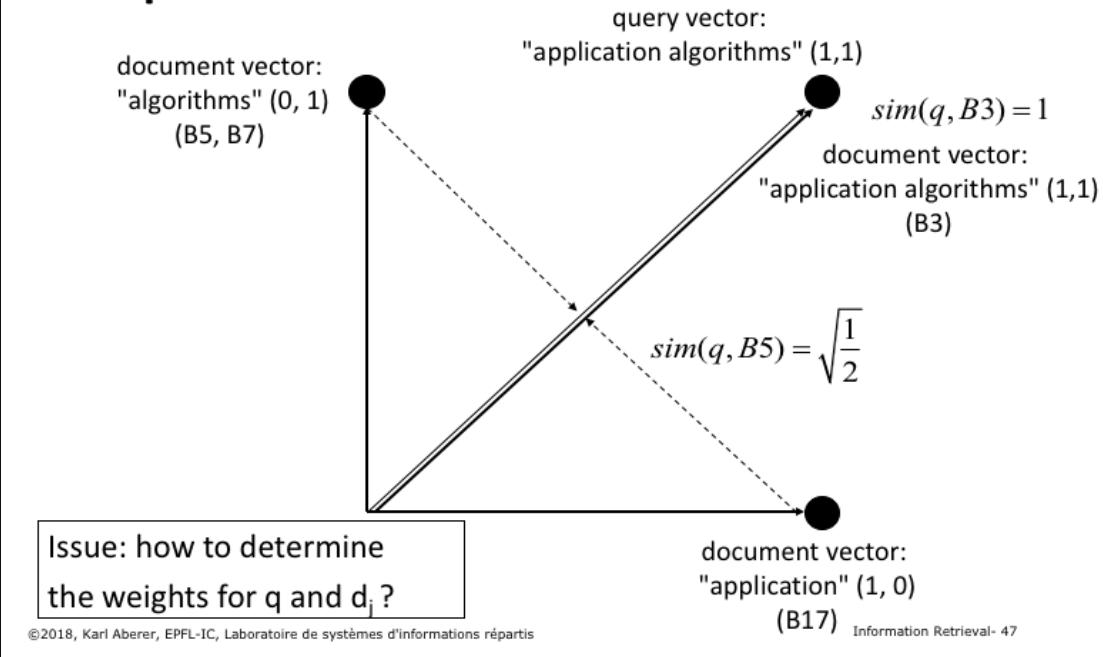
- Ranking of documents according to similarity value
- Documents can be retrieved even if they don't contain some query keyword

## Today's standard text retrieval technique

- Web Search Engines
- The vector model is the basis of most search engines, however they do not rely on it exclusively
- It is simple and fast to compute

The vector space retrieval model is the standard retrieval technique used both on the Web and for classical text retrieval.

## Example



We apply the same weighting scheme for the document and query vectors as in the case of Boolean retrieval, and show the results vector space retrieval produces. We observe that also documents containing only one of the two keywords occurring in the query, would show up in the result, although with lower similarity value.

Since in vector space retrieval no longer exclusively binary weights are used, a central question is of how to determine weights that more precisely determine the importance of a term for the document.

Obviously not all terms carry the same amount of information on the meaning of a document. This was for example one of the reasons to eliminate stop words, as they normally carry no meaning at all.

## Term Frequency

Documents are similar if they contain the same keywords (frequently)

- Therefore use the frequency  $freq(i,j)$  of the keyword  $k_i$  in the document  $d_j$  to determine the weight of the document vectors

(Normalized) term frequency of term  $k_i$  in Document  $d_j$

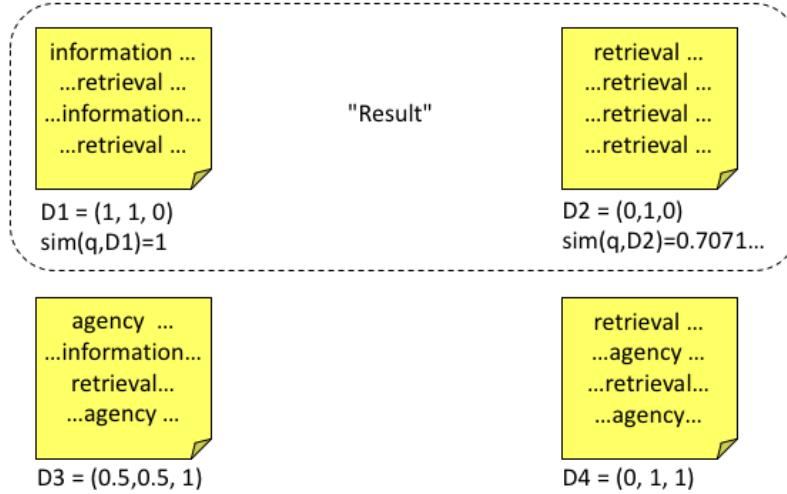
$$tf(i, j) = \frac{freq(i, j)}{\max_{k \in T} freq(k, j)}$$

An obvious difference that can be made among terms is with respect to their frequency of occurrence in a document. Thus a weighting scheme for documents can be defined by considering the (relative) frequency of terms within a document. The term frequency is normalized with respect to the maximal frequency of all terms occurring within the document.

## Example

Vocabulary  $T = \{\text{information}, \text{retrieval}, \text{agency}\}$   
 Query  $q = (\text{information}, \text{retrieval}) = (1, 1, 0)$

$$\text{sim}(\vec{q}, \vec{d}_j) = \frac{\sum_{i=1}^m w_{ij} w_{iq}}{\|\vec{d}_j\| \|\vec{q}\|}$$



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This example illustrates the use of term frequency. Assume we form the query vector by simply setting the weight to 1 if the keyword appears in the query. Then we would obtain D1 and D2 as result. Actually, this result appears to be non-intuitive, since we would expect that D3 is much more similar to q than D2. What has gone wrong?

The problem is that the term "retrieval", since it occurs very frequently in D2, leads to a high similarity value for D2. On the other hand the term retrieval has very little power to disambiguate meaning in this document collection, since every document contains this term. From an information-theoretic perspective one can state, that the term "retrieval" does not reduce the uncertainty about the result at all.

## Inverse Document Frequency

We have not only to consider how frequent a term occurs within a document (measure for similarity), but also how frequent a term is in the document collection of size n (measure for distinctiveness)

Inverse document frequency of term  $k_i$

$$idf(i) = \log\left(\frac{n}{n_i}\right) \in [0, \log(n)]$$

$n_i$  number of documents in which term  $k_i$  occurs

Inverse document frequency can be interpreted as the amount of information associated with the term  $k_i$

Term weight (tf-idf)  $w_{ij} = tf(i,j) idf(i)$

Thus we have to take into account not only the frequency of a term within a document, when determining the importance of the term for characterizing the document, but also the discriminative power of the term with respect to the document collection as a whole. For that purpose, the inverse document frequency is computed and included into the term weight.

We can see now from this weighting scheme that eliminating stop words is actually an optimization of computing similarity measures in vector space retrieval. Since stop words normally occur in every document of a collection, their term weights will normally be 0 and thus the terms do not play a role in retrieval. Thus it is of advantage to exclude them already from the retrieval process at the very beginning.

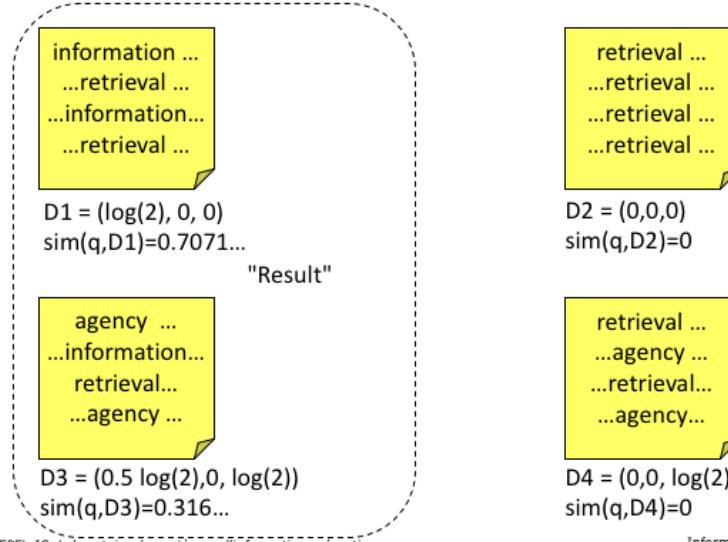
0 if term is frequent in collection - i.e. appears everywhere  
log n if term appears only in 1 document

$$idf(i) = \log\left(\frac{n}{n_i}\right) \in [0, \log(n)]$$

## Example

Vocabulary T = {information, retrieval, agency}  
 Query q = (information, retrieval) = (1,1,0)

idf(information)=idf(agency)=log(2)  
 idf(retrieval)=log(1)=0



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We have now:  $n=4$ ,  $n_{\text{information}}=2$ ,  $n_{\text{retrieval}}=4$ ,  $n_{\text{agency}}=2$

The result corresponds much better to the "expectation" when using the inverse document frequencies.

## Query Weights

The same considerations as for document term weights apply also to query term weights

Query weight for query q

$$w_{iq} = \frac{\text{freq}(i, q)}{\max_{k \in T} \text{freq}(k, q)} \log\left(\frac{n}{n_i}\right)$$

Example: Query q = (information, retrieval)

- Query vector:  $(\log(2), 0, 0)$
- Scores:
  - $\text{sim}(q, D1) = 0.569\dots$
  - $\text{sim}(q, D2) = 0$
  - $\text{sim}(q, D3) = 0.254$
  - $\text{sim}(q, D4) = 0$

Finally, we have to look at the question of how to determine the weights for the query vector. One can apply the same principles as for determining the document vector, as is shown. In practice there exist a number of variations of this approach.

## Example

Query  $q = \text{"application theory"}$

Boolean retrieval result

- application AND theory: B3, B17
- application OR theory: B3, B11, B12, B17

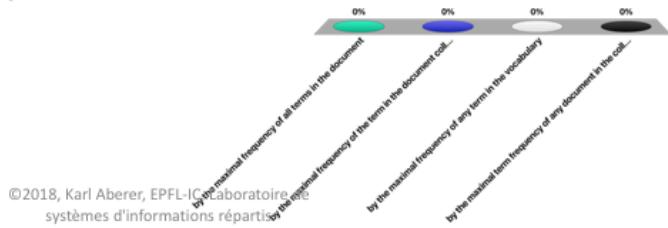
Vector retrieval result

- Query vector  $(0, 2.14\ldots, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1.447\ldots)$
- Ranked Result:
  - B17 0.770078...
  - B3 0.684042...
  - B12 0.232951...
  - B11 0.232951...

This examples provides an illustration of the differences of Boolean and vector space retrieval.

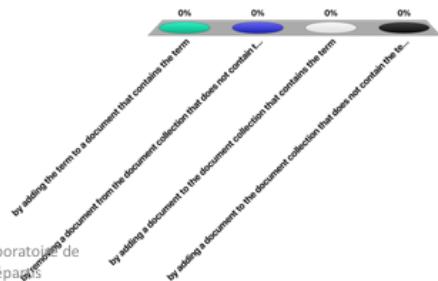
## The term frequency of a term is normalized ...

1. by the maximal frequency of all terms in the document
2. by the maximal frequency of the term in the document collection
3. by the maximal frequency of any term in the vocabulary
4. by the maximal term frequency of any document in the collection



# The inverse document frequency of a term can increase ...

1. by adding the term to a document that contains the term
2. by removing a document from the document collection that does not contain the term
3. by adding a document to the document collection that contains the term
4. by adding a document to the document collection that does not contain the term



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## Variants of Vector Space Retrieval Model

The vector model with tf-idf weights is a good ranking strategy for general collections

- many alternative weighting schemes exist, but are not fundamentally different

Term frequency	Document frequency	Normalization
n (natural) $tf_{t,d}$	n (no)      1	n (none)      1
l (logarithm) $1 + \log(tf_{t,d})$	t (idf) $\log \frac{N}{df_t}$	c (cosine) $\frac{1}{\sqrt{w_1^2 + w_2^2 + \dots + w_M^2}}$
a (augmented) $0.5 + \frac{0.5 \times tf_{t,d}}{\max_t(tf_{t,d})}$	p (prob idf) $\max\{0, \log \frac{N-df_t}{df_t}\}$	u (pivoted unique) $1/u$
b (boolean) $\begin{cases} 1 & \text{if } tf_{t,d} > 0 \\ 0 & \text{otherwise} \end{cases}$		b (byte size) $1/CharLength^\alpha, \alpha < 1$
L (log ave) $\frac{1+\log(tf_{t,d})}{1+\log(\text{ave}_{t \in d}(tf_{t,d}))}$		

Different variants of tf-idf weighting schemes have been developed and used over time. They can be combined with each other, also independently for the weighting of document and query terms. One important variant is the logarithmic weighting of term frequencies, which moderates the influence of very frequently occurring terms in documents.

# Discussion of Vector Space Retrieval Model

## Advantages

- term-weighting improves quality of the answer set
- partial matching allows retrieval of docs that approximate the query conditions
- cosine ranking formula sorts documents according to degree of similarity to the query

## Disadvantages

- assumes independence of index terms; not clear that this is a disadvantage
- No theoretical justification why the model works

We summarize here the main advantages of the vector space retrieval model. It has proven to be a very successful model for general text collections, i.e., if there exists no additional (context) information on the documents that could be exploited, e.g., from a specific application domain. Providing a ranked result improves the usability of the approach, as users can more easily distinguish more relevant documents from less relevant documents. The model inherently assumes that there exist no mutual dependencies in the occurrences of the terms, i.e., that certain terms appear together more frequently than others. Studies have however shown that taking such co-occurrence probabilities additionally into account, can actually HURT the performance of the retrieval system. The reason is that co-occurrence probabilities are often related to specific application domains and thus do not easily transfer to general-purpose retrieval.

One of the principal criticisms of the vector space model is the lack of theoretical explanation why it works. At the end, it is a heuristics. This drawback has been addressed with other models, in particular probabilistic retrieval models.

## **4. PROBABILISTIC INFORMATION RETRIEVAL**

## Probabilistic Information Retrieval

The notion of similarity in the vector space model does not directly imply relevance

- The highest ranked result might be meaningless
- The similarity values have no interpretation, they are just used to rank

Probabilistic IR models attempt to directly model relevance as a probability

One of the key drawbacks of the vector space retrieval model is the lack of interpretability of the similarity values. This gave rise to the development of probabilistic retrieval models, that attempt to “compute” relevance as a probability.

## Query Likelihood Model

Given query  $q$ , determine the probability  $P(d|q)$  that document  $d$  is relevant to query  $q$

### Assumptions

- $P(d)$ , the probability of a document occurring is uniform across a collection
- $P(q)$  is the same for all documents

$$\text{Bayes Rule } P(d|q) = \frac{P(q|d)P(d)}{P(q)}$$

Thus:  $P(d|q)$  can be derived from  $P(q|d)$

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The problem of retrieval can be understood in a probabilistic model as the problem of determining the probability of a document being relevant, given a query. We observe that the probability of document to occur in a collection is constant (which makes sense assuming all documents are different), and the probability of a query to occur is the same for all documents. Thus, using Bayes rule the problem of determining whether a document is relevant for a query is equivalent to the problem of determining whether a query is relevant to a document. The latter probability  $P(q|d)$  is also called the query likelihood.

## Language Modeling

Determine  $P(q|d)$  (= query likelihood)

Assume each document  $d$  is generated by a Language Model  $M_d$

- a language model is a mechanism that generates the words of the language

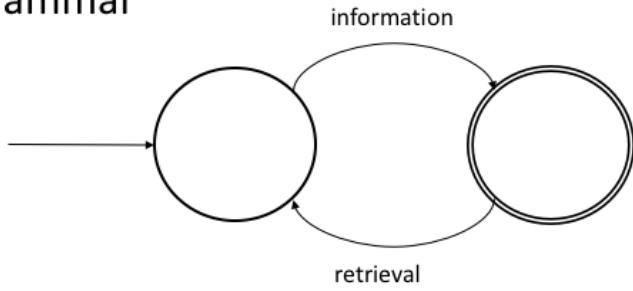
Then  $P(q|d)$  can be interpreted as the probability that the query  $q$  was generated by the language model  $M_d$

The notion of query likelihood gives now rise to the following approach to model relevance. We assume that documents are the result of language model. A language model is a (in general probabilistic) process that produces text, and a given document  $d$  is assumed to be produced by its specific language model  $M_d$ . The problem of retrieval can be viewed in the following way: if a query is relevant to document, it should have been produced by the same language model as the document. Using this argument, the query likelihood corresponds to the probability that the query has been produced by the same language model as the document.

Let's have now a more detailed look in what a language model us and how we use it make this intuitive model operational.

## What is a Language Model?

Deterministic language model = automaton =  
grammar



Can produce:

information retrieval  
information retrieval information retrieval

Cannot produce:

retrieval information

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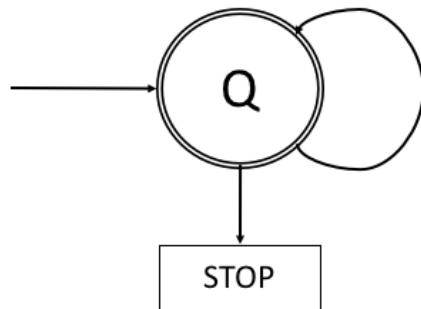
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In the simplest case a language model is a **deterministic automaton**. In theoretical computer science deterministic automata are those that can recognize (or produce) regular languages.

## Probabilistic Language Model

Unigram model: assign a probability to each term to appear

- More complex models can be used, e.g., bigrams



	Model M <sub>1</sub>		Model M <sub>2</sub>
STOP	0.2	STOP	0.25
the	0.2	the	0.15
a	0.1	a	0.12
frog	0.03	frog	0.0002
toad	0.03	toad	0.0001
said	0.02	said	0.01
likes	0.015	likes	0.01
dog	0.01	dog	0.04

Two different language models  
derived from 2 documents

Instead of using a deterministic automaton, we can also use a probabilistic state automaton, in other words, a Markov process. In the simplest case the automaton has a single state, and every state transition emits with a certain probability one term out of a vocabulary. In addition, the automaton can stop with a certain probability. In the two models displayed as examples, this probability is given as  $P(\text{STOP}|Q) = 0.2$

## Probability to Create a Query

What is the probability that a query q has been generated by model M?

*Example:* q = the frog said dog STOP

$$P(q|M_1) = 0.2 * 0.03 * 0.02 * 0.01 * 0.2 = 0.00000024$$

So retrieval becomes the problem of computing for a query q the probability  $P(q|M_d)$  for all the documents d

Given a language model for the generation of documents, we can now compute within that model the probability that a given query q has been generated by the model. We give one example showing such a computation. With this approach we are now ready to compute relevance of a query for all documents of a document collection.

## Learning and Using the Model

Maximum Likelihood Estimation of probabilities under Unigram Model

$$\hat{P}_{mle}(t|M_d) = \frac{tf_{t,d}}{L_d}$$

where

- $tf_{t,d}$  is the number of occurrences of  $t$  in  $d$  (term frequency)
- $L_d$  is the number of terms in the document (document length)

Using the model

$$\hat{P}(q|M_d) = \prod_{t \in q} \hat{P}_{mle}(t|M_d)$$

For applying the probabilistic retrieval method described before, we need first to learn the language model of each document. The learning is performed using Maximum Likelihood Estimation (MLE). In the case of the unigram, this results in a very straightforward result. We just estimate the term probabilities by counting the document frequencies and normalizing by document length. When using the model for a query  $q$ , we then use those estimates, to estimate the relevance of a query for the document, as illustrated before.

Consider the document:

"Information retrieval is the task of finding the documents satisfying the information needs of the user"

Using MLE to estimate the unigram probability model, what is  $P(\text{the} | M_d)$  and  $P(\text{information} | M_d)$ ?

1. 1/16 and 1/16
2. 1/12 and 1/12
3. 1/4 and 1/8
4. 1/3 and 1/6

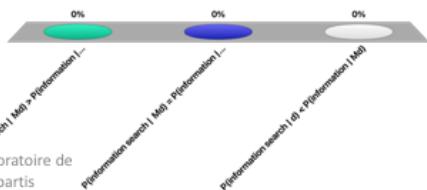


term frequency not normalized ?

Consider the following document

$d = \text{"information retrieval and search"}$

1.  $P(\text{information search} | M_d) > P(\text{information} | M_d)$
2.  $P(\text{information search} | M_d) = P(\text{information} | M_d)$
3.  $P(\text{information search} | d) < P(\text{information} | M_d)$



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## Issues with MLE Estimation

Problem 1: if query contains a term not occurring in the document  $\hat{P}(q|M_d) = 0$  !

Problem 2: this is an estimation! A term that occurs once, might have been “lucky” whereas other ones with same probability to occur is not in the document

- need to give non-zero probability to unseen terms!

Applying the afore mentioned approach to estimate relevance of a document to a query incurs a practical issue: if the query contains a term not occurring in the document the estimated probability will be unavoidable zero, since one of the factors of the product computing that probability will be zero. In other words, the query cannot be generated by the document model, thus the document is not relevant to the query. This is not only impractical, but also not meaningful from a more theoretical perspective. Since we used MLE to generate the model, we were using the statistics of one specific document, that has been generated by a probably more complex model, that may contain other terms that just were not selected.

## Smoothing

Idea: add a small weight for non-occurring terms in a document, that is smaller than the collection frequency

$$\hat{P}(t|M_c) \leq cf_t/T$$

$cf_t$  = number of times term t occurs in collection

$T$  = total number of terms in collection

Smoothed estimate

$$\hat{P}(t|d) = \lambda \hat{P}_{mle}(t|M_d) + (1 - \lambda) \hat{P}_{mle}(t|M_c)$$

$M_c$  = language model over whole collection

$\lambda$  = tuning parameter

To fix the aforementioned problem an approach called smoothing is applied. The basic idea is to assume that in fact every term potentially could occur in the document generated by its document model, including those that are not part of the actual document; only that the probability of terms not seen in the document is presumably less likely to occur as it would be expected to occur in the overall document collection. The smoothed estimate then combines the estimated likelihood to occur in the document according to the model generated from the document, with the estimated likelihood of a term occurring in the general document collection, modeled as a generic language model using the statistics from the document collection.

## Probabilistic Retrieval

With smoothing the relevance is computed as

$$P(d|q) \propto P(d) \prod_{t \in q} ((1 - \lambda)P(t|M_c) + \lambda P(t|M_d))$$

From a technical perspective the probabilities are computed using term frequencies, thus equivalent to vector space retrieval

Probabilistically motivated models show generally better performance

- But parameter tuning ( $\lambda$ ) is critical
- $\lambda$  can be query-dependent, e.g. query size

Here we summarize the approach for probabilistic retrieval. From a more technical perspective or the perspective of computational complexity probabilistic retrieval is not very different from vector space retrieval. The computation of the likelihoods for the document models requires the knowledge of term frequencies, so in that sense it is equivalent. For the collection models the global term frequencies need to be computed, which again is similar to computing inverse document frequencies in a document collection.

In practical use the fine tuning of the model parameters (in that case  $\lambda$ ) is essential for the good working of the model. Different methods have been devised for that. It is also possible to make the parameters dependent on the query, in particular on the query size.

## Example

Collection consisting of d1 and d2

d1: Einstein was one of the greatest scientists

d2: Albert Einstein received the Nobel prize

Query q: Albert Einstein

Using  $\lambda=1/2$

$$P(q|d1) = \frac{1}{2} * (0/7 + 1/13) * \frac{1}{2} * (1/7 + 2/13) \approx 0.0057$$

$$P(q|d2) = \frac{1}{2} * (1/6 + 1/13) * \frac{1}{2} * (1/6 + 2/13) \approx 0.0195$$

This is a simple example illustrating the use of probabilistic retrieval.  
Note that the document lengths of d1 and d2 are 7 and 6, and that  
the collection length is 13.

## Example: Comparing VS and PR

Precision				
Rec.	tf-idf	LM	%chg	
0.0	0.7439	0.7590	+2.0	
0.1	0.4521	0.4910	+8.6	
0.2	0.3514	0.4045	+15.1	*
0.3	0.2761	0.3342	+21.0	*
0.4	0.2093	0.2572	+22.9	*
0.5	0.1558	0.2061	+32.3	*
0.6	0.1024	0.1405	+37.1	*
0.7	0.0451	0.0760	+68.7	*
0.8	0.0160	0.0432	+169.6	*
0.9	0.0033	0.0063	+89.3	
1.0	0.0028	0.0050	+76.9	
Ave	0.1868	0.2233	+19.55	*

Ponte & Croft, 1998

This is a result reported from comparing vector space retrieval with probabilistic retrieval. It shows that in this experiment probabilistic retrieval improves precision, in particular for higher values of recall. (LM = language model).

## Overview of Retrieval Model Properties

	Vector Space Model	Language Model	BM25 (another prob. Model)
Model	geometric	probabilistic	probabilistic
Length normalization	Requires extensions (pivot normalization)	Inherent to model	Tuning parameters
Inverse document frequency	Used directly	Smoothing and collection frequency has similar effect	Used directly
Multiple term occurrences	Taken into account	Taken into account	Ignored
Simplicity	No tuning required	Tuning essential	Tuning essential

Here we compare the characteristics of the vector space model with the probabilistic retrieval model based on language models, and BM25 another model based on probabilistic foundations, that is considered as one of the most performant retrieval models.

One aspect that is taken implicitly care off in the probabilistic retrieval model based on language models is normalization for document length. For vector space retrieval specific extensions have been developed, that modify the weighting parameters with the document length. For collections with widely varying document lengths this proved to be a useful improvement. In general, the vector space model is preferred when a quick and simple solution is sought. For probabilistic models better performance can be achieved, but this depends on careful parameter tuning which requires specialized expertise.

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